

1. For  $x > 0$ ,  $e^{-\ln x}$  may be expressed as

- (A)  $\ln \frac{1}{x}$   
 (B)  $-\ln x$   
 (C)  $-x$   
 (D)  $\frac{1}{x}$

2.  $\frac{x+5}{x(x^2+6x+17)}$  may be expressed as

- (A)  $\frac{P}{x} + \frac{Q}{(x-1)} + \frac{R}{x+17}$   
 (B)  $\frac{P}{x} + \frac{Qx+R}{(x-1)(x+17)}$   
 (C)  $\frac{P}{x} + \frac{Qx+R}{x^2+6x+17}$   
 (D)  $\frac{P}{x} + \frac{Qx}{x^2+6x+17}$

3. Given that  $a$ ,  $b$ ,  $c$  and  $k$  are constants, then

$\int \frac{3}{x^2(x-1)} dx$  can be expressed as

- (A)  $\frac{a}{x} + b \ln |x-1| + k$   
 (B)  $a \ln |x| + b \ln |x-1| + k$   
 (C)  $a \ln |x| + \frac{b}{x} + \frac{c}{x-1} + k$   
 (D)  $a \ln |x| + \frac{b}{x} + c \ln |x-1| + k$

4.  $\int (\cos 5x \cos 3x) dx =$

- (A)  $\frac{1}{2} \int (\cos 8x + \cos 2x) dx$   
 (B)  $\frac{1}{2} \int (\cos 8x - \cos 2x) dx$   
 (C)  $\int (\cos 8x - \cos 2x) dx$   
 (D)  $\int (\cos 8x + \cos 2x) dx$

5. The general solution for the second-order differential equation  $\frac{d^2 y}{dx^2} - 3 \frac{dy}{dx} + 2y = 0$  is

- (A)  $y = Ae^{2x} + x Be^x$   
 (B)  $y = Ae^{2x} + Be^x$   
 (C)  $y = e^x (A + Bx)$   
 (D)  $y = e^{2x} (A + Bx)$

6. If  $x = \log_a m$ , then  $\log_m \frac{a^5}{m} =$

- (A)  $\frac{1}{x^5} - 1$   
 (B)  $\frac{5}{x} - 1$   
 (C)  $5x - 1$   
 (D)  $x^5 - 1$

7.  $\frac{d}{dx} \sin^{-1}(2x)$  is equal to

- (A)  $\sqrt{1-4x^2}$   
 (B)  $2\sqrt{1-4x^2}$   
 (C)  $\frac{2}{\sqrt{1-4x^2}}$   
 (D)  $\frac{1}{\sqrt{1-4x^2}}$

8. Given  $\sec^2 x = 1 + \tan^2 x$ ,  $\int_0^{\pi} \frac{\tan^2 x}{4} dx$  is

- (A)  $-\frac{\pi}{4}$
- (B)  $\frac{\pi}{4}$
- (C)  $\frac{\pi}{4} - 1$
- (D)  $1 - \frac{\pi}{4}$

9.  $\int \frac{dx}{\sqrt{16-x^2}}$  is

- (A)  $\frac{1}{16} \sin^{-1} \frac{x}{4} + c$
- (B)  $\frac{1}{4} \sin^{-1} \frac{x}{4} + c$
- (C)  $\sin^{-1} \frac{x}{4} + c$
- (D)  $\sin^{-1} 4x + c$

10.  $\int \frac{1}{1+9x^2} dx$  is

- (A)  $\frac{1}{3} \tan^{-1} \left( \frac{x}{3} \right) + c$
- (B)  $\frac{1}{3} \tan^{-1} (3x) + c$
- (C)  $3 \tan^{-1} \left( \frac{x}{3} \right) + c$
- (D)  $3 \tan^{-1} (3x) + c$

