

# Algoritmos y Estructuras de Datos II

Primer Cuatrimestre de 2015

Departamento de Computación  
Facultad de Ciencias Exactas y Naturales  
Universidad de Buenos Aires

## Trabajo Práctico 1

Especificación

Integrante	LU	Correo electrónico
BENITEZ, Nelson	945/13	nelson.benitez92@gmail.com
ROIZMAN, Violeta	273/11	violeroizman@gmail.com
VÍZQUEZ, Jásica	318/13	jesis_93@hotmail.com
ZAVALLA, Agustín	670/13	nkm747@gmail.com

Reservado para la cátedra

Instancia	Docente	Nota
Primera entrega		
Segunda entrega		

## Índice

# 1. TAD AS

## TAD AS

**géneros** as

**igualdad observacional**

$$(\forall facu, facu' : as) \left( facu =_{\text{obs}} facu' \iff \left( campus(facu) = campus(facu') \wedge seguridad(facu) = seguridad(facu') \right) \right)$$

**usa** CAMPUS

**exporta**

**observadores básicos**

campus : as  $\rightarrow$  campus

seguridad : as  $\rightarrow$  conj(seguridad)

hayEst? : as  $a \times$  pos  $p \rightarrow$  bool  $\{posValida(campus(a), p)\}$

hayHippie? : as  $a \times$  pos  $p \rightarrow$  bool  $\{posValida(campus(a), p)\}$

#capturas : as  $a \times$  seg  $s \rightarrow$  nat  $\{s \in seguridad(a)\}$

#sanciones : as  $a \times$  seg  $s \rightarrow$  nat  $\{s \in seguridad(a)\}$

**generadores**

nueva : campus  $\times$  conj(seguridad)  $\rightarrow$  as  
 $\{(\forall segs:e) posValida(c, pos(e)) \wedge (\forall segs:s, s1) id(s) \neq id(s1) \Rightarrow pos(s) \neq pos(s1)\}$

moverEst : as  $a \times$  pos  $pe \times$  pos  $pd \rightarrow$  as  
 $\left\{ \begin{array}{l} posValida(campus(a), pe) \wedge_L hayEst?(a, pe) \wedge adyacente(campus(a), pe, pd) \wedge \\ posValidaPersona(as, pd) \end{array} \right\}$

nuevoHippie : as  $a \times$  pos  $p \rightarrow$  as  $\{posIngreso(campus(a), p) \wedge posValidaPersona(a, p)\}$

nuevoEst : as  $a \times$  pos  $p \rightarrow$  as  $\{posIngreso(campus(a), p) \wedge posValidaPersona(a, p)\}$

sacarEst : as  $a \times$  pos  $p \rightarrow$  as  $\{posValida(campus(a), p) \wedge_L hayEst?(a, p) \wedge posIngreso(a, p)\}$

**otras operaciones**

haySeg? : as  $a \times$  pos  $p \rightarrow$  bool

posValidaPersona : as  $a \times$  pos  $p \rightarrow$  bool

posIngreso : as  $a \times$  pos  $p \rightarrow$  bool

moverTodos : as  $a \times$  conj(seguridad)  $segs \rightarrow$  conj(seguridad)

moverSeg : as  $a \times$  seguridad  $seg \times$  pos  $posSig \rightarrow$  seguridad

proxPoss : as  $a \times$  conj(pos)  $minPos \times$  pos  $posAct \rightarrow$  conj(pos)  
 $\{\neg(emptyset?(minPos)) \wedge_L posValida(campus(a), posAct) \wedge posicionesValidas(campus(a), minPos)\}$

proxPossHippies : as  $a \times$  conj(pos)  $poss \rightarrow$  conj(pos)  
 $\{(\forall poss:p) posValida(a, p) \wedge_L hayHippie?(a, p)\}$

estsCerca : as  $a \times$  pos  $p \rightarrow$  conj(pos)

