#### 객체지향프로그래밍과 자료구조 (실습)

## Lab. 4 (보충설명) Class Mtrx and Class MtrxArray with Operator Overloading



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#### **Outline**

- ◆연산자 오버로딩
- class Mtrx with Operator Overloading
- class MtrxArray with Operator Overloading



## 연산자 오버로딩 (Operator Overloading)

- **♦** Operators +, -, %, ==,<<, >>, ^, ~ etc.
  - Really just functions!
- **♦** Simply "called" with different syntax: x + 7
  - "+" is binary operator with x and 7 as operands
  - We "like" this notation as humans
- ◆ Think of it as: +(x, 7)
  - "+" is the function name
  - x, 7 are the arguments
  - Function "+" returns "sum" of it's arguments

## 연산자 오버로딩

## **♦** *Built-in* operators

- e.g., +, -, = , %, ==, /, \*
- Already work for C++ built-in types
- In standard "binary" notation

#### **♦** We can overload them!

- To work with user-defined class/types!
- To add "Mtrx" types, or "Cmplx" types
  - As appropriate for our needs
  - In "notation" we're comfortable with

## **◆**Always overload with "similar actions"!

#### 연산자 오버로딩이 필요한 이유

#### ◆ 간략한 표현과 쉬운 이해

 using the usual mathematical operators, concise notations are possible

```
/* What you have use */

double mA[N][N], mB[N][N], mC[N][N],
 mD[N][N], mE[N][N], mF[N][N];

getMtrx(mA, N);
getMtrx(mB, N);

mtrxAdd(mA, mB, mC, N);
 mtrxSubtract(mA, mB, mD, N);
 mtrxMultiply(mA, mB, mE, N);
 mtrxInverse(mA, mF, N);
```

```
/* What can be possible with */
// Class definition for Mtrx
Mtrx mA, mB, mC, mD, mE, mInv;
cin >> mA;
cin >> mB;
mC = mA + mB;
mD = mA - mB;
mE = mA * mB;
mInv = \sim mA;
```

## Operators that can be Overloaded and that cannot be overloaded

**♦** Operators that can be overloaded

**♦** Operators that cannot be overloaded

. .\* :: ?:

## 연산자의 오버로딩 구현 (1)

## Overloading operators

- VERY similar to overloading functions
- Operator itself is "name" of function

#### **Example Declaration:**

```
const Cmplx operator +( const Cmplx & c1, const Cmplx & c2);
```

- Overloads + for operands of type Cmplx
- Uses constant reference parameters for efficiency
- Returned value is type Cmplx
  - Allows addition of "Cmplx" objects

## 연산자의 오버로딩 구현 (2)

#### ◆ 연산자 오버로딩 구현의 2가지 방법

- case 1: implementation as a non-member function
  - similar to usual function overloading
  - standalone function
  - operator overloading is not included in class definition
  - generally simple to implement
- case 2: implementation as a member function
  - operator overloading is included in class definition
  - principles suggest member operators, to maintain the "sprit" of objectoriented programming

#### "+" 연산자의 오버로딩

- **♦**Given previous example:
  - Note: overloaded "+" NOT member function
  - Definition is "more involved" than simple "add"
    - Requires issues of Cmplx type addition
    - Must handle negative/positive values
- **◆Operator overload definitions generally very simple** 
  - Just perform "addition" particular to "your" type

## Class Cmplx를 위한 "+" 연산자

◆ 개별적인 함수 오버로딩으로 연산자 오버로딩 구현

```
const Cmplx operator+(const Cmplx &c1, const Cmplx &c2)
{
    double real, imag;

    real = c1.real + c2.real;
    imag = c1.imag + c2.imag;

    return Cmplx(real, imag);
}
```

#### 클래스의 멤버함수로 연산자 오버로딩을 구현

- **♦**Cmplx c1(3, 4), c2(1, 2), c3; c3 = c1 + c2;
  - If "+" overloaded as member operator:
    - Variable/object cost is calling object
    - Object tax is single argument
  - Think of as: c3 = c1+(c2);
- **◆** Declaration of "+" in class definition (header file):
  - const Cmplx operator+(const Cmplx& c);
  - Notice only ONE argument



