Towards detecting critical crowd density with Wi-Fi positioning: Case Amsterdam ArenA

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Abstract

We present a new methodology for estimating crowd density during festivals. Our motivation comes from the fact that many crowd disasters have happened because of abnormal crowd density. We exploit the ubiquity of smart phones, without requiring participation from the crowd, and we use Amsterdam ArenA as a living laboratory. We build upon previous work, where the location of a visitor is estimated anonymously based on the strengths of the Wi-Fi signals received at the ArenA Wi-Fi routers, by a method similar to trilateration. However, because in dense crowds a Wi-Fi signal is partially absorbed and partially reflected by the human bodies, the localization based on signals strengths alone does not suffice to estimate the crowd density. Moreover, since we don't rely on the smart phones being connected to the Wi-Fi network, the signal rates are quite volatile, and the MAC addresses of the phones may change, depending on the vendor's privacy policy. In this paper, we address those issues. We borrow ideas from statistical mechanics to estimate the crowd density. The advantage of our methodology when compared to similar methodologies is that our estimation becomes more (rather than less) precise when the number of people increases. This suits the purpose of being able to detect raised crowd density. We also validate our methodology experimentally by comparing the crowd density estimation to the ground truth obtained from security cameras.

val. to be done

1 Introduction

Crowd disasters have taken many human lives. The Love Parade disaster (Duisburg, 2010), the Ellis Park Stadium disaster (Johannesburg, 2001), the PhilSports Stadium stampede (Manila, 2006) are just a few recent examples. One of the reasons that disasters happen is a "lack of overview of everybody" [7], that is, a lack of macroscopic overview of the crowd. Critical crowd density [7, 11] is a contributing factor to crowd disasters. Yet, it is still challenging to determine timely when it occurs, so that a disaster can be prevented by navigating the rest of the crowd away from the congestion.

In our work we estimate crowd density during concerts in indoor spaces. A lot of research on estimating crowd density has been done using video processing from security cameras [10, 8]. However, this approach does not suffice to detect raised crowd density. First, it is difficult to obtain macroscopic overview of the crowd. Second, the lighting conditions during concert hours might not be sufficient for video-based crowd analysis only. Finally, the error of video-based density estimation increases with the increase of the actual crowd density.

In our approach, which can complement the video-based analysis, we combat the three above mentioned issues by exploiting the ubiquity of smart phones, as has been done in (citations). Contrarily to most such approaches (citations), we don't require participation from the crowd. Our living laboratory is the Amsterdam Arena [1]. We build upon previous work [2], where the location of a visitor is estimated anonymously based on the strengths of the Wi-Fi signals received at the ArenA Wi-Fi routers, by a method similar to trilateration (the way the Global Positioning System is implemented). However, because in dense crowds a Wi-Fi signal is partially absorbed and partially reflected by the human bodies, the localization based on signals strengths alone does not suffice to estimate the crowd density; e.g. multiple optimal position estimations are possible. Moreover, since we don't rely on the smart phones being connected to the Wi-Fi network, the signal rates are quite volatile, and the MAC

add missing citations twice

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*authors and order could change by the time the paper is submitted

addresses of the phones may change (be "randomized"), complying to some vendors' privacy policy. In this paper, we address those issues. We borrow ideas from statistical mechanics to estimate the crowd density: rather than estimating the most likely position of a visitor in real time, we create an evolving continuous probability distribution over all possible positions (which turns out to be usually bimodal). We rely on the law of the large numbers, with adaptation to correlated variables, to estimate the crowd density by aggregating the individual distributions. The individual probability distribution turns gradually into a uniform distribution, with which we address the problem of outdated signals. Finally, we use the law of large numbers again and the "randomized MAC address" tag, that is available with the data, to account for the fact that a portion of the MAC addresses are randomized. Thus, the advantage of our methodology when compared to other methodologies is that our estimation becomes more (rather than less) precise when the number of people increases. This suits the purpose of being able to detect raised crowd density. We also validate our methodology experimentally by comparing the crowd density estimation time series to the ground truth obtained from security cameras.

The rest of the paper is organized as follows. In Sec. 2 we explain the process of trilateration, that estimates the position of a Wi-Fi device based on the strength of the signals captured by the Wi-Fi routers in the stadium. In Sec. 3 we present our methodology for estimating in real-time the spatial density distribution of the crowd. We first identify which issues have not been resolved by the positioning in order to estimate crowd density, and which are not related to the mathematical methodology behind the positioning step. Then, we present our approach towards resolving the issues. In Sec. 4 we compare our estimation of density to the one obtained by video analysis. In Sec. 5 we put our approach into a perspective by comparing it to other approaches that are using the smart phones. We conclude and point to future research directions in Sec. 6.

2 Positioning of visitors using Wi-Fi sensors and smart phones

We estimate the positions of smart phones using a method based on lateration. The lateration method uses the distances between a smart phone and multiple reference points, which in this case are the existing Wi-Fi access points (AP's) in the stadium (see Fig. 1[1]). Smart phones transmit Wi-Fi signals which are captured at the AP's. The captured Wi-Fi signals contain information about the measured signal strength. Using a physical model for the relationship between the received signal strength (RSS) of the Wi-Fi signal and the distance between a transmitter and receiver, the distance between the smart phone and the AP is estimated. When we have the distances from a smart phone to at least three AP's, the position of the smart phone can be uniquely determined at the intersection of three circles (Fig. 1a.) [9].
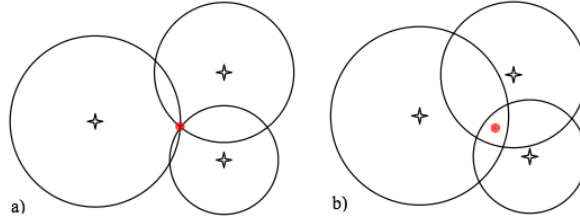

Figure 1: Estimating position with trilateration: a) precise b) rough

The RSS value of a signal decreases when the distance between transmitter and receiver increases. The decrease is given by a path loss model, given by the Friis equation

$$P_R = P_T + 10\lambda \log_{10}(\frac{c}{4\pi f r}) \tag{1}$$

where we use $\lambda = 2$ (line of sight condition), c is the speed of light, f is 2.4 GHz, and r is the distance between the mobile device and the AP.
The measured RSS values contain unpredictable variation due to noise, and interference such as absorption and reflection by obstacles between transmitter and receiver (shadowing and multipath effects) [6].

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[1]Image courtesy of http://rvmiller.com/2013/05/part-1-wifi-based-trilateration-on-android/

The positions of these obstacles may change in time, in particular in the case of human bodies. As a result, the circles in the lateration method do not intersect at a unique point (see e.g. Fig.1). In this case an optimization procedure is undertaken for positioning of the smart phone. We use the least squares optimization method, which in our case takes the form of a chi-square data fit. Exact description of the method is beyond the scope of this paper and we refer the reader to [3] for details. We note, however, that the statistical estimation of the position provides as also with standard deviation σ of the estimation, which we will use in Sec. 3.

3 From positioning to estimation of density

3.1 Positioning only is not enough

Under ideal circumstances, the positioning itself would suffice to estimate the spatial crowd density distribution: every second we would only need to count the number of estimates per square meter. However, we have observed several issues, which are not related to the mathematical methodology behind the positioning step, that prevent us to apply direct counting.

1. *Issue 1: bimodal distributions of coordinates estimations.* We have sampled randomly 20 MAC addresses and plotted the estimations of their coordinates through time, where we have plotted only the estimations with a relatively small (conditional) uncertainty. We observed persistent bimodal distribution of the estimations, an example of which can be seen in Fig. 2. This figure shows the
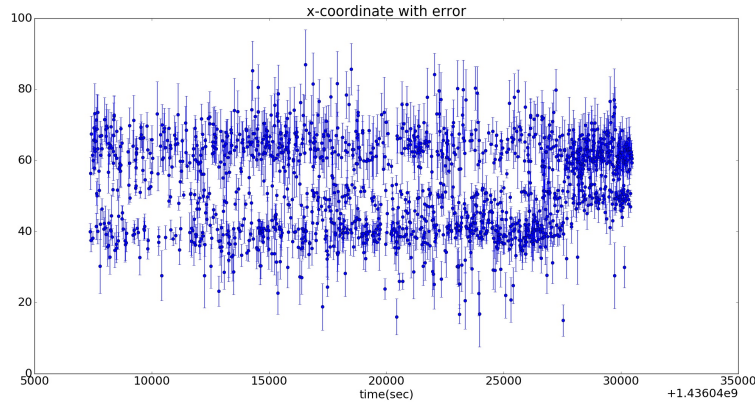

Figure 2: Estimation of x-coordinate of a static MAC device through time with error

   estimated x-coordinates in meters through time of a static MAC address that was persistent for 24 hours. Because we did not observe bi-modal distributions in the signal strengths, the bi-modal distribution of the positions estimates can be explained by a "multiple local optima" situation. Namely, in a dense crowd, when optimizing the positioning of a MAC device, there can be multiple local optima that are equally good candidates. For example, consider Fig. 3 [2]. In the center of every ring there is a Wi-Fi router, that has estimated signal strength to the MAC device with a certain error range. The error range is represented by the thickness of the ring. Then, there are two possible regions which are equally good candidates for the positioning of the MAC device, and those regions are the two darkest regions where all three rings overlap. Note that the problem can arise regardless of the thickness of the rings and the number of Wi-Fi routers.

   change the position of the label and put units (meters)

2. *Issue 2: volatility of packet rates.* When a MAC device is connected to the Wi-Fi internet, it sends packets with a relatively stable and frequent rate. However, during concert hours, very few devices are actually connected to the internet. So, most of our estimations of positions come from signals that the device sends in a "probing" mode, i.e. while searching for a network. In this case the packet rate is quite volatile, ranging from a few seconds to a few minutes (citation?). This means

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[2] Picture courtesy of http://math.stackexchange.com/questions/42537/trilateration-with-bounds
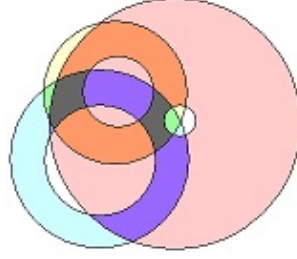
Figure 3: Trilateration can lead to multiple local optima

that when we make a snapshot of the MAC addresses visible in a certain moment, we are detecting a only a very small fraction of the MAC devices.

3. *Issue 3: MAC address randomization.* Due to ever increasing privacy concerns and possibly other business reasons, starting from 2014, the Apple I-phones have introduced randomization of the MAC address when the device is in a probing mode (not connected to internet) (citation?). This means that when the device switches from a probing to an online mode or vice versa, the MAC address suddenly changes and thus the device cannot be followed anymore. It is worth noting, however, that from the MAC address itself it can be determined whether the address is an original MAC address (non-randomized) or randomized.

add citation

3.2 Crowd density estimation

3.2.1 Bimodal distributions of coordinates estimations: Creating statistical ensembles

In order to deal with issue 1 from above, let us start with the following observation: we are not interested in the individual locations of the MAC devices, but rather in the density of the crowd. Also, we would especially like to have more precise estimation when the density reaches a certain threshold, so that the crowd outside the dense region can be promptly navigated away from it. This situation (dense crowd), means that there is more blockage and absorption of signals from bodies. This leads to less precise estimation of the distance between a MAC device and a Wi-Fi router based on Wi-Fi signal strength, which means that the rings in e.g. Fig.3 would be even thicker. This exaggerates the effect of "bimodal" or even multi-modal distribution of position estimates. Thus, in a dense crowd, the best that we can derive from the positioning method for a MAC device is a probability distribution over all possible locations. For example, in the scenario in Fig. 3, we can say that the MAC device is with a probability of 0.5 in the left grey region (region where all three rings overlap) and with a probability of 0.5 in the right grey region [3]. While this does not provide us with very useful information about the location of the MAC device, if we apply the same reasoning for all MAC devices, and we add together the spatial probability density functions for all MAC devices, we end up with a spatial distribution of the crowd density. If we assume that the locations of the MAC devices are mutually independent, we can apply directly the law of the large numbers and conclude that for a dense crowd the error of the estimation of the density per square meter will vanish. However, we cannot assume the mentioned independence, because people tend to go to concerts in groups. In this case, the variance of the estimation in the limiting case is equal to the average correlation between the locations. Nevertheless, we can safely assume that for a regular crowd at a concert the group size is relatively small compared to the whole crowd and thus the average correlation tends to zero as the number of people increases. Thus, the error of the estimation of the crowd density will in anyway diminish as the number of people grows.