11. If  $\frac{dy}{dx} = 2xy$ , then the value of  $\frac{d^2y}{dx^2}$  at the point (1, 2) is

- (A) 6
- (B) 8
- (C) 12
- (D) 16

12.  $\int \sin^2 x dx =$

- (A)  $\frac{1}{3} \sin^3 x + c$
- (B)  $\frac{1}{3} \cos^3 x + c$
- (C)  $\frac{1}{2} x + \frac{1}{4} \sin 2x + c$
- (D)  $\frac{1}{2} x - \frac{1}{4} \sin 2x + c$

13. A function  $f$  is defined by  $f(x) = 2e^{3x} - 1$  for all real values of  $x$ . The inverse function,  $f^{-1}$  of  $f$ , is defined by

- (A)  $3 \ln(x+1), x \in R$
- (B)  $\frac{1}{3} \ln(x+1), x \in R$
- (C)  $\frac{1}{3} \ln \left( \frac{x+1}{2} \right), x > -1$
- (D)  $\frac{1}{3} \ln \left( \frac{x+1}{2} \right), x \in R$

14. If  $\log_{10} 2 = x$ , then  $\log_{10} 0.128$ , in terms of  $x$ , is

- (A)  $7x - 3$
- (B)  $7 - 3x$
- (C)  $\frac{7x}{3}$
- (D)  $4x$

15. The number of bacteria present in a culture is modelled by  $y = y_0 e^{kt}$ , where  $k > 0$ ,  $y$  is the population after  $t$  hours, and  $y_0$  is the initial population. The rate of growth,  $c$ , when  $t = 5$  is given by

- (A)  $c = e^{5k}$   
 (B)  $c = ke^5$   
 (C)  $c = ky_0 e^{5k}$   
 (D)  $c = 5e^{5k}$

16. For  $2n < 1$ ,  $\sum_{r=0}^{\infty} (2n)^r =$

- (A)  $\frac{2}{1-n}$   
 (B)  $\frac{1}{1-2n}$   
 (C)  $\frac{2n}{1+2n}$   
 (D)  $\frac{2n}{1-2n}$

17. Given that  $\sum_{k=1}^n k(k+1) = S_n$  then, for  $m < n$ ,

$$\sum_{k=m+1}^n k(k+1) =$$

- (A)  $S_n - S_{m+1}$   
 (B)  $S_{m+1} - S_m$   
 (C)  $S_n - S_{n-1}$   
 (D)  $S_n - S_m$

18. For what values of  $x$  is the series  $\sum_{r=0}^{\infty} x^r$  convergent?

- (A)  $x > 1$   
 (B)  $x \leq 1$   
 (C)  $-1 < x < 1$   
 (D)  $-1 \leq x \leq 1$

19. The binomial coefficient  $\binom{n}{2}$  is equivalent to

- (A)  $\binom{n}{1} + \binom{n}{1}$   
 (B)  $\binom{n}{n-2}$   
 (C)  $\binom{n-2}{n}$   
 (D)  $\binom{n}{n+2}$

20. The coefficient of  $a^2b^5$  in the expansion of  $(a+b)^7$  is

- (A)  ${}^3C_2$   
 (B)  ${}^5C_3$   
 (C)  ${}^7C_3$   
 (D)  ${}^7C_5$

21. A sequence is defined as  $u_{n+1} = 1 - \frac{1}{1+u_n}$  where  $u_1 = 1$ , ( $n \in \mathbb{N}$ ). The 20<sup>th</sup> term of the sequence is

- (A)  $\frac{1}{20}$   
 (B)  $\frac{1}{21}$   
 (C)  $\frac{19}{20}$   
 (D)  $\frac{20}{21}$

