

Given Information about ZNTA's location

First information: Probability of location depending on the distance to river Spree

The first information reads as follows:

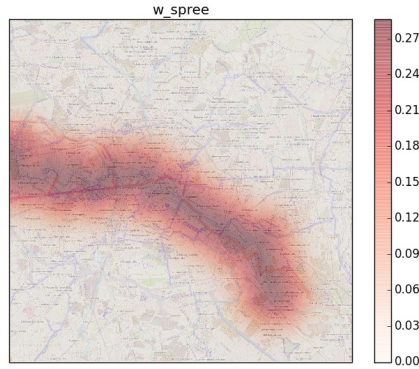
"The candidate is likely to be close to the river Spree. The probability at any point is given by a Gaussian function of its shortest distance to the river. The function peaks at zero and has 95% of its total integral within $\pm 2730\text{m}$."

First, we calculate the distance x_1 of a point (x, y) on the map to the river Spree. This distance is then fed into the following probability density function which we derived from the given information:

$$f_1(x_1) = \frac{1}{\sigma_1 \sqrt{2\pi}} \exp \left(-0.5 \left(\frac{x_1 - \mu_1}{\sigma_1} \right)^2 \right),$$

where $\mu_1 = 0.0$ and $\sigma_1 = 2.730/1.959964 = 1.39288$.

Doing this for each point yields the following map. The darker the red on the map, the more probable it is to find ZNTA at this location, with a maximum of approximately 28%:



Second information: Probability of location depending on the distance to the Brandenburg Gate

The second information reads:

"A probability distribution centered around the Brandenburg Gate also informs us of the candidate's location. The distribution's radial profile is log-normal with a mean of 4700m and a mode of 3877m in every direction."

This yields the following lognormal probability density function for x_2 =distance to the Brandenburg Gate:

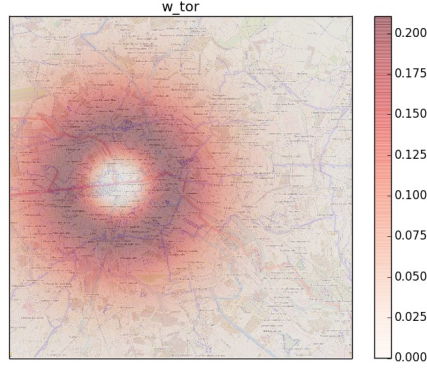
$$f_2(x_2) = \frac{1}{x_2 \sigma_2 \sqrt{2\pi}} \exp \left(- \left(\frac{(\ln(x_2) - \mu_2)^2}{2\sigma_2^2} \right) \right).$$

We have

$$\exp \left(\frac{\mu_2 + \sigma_2^2}{2} \right) = 4.7 \text{ and } \exp \left(\mu_2 - \sigma_2^2 \right) = 3.877,$$

which yields $\mu_2 = 1.40318$ and $\sigma_2 = 0.53735$.

By calculating the probability for each point, we obtain the following map:



Third information: Probability of location depending on the distance to a satellite's path

Finally, information three reads:

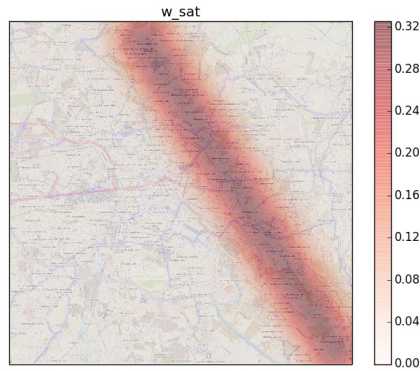
"A satellite offers further information: with 95% probability she is located within 2400m distance of the satellites path (assuming a normal probability distribution)."

That tells us that for x_3 =distance to the satellite's path, we have

$$f_3(x_3) = \frac{1}{\sigma_3 \sqrt{2\pi}} \exp \left(-0.5 \left(\frac{x_3 - \mu_3}{\sigma_3} \right)^2 \right),$$

where $\mu_3 = 0.0$ and $\sigma_3 = 2.400/1.959964 = 1.22451$.

This yields the following map:



Result: A map to find ZNTA

Now it remains to calculate the three distances x_1 , x_2 and x_3 for each point on the map and pass them to the respective probability density functions. The last step is to multiply the three probabilities and we obtain a map which colors the most probable locations of ZNTA:

