

## TIMBER BEAM N. 001

| Caratteristiche meccaniche legno GL24c←← |                                  |                                  |
|--|----------------------------------|----------------------------------|
| $\gamma_M = 1.35$ $k_{mod} = 0.8$        |                                  |                                  |
| $f_{m,k} = 24 \text{ MPa}$               | $f_{m,d} = 14.22 \text{ MPa}$    | $E_{0,mean} = 11000 \text{ MPa}$ |
| $f_{t,0,k} = 17 \text{ MPa}$             | $f_{t,0,d} = 10.07 \text{ MPa}$  | $E_{0,05} = 9100 \text{ MPa}$    |
| $f_{t,90,k} = 0.5 \text{ MPa}$           | $f_{t,90,d} = 0.296 \text{ MPa}$ | $E_{90,mean} = 300 \text{ MPa}$  |
| $f_{c,0,k} = 21.5 \text{ MPa}$           | $f_{c,0,d} = 12.74 \text{ MPa}$  | $G_{mean} = 650 \text{ MPa}$     |
| $f_{c,90,k} = 2.5 \text{ MPa}$           | $f_{c,90,d} = 1.48 \text{ MPa}$  | $r_k = 365 \text{ kg/m}^3$       |
| $f_{v,k} = 3.5 \text{ MPa}$              | $f_{v,d} = 2.07 \text{ MPa}$     | $r_{mean} = 400 \text{ kg/m}^3$  |

| Caratteristiche sezione rettangolare  |                              |
|---|------------------------------|
| $b = 200 \text{ mm}$ $h = 400 \text{ mm}$ $\gamma = 5 \frac{\text{kN}}{\text{m}^3}$ |                              |
| $A = 800 \text{ cm}^2$  | $g_{1,k} = 0.4 \text{ kN/m}$ |
| $I_y = 106667 \text{ cm}^4$   | $I_z = 26666.7 \text{ cm}^4$ |
| $W_y = 5333.33 \text{ cm}^3$  | $W_z = 2666.67 \text{ cm}^3$ |
| $i_y = 11.55 \text{ cm}$  | $i_z = 5.77 \text{ cm}$      |

$$l = 8.79 \text{ m}$$

$$k_m = 0.7 \text{ legno massiccio, sezioni rettangolari}$$

$$\beta_c = 0.1 \text{ legno lammellare}$$

$$l_{0,y} = 8.79 \text{ m}$$

$$l_{0,z} = 8.79 \text{ m}$$

$$\beta = 1 \text{ coef. di vincolo}$$

### Azioni agenti

$$M_{Ed,y} = 218.47 \text{ kNm}$$

$$M_{Ed,z} = 0 \text{ kNm}$$

$$N_{Ed} = 0 \text{ kN}$$

$$V_{Ed,y} = 0 \text{ kN}$$

$$V_{Ed,z} = 73.27 \text{ kN}$$

### Tensioni agenti

$$\sigma_{c,0,d} = \frac{N_{Ed}}{A} = \frac{0 \text{ kN}}{800 \text{ cm}^2} = 0 \text{ MPa}$$

$$\sigma_{m,y,d} = \frac{M_{Ed,y}}{W_y} = \frac{218.47 \text{ kNm}}{5333.33 \text{ cm}^3} = 40.96 \text{ MPa}$$

$$\sigma_{m,z,d} = \frac{M_{Ed,z}}{W_z} = \frac{0 \text{ kNm}}{2666.67 \text{ cm}^3} = 0 \text{ MPa}$$

$$k_{cr} = \frac{2.5 \text{ MPa}}{f_{v,k}} = \frac{2.5 \text{ MPa}}{3.5 \text{ MPa}} = 0.714$$

$$\tau_{y,d} = \frac{1.5 \cdot V_{Ed,y}}{k_{cr} \cdot A} = \frac{1.5 \cdot 0 \text{ kN}}{0.714 \cdot 800 \text{ cm}^2} = 0 \text{ MPa}$$

$$\tau_{z,d} = \frac{1.5 \cdot V_{Ed,z}}{k_{cr} \cdot A} = \frac{1.5 \cdot 73.27 \text{ kN}}{0.714 \cdot 800 \text{ cm}^2} = 1.92 \text{ MPa}$$

### Verifica flessione

$$\frac{\sigma_{m,y,d}}{f_{m,d}} + k_m \frac{\sigma_{m,z,d}}{f_{m,d}} = \frac{40.96 \text{ MPa}}{14.22 \text{ MPa}} + 0.7 \cdot \frac{0 \text{ MPa}}{14.22 \text{ MPa}} = 2.88 > 1 = 1 \text{ NO ✗}$$

$$k_m \frac{\sigma_{m,y,d}}{f_{m,d}} + \frac{\sigma_{m,z,d}}{f_{m,d}} = 0.7 \cdot \frac{40.96 \text{ MPa}}{14.22 \text{ MPa}} + \frac{0 \text{ MPa}}{14.22 \text{ MPa}} = 2.02 > 1 = 1 \text{ NO ✗}$$