22. The sum to infinity of the geometric series  $16 + 12 + 9 + \dots$  is
- (A) 64  
(B) 37  
(C) 16  
(D) 6
23. If  $\sum_{n=2}^{\infty} 2^{-n} = a$ , then  $a$  is
- (A)  $\frac{1}{4}$   
(B)  $\frac{1}{2}$   
(C) 2  
(D) 4
24. The coefficient of  $x^2$  in the series expansion of  $(1-3x)^{\frac{1}{3}}$  is
- (A)  $-\frac{1}{2}$   
(B)  $\frac{1}{2}$   
(C) -2  
(D) 2
25. If the coefficient of  $x^3$  in  $(6-ax)^9$  is -84, then the value of  $a$  is
- (A)  $\frac{1}{36}$   
(B)  $-\frac{1}{36}$   
(C) 36  
(D) -36
26. If the true length of a piece of pipe is 50 cm and its measured length is 51 cm, then the relative error in length is
- (A) 1%  
(B) 2%  
(C) 3%  
(D) 4%
27. By using the Newton-Raphson method with a first approximation  $x_n$ , the second approximation  $x_{n+1}$  for a root of the equation  $x^5 = x^3 + 25$  may be expressed as
- (A)  $\frac{x_n - x_n^5 - x_n^3 + 25}{5x_n^4 - 3x_n^2}$   
(B)  $\frac{x_n - x_n^5 - x_n^3 - 25}{5x_n^4 - 3x_n^2}$   
(C)  $\frac{4x_n^5 - 4x_n^3 - 25}{5}$   
(D)  $\frac{4x_n^5 - 2x_n^3 + 25}{5x_n^4 - 3x_n^2}$
28. The sum of the first  $n$  terms of a series is  $1 - \left(\frac{1}{4}\right)^n$ . The value of the SECOND term is
- (A)  $\frac{3}{16}$   
(B)  $\frac{3}{4}$   
(C)  $\frac{15}{16}$   
(D) 1

29. A music artist sells 48 000 CDs in the first year of release. Sales are halved each subsequent year. If each CD is sold for \$25, then the value of sales for a particular year,  $n$ , can be expressed as

- (A)  $P = 25(48\,000)\left(\frac{1}{2}\right)^n$   
 (B)  $P = 25(48\,000)\left(\frac{1}{2}\right)^{n-1}$   
 (C)  $P = \frac{25}{2}(48\,000)^n$   
 (D)  $P = 25(24\,000)^{n-1}$

30. Two quantities,  $y$  and  $z$ , were measured. The results, rounded correct to two significant figures, were  $y = 9.8$  and  $z = 9.3$ . The lower and upper bounds respectively for the value of  $y - z$  are

- (A) 0.4 and 0.5  
 (B) 0.5 and 0.5  
 (C) 0.4 and 0.6  
 (D) 0.5 and 0.6

31. Two events  $A$  and  $B$  are such that  $P(A) = 0.5$ ,  $P(B) = 0.16$ ,  $P(A \cup B) = 0.48$ .  $P(A \cap B) =$

- (A) 0.14  
 (B) 0.18  
 (C) 0.26  
 (D) 0.82

32. If  $M = \begin{bmatrix} 1 & 3 & 3 \\ -2 & 4 & 1 \\ 0 & 5 & 6 \end{bmatrix}$ , the FIRST ROW of the co-factor matrix of  $M$  is:

- (A)  $\begin{bmatrix} 19 & 12 & -10 \\ * & * & * \\ * & * & * \end{bmatrix}$   
 (B)  $\begin{bmatrix} -19 & -12 & 10 \\ * & * & * \\ * & * & * \end{bmatrix}$   
 (C)  $\begin{bmatrix} 1 & -2 & 0 \\ * & * & * \\ * & * & * \end{bmatrix}$   
 (D)  $\begin{bmatrix} -1 & 2 & 0 \\ * & * & * \\ * & * & * \end{bmatrix}$

33. Given that  $H$  is a non-singular, square matrix, the determinant,  $|H^2|$ , of  $H^2$ , is

- (A)  $2|H|$   
 (B)  $\frac{1}{2}|H|$   
 (C)  $|H|^2$   
 (D)  $\frac{1}{|H|^2}$