# class Cmplx with operator overloadings

#### **♦** Example Cmplx (1)

```
/** Cmplx.h */
#include <iostream>
using namespace std;
class Cmplx
{
        friend ostream & operator<< (ostream &, const Cmplx &);
        friend istream & operator>> (istream &, Cmplx &);
public:
        Cmplx(double real=0.0, double imag=0.0); // constructor
        const Cmplx operator+(const Cmplx &);
        const Cmplx operator-(const Cmplx &);
private:
        double real;
        double imag;
};
```

#### **♦** Example Cmplx (2)

```
/** Cmplx.cpp */
#include <iostream>
#include "Cmplx.h"
using namespace std;
Cmplx::Cmplx(double r, double i) :real(r), imag(i) { }
ostream &operator<<(ostream &output, const Cmplx &c)
         output << "Complex (" << c.real << ", " << c.imag << ")" << endl;
         return output;
istream & operator >> (istream & input, Cmplx &c)
         input >> c.real:
         input >> c.imag;
         return input;
```

#### **♦** Example Cmplx (3)

```
/* Cmplx.cpp (cont.) */
const Cmplx Cmplx::operator+(const Cmplx &c)
           Cmplx result;
           result.real = real + c.real;
result.imag = imag + c.imag;
           return result;
const Cmplx Cmplx::operator-(const Cmplx &c)
{
           Cmplx result;
           result.real = real - c.real;
result.imag = imag - c.imag;
           return result;
```

#### **♦** Example Cmplx (4)

#### <Result of Execution>

```
input c1.real and c1.imagin: 3.3 4.4
    main.cpp */
                                             c1 : Complex (3.3, 4.4)
#include <iostream>
                                             input c2.real and c2.imagin: 1.1 2.2
#include "Cmplx.h"
                                             c2 : Complex (1.1, 2.2)
using namespace std;
                                             c3 = c1 + c2: Complex (4.4, 6.6)
void main()
                                             c4 = c1 - c2: Complex (2.2, 2.2)
         Cmplx c1, c2, c3, c4;
         cout << "input c1.real and c1.imag: ";</pre>
        cin >> c1; cout << "c1 : " << c1 << endl;
         cout << "input c2.real and c2.imag: ";</pre>
         cin >> c2;
         cout << "c2 : " << c2 << endl;
        c3 = c1 + c2;
         cout << "c3 = c1 + c2: " << c3 << endl;
        c4 = c1 - c2;
        cout << "c4 = c1 - c2: " << c4 << endl;
```

#### **const Functions**

#### **♦**When to make function const?

- Constant functions not allowed to alter class member data
- Constant objects can ONLY call constant member functions
- **♦**Good style dictates:
  - Any member function that will NOT modify data should be made const
- ◆Use keyword const after function declaration and heading

## class Mtrx and class MtrxArray with operator overloadings

#### class Mtrx

```
/** Class Mtrx.h */
#ifndef MTRX H
#define MTRX H
#include <iostream>
#include <fstream>
using namespace std;
#define MAX SIZE 100
class Mtrx {
public:
   Mtrx(string nm, int num row, int num col);
   Mtrx(string nm, double dA[], int num row, int num col);
   Mtrx(istream& fin);
   ~Mtrx(); // destructor
   int getN_row() const { return n_row; }
   int getN col() const { return n col; }
   void fprintMtrx(ostream& fout);
   void setName(string nm) { name = nm;};
   string getName() { return name;};
   const Mtrx add(const Mtrx&);
   const Mtrx sub(const Mtrx&);
   const Mtrx multiply(const Mtrx&);
   const Mtrx transpose();
private:
   string name;
   int n row;
   int n col;
   double **dM;
```