In what follows we formalize the discussion above. Let $\{mac_1, mac_2, ...mac_n\}$ be all MAC devices detected at time t. Let R be an arbitrary region from the stadium. Let X_i be a random variable defined by

$$X_i = \begin{cases} 1 & \text{if } mac_i \in R \\ 0 & \text{if } mac_i \notin R \end{cases}$$

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[3]In this example we assign the probabilities in a trivial way for the purpose of demonstrating our idea

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Denote by X the total number of devices in R detected at time t. Clearly, $X = \sum_{i=1}^{n} X_i$. Then $E(X)$, the expected value of X is

$$E(X) = E(\sum_{i=1}^{n} X_i) = \sum_{i=1}^{n} E(X_i) = \sum_{i=1}^{n} (1 \cdot Prob(mac_i \in R) + 0 \cdot Prob(mac_i \notin R)) = \sum_{i=1}^{n} Prob(mac_i \in R),$$

where by $Prob(mac_i \in R)$ we denote the probability that mac_i is in the region R at time t. We postpone the derivation of $Prob(mac_i \in R)$ a bit. Instead, we first show that the variance of X/n, that is, the variance of the proportion of devices detected in R out of all detected devices, diminishes when n becomes large (note that the variance of X in the limiting case is out of our interest because then $E(X)$ is potentially infinite). This suffices to show that our method of estimation of crowd density is theoretically sound, given the probabilities $Prob(mac_i \in R)$. We have

$$Var(\frac{X}{n}) = Var(\frac{1}{n} \cdot \sum_{i=1}^{n} X_i) = \frac{1}{n^2} \cdot Var(\sum_{i=1}^{n} X_i) = \frac{1}{n^2} \cdot (\sum_{i=1}^{n} Var(X_i) + \sum_{i \neq j} Cov(X_i, X_j)) \qquad (2)$$

We can assume that there is an upper limit λ of a number of people that go to a concert together (a group), that is, whose locations are correlated[4]. Denote by κ the maximal covariance between any X_i and X_j and let us write $i \sim j$ if and only if i and j are in the same group. Then,

$$\sum_{i \neq j} Cov(X_i, X_j) = 2 \sum_{1 \leq i < j \leq n} Cov(X_i, X_j) = 2 \sum_{i,j : i \sim j} Cov(X_i, X_j) \leq 2n \cdot \frac{\lambda(\lambda - 1)}{2} \cdot \kappa = n\kappa\lambda(\lambda - 1) \quad (3)$$

where the inequality holds because the maximal number of groups is n and the maximal number of pairs (i, j) in a group is $\lambda(\lambda - 1)/2$. Let

$$\mu = \frac{1}{n} \sum_{i=1}^{n} Var(X_i),$$

that is, denote by μ the average variance of $X_1, X_2, ..., X_n$. From (2) and (3) we have

$$Var(\frac{X}{n}) \leq \frac{1}{n^2}(n\mu + n\kappa\lambda(\lambda - 1)) = \frac{1}{n}(\mu + \kappa\lambda(\lambda - 1)), \qquad (4)$$

which tends to 0 when $n \to \infty$. Note that we have greatly overestimated the covariance with the inequation in (3), which means that in practice the variance converges to 0 much faster than as presented.

Next, we can proceed with derivation of $Prob(mac_i) \in R$ for arbitrary i in order to be able to evaluate $E(X)$, the estimated crowd density per region.

The data provides us with a series of estimated positions of mobile devices, together with their corresponding values of measurement uncertainty (see Sec.2).