hippieEncerrado? : as  $a \times$  pos  $p \rightarrow$  bool

hippieEncerradoEst? : as  $a \times$  pos  $p \times$  conj(pos)  $poss \rightarrow$  bool

hippieEncerradoSeg? : as  $a \times$  pos  $p \times$  conj(pos)  $poss \rightarrow$  bool

hippiesMasCerca : as  $a \times$  seguridad  $seg \rightarrow$  conj(pos)  $\{seg \in seguridad(a) \wedge hayHippies(a)\}$

encerrado : as  $a \times$  pos  $p \rightarrow$  bool  $\{hayEst?(p)\}$

#hippies : as  $a \rightarrow$  nat

```

#estudiantes : as  $a \rightarrow \text{nat}$ 
#masVigilante : as  $a \rightarrow \text{nat}$ 
contarHippies : as  $a \times \text{conj}(\text{pos}) \text{ poss} \rightarrow \text{nat}$ 
contarEstudiantes : as  $a \times \text{conj}(\text{pos}) \text{ poss} \rightarrow \text{nat}$ 
#masCapturas : as  $a \times \text{conj}(\text{seg}) \text{ segs} \rightarrow \text{conj}(\text{seg})$   $\{(\forall \text{ segs:s}) s \in \text{seguridad}(a)\}$ 
#maxCapturas : as  $a \times \text{conj}(\text{seg}) \text{ segs} \rightarrow \text{nat}$   $\{(\forall \text{ segs:s}) s \in \text{seguridad}(a)\}$ 
captura? : as  $a \times \text{pos } p \rightarrow \text{bool}$ 

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**axiomas**

```

campus(nueva( $c, \text{segs}$ ))  $\equiv c$ 
campus(moverEst( $a, p_1, p_2$ ))  $\equiv \text{campus}(a)$ 
campus(nuevoEst( $a, p_1$ ))  $\equiv \text{campus}(a)$ 
campus(nuevoHippie( $a, p_1$ ))  $\equiv \text{campus}(a)$ 
campus(sacarEst( $a, p_1$ ))  $\equiv \text{campus}(a)$ 
seguridad(nueva( $c, \text{segs}$ ))  $\equiv \text{segs}$ 
seguridad(moverEst( $a, p_1, p_2$ ))  $\equiv \text{moverTodos}(a, \text{seguridad}(a))$ 
seguridad(nuevoEst( $a, p_1$ ))  $\equiv \text{moverTodos}(a, \text{seguridad}(a))$ 
seguridad(nuevoHippie( $a, p_1$ ))  $\equiv \text{seguridad}(a)$ 
seguridad(sacarEst( $a, p_1$ ))  $\equiv \text{seguridad}(a)$ 
hayEst?(nueva( $c, \text{segs}$ ),  $p$ )  $\equiv \text{False}$ 
hayEst?(nuevoEst( $a, p_1$ ),  $p$ )  $\equiv \text{if } p_1 = p \text{ then True else hayEst?}(a, p) \text{ fi}$ 
hayEst?(moverEst( $a, p_1, p_2$ ),  $p$ )  $\equiv \text{if } p_1 = p \text{ then False else if } p_2 = p \text{ then True else hayEst?}(a, p) \text{ fi}$ 
hayEst?(nuevoHippie( $a, p_1$ ),  $p$ )  $\equiv \text{hayEst?}(a, p)$ 
hayEst?(sacarEst( $a, p_1$ ),  $p$ )  $\equiv \text{if } p_1 = p \text{ then False else hayEst?}(a, p) \text{ fi}$ 
hayHippie?(nueva( $c, \text{segs}$ ),  $p$ )  $\equiv \text{False}$ 
hayHippie?((nuevoHippie( $a, p_1$ ),  $p$ ))  $\equiv \text{if } p_1 = p \text{ then True else hayHippie?}(a, p) \text{ fi}$ 
hayHippie?((moverEst( $a, p_0, p_1$ ),  $p$ ))  $\equiv \text{if hayHippie?}(a, p) \text{ then if } \neg(\text{hippieEncerrado?}(a, p)) \text{ then } p \in \text{proxPossHippies}(a, \text{possHippies}(a)) \text{ else False fi else if hayEst?}(a, p) \text{ then estEncerradoPorHippies}(a, p) \text{ else } p \in \text{proxPossHippies}(a, \text{possHippies}(a)) \text{ fi fi}$ 
hayHippie?(nuevoEst( $a, p_1$ ),  $p$ )  $\equiv \text{hayHippie?}(a, p)$ 
hayHippie?(sacarEst( $a, p_1$ ),  $p$ )  $\equiv \text{hayHippie?}(a, p)$ 
#capturas(nueva( $a, \text{segs}$ ),  $s$ )  $\equiv 0$ 
#capturas(moverEst( $a, p_1, p_2$ ),  $s$ )  $\equiv \#capturas(a, s)$ 

```

$\#capturas(nuevoHippie(a, p_1), s)$	$\equiv$	<b>if</b> ( $adyacente(a, p_1, posSeg(a, s)) \wedge encerrado(a, p_1)$ ) <b>then</b> $1 + \#capturas(a, s)$ <b>else</b> $\#capturas(a, s)$ <b>fi</b>
$\#capturas(nuevoEst(a, p_1), s)$	$\equiv$	$\#capturas(a, s)$
$\#capturas(sacarEst(a, p_1), s)$	$\equiv$	$\#capturas(a, s)$