#### class Mtrx 멤버함수 구현

```
/** Matrix.cpp (1) */
#include "Class Mtrx.h"
#include <iostream>
#include <iomanip>
using namespace std;
typedef double * DBLPTR;
Mtrx::Mtrx(string nm, int num_row, int num_col)
: name(nm), n row(num row), n col(num col)
   int i, j;
   //cout <<"Mtrx constructor (int size: "
          << size << ")\n";
   dM = new DBLPTR[n row];
   for (i=0; i<n_row; i++)
      dM[i] = new double[n_col];
   for (i=0; i< n row; i++) {
      for (j=0; j<n_col; j++) {
         dM[i][i] = 0.0;
   // cout <<"End of Mtrx constructor... \n";
```

```
/** Matrix.cpp (3) */
Mtrx::Mtrx(istream& fin)
   // DBLPTR *dM; /* defined in class, as private data member
   int i, j, size_row, size_col, num_data, cnt;
   double d;
   //cout <<"Mtrx constructor (double **dA, int size: " << size << ") \n";
   fin >> size row >> size col;
   n_row = size_row;
   n_col = size_col;
   dM = new DBLPTR[n row];
   for (i = 0; i < n_row; i++)
      dM[i] = new double[n_col];
   for (i = 0; i < n_row; i++) {
      for (j = 0; j < n_{col}; j++) {
          if (fin.eof())
              dM[i][j] = 0.0;
          else
             fin >> d;
              dM[i][j] = d;
   //cout <<"End of Mtrx constructor... \n";
```

```
Matrix.cpp (4) */
#define SETW 6
void Mtrx::fprintMtrx(ostream& fout)
    unsigned char a6 = 0xA6, a1 = 0xA1, a2 = 0xA2;
    unsigned char a3 = 0xA3, a4 = 0xA4, a5 = 0xA5;
    fout << name << endl;
    for (int i=0; i < n row; i++) {
       for (int j=0; j < n col; j++)
         fout.setf(ios::fixed);
         fout.precision(2);
         if ((i==0) \&\& (i==0))
            fout << a6 << a3 << setw(SETW) << dM[i][j];
         else if ((i==0) \&\& (j== (n\_col-1)))
            fout << setw(SETW) << dM[i][i] << a6 << a4;
         else if ((i>0) \&\& (i<(n_row-1)) \&\& (j==0))
            fout << a6 << a2 << setw(SETW) << dM[i][j];
         else if ((i>0) && (i<(n_row-1)) && (j==(n_col-1)))
            fout << setw(SETW) << dM[i][j] << a6 << a2;
         else if ((i==(n_row-1)) & (j==0))
            fout << a6 << a6 << setw(SETW) << dM[i][j];
         else if ((i==(n \text{ row}-1)) \&\& (j==(n \text{ col}-1)))
            fout << setw(SETW) << dM[i][i] << a6 << a5;
         else
            fout << setw(SETW) << dM[i][j];
       fout << endl;
    fout << endl;
```

출력 결과	확장 완성형 코드
	0xA6, 0xA1
	0xA6, 0xA2
Г	0xA6, 0xA3
٦	0xA6, 0xA4
	0xA6, 0xA5
L	0xA6, 0xA6

M	trxA =				
г	1.00	2.00	3.00	4.00	5.007
	2.00	3.00	4.00	5.00	1.00
	3.00	2.00	5.00	3.00	2.00
	4.00				
L	5.00	4.00	3.00	2.00	9.00

```
/** Matrix.cpp (5) */
const Mtrx Mtrx::add(const Mtrx& mA)
{
   int i, j;
   Mtrx mR("mR", n_row, n_col);
   for (i=0; i<n_row; i++) {
      for (j=0; j<n_col; j++) {
        mR.dM[i][j] = dM[i][j] + mA.dM[i][j];
      }
   }
   return mR;
}</pre>
```

```
/** Matrix.cpp (6) */
const Mtrx Mtrx::sub(const Mtrx& mA)
{
   int i, j;

   Mtrx mR("mR", n_row, n_col);

   for (i=0; i<n_row; i++) {
      for (j=0; j<n_col; j++) {
        mR.dM[i][j] = dM[i][j] - mA.dM[i][j];
      }
   }
   return mR;
}</pre>
```

```
Matrix.cpp (7) */
const Mtrx Mtrx::multiply(const Mtrx& mA)
  int i, j, k;
  Mtrx mR("mR", n_row, mA.n_col);
  for (i=0; i<n_row; i++) {
      for (j=0; j<mA.n_col; j++) {
          mR.dM[i][i] = 0.0;
          for (k=0; k<n_col; k++) {
            mR.dM[i][j] += dM[i][k] * mA.dM[k][j];
      }
   return mR;
```

```
/** Matrix.cpp (8) */
const Mtrx Mtrx::transpose()
{
   int i, j;

   Mtrx mR("mR", n_col, mA.n_row);

   for (i=0; i<n_row; i++) {
      for (j=0; j<mA.n_col; j++) {
        mR.dM[j][i] = dM[i][j];
      }
   }
   return mR;
}</pre>
```

