

Lab 03 - Orders of Growth

Edwin (Benny) Sparks
9-9-21

1) a.

$$\log_2 n \rightarrow \log_2 4n - \log_2 n = \log_2 \left(\frac{4n}{n} \right) = \log_2(4) = 2$$

b.

$$\sqrt{n} \rightarrow \sqrt{4n}/\sqrt{n} = \sqrt{4} = 2 \quad [2\times \text{ longer for } 4\times \text{ larger}]$$

c.

$$n \rightarrow 4n/n = 4 \quad [4\times \text{ longer for } 4\times \text{ larger}]$$

d.

$$n^2 \rightarrow (4n)^2/n^2 = \frac{16n^2}{n^2} = 16 \quad [16\times \text{ longer for } 4\times \text{ larger}]$$

e.

$$n^3 \rightarrow (4n)^3/n^3 = \frac{64n^3}{n^3} = 64 \quad [64\times \text{ longer for } 4\times \text{ larger}]$$

f.

$$2^n \rightarrow 2^{4n}/2^n = 2^{4n-n} = 2^{3n} \quad [\text{bad, just really bad}]$$

2) proof.

$$\frac{\log_2 a}{\log_2 b} \stackrel{?}{=} \frac{\ln a}{\ln b} = \frac{\log_2 a \cdot \log_e 2}{\log_2 b \cdot \log_e 2} = \frac{\log_2 a}{\log_2 b} \quad \checkmark$$

$$\lim_{x \rightarrow \infty} \log(4x)/\log(x) = \lim_{x \rightarrow \infty} \frac{\log 4}{\log x} + 1 = 0 + 1 = 1$$

3)

$$\frac{1\text{mil}^2 + \sqrt{1\text{mil}}}{1000^2 + \sqrt{1000}} = \frac{(1000, 1000)^2 + \sqrt{1000+1000}}{1000^2 + \sqrt{1000}}$$

$$\Rightarrow \frac{\frac{1000^2}{1000^2 + \sqrt{1000}}}{1000^2} \approx \frac{1000 \cdot 1000 + 0}{1 + 0}$$

$$\text{or} \quad = \frac{1\text{mil}^2}{1000^2} + \frac{\sqrt{1\text{mil}}}{\sqrt{1000}} = 1000^2 + \frac{1000}{32} \approx 1\text{million}$$

$$= n^2 + \sqrt{n} \in \mathcal{O}(n^2)$$

$$\approx 10^6 \cdot 2 \text{ min} = 1388 \text{ days} \approx 3 \text{ years}$$

$$4) 25 \cdot n^2 \cdot \log_2(n) = \frac{25 \cdot 100,000^2 \cdot \log_2(100,000)}{25 \cdot 500^2 \cdot \log_2(500)}$$

$$= \frac{4.152 \times 10^{12}}{5.603 \times 10^7} \approx 74,102 \text{ minutes or } \approx 51 \text{ days}$$

$$5) C_{avg}(n) = \frac{P(n+1)}{2} + n(1-P), \quad n = 10,000$$

$$P\%1 = 0.01(10,000+1)/2 + 10,000(1-0.01) = 9950.01$$

$$P\%20 = 0.2(10,000+1)/2 + 10,000(1-0.2) = 9000.1$$

$$P\%50 = 0.5(10,000+1)/2 + 10,000(1-0.5) = 7500.25$$

$$P\%80 = 0.8(10,000+1)/2 + 10,000(1-0.8) = 6000.4$$

$$P\%99 = .99(10,000+1)/2 + 10,000(1-0.99) = 5050.5$$

6)

$$C_1(n) = n^2 \quad C_2(n) = 10 \cdot n \cdot \log_2(n) \quad \left[\log_2(n) = \frac{\log_e n}{\log_e 2} \right]$$

for all values > 60 n^2 will
take substantially longer.

Data_Structures_Lab_03 > main.c

```

3 // Edwin (Sonny) Sparks
4 // September 8, 2021
5 #include <stdio.h>
6 #include <math.h>
7 #define SIZE 20
8
9 int main() {
10     float ratios[SIZE];
11     float n;
12     printf(_Format: "The Values of n are: \n");
13     for(int i=0;i<SIZE;i++) {
14         n=10*(i+1);
15         ratios[i] = (log(_X: 4 * n)/(log(n)));
16         printf(_Format: "%.f\t", n);
17     }
18     printf(_Format: "\nThe Ratios for 10 to 200, incrementing by 10 is: \n");
19     for(int i=0;i<SIZE;i++) {
20         printf(_Format: "%.2f\t", ratios[i]);
21     }
22     return 0;
23 }
24

```

Run: Data_Structures_Lab_03

"C:\Users\Sonny Sparks\OneDrive\Documents\Tarleton Fall 21'\Data Structures Lab\Data_Structures_Lab_03\cmake-build-debug\Data_Structures_Lab_03.exe"

The Values of n are:

10	20	30	40	50	60	70	80	90	100	110	120	130	140	150
	160	170	180	190	200									

The Ratios for 10 to 200, incrementing by 10 is:

1.60	1.46	1.41	1.38	1.35	1.34	1.33	1.32	1.31	1.30	1.29	1.29	1.28	1.28	1.28
	1.27	1.27	1.27	1.26	1.26									

Process finished with exit code 0

Run TODO Problems Terminal Python Packages CMake Messages

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Data_Structures_Lab_03

main.c

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Scratches and Consoles

main.c

1

// Data Structures Lab 3

2

// Data Structures

3

// Edwin (Sonny) Sparks

4

// September 8, 2021

5

#include <stdio.h>

6

#include <math.h>

7

#define SIZE 20

8

9

int main() {

10

float ratios[SIZE], n[SIZE];

11

for(int i=0;i<SIZE;i++) {

12

n[i]=i*10;

13

}

14

printf(_Format: "\nThe ratios values are:\n");

15

for(int i=0;i<SIZE;i++){

16

ratios[i]=(n[i]*n[i])/(10*n[i]*logf(n[i])/log(_X: 2));

17

printf(_Format: "%.f : %.3f\n",n[i], ratios[i]);

18

}

19

return 0;

20

}

21

Run: Data_Structures_Lab_03

"C:\Users\Sonny Sparks\OneDrive\Documents\Tarleton Fal

The ratios values are:

0 : -nan(ind)

10 : 0.301

20 : 0.463

30 : 0.611

40 : 0.752

50 : 0.886

60 : 1.016

70 : 1.142

80 : 1.265

90 : 1.386

100 : 1.505

110 : 1.622

120 : 1.737

130 : 1.851

140 : 1.964

150 : 2.075

160 : 2.185

170 : 2.294

180 : 2.403

190 : 2.510

Process finished with exit code 0

main

main

TODO

Problems

Terminal

Python Packages

CMake

Messages

Event Log