From this data we wish to estimate the spatial probability distribution for an arbitrary MAC device m, along a moving time window. So, our first step is to select from the data the estimated N positions whose time stamps fall within a specified time interval $[t - \Delta t, t]$. A natural way to construct a two-dimensional probability distribution would be to construct a histogram, by binning the positions and normalizing with N. However, we also wish to preserve the uncertainty that corresponds to each estimated position. Therefore, we first "smooth" each position into a bivariate Gaussian distribution ('bump'), using the uncertainty values (σ_x and σ_y) provided by the position estimation method as standard deviations. Then, for m we construct a two-dimensional probability density function (p.d.f.) by adding up these bumps, and dividing the sum by N.. (In Fig. 4 we show the result of smoothing a histogram of the device discussed in Fig.2.)

The implementation of our method is similar to that of kernel density estimation [13][14]. In our case the amount of smoothing is variable and determined by the measurement uncertainty values σ_x and σ_y. The p.d.f. for a mobile device with an address m at a location (x, y) is defined by

make viz. smooth and not dark

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[4]Actually, when the crowd is so dense that people can not move freely anymore, the whole crowd becomes a "group" (as in the Love Parade disaster) and all locations are correlated. But we aim to detect a high density with our method *before* this happens, to react preventively; otherwise, it is too late.
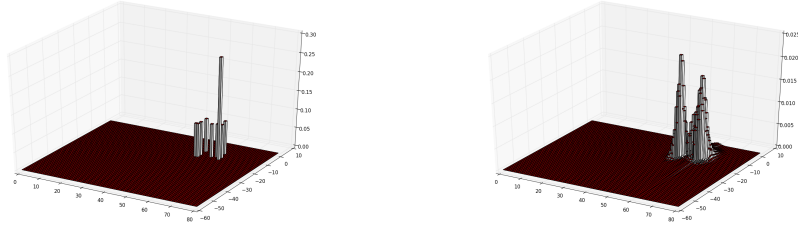
Figure 4: Smoothing a histogram with Gaussian kernels. Left: Original histogram. Right: The smoothed histogram.

$$\hat{f}_m(x,y) = \frac{1}{N} \sum_{i=1}^{N} K((x-x_i), \sigma_x) K((y-y_i), \sigma_y) \tag{5}$$

where the kernel function K is given by

$$K(u, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp(-\frac{u^2}{2\sigma^2}) \tag{6}$$

The final crowd density estimation is given by

$$\hat{f}_T(x,y) = \sum_m \hat{f}_m(x,y) \tag{7}$$

To finish our discussion, in order to evaluate $Prob(mac_i) \in R$ we need to integrate $\hat{f}_m(x,y)$ for $(x,y) \in R$.

Note that so far we assumed that in every time window there is at least one estimate for every MAC address ever detected. In what follows we explain how we capture the cases when this assumption does not hold.

3.2.2 Volatility of packet rates: Applying "conservation of mass" principle

(Needs to be finished.) To address the second issue, *Volatility of packet rates*, we ensure that we do not forget about the MAC devices that were not observed in the last time window. In fact, for every MAC device that was ever observed, until it has been observed again we maintain the old probability distribution, too. Over time this probability distribution turns gradually into a uniform by smoothing it every epoch with a Gaussian kernel (see Fig. 5 for an example). The size of the kernel changes over time and is related to the maximal speed that the MAC device can have under the current density distribution of the crowd. In other words, we assume a Brownian motion of the MAC device, where the speed is limited by the maximal speed of a pedestrian under the current crowd conditions (cite paper Johansson et al). When the MAC device is observed again, its old probability distribution is simply overwritten by the probability distribution that is computed as above.   ref. picture
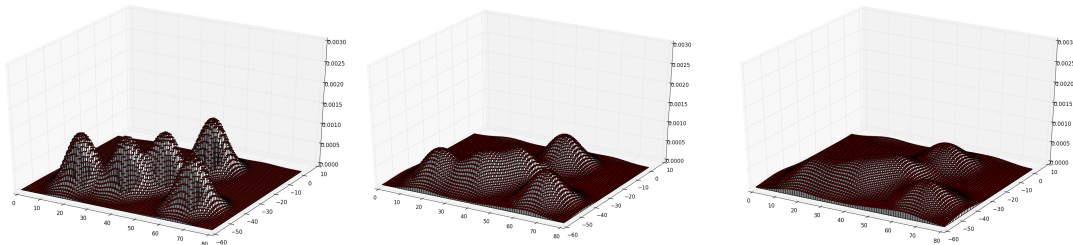

