Sonish Lamsal / Bradley Thompson
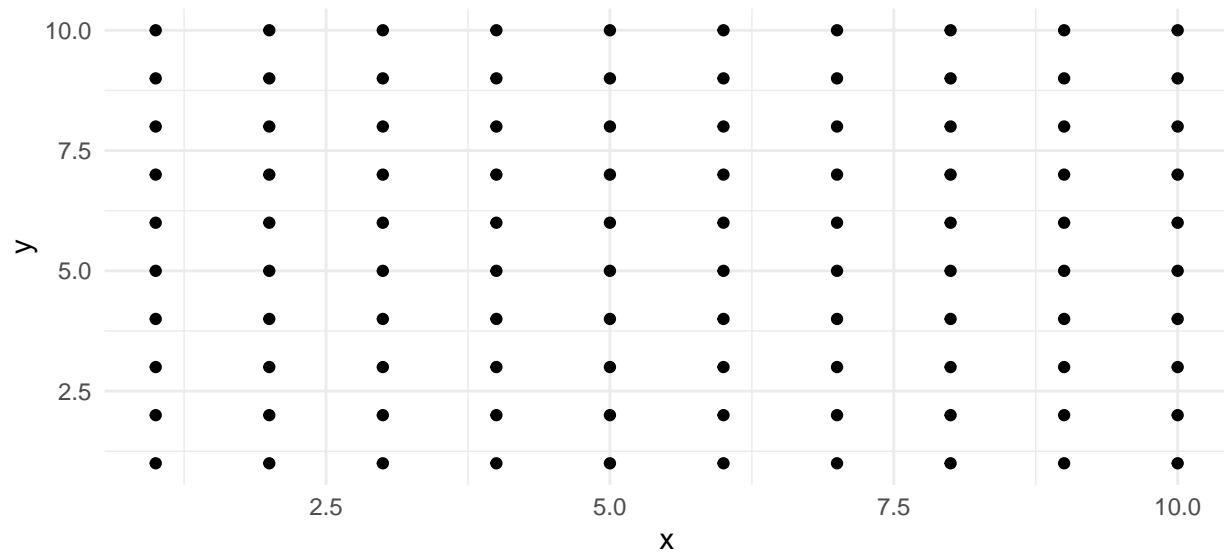
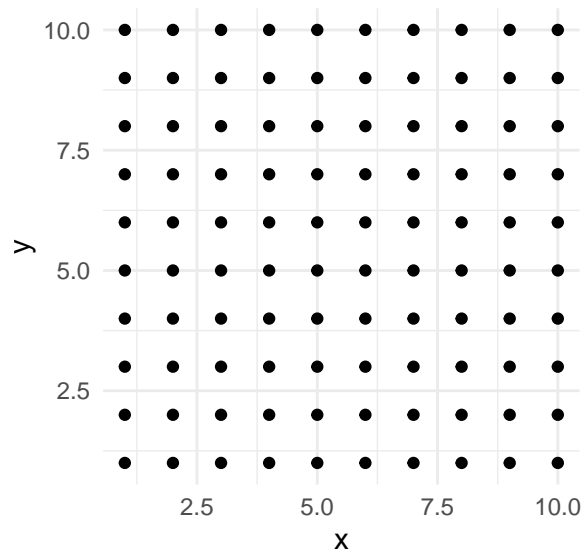STA6375: Computational Statistics I