```

#capturas(moverEst(a, p1, p2), s)
≡ if (PosValida(campus(a), < π1(posSeg) + 1, π2(posSeg) >))
  then
    if (hayHippie(a, < π1(posSeg) + 1, π2(posSeg) >)) then
      if (captura?(a, < π1(posSeg) + 1, π2(posSeg) >)) then
        1
      else
        0
    fi
  else
    0
  fi
else
  0
fi

+

if (PosValida(campus(a), < π1(posSeg) - 1, π2(posSeg) >))
then
  if (hayHippie(a, < π1(posSeg) - 1, π2(posSeg) >)) then
    if (captura?(a, < π1(posSeg) - 1, π2(posSeg) >)) then
      1
    else
      0
    fi
  else
    0
  fi
else
  0
fi

+

if (PosValida(campus(a), < π1(posSeg), π2(posSeg) + 1 >))
then
  if (hayHippie(a, < π1(posSeg), π2(posSeg) + 1 >)) then
    if (captura?(a, < π1(posSeg), π2(posSeg) + 1 >)) then
      1
    else
      0
    fi
  else
    0
  fi
else
  0
fi

+

if (PosValida(campus(a), < π1(posSeg), π2(posSeg) - 1 >))
then
  if (hayHippie(a, < π1(posSeg), π2(posSeg) - 1 >)) then
    if (captura?(a, < π1(posSeg), π2(posSeg) - 1 >)) then
      1
    else
      0
    fi
  else
    0
  fi
else
  0
fi