Figure 5: Turning a distribution gradually into uniform

Formally, in case we have no new observations, we smooth the probability distribution of the previous epoch by convolution with a Gaussian probability function. The width σ of the Gaussian PDF is

determined through the conceptual equivalence of this approach with assuming Brownian motion of pedestrians. Brownian motion (without drift), is given by

$$dB(t) = \sqrt{2D}dW(t) \tag{8}$$

where $W(t)$ is a Wiener process, and σ is related to the diffusion constant D using the relationship

$$\sigma = \sqrt{2Dt} \tag{9}$$

The variance σ^2 is thus determined by the length t of the time interval (epoch), and the diffusion constant D, which in turn can be determined by the walking speed of pedestrians [5].

3.2.3 MAC address randomization: using Big data again

To address the last issue, *MAC address randomization*, we rely once again on the fact that we have a lot of data. Namely, we know from the structure of the MAC address whether it has been randomized or not. Figure 8 shows the ratio between randomized and non-randomized addresses observed per minute from midnight until 6:00 am. We can see that it is quite stable through time; in fact, the Pearson correlation coefficient between the time series of randomized and non-randomized addresses is 0.88.
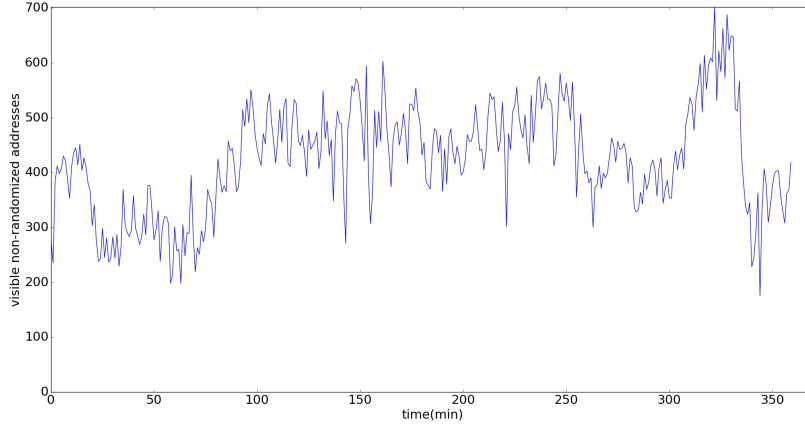

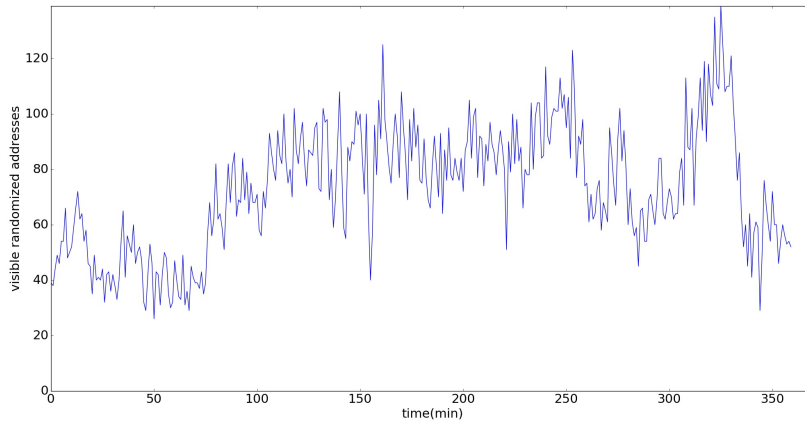Figure 6: Non-randomized addresses observed per minute