Homework 3

1a.

```r
library("tidyverse")
```

```r
df <- expand.grid("x" = 1:10, "y" = 1:10)
ggplot(df, aes(x, y)) +
  geom_point() +
  theme_minimal()
```
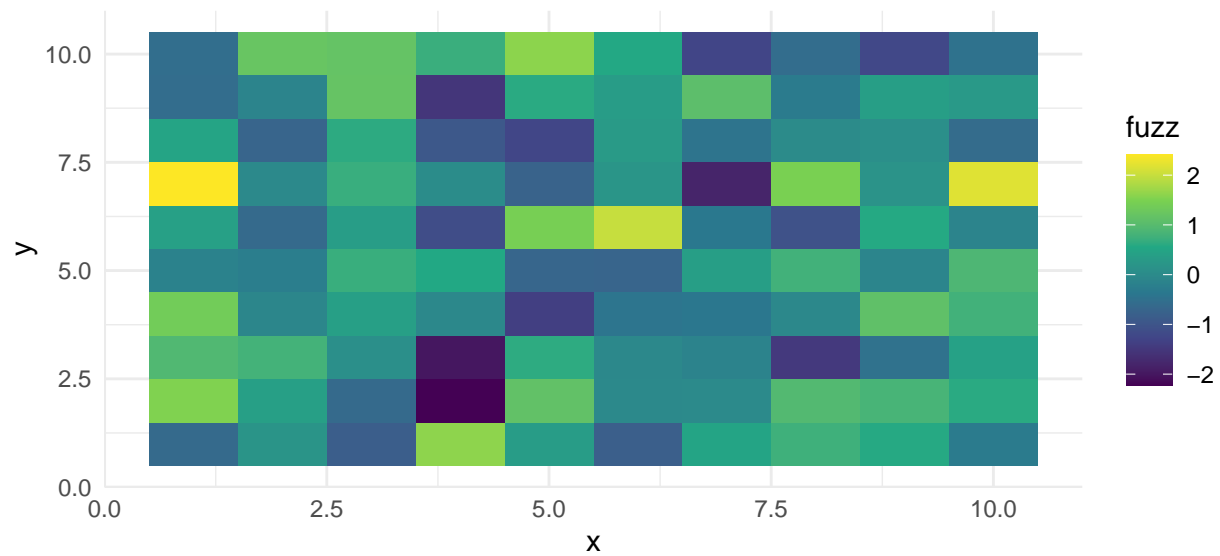

1b.

```r
ggplot(df, aes(x, y)) +
  geom_point() +
  theme_minimal() +
  coord_equal()
```
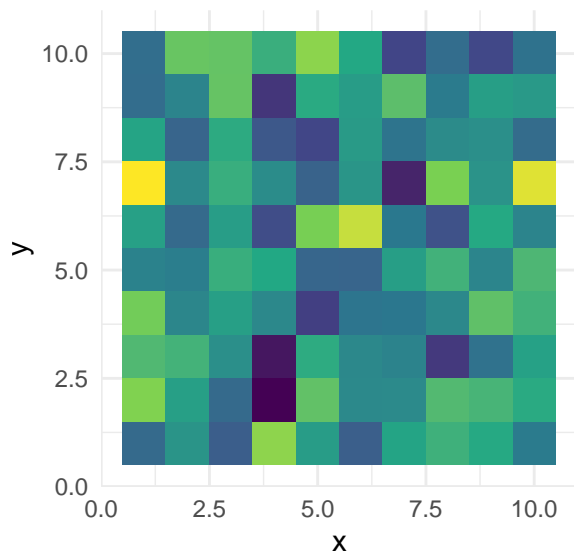
1c.

```r
set.seed(1)
fuzz <- rnorm(nrow(df))
  ggplot(df,aes(x,y)) +
  geom_raster(aes(fill=fuzz))+
  theme_minimal()
```
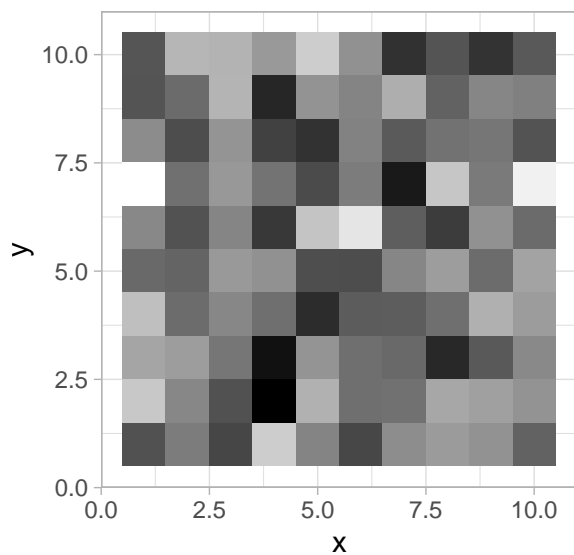