+ #capturas(a, s)

```

#sanciones(nueva(a, segs),s)	≡ 0
#sanciones(moverEst(a, p <sub>1</sub> , p <sub>2</sub> ),s)	≡ #sanciones(a, s)
#sanciones(nuevoHippie(a, p <sub>1</sub> ),s)	≡ <b>if</b> (cercanos?(a, p <sub>1</sub> , posSeg(a, s)) <span style="float: right;">∧<sub>L</sub></span> (hayEst?(casilleroEnComun(a, p <sub>1</sub> , posSeg(a, s))) <span style="float: right;">∧</span> encerrado(casilleroEnComun(a, p <sub>1</sub> , posSeg(a, s)))) <b>then</b> 1 + #sanciones(a, s) <b>else</b> #sanciones(a, s) <b>fi</b>
#sanciones(nuevoEst(a, p <sub>1</sub> ),s)	≡ #sanciones(a, s)
#sanciones(sacarEst(a, p <sub>1</sub> ),s)	≡ #sanciones(a, s)
#sanciones(a,moverSeg(a, s, p <sub>1</sub> ))	≡ β(posValida(campus(a), < π <sub>1</sub> (p <sub>1</sub> )+1, π <sub>2</sub> (p <sub>1</sub> ) >) ∧ <sub>L</sub> (hayEst?(a, < π <sub>1</sub> (p <sub>1</sub> ) + 1, π <sub>2</sub> (p <sub>1</sub> ) >) ∧ <sub>L</sub> encerrado(a, < π <sub>1</sub> (p <sub>1</sub> ) + 1, π <sub>2</sub> (p <sub>1</sub> ) >))) + β(posValida(campus(a), < π <sub>1</sub> (p <sub>1</sub> )-1, π <sub>2</sub> (p <sub>1</sub> ) >) ∧ <sub>L</sub> (hayEst?(a, < π <sub>1</sub> (p <sub>1</sub> ) - 1, π <sub>2</sub> (p <sub>1</sub> ) >) ∧ <sub>L</sub> encerrado(a, < π <sub>1</sub> (p <sub>1</sub> ) - 1, π <sub>2</sub> (p <sub>1</sub> ) >))) + β(posValida(campus(a), < π <sub>1</sub> (p <sub>1</sub> ), π <sub>2</sub> (p <sub>1</sub> )+1 >) ∧ <sub>L</sub> (hayEst?(a, < π <sub>1</sub> (p <sub>1</sub> ), π <sub>2</sub> (p <sub>1</sub> ) + 1 >) ∧ <sub>L</sub> encerrado(a, < π <sub>1</sub> (p <sub>1</sub> ), π <sub>2</sub> (p <sub>1</sub> ) + 1 >))) + β(posValida(campus(a), < π <sub>1</sub> (p <sub>1</sub> ), π <sub>2</sub> (p <sub>1</sub> )-1 >) ∧ <sub>L</sub> (hayEst?(a, < π <sub>1</sub> (p <sub>1</sub> ), π <sub>2</sub> (p <sub>1</sub> ) - 1 >) ∧ <sub>L</sub> encerrado(a, < π <sub>1</sub> (p <sub>1</sub> ), π <sub>2</sub> (p <sub>1</sub> ) - 1 >))) + #sanciones(a, s)
moverTodos(a,segs)	≡ <b>if</b> (∅?(segs)) <b>then</b> ∅ <b>else</b> <b>if</b> (hayHippies?(a)) <b>then</b> Ag(moverTodos(a, sinUno(segs)), moverSeg(a, dameUno(segs), dameUno(proxPoss(hippiesMasCerca(a, dameUno(segs)))))) <b>else</b> moverIngreso(a, segs) <b>fi</b> <b>fi</b>
moverIngreso(a,segs)	≡ <b>if</b> ∅?(segs) <b>then</b> ∅ <b>else</b> <b>if</b> (alto(campus(a)) - 1) - π <sub>2</sub> (dameUno(segs)) > π <sub>2</sub> (dameUno(segs)) <b>then</b> ag(moverIngreso(a, sinUno(segs)), mover(dameUno(segs), < (π <sub>1</sub> (dameUno(segs)), π <sub>2</sub> (segs) - 1) >)) <b>else</b> <b>if</b> (alto(campus(a)) - 1) - π <sub>2</sub> (dameUno(segs)) < π <sub>2</sub> (dameUno(segs)) <b>then</b> ag(moverIngreso(a, sinUno(segs)), mover(dameUno(segs), < (π <sub>1</sub> (dameUno(segs)), π <sub>2</sub> (segs) + 1) >)) <b>else</b> ag(moverIngreso(a, sinUno(segs)), mover(dameUno(segs), dameUno({< (π <sub>1</sub> (dameUno(segs)), π <sub>2</sub> (segs) - 1) >, < (π <sub>1</sub> (dameUno(segs)), π <sub>2</sub> (segs) + 1) >}))) <b>fi</b> <b>fi</b> <b>fi</b>

proxPoss(entCerca, p)