## class Mtrx 응용 프로그램

```
/** main.c (1) */
#include <iostream>
#include <fstream>
#include "Class Mtrx.h"
using namespace std;
void main()
   ifstream fin;
   ofstream fout;
   fin.open("Matrix_5x5_data.txt");
   if (fin.fail())
     cout << "Error in opening Matrix_5x5_data.txt !!" << endl;</pre>
     exit;
   fout.open("output.txt");
   if (fout.fail())
     cout << "Error in opening Matrix_operations_results.txt !!" << endl;</pre>
     exit;
```

```
/** main.c (2) */
                                                          main.c (3) */
   Mtrx mtrxA(fin);
                                                          Mtrx mtrxE("", n_row, n_col);
   mtrxA.setName("MtrxA =");
                                                          mtrxE = mtrxA.multiply(mtrxB);
   fout <<" MtrxA:\n":
                                                          mtrxE.setName("MtrxC = mtrxA.multiply(mtrxB) =");
   mtrxA.fprintMtrx(fout);
                                                          mtrxE.fprintMtrx(fout);
   Mtrx mtrxB(fin);
                                                         fout.close();
   mtrxB.setName("MtrxB =");
                                                      } // end of main()
   fout <<" MtrxB:\n":
   mtrxB.fprintMtrx(fout);
                                                                                      MtrxA =
   int n row = mtrxA.getN row();
   int n col = mtrxB.getN col();
                                                                                      MtrxB =
                                                                 1.0 2.0 3.0 4.0 5.0
   Mtrx mtrxC("", n_row, n_col);
                                                                 2.0 3.0 4.0 5.0 1.0
   mtrxC = mtrxA.add(mtrxB);
                                                                 3.0 2.0 5.0 3.0 2.0
                                                                 4.0 3.0 2.0 7.0 2.0
   mtrxC.setName("MtrxC = mtrxA.add(mtrxB) =");
                                                                 5.0 4.0 3.0 2.0 9.0
   mtrxC.fprintMtrx(fout);
                                                                 5 5
                                                                 1.0 0.0 0.0 0.0 0.0
                                                                 0.0 1.0 0.0 0.0 0.0
                                                                 0.0 0.0 1.0 0.0 0.0
   Mtrx mtrxD("", n row, n col);
                                                                 0.0 0.0 0.0 1.0 0.0
   mtrxD = mtrxA.sub(mtrxB);
                                                                 0.0 0.0 0.0 0.0 1.0
   mtrxD.setName("MtrxD = mtrxA.sub(mtrxB) =");
```

```
1.00 2.00 3.00 4.00 5.00-
  2.00 3.00 4.00 5.00
  3.00 2.00 5.00 3.00 2.00
  4.00 3.00 2.00 7.00 2.00
       4.00 3.00 2.00
  1.00 0.00 0.00 0.00 0.00-
  0.00 1.00 0.00 0.00 0.00
 0.00 0.00 0.00 1.00 0.00
L 0.00 0.00 0.00 0.00
MtrxC = mtrxA.add(mtrxB) =
  2.00 2.00 3.00 4.00 5.00-
  2.00 4.00 4.00 5.00 1.00
  3.00 2.00 6.00 3.00
  4.00 3.00 2.00 8.00 2.00
MtrxD = mtrxA.sub(mtrxB) =
  0.00 2.00 3.00 4.00 5.00
  2.00 2.00 4.00 5.00 1.00
  3.00 2.00 4.00 3.00
  4.00 3.00 2.00 6.00 2.00
  5.00 4.00 3.00 2.00
MtrxE = mtrxA.multiplv(mtrxB) =
  1.00 2.00 3.00 4.00 5.007
  2.00 3.00 4.00 5.00 1.00
  3.00 2.00 5.00 3.00 2.00
  4.00 3.00 2.00 7.00 2.00
  5.00 4.00 3.00 2.00 9.00-
 mtrxA and mtrxE are same
```



mtrxD.fprintMtrx(fout);

(Input data)