1d.

```r
ggplot(df,aes(x,y)) +
  geom_raster(aes(fill=fuzz)) +
  theme_minimal() +
  theme(legend.position="none") +
  coord_equal()
```

1e

```
ggplot(df, aes(x = x, y = y)) +
  geom_raster(aes(fill = fuzz)) +
  scale_fill_gradient(low = "black", high = "white") +
  coord_equal() +
  theme_light() +
  theme(legend.position = "none")
```
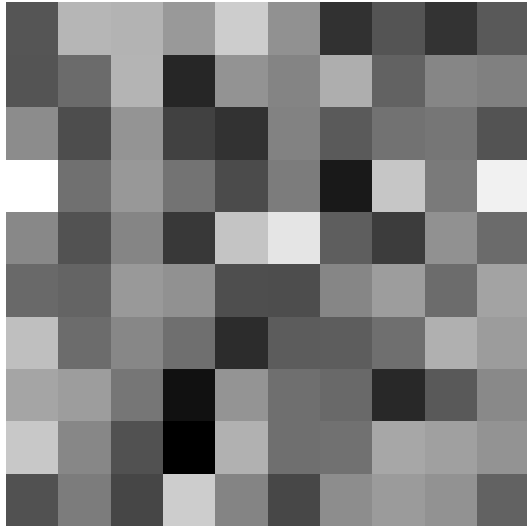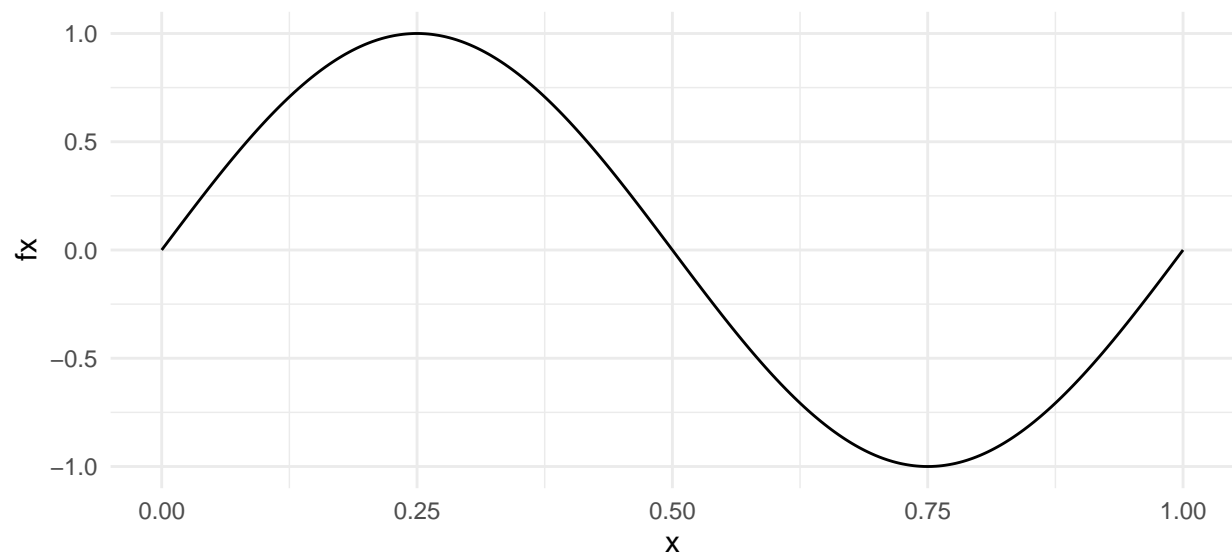