```

≡ if  $\emptyset?(entCerca)$  then
     $\emptyset$ 
else
    if  $\pi_1(dameUno(entCerca)) > \pi_1(p)$  then
        if  $\pi_2(dameUno(entCerca)) > \pi_2(pos)$  then
            if  $\emptyset?(validas(a, \{< \pi_1(pos) + 1, \pi_2(p) > < \pi_1(p), \pi_2(p) + 1 > \}))$ 
            then
                proxPoss(sinUno(entCerca), p)
            else
                Ag(proxPoss(sinUno(entCerca), p), dameUno(validas
                    (a,  $\{< \pi_1(p) + 1, \pi_2(p) > < \pi_1(p), \pi_2(p) + 1 > \}$ )))
            fi
        else
            if  $\pi_2(dameUno(entCerca)) < \pi_2(p)$  then
                if  $\emptyset?(validas(a, \{< \pi_1(p) + 1, \pi_2(p) > < \pi_1(p), \pi_2(p) - 1 > \}))$ 
                then
                    proxPoss(sinUno(entCerca), p)
                else
                    Ag(proxPoss(sinUno(entCerca), p), dameUno(validas
                        (a,  $\{< \pi_1(p) + 1, \pi_2(p) > < \pi_1(p), \pi_2(p) - 1 > \}$ )))
                    fi
                else
                    if  $\emptyset?(validas(a, \{< \pi_1(p) + 1, \pi_2(p) > \}))$  then
                        proxPoss(sinUno(entCerca), p)
                    else
                        Ag(proxPoss(sinUno(entCerca), p), dameUno(validas
                            (a,  $\{< \pi_1(p) + 1, \pi_2(p) > \}$ )))
                        fi
                    fi
                fi
            fi
        else
            if  $\pi_1(dameUno(hscerca)) < \pi_1(p)$  then
                if  $\pi_2(dameUno(hscerca)) > \pi_2(p)$  then
                    if  $\emptyset?(validas(a, \{< \pi_1(p) - 1, \pi_2(p) > < \pi_1(p), \pi_2(p) + 1 > \}))$ 
                    then
                        proxPoss(sinUno(entCerca), p)
                    else
                        Ag(proxPoss(sinUno(entCerca), p), dameUno(validas
                            (a,  $\{< \pi_1(p) - 1, \pi_2(p) > < \pi_1(p), \pi_2(p) + 1 > \}$ )))
                        fi
                    else
                        if  $\emptyset?(validas(a, \{< \pi_1(p) - 1, \pi_2(p) > < \pi_1(p), \pi_2(p) - 1 > \}))$ 
                        then
                            proxPoss(sinUno(entCerca), p)
                        else
                            Ag(proxPoss(sinUno(entCerca), p), dameUno(validas
                                (a,  $\{< \pi_1(p) - 1, \pi_2(p) > < \pi_1(p), \pi_2(p) - 1 > \}$ )))
                                fi
                            fi
                        fi
                    fi
                else
                    if  $\pi_2(dameUno(hscerca)) > \pi_2(p)$  then
                        if  $\emptyset?(validas(a, \{< \pi_1(p), \pi_2(p) + 1 > \}))$  then
                            proxPoss(sinUno(entCerca), p)
                        else
                            Ag(proxPoss(sinUno(entCerca), p),
                                dameUno(validas(a,  $\{< \pi_1(p), \pi_2(p) + 1 > \}$ )))
                            fi
                        else
                            if  $\emptyset?(validas(a, \{< \pi_1(p), \pi_2(p) - 1 > \}))$  then
                                proxPoss(sinUno(entCerca), p)
                            else
                                Ag(proxPoss(sinUno(entCerca), p),
                                    dameUno(validas(a,  $\{< \pi_1(p), \pi_2(p) - 1 > \}$ )))
                                    fi
                                fi
                            fi
                        fi
                    fi
                fi
            fi
        fi
    fi

```



$validas(a, poss)$	$\equiv$ <b>if</b> $\emptyset?(poss)$ <b>then</b> $\emptyset$ <b>else</b> <b>if</b> $posValida(dameUno(poss)) \wedge$ $\neg(hayHippie?(a, dameUno(poss))) \wedge$ $\neg(hayEst?(a, dameUno(poss)))$ $\neg(haySeg?(a, dameUno(poss)))$ <b>then</b> $Ag(validas(a, sinUno(poss)), dameUno(poss))$ <b>else</b> $validas(a, sinUno(poss))$ <b>fi</b> <b>fi</b>	
$hippieEncerrado?(a, p)$	$\equiv$ $hipEncerradoEst?(a, p, adjacentes(campus(a), p))$ $hipEncerradoSeg?(a, p, adjacentes(campus(a), p))$	$\wedge$
$hipEncerradoEst?(a, p, adys)$	$\equiv$ <b>if</b> $\emptyset?(adys)$ <b>then</b> $True$ <b>else</b> <b>if</b> $posValida?(campus(a), dameUno(adys))$ <b>then</b> $hayEst?(a, p) \wedge hipEncerradoEst?(a, p, sinUno(adys))$ <b>else</b> $False$ <b>fi</b> <b>fi</b>	
$hipEncerradoSeg?(a, p, adys)$	$\equiv$ <b>if</b> $\emptyset?(adys)$ <b>then</b> $True$ <b>else</b> <b>if</b> $posValida?(campus(a), dameUno(adys))$ <b>then</b> $haySeg?(a, p) \wedge hipEncerradoSeg?(a, p, sinUno(adys))$ <b>else</b> $False$ <b>fi</b> <b>fi</b>	
$moverSeg(a, seg, nPos)$	$\equiv$ <b>if</b> $(distMan(campus(a), \pi_2(seg), nPos) \geq 2$ $\vee \neg(posValida(campus(a), nPos)))$ <b>then</b> $seg$ <b>else</b> <b>if</b> $\#sanciones(a, seg) < 3$ <b>then</b> $< \pi_1(seg), nPos >$ <b>else</b> $seg$ <b>fi</b> <b>fi</b>	
$proxPossHippies(a, possHippies)$	$\equiv$ <b>if</b> $\emptyset?(possHippies)$ <b>then</b> $\emptyset$ <b>else</b> $proxPoss(a, estsCerca(dameUno(possHippies), dameUno(possHippies))$ $proxPossHippies(a, sinUno(possHippies))$ <b>fi</b>	
$hippiesMasCerca(a, seg)$	$\equiv$ $minDistsPos(campus(a), \pi_2(seg), posHippies(a))$	
$\#hippies(a)$	$\equiv$ $contarHippies(a, conjPos(campus(a), 0, 0))$	
$\#estudiantes(a)$	$\equiv$ $contarEstudiantes(a, conjPos(campus(a), 0, 0))$	