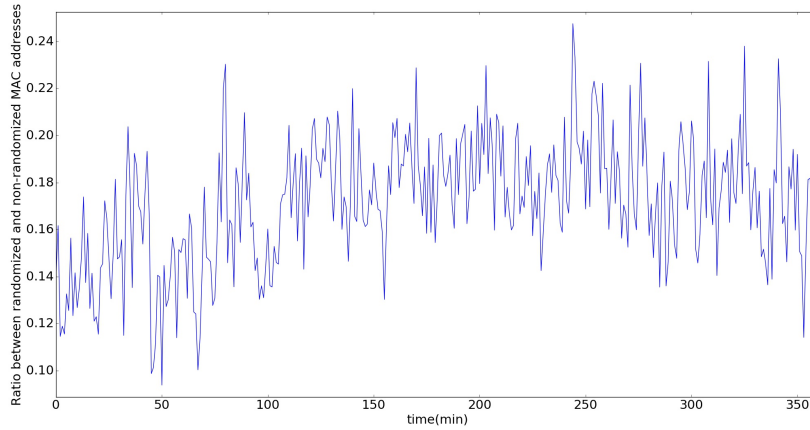Figure 7: Randomized addresses observed per minute

Figure 8: Ratio between randomized and non-randomized addresses observed per minute

Thus, when estimating crowd density, we ignore the MAC devices that have a randomized address and at the end we multiply the crowd density by 1.225, to account for the ignored MAC devices. We choose factor 1.225 to allow for a safety margin: in the peaks of the graph in Fig. 8 the values are 0.225, and we would rather overestimate than underestimate the crowd density. Note that this ratio should be re-computed periodically, to account for the changing conditions at the smart phones market.

in general: calculate it automatically, with a confidence interval mention the absolute numbers, or give graphs

4 Validation

To be done. Hopefully with official videos from the organizational team of Sensation 2015 Amsterdam White. Note that by validation we mean more of calibration. In general the approach is theoretically valid, which we show in Sec.3.2.1, but we are using parameters in the model that need to be calibrated. We need independent data sets (videos) for calibration and testing, to avoid overfitting. Also the paremeters should be as much as possible initially optimized from the Wi-Fi data itself and from theory.

5 Related work

In progress.

In the Introduction we mentioned the benefits of using smart phones based over video-based approach for density estimation of indoor concerts crowd; in fact, it is our opinion that the two approaches complement each other and in the future we plan to integrate both techniques in real time. Thus, in this section we are going to focus on previous work that estimates crowd density using wireless technologies.

[16] estimate crowd densities by distributing volunteers in the crowd, who are carrying smart phones scanning for Bluetooth devices. They then use statistics to combine the different measurements in space and time. They improve their method from mere counting to more advanced statistical analysis in [17], by using relative features that are more robust against statistical variations of the number of devices. The features include the average speed of scanning devices, the average bluetooth signal strength and its variance, etc.

In [18] the authors follow a participatory sensing approach in which pedestrians share their locations on a voluntary basis. Since only a fraction of all pedestrians share location information, they present a methodology to infer the crowd density from their walking speed, by inverting the formula for estimating maximal pedestrian speed given a crowd density, presented in [?]. Note that in our case study the visitors of the concerts with a stage are mostly static without intention to reach a destination, so this technique cannot be directly applied.

A number of studies use Bluetooth to estimate crowd densities at a wide range of places and events. In these studies the position of a mobile phone is approximated to the location of the sensor by which it is detected.

Schauer *et al.* (2014) [12] count unique MAC devices detected by two sensors (nodes) at both sides (public and security) of a security check inside a major German airport, to estimate pedestrian densities and pedestrian flow. They consider time information, to determine the direction of a person's movement, and at least one RSSI value, to reduce the number of false positives in case devices are captured by both sensors. They compare Bluetooth and Wi-Fi based methods, and compare their methods to a known ground truth provided by the number of security checks.

Versichele *et al.* (2012) [15] use Bluetooth scanners at strategic locations during the 10-day Ghent Festivities, to analyze spatio-temporal dynamics of pedestrians.

Yoshimura *et al.* (2016) [19] use Bluetooth detection to analyze visitors' behavior at the Louvre museum in Paris.

Delafontaine *et al.* (2012) [4] use a similar approach (of Bluetooth tracking) and apply (genetic) sequence alignment methods to analyze the resulting data which consists of different sequences of sensors (nodes) for detected mobile devices.