#### class Mtrx와 연산자 오버로딩

```
/** Class Mtrx.h */
#define CLASS MTRX H
#define MAX SIZE 100
#include <string>
using namespace std;
class MtrxArray;
class Mtrx {
           friend ostream & operator << (ostream &, const Mtrx &);
           friend istream& operator>> (istream&, Mtrx&);
           friend class MtrxArray;
public:
           Mtrx(); // default constructor
           Mtrx(string nm, int n_row, int n_col);
           Mtrx(string nm, double *pA, int num row, int num col);
           ~Mtrx();
           void init(int n_row, int n_col);
           void set_name(string nm) { name = nm; }
           string get_name() const { return name; }
           int get_n_row() const { return n_row; }
           int get_n_col() const { return n_col; }
           const Mtrx operator+(const Mtrx&);
           const Mtrx operator-(const Mtrx&);
           const Mtrx operator*(const Mtrx&);
           const Mtrx operator~(); // transpose()
           const Mtrx& operator=(const Mtrx&);
bool operator==(const Mtrx&);
           bool operator!=(const Mtrx&);
private:
           string name;
           int n row;
           int n col;
           double *'*dM:
```

## class Mtrx를 위한 operator<<()

```
ostream& operator<<(ostream& fout, Mtrx& m)
    unsigned char a6 = 0xA6, a1 = 0xA1, a2 = 0xA2;
    unsigned char a3 = 0xA3, a4 = 0xA4, a5 = 0xA5;
    fout << m.get name() << endl;
    for (int i=0; i < n row; i++) {
        for (int j=0; j < n col; j++)
          fout.setf(ios::fixed);
          fout.precision(2);
          if ((i==0) \&\& (i==0))
            fout << a6 << a3 << setw(SETW) << m.dM[i][j];
          else if ((i==0) \&\& (j== (n col-1)))
            fout << setw(SETW) << m.dM[i][j] << a6 << a4;
          else if ((i>0) && (i<(n_row-1)) && (j==0))
             fout << a6 << a2 << setw(SETW) << m.dM[i][j];
          else if ((i>0) && (i<(n_row-1)) && (j==(n_col-1)))
            fout << setw(SETW) << m.dM[i][j] << a6 << a2;
          else if ((i==(n_row-1)) && (j==0))
             fout << a6 << a6 << setw(SETW) << m.dM[i][i];
          else if ((i==(n_row-1)) & (j==(n_col-1)))
            fout << setw(SETW) << m.dM[i][i] << a6 << a5;
          else
            fout << setw(SETW) << m.dM[i][j];
        fout << endl;
    fout << endl;
    return fout;
```

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	0xA6, 0xA1
	0xA6, 0xA2
Г	0xA6, 0xA3
٦	0xA6, 0xA4
	0xA6, 0xA5
L	0xA6, 0xA6

```
1.00 2.00 3.00 4.00
                      5.00-
2.00
    3.00 4.00 5.00
                     1.00
    2.00 5.00
3.00
               3.00
                      2.00
4.00
     3.00
          2.00
                7.00
                      2.00
5.00
     4.00
           3.00
                      9.004
```



## class Mtrx를 위한 operator+()

```
const Mtrx Mtrx::operator+(Mtrx& mA)
{
   int i, j;

   Mtrx mR("mR", n_row, n_col);

   for (i=0; i<n_row; i++) {
      for (j=0; j<n_col; j++) {
        mR.dM[i][j] = dM[i][j] + mA.dM[i][j];
      }
   }
}

return mR;
}</pre>
```

#### **class MtrxArray**

```
/* MtrxArray.h */
#ifndef MTRX_ARRAY_H
#define MTRX ARRAY H
#include <iostream>
#include "Mtrx.h"
using namespace std;
class Mtrx;
class MtrxArray
public:
     MtrxArray(int); // constructor
     ~MtrxArray(); // destructor
     Mtrx & operator[](int);
     int getSize() {return mtrxArrySize;}
private:
     Mtrx *pMtrx;
     int mtrxArrySize;
};
#endif
```

```
/** MtrxArray.cpp (1) */
#include "MtrxArray.h"
#include "Mtrx.h"
MtrxArray::MtrxArray(int arraySize) // constructor
      mtrxArrySize = arraySize;
      pMtrx = new Mtrx[arraySize];
MtrxArray::~MtrxArray()
      //cout << "MtrxArray :: destructor" << endl;
      if (pMtrx != NULL){
            delete[] pMtrx;
Mtrx &MtrxArray::operator [](int sub)
      if (sub < 0 || sub >= mtrxArrySize)
            cout << "ERROR: Subscript out of range.\\";
            exit(0);
      return pMtrx[sub];
```