```

contarHippies(a,poss)
≡ if ¬(∅?(poss)) then
    if posValida(campus(a), dameUno(poss)) then
        if hayHippie(a, dameUno(poss)) then
            1 + contarHippies(a, sinUno(poss))
        else
            contarHippies(a, sinUno(poss))
    fi
else
    contarHippies(a, sinUno(poss))
fi
else
    0
fi

contarEstudiantes(a,poss)
≡ if ¬(∅?(poss)) then
    if posValida(campus(a), dameUno(poss)) then
        if hayEst?(a, dameUno(poss)) then
            1 + contarEstudiantes(a, sinUno(poss))
        else
            contarEstudiantes(a, sinUno(poss))
    fi
else
    contarEstudiantes(a, sinUno(poss))
fi
else
    0
fi

masVigilante(a)
≡ dameUno(masCapturas(a, seguridad(a)))

masCapturas(a,segs)
≡ if ¬(∅?(segs)) then
    if #capturas(a, dameUno(segs)) ≥ maxCapturas(a, segs)
    then
        ag(masCapturas(a, sinUno(segs)), dameUno(segs))
    else
        masCapturas(a, sinUno(segs))
    fi
else
    ∅
fi

maxCapturas(a,segs)
≡ if ∅?(segs) then
    0
else
    if #capturas(a, dameUno(segs)) ≥
        maxCapturas(a, sinUno(segs))
    then
        #capturas(a, dameUno(segs))
    else
        maxCapturas(a, sinUno(segs))
    fi
fi

```

