

Data Structures: Homework Ch. 6

$$1) \quad \begin{aligned} 2x + y - z &= 8 \\ -3x - y + 2z &= -11 \\ -2x + y + 2z &= -3 \end{aligned} \Rightarrow \left[\begin{array}{ccc|c} 2 & 1 & -1 & 8 \\ -3 & -1 & 2 & -11 \\ -2 & 1 & 2 & -3 \end{array} \right]$$

$$\Rightarrow \begin{aligned} R_3 &= R_1 + R_3 \\ \Rightarrow \left[\begin{array}{ccc|c} 2 & 1 & -1 & 8 \\ -3 & -1 & 2 & -11 \\ 0 & 2 & 1 & 5 \end{array} \right] &\Rightarrow \left[\begin{array}{ccc|c} 2 & 1 & -1 & 8 \\ 0 & -5 & 5 & -46 \\ 0 & 2 & 1 & 5 \end{array} \right] &\Rightarrow 2R_2 + 5R_3 \\ R_2 &= 2R_2 + -3(R_1) \end{aligned}$$

$$\Rightarrow \begin{aligned} \begin{array}{ccc|c} x & y & z & \\ 2 & 1 & -1 & 8 \\ 0 & -5 & 5 & -46 \\ 0 & 0 & 15 & -67 \end{array} &\Rightarrow \begin{aligned} 2x + y - z &= 8 \\ -5y + 5z &= -46 \\ 15z &= -67 \end{aligned} \end{aligned}$$

$$\begin{aligned} x &= -3/5 \\ y &= 71/15 \\ z &= -67/15 \end{aligned}$$

$$2) \quad L = \begin{bmatrix} 1 & 0 & 0 \\ -3 & 1 & 0 \\ 1 & 2 & 1 \end{bmatrix} \quad U = \begin{bmatrix} 2 & 1 & -1 \\ 0 & -5 & 5 \\ 0 & 0 & 15 \end{bmatrix}$$

$$y_1 = 8$$

$$y_2 = -11 - 3(8) = -35$$

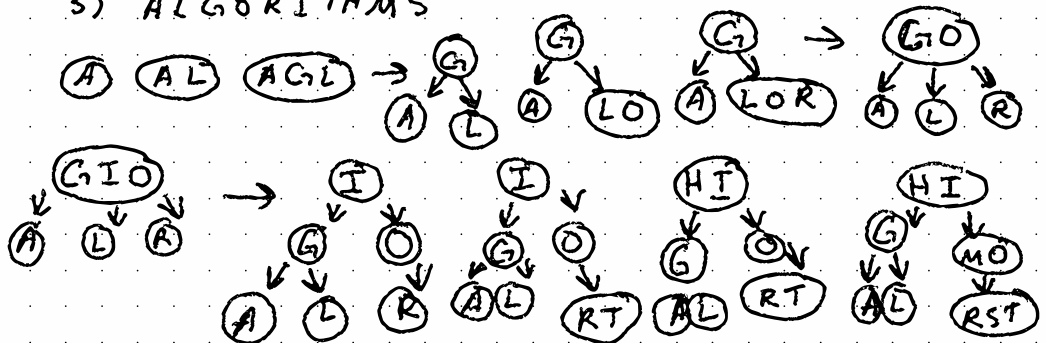
$$y_3 = -3 - 35(2) + 8 = -67$$

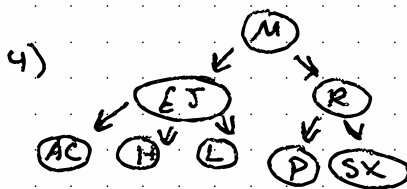
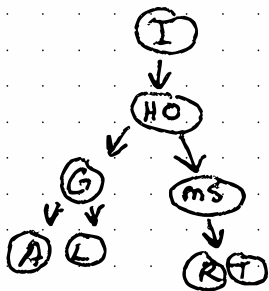
$$x_3 = -67/15$$

$$x_2 = (-5 - (-5/15)) / -35 = 71/15$$

$$x_1 = (2 + 71/15 + 2) / 8 = -3/5$$

3) ALGORITHMS





$$\frac{m}{1} \quad \frac{E}{2} \quad \frac{J}{3} \quad \frac{A}{4} \quad \frac{C}{5} \quad \frac{H}{4} \quad \frac{L}{4} \quad \frac{R}{2} \quad \frac{P}{3} \quad \frac{S}{4} \quad \frac{X}{5}$$

$$\Rightarrow 37/11$$

Long