34. The number of possible values of  $x$  which satisfy the system of simultaneous equations,

$$2x + 3y + 2z = -5$$

$$4x + 6y + 4z = -10$$

$$6x + 9y + 6z = -25$$

is

- (A) 0
- (B) 1
- (C) 2
- (D) 3

35. The roots of the equation  $x^2 + 1 = 0$  are

- (A)  $x = -1, 1$
- (B)  $x = -1, i$
- (C)  $x = 1, -i$
- (D)  $x = -i, i$

36. The FIRST ROW of the product PQ of the two  $3 \times 3$  matrices

$$P = \begin{pmatrix} 2 & -3 & 1 \\ 5 & -6 & 5 \\ -1 & 2 & 3 \end{pmatrix} \text{ and } Q = \begin{pmatrix} 2 & 1 & 3 \\ 5 & 0 & -1 \\ -3 & -2 & 4 \end{pmatrix}$$

is

- (A)  $(4 \ -3 \ 3)$
- (B)  $(4 \ -2 \ 4)$
- (C)  $(-14 \ 0 \ 13)$
- (D)  $(-14 \ 35 \ -1)$

37. The determinant of the matrix

$$M = \begin{pmatrix} 3 & -1 & 5 \\ 2 & 3 & -2 \\ 0 & 5 & 4 \end{pmatrix} \text{ is}$$

- (A) 20
- (B) 64
- (C) 104
- (D) 124

38. The roots of a quadratic equation  $ax^2 + bx + c = 0$ , are the complex numbers  $1 + 2i$  and  $2 - i$ . The equation is

- (A)  $x^2 - (3 + i)x - 4 - 3i = 0$
- (B)  $x^2 - (3 + i)x + 4 + 3i = 0$
- (C)  $x^2 - (3 - i)x + 4 + 3i = 0$
- (D)  $x^2 + (3 + i)x + 4 + 3i = 0$

39.  $\frac{2-i}{3+2i} =$

- (A)  $\frac{8-i}{13}$
- (B)  $\frac{8+i}{13}$
- (C)  $\frac{7-4i}{13}$
- (D)  $\frac{4-7i}{13}$

40. The expression  $i[(1+i)^2 - (1-i)^2]$  is equal to

- (A) -4
- (B) -2
- (C) 2
- (D) 4

41. The principal value of the argument of the complex number  $2 - 2i$  is
- (A)  $\frac{-3\pi}{4}$   
 (B)  $\frac{-\pi}{4}$   
 (C)  $\frac{\pi}{4}$   
 (D)  $\frac{3\pi}{4}$
42. The complex number  $Z = -\frac{1}{2} + i\frac{\sqrt{3}}{2}$  can be expressed as
- (A)  $\frac{1}{2} \left( \cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3} \right)$   
 (B)  $\frac{1}{2} \left( \cos \frac{\pi}{6} + i \sin \frac{\pi}{6} \right)$   
 (C)  $\left( \cos \frac{\pi}{6} + i \sin \frac{\pi}{6} \right)$   
 (D)  $\left( \cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3} \right)$
43. In how many ways can the letters PQRST be arranged so that the letters R and S are always together?
- (A)  $5! - 4! \times 2$   
 (B)  $\frac{5!}{2} - 4!$   
 (C)  $4! \times 2$   
 (D)  $4!$
44. The letters of the word I R R E G U L A R are to be arranged in a line. The number of possible arrangements in which the 3 Rs are not together is
- (A)  $7!$   
 (B)  $\frac{9!}{3!} - 7!$   
 (C)  $9! - 7!$   
 (D)  $9! - 7! \times 3!$
45. The locus of the points described by a complex number  $z$  is given by  $|z - 1 - 2i| = 3$ . The locus describes a circle with
- (A) centre  $(-1, -2)$  and radius 3 units  
 (B) centre  $(-1, -2)$  and radius 9 units  
 (C) centre  $(1, 2)$  and radius 3 units  
 (D) centre  $(1, 2)$  and radius 9 units

IF YOU FINISH BEFORE TIME IS CALLED, CHECK YOUR WORK ON THIS TEST.