```

captura?(a, p)
≡ if (posValida(campus(a), < π1(p) + 1, π2(p) >) then
    (hayObstaculo?(campus(a), < π1(p) + 1, π2(p) >)
    ) ∨ haySeg?(a, < π1(p) + 1, π2(p) >))
else
    ¬(hayEst?(a, < π1(p), π2(p) >))
fi
∧
if (posValida(campus(a), < π1(p) - 1, π2(p) >) then
    (hayObstaculo?(campus(a), < π1(p) - 1, π2(p) >)
    ) ∨ haySeg?(a, < π1(p) - 1, π2(p) >))
else
    ¬(hayEst?(a, < π1(p), π2(p) >))
fi
∧
if (posValida(campus(a), < π1(p), π2(p) + 1 >) then
    (hayObstaculo?(campus(a), < π1(p), π2(p) + 1 >)
    ) ∨ haySeg?(a, < π1(p), π2(p) + 1 >))
else
    True
fi
∧
if (posValida(campus(a), < π1(p), π2(p) - 1 >) then
    (hayObstaculo?(campus(a), < π1(p), π2(p) - 1 >)
    ) ∨ haySeg?(a, < π1(p), π2(p) - 1 >))
else
    True
fi
fi

```

Fin TAD

## 2. TAD CAMPUS

TAD CAMPUS

**géneros**      campus

**usa**            CAMPUS

**exporta**

**observadores básicos**

alto : campus → nat

ancho : campus → nat

obstaculos : campus → conj(pos)

**generadores**

nuevo : nat ancho × nat alto × conj(pos) obst → campus  
 $\{1 \leq ancho \wedge 1 \leq alto \wedge (\forall p:pos) p \in obst \Rightarrow_L posValida(c, p)\}$

**otras operaciones**

adyacente : as  $a \times pos\ pe \times pos\ pd \rightarrow bool$        $\{posValida(c, pe) \wedge posValida(c, pd)\}$

posValida : as  $a \times pos\ p \rightarrow bool$

posIngreso : as  $a \times pos\ p \rightarrow bool$

minDistsPos : campus  $c \times pos\ p \times conj(pos)\ posiciones \rightarrow conj(pos)$        $\{\neg(\emptyset?(posiciones))\}$

minDist : campus  $c \times pos\ p \times conj(posiciones)\ posiciones \rightarrow nat$        $\{\neg(\emptyset?(posiciones))\}$

$\text{distMan} : \text{campus } c \times \text{pos } p1 \times \text{pos } p2 \longrightarrow \text{nat}$

$\text{restaAbs} : \text{nat} \times \text{nat} \longrightarrow \text{nat}$

$\text{conjPos} : \text{campus} \times \text{nat} \times \text{nat} \longrightarrow \text{conj}(\text{pos})$

$\text{adyacentes} : \text{campus} \times \text{pos} \longrightarrow \text{conj}(\text{pos})$

**axiomas**  $\forall \text{alto}:\text{nat}, \forall \text{ancho}:\text{nat}, \forall \text{obst}:\text{conj}(\text{pos})$   
 $\forall p_1:\text{pos} \forall p_2:\text{pos}$

$\text{alto}(\text{nuevo}(\text{ancho}, \text{alto}, \text{obst}))$

$\equiv \text{alto}$

$\text{ancho}(\text{nuevo}(\text{ancho}, \text{alto}, \text{obst}))$

$\equiv \text{ancho}$

$\text{obstaculos}(\text{nuevo}(\text{ancho}, \text{alto}, \text{obst}))$

$\equiv \text{obst}$

$\text{posValida}(\text{nuevo}(\text{ancho}, \text{alto}, \text{obst}), p_1)$