Finally, none of the mentioned work uses our approach of modeling the position of an individual as a probability distribution; our method is designed to attack the problem of having a dense crowd; we are not interested in precise estimations for freely moving crowds; rather, we are interested in obtaining precise estimation when the concert crowds is dense and static...

6   Conclusion

To be done. Sonja:Mention somewhere that in the documentary of the LP disaster people were raising their phones up to look for a way out. (which is good , less blockage of signals)

Future work: include map of the venue in the calculations, perhaps not both dark regions in 3 are accessible by people!

Also future work: the speed in the brownian motion should depend on the local crowd density, rather than on the average crowd density.

References

[1] Amsterdam arena opens smart city testing centre. *Telecompaper*, 2015.

[2] Jan Amoraal. Thou customers, where are thou: Kpmg's indoor (wi-fi) tracking: From simulation to implementation. *TopQuants*, 2014.

[3] P.R. Bevington and D. K. Robinson. *Data Reduction and Error Analysis for the Physical Sciences*. McGraw-Hill, third edition, 2003.

[4] M. Delafontaine, M. Versichele, T. Neutens, and N. Van de Weghe. Analysing spatiotemporal sequences in bluetooth tracking data. *Applied Geography*, 34:659–668, 2012.

[5] W. Ebeling and I.M. Sokolov. *Statistical Thermodynamics and Stochastic Theory of Nonequilibrium Systems*. World Scientific, 2005.

[6] A. Goldsmith. *Wireless Communications*. Cambridge University Press, 2004.

[7] Dirk Helbing and Pratik Mukerji. Crowd disasters as systemic failures: analysis of the love parade disaster. *EPJ Data Science*, 1(1):1–40, 2012.

[8] Barbara Krausz and Christian Bauckhage. Loveparade 2010: Automatic video analysis of a crowd disaster. *Computer Vision and Image Understanding*, 116(3):307 – 319, 2012. Special issue on Semantic Understanding of Human Behaviors in Image Sequences.

[9] A. Kushki, K.N. Plataniotis, and A.N. Venetsanoploulos. *WLAN Positioning Systems: Principles and Applications in Location-Based Services*. Cambridge University Press, 2012.

[10] T. Li, H. Chang, M. Wang, B. Ni, R. Hong, and S. Yan. Crowded scene analysis: A survey. *IEEE Transactions on Circuits and Systems for Video Technology*, 25(3):367–386, March 2015.

[11] Dirk Oberhagemann. Static and dynamic crowd densities at major public events. Technical report, vfdb, Postfach 1231, 48338 Altenberge, March 2012.

[12] L. Schauer, M. Werner, and P. Marcus. Estimating crowd densities and pedestrian flows using wi-fi and bluetooth. In *11th International Conference on Mobile and Ubiquitous Systems: Computing, Networking and Services (MOBIQUITOUS 2014)*, 2014.

[13] D.W. Scott. *Multivariate Density Estimation.* New York: Wiley, 1992.

[14] B.W. Silverman. *Density Estimation for Statistics and Data Analysis.* London: Chapman and Hall, 1986.

[15] M. Versichele, T. Neutens, M. Delafontaine, and N. Van de Weghe. The use of bluetooth for analysing spatiotemporal dynamics of human movement at mass events: A case study of the ghent festivities. *Applied Geography*, 32:208–220, 2012.

[16] J. Weppner and P. Lukowicz. Bluetooth based collaborative crowd density estimation with mobile phones. In *IEEE International Conference on Pervasive Computing and Communications (PerCom)*, 2013.

[17] J. Weppner, P. Lukowicz, U. Blanke, and G. Tröster. Participatory bluetooth scans serving as urban crowd probes. *IEEE SENSORS JOURNAL*, 14(12), 2014.

[18] M. Wirz, T. Franke, D. Roggen, E. Mitleton-Kelly, P. Lukowicz, and G. Tröster. Probing crowd density through smartphones in city-scale mass gatherings. *EPJ Data Science*, 2(5), 2013.

[19] Y. Yoshimura, A. Krebs, and C. Ratti. An analysis of visitors' length of stay through noninvasive bluetooth monitoring in the louvre museum. arXiv:1605.00108, 2016.