## main()

```
/** main.cpp (1) */
#include <iostream>
#include <fstream>
#include <string>
#include "Mtrx.h"
#include "MtrxArray.h"
using namespace std;
#define NUM_MTRX 7
int main()
           ifstream fin;
           ofstream fout;
           int n_row, n_col;
           fin.open("Matrix_data.txt");
           if (fin.fail())
                       cout << "Error in opening input data file !!" << endl;
                       exit;
           fout.open("Result.txt");
           if (fout.fail())
                       cout << "Error in opening output data file !!" << endl;
                       exit;
            }
```

```
/** main.cpp (2) */
           MtrxArray mtrx(NUM MTRX);
           fin >> mtrx[0] >> mtrx[1] >> mtrx[2];
           mtrx[0].set_name("mtrx[0] =");
           mtrx[1].set_name("mtrx[1] =");
mtrx[2].set_name("mtrx[2] =");
           fout << mtrx[0] << endl;
           fout << mtrx[1] << endl;
           fout << mtrx[2] << end[:
           mtrx[3] = mtrx[0] + mtrx[1];
           mtrx[3].set_name("mtrx[3] = mtrx[0] + mtrx[1] = ");
           fout << mtrx[3] << end];
           mtrx[4] = mtrx[0] - mtrx[1];
           mtrx[4].set_name("mtrx[4] = mtrx[0] - mtrx[1] = ");
           fout << mtrx[4] << end];
           mtrx[5] = mtrx[0] * mtrx[2];
           mtrx[5].set_name("mtrx[5] = mtrx[0] * mtrx[2] = ");
           fout << mtrx[5] << end];
           mtrx[6] = \sim mtrx[5];
           mtrx[6].set_name("mtrx[6] = \sim mtrx[5] (transposed matrix) = ");
           fout << mtrx[6] << endl:
           if (mtrx[5] == mtrx[6])
                       fout << "mtrx[5] and mtrx[6] are equal.₩n";
           if (mtrx[5] != mtrx[6])
                       fout << "mtrx[5] and mtrx[6] are not equal.\foralln";
           fin.close();
           fout.close();
           return 0;
```



### input data file (Matrix\_data.txt)

```
1.0 2.0 3.0 4.0 5.0 6.0 7.0
2.0 3.0 4.0 5.0 1.0 7.0 8.0
3.0 2.0 5.0 3.0 2.0 4.0 6.0
4.0 3.0 2.0 7.0 2.0 1.0 9.0
5.0 4.0 3.0 2.0 9.0 6.0 9.0
1.0 0.0 0.0 0.0 0.0 1.0 2.0
0.0 1.0 0.0 0.0 0.0 2.0 3.0
0.0 0.0 1.0 0.0 0.0 3.0 4.0
0.0 0.0 0.0 1.0 0.0 4.0 5.0
0.0 0.0 0.0 0.0 1.0 5.0 6.0
1.0 2.0 3.0 4.0 5.0
6.0 7.0 2.0 3.0 4.0
5.0 1.0 7.0 8.0 3.0
2.0 5.0 3.0 2.0 4.0
6.0 4.0 3.0 2.0 7.0
2.0 1.0 9.0 5.0 4.0
3.0 2.0 9.0 6.0 9.0
```