$\equiv \pi_1(p_1) < \text{ancho} \wedge \pi_2(p_1) < \text{alto}$

$\text{adyacente}(\text{nuevo}(\text{ancho}, \text{alto}, \text{obst}), p_1, p_2)$

$\equiv (\pi_1(p_1) = \pi_1(p_2) - 1 \vee \pi_1(p_1) = \pi_1(p_2) + 1) \wedge$   
 $(\pi_2(p_1) = \pi_2(p_2) - 1 \vee \pi_2(p_1) = \pi_2(p_2) + 1)$

$\text{posValida}(\text{nuevo}(\text{ancho}, \text{alto}, \text{obst}), p_1)$

$\equiv \pi_2(p_1) = \text{alto} - 1 \vee \pi_2(p_1) = 0$

$\text{minDistsPos}(c, p, \text{posiciones})$

$\equiv \text{if } \emptyset?(\text{sinUno}(\text{posiciones})) \text{ then}$   
 $\quad \text{dameUno}(\text{posiciones})$   
 $\text{else}$   
 $\quad \text{if } \text{distMan}(c, p, \text{dameUno}(\text{posiciones})) \leq$   
 $\quad \text{minDist}(c, p, \text{posiciones}) \text{ then}$   
 $\quad \quad \text{Ag}(\text{minDistsPos}(c, \text{sinUno}(\text{posiciones})),$   
 $\quad \quad \text{dameUno}(\text{posiciones}))$   
 $\quad \text{else}$   
 $\quad \quad \text{minDistsPos}(c, \text{seg}, \text{sinUno}(\text{posiciones}))$   
 $\quad \text{fi}$   
 $\text{fi}$

$\text{minDist}(c, p, \text{posiciones})$

$\equiv \text{if } \emptyset?(\text{sinUno}(\text{posiciones})) \text{ then}$   
 $\quad \text{distMan}(c, p, \text{dameUno}(\text{posiciones}))$   
 $\text{else}$   
 $\quad \text{if } \text{distMan}(c, p, \text{dameUno}(\text{posiciones})) \leq$   
 $\quad \text{minDist}(c, \text{pos}/p, \text{sinUno}(\text{posiciones}))$   
 $\quad \text{then}$   
 $\quad \quad \text{distMan}(c, p, \text{dameUno}(\text{posiciones}))$   
 $\quad \text{else}$   
 $\quad \quad \text{minDist}(c, p, \text{sinUno}(\text{posiciones}))$   
 $\quad \text{fi}$   
 $\text{fi}$

$\text{distMan}(c, p_1, p_2)$

$\equiv \text{restaAbs}(\pi_2(p_1), \pi_2(p_2)) + \text{restaAbs}(\pi_1(p_1), \pi_1(p_2))$

$\text{restaAbs}(n1, n2)$

$\equiv \text{if } n2 > n1 \text{ then } n2 - n1 \text{ else } n1 - n2 \text{ fi}$

$\text{conjPos}(c, x, y)$

$\equiv \text{if } x \geq \text{ancho}(c) \text{ then}$   
 $\quad \emptyset$   
 $\text{else}$   
 $\quad \text{if } y \geq \text{alto}(c) \text{ then}$   
 $\quad \quad \text{conjPos}(c, x + 1, 0)$   
 $\quad \text{else}$   
 $\quad \quad \text{ag}(\text{conjPos}(c, x, y + 1), \langle x, y \rangle)$   
 $\quad \text{fi}$   
 $\text{fi}$

$\text{adyacentes}(\text{campus}, p)$

$\equiv \{ \langle \pi_1(p) + 1, \pi_2(p) + 1 \rangle, \langle \pi_1(p) - 1, \pi_2(p) - 1 \rangle, \langle \pi_1(p) + 1, \pi_2(p) \rangle, \langle \pi_1(p), \pi_2(p) + 1 \rangle \}$

**Fin TAD**