1f.

```
ggplot(df, aes(x = x, y = y)) +
  geom_tile(aes(fill = fuzz)) +
  scale_fill_gradient(low = "black", high = "white") +
  coord_equal() +
  theme_void() +
  theme(legend.position = "none")
```
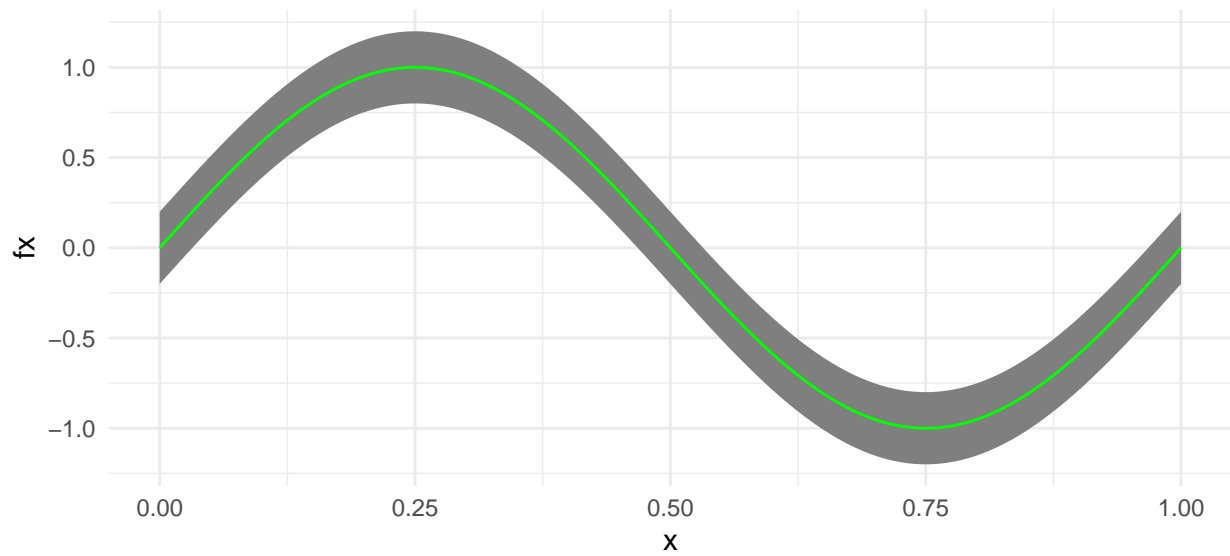
1g

```r
x<- seq(0,1, length.out=1001)
FX <- sinpi(2*x)
values<- data.frame(x=c(x),y=c(FX))
ggplot(values,aes(x,y)) +
  geom_line() +
  xlim(0,1) +
  ylim(-1,1) +
  theme_minimal() +
  ylab("fx")
```


1h

```r
ggplot(values,aes(x,y)) +
  geom_ribbon(aes(ymin=y-0.2,ymax=y+0.2),fill="grey50")+
  geom_line(aes(y=y),colour="green") +
  xlim(0,1) +
  ylim(-1.2,1.2) +
  theme_minimal() +
```

```
ylab("fx")
```


1i

```
x<- vector()
y<-vector()
for (i in 1:10) {
  x[i]=cos((i-1)*36*pi/180)
  y[i]=sin((i-1)*36*pi/180)
}
df<- data.frame(x=x,y=y)
ggplot(df,aes(x,y))+
  geom_polygon(colour="black",fill=NA)+
  theme_minimal()+
  geom_point()+
  coord_equal()
```
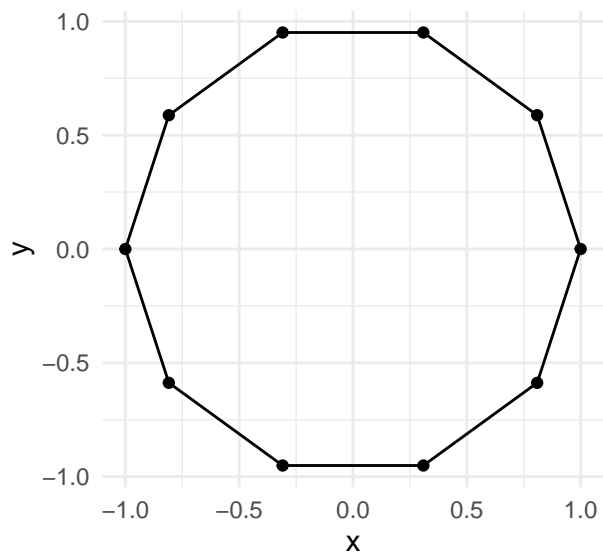

1j

```
set.seed(1)
df<- data.frame(x=rnorm(1e3, mean= 3, sd=2 ))
  ggplot(df, aes(x)) +
  geom_density() +
  stat_function(fun=dnorm, args = list(mean=3, sd=2), colour = "red")+
  geom_vline(xintercept = 8, colour="red", linetype="twodash") +
  theme_minimal()
```