#### 실행 결과

```
mtrx[0] =
                                                          mtrx[3] = mtrx[0] + mtrx[1] =
    1.00
                          4.00
                                 5.00
                                         6.00
                                                7.00-
           2.00
                   3.00
                                                                      2.00
                                                                             3.00
                                                                                     4.00
                                                                                            5.00
                                                                                                   7.00
                                                                                                           9.00-
                                         7.00
    2.00
           3.00
                  4.00
                          5.00
                                 1.00
                                                8.00
                                                               2.00
                                                                      4.00
                                                                             4.00
                                                                                     5.00
                                                                                            1.00
                                                                                                   9.00
                                                                                                         11.00
    3.00
           2.00
                   5.00
                          3.00
                                 2.00
                                         4.00
                                                6.00
                                                               3.00
                                                                      2.00
                                                                             6.00
                                                                                     3.00
                                                                                            2.00
                                                                                                   7.00
                                                                                                         10.00
                          7.00
                                 2.00
                                        1.00
                                                9.00
    4.00
           3.00
                  2.00
                                                                                                         14.00
                                                               4.00
                                                                      3.00
                                                                             2.00
                                                                                     8.00
                                                                                            2.00
                                                                                                   5.00
    5.00
           4.00
                  3.00
                          2.00
                                 9.00
                                         6.00
                                                9.00
                                                               5.00
                                                                      4.00
                                                                             3.00
                                                                                     2.00
                                                                                           10.00
                                                                                                  11.00
                                                                                                         15.00
mtrx[1] =
                                                          mtrx[4] = mtrx[0] - mtrx[1] =
                                                2.00-
                          0.00
                                 0.00
                                         1.00
    1.00
           0.00
                  0.00
                                                                      2.00
                                                                             3.00
                                                                                     4.00
                                                                                            5.00
                                                                                                   5.00
                                                                                                           5.00-
    0.00
                  0.00
                          0.00
                                 0.00
                                         2.00
                                                3.00
           1.00
                                                                      2.00
                                                                                                    5.00
                                                                                                           5.00
                                                               2.00
                                                                             4.00
                                                                                     5.00
                                                                                            1.00
                                 0.00
                                         3.00
                                                4.00
    0.00
           0.00
                  1.00
                          0.00
                                                               3.00
                                                                      2.00
                                                                             4.00
                                                                                     3.00
                                                                                            2.00
                                                                                                   1.00
                                                                                                           2.00
                                 0.00
                                                5.00
    0.00
           0.00
                  0.00
                          1.00
                                         4.00
                                                                      3.00
                                                                                                           4.00
                                                               4.00
                                                                             2.00
                                                                                     6.00
                                                                                            2.00
                                                                                                  -3.00
    0.00
           0.00
                  0.00
                          0.00
                                 1.00
                                         5.00
                                                6.00
                                                               5.00
                                                                      4.00
                                                                             3.00
                                                                                                   1.00
                                                                                                           3.00
                                                                                     2.00
                                                                                            8.00
mtrx[2] =
                                                          mtrx[5] = mtrx[0] * mtrx[2] =
    1.00
                          4.00
                                 5.00-
           2.00
                   3.00
                                                              99.00 79.00 172.00 124.00 160.007
    6.00
           7.00
                  2.00
                          3.00
                                 4.00
                                                              94.00 81.00 193.00 144.00 161.00
                          8.00
                                 3.00
    5.00
           1.00
                  7.00
                                                             84.00 64.00 153.00 124.00 134.00
    2.00
           5.00
                  3.00
                          2.00
                                 4.00
                                                             87.00 93.00 149.00 118.00 165.00
                          2.00
                                 7.00
    6.00
           4.00
                  3.00
                                                            141.00 111.00 212.00 162.00 226.00
                          5.00
                                 4.00
    2.00
           1.00
                  9.00
    3.00
           2.00
                   9.00
                          6.00
                                 9.00
                                                          mtrx[6] = ~mtrx[5] (transposed matrix) =
                                                              99.00 94.00 84.00 87.00 141.00-
                                                             79.00 81.00 64.00 93.00 111.00
                                                            172.00 193.00 153.00 149.00 212.00
                                                            124.00 144.00 124.00 118.00 162.00
                                                           L 160.00 161.00 134.00 165.00 226.00
                                                          mtrx[5] and mtrx[6] are not equal.
```

#### Lab. 4 Oral Test

- Q 4.1 C++ 프로그래밍에서 연산자 오버로딩 (operator overloading)의 필요성에 대하여 예를 들어 설명하라. (핵심포인트: 사용자 편의성)
- Q 4.2 C++ 클래스인 class Mtrx의 friend 함수로 operator<<()를 구현에서 call-by-reference, return-by-reference, const 를 사용하는 이유에 대하여 설명하라. (핵심 포인트: C++ 클래스에 대한 operator<<() 함수의 구현에서 call-by-reference, return-by-reference, const를 사용 이유, chained operation이 가능하도록 하기 위한 구조)
- Q 4.3 C++ 클래스인 class Mtrx의 멤버함수로 덧셈 계산을 위한 '+' 연산자의 operator overloading 함수를 구현하는 방법에 대하여 설명하라. (핵심포인트: 전달되는 인수, 내부 실행 절차, 결과의 반환)
- Q 4.4 C++ 클래스인 class Mtrx의 멤버함수로 대입연산을 위한 '=' 연산자의 operator overloading 함수를 구현하는 방법에 대하여 설명하라. (핵심포인트: 전달되는 인수, 내부 실행 절차, 결과의 반환)