2a.

```
A <- matrix(c(-1,3,1,
              -7,9,1,
              -2,2,4), nrow = 3, byrow = TRUE)
ev <- eigen(A)
V <- ev$vectors
L <- ev$values
Lamda <- diag(L)
V_1 <- solve(V)
A
```

```
#      [,1] [,2] [,3]
# [1,]   -1    3    1
# [2,]   -7    9    1
# [3,]   -2    2    4
```

```
V %*% Lamda %*% V_1
```

```
#      [,1] [,2] [,3]
# [1,]   -1    3    1
# [2,]   -7    9    1
# [3,]   -2    2    4
```

2b.

```
A <- matrix(c(10,2,-6,2,7,0,-6,0,2), nrow = 3, byrow = TRUE)
ev <- eigen(A)
V <- ev$vectors
L <- ev$values
Lamda <- diag(L)
```

```
VT <-t(V)
A
```

```
#      [,1] [,2] [,3]
# [1,]   10    2   -6
# [2,]    2    7    0
# [3,]   -6    0    2
```

```
zapsmall(V %*% Lamda %*% VT)
```

```
#      [,1] [,2] [,3]
# [1,]   10    2   -6
# [2,]    2    7    0
# [3,]   -6    0    2
```

```
zapsmall(crossprod(V))
```

```
#      [,1] [,2] [,3]
# [1,]    1    0    0
# [2,]    0    1    0
# [3,]    0    0    1
```

2c.

```
A <- matrix(c(1,2,3,4,5,6,7,8,6,8,10,12), nrow = 4, byrow = FALSE)
s_v_d <- svd(A)
U <- s_v_d$u
D <- s_v_d$d
E <- diag(D)
V <- s_v_d$v
A
```

```
#      [,1] [,2] [,3]
# [1,]    1    5    6
# [2,]    2    6    8
# [3,]    3    7   10
# [4,]    4    8   12
```

```
zapsmall(U %*% E %*% t(V))
```

```
#      [,1] [,2] [,3]
# [1,]    1    5    6
# [2,]    2    6    8
# [3,]    3    7   10
# [4,]    4    8   12
```

2d/e

```
A <- matrix(c(4,2,1,
              2,4,2,
              1,2,4), nrow = 3, byrow = TRUE)
ev <- eigen(A)
ev
```

```
# eigen() decomposition
# $values
# [1] 7.372281 3.000000 1.627719
#
# $vectors
```

```
#              [,1]          [,2]        [,3]
# [1,] -0.5417743 -7.071068e-01  0.4544013
# [2,] -0.6426206 -1.110223e-16 -0.7661846
# [3,] -0.5417743  7.071068e-01  0.4544013
```

```
#you can do a Cholesky decomposition of A becasue A is positive definite since
#all of its eigenvalues are positive and it's symmetric.
C <- chol(A)
C
```

```
#      [,1]     [,2]      [,3]
# [1,]    2 1.000000 0.5000000
# [2,]    0 1.732051 0.8660254
# [3,]    0 0.000000 1.7320508
```

```
A
```

```
#      [,1] [,2] [,3]
# [1,]    4    2    1
# [2,]    2    4    2
# [3,]    1    2    4
```

```
t(C) %*% C
```

```
#      [,1] [,2] [,3]
# [1,]    4    2    1
# [2,]    2    4    2
# [3,]    1    2    4
```

2f.

```
A <- matrix(c(1,3,2,
              3,0,0,
              0,1,3,
              0,1,0), nrow = 4, byrow = TRUE)
QR <- qr(A)
R <- qr.R(QR)
Q <- qr.Q(QR)
X <- qr.X(QR)
X
```

```
#      [,1] [,2] [,3]
# [1,]    1    3    2
# [2,]    3    0    0
# [3,]    0    1    3
# [4,]    0    1    0
```

```
zapsmall(Q %*% R)
```

```
#      [,1] [,2] [,3]
# [1,]    1    3    2
# [2,]    3    0    0
# [3,]    0    1    3
# [4,]    0    1    0
```