### Verifica flessione e compressione combinata

$$\left( \frac{\sigma_{c,0,d}}{f_{c,0,d}} \right)^2 + \frac{\sigma_{m,y,d}}{f_{m,d}} + k_m \frac{\sigma_{m,z,d}}{f_{m,d}} = \left( \frac{0 \text{ MPa}}{12.74 \text{ MPa}} \right)^2 + \frac{40.96 \text{ MPa}}{14.22 \text{ MPa}} + 0.7 \cdot \frac{0 \text{ MPa}}{14.22 \text{ MPa}} = 2.88 > 1 = 1 \text{ NO ✗} \quad [\text{EC5 §6.2.4}]$$

$$\left( \frac{\sigma_{c,0,d}}{f_{c,0,d}} \right)^2 + k_m \frac{\sigma_{m,y,d}}{f_{m,d}} + \frac{\sigma_{m,z,d}}{f_{m,d}} = \left( \frac{0 \text{ MPa}}{12.74 \text{ MPa}} \right)^2 + 0.7 \cdot \frac{40.96 \text{ MPa}}{14.22 \text{ MPa}} + \frac{0 \text{ MPa}}{14.22 \text{ MPa}} = 2.02 > 1 = 1 \text{ NO ✗}$$

### Verifica instabilità di colonna

$$\lambda_y = \frac{l_{0,y}}{i_y} = \frac{8.79 \text{ m}}{11.55 \text{ cm}} = 76.09 \quad [\text{EC5 §6.3.2}]$$

$$\lambda_{\text{rel},y} = \frac{\lambda_y}{\pi} \sqrt{\frac{f_{c,0,k}}{E_{0,05}}} = \frac{76.09}{3.14} \sqrt{\frac{21.5 \text{ MPa}}{9100 \text{ MPa}}} = 1.18$$

$$k_y = 0.5 \cdot (1 + \beta_c \cdot (\lambda_{\text{rel},y} - 0.3) + \lambda_{\text{rel},y}^2) = 0.5 \cdot (1 + 0.1 \cdot (1.18 - 0.3) + 1.18^2) = 1.24$$

$$k_{c,y} = \frac{1}{k_y + \sqrt{k_y^2 - \lambda_{\text{rel},y}^2}} = \frac{1}{1.24 + \sqrt{1.24^2 - 1.18^2}} = 0.619$$

$$\lambda_z = \frac{l_{0,z}}{i_z} = \frac{8.79 \text{ m}}{5.77 \text{ cm}} = 152.18$$

$$\lambda_{\text{rel},z} = \frac{\lambda_z}{\pi} \sqrt{\frac{f_{c,0,k}}{E_{0,05}}} = \frac{152.18}{3.14} \sqrt{\frac{21.5 \text{ MPa}}{9100 \text{ MPa}}} = 2.35$$

$$k_z = 0.5 \cdot (1 + \beta_c \cdot (\lambda_{\text{rel},z} - 0.3) + \lambda_{\text{rel},z}^2) = 0.5 \cdot (1 + 0.1 \cdot (2.35 - 0.3) + 2.35^2) = 3.37$$

$$k_{c,z} = \frac{1}{k_z + \sqrt{k_z^2 - \lambda_{\text{rel},z}^2}} = \frac{1}{3.37 + \sqrt{3.37^2 - 2.35^2}} = 0.173$$

$$\frac{\sigma_{c,0,d}}{k_{c,y} \cdot f_{c,0,d}} + \frac{\sigma_{m,y,d}}{f_{m,d}} + k_m \frac{\sigma_{m,z,d}}{f_{m,d}} = \frac{0 \text{ MPa}}{0.619 \cdot 12.74 \text{ MPa}} + \frac{40.96 \text{ MPa}}{14.22 \text{ MPa}} + 0.7 \cdot \frac{0 \text{ MPa}}{14.22 \text{ MPa}} = 2.88 > 1 = 1 \text{ NO ✗}$$

$$\frac{\sigma_{c,0,d}}{k_{c,z} \cdot f_{c,0,d}} + k_m \frac{\sigma_{m,y,d}}{f_{m,d}} + \frac{\sigma_{m,z,d}}{f_{m,d}} = \frac{0 \text{ MPa}}{0.173 \cdot 12.74 \text{ MPa}} + 0.7 \cdot \frac{40.96 \text{ MPa}}{14.22 \text{ MPa}} + \frac{0 \text{ MPa}}{14.22 \text{ MPa}} = 2.02 > 1 = 1 \text{ NO ✗}$$

### Verifica instabilità di trave

$$l_{\text{ef}} = \beta \cdot l = 1 \cdot 8.79 \text{ m} = 8.79 \text{ m} \quad [\text{EC5 §6.3.3}]$$

$$\sigma_{m,\text{crit}} = \frac{0.78 \cdot b^2}{h \cdot l_{\text{ef}}} \cdot E_{0,05} = \frac{0.78 \cdot (200 \text{ mm})^2}{400 \text{ mm} \cdot 8.79 \text{ m}} \cdot 9100 \text{ MPa} = 80.79 \text{ MPa}$$

$$\lambda_{\text{rel},m} = \sqrt{\frac{f_{m,k}}{\sigma_{m,\text{crit}}}} = \sqrt{\frac{24 \text{ MPa}}{80.79 \text{ MPa}}} = 0.545$$

$$k_{\text{crit}} = \begin{cases} \text{if } \lambda_{\text{rel},m} < 0.75: 1 \\ \text{if } \lambda_{\text{rel},m} < 1.4: 1.56 - 0.75 \cdot \lambda_{\text{rel},m} \\ \text{else: } \frac{1}{\lambda_{\text{rel},m}^2} \end{cases} = \begin{cases} \text{if } 0.545 < 0.75: 1 \\ \text{if } 0.545 < 1.4: 1.56 - 0.75 \cdot 0.545 \\ \text{else: } \frac{1}{0.545^2} \end{cases} = 1$$

$$\frac{\sigma_{m,y,d}}{k_{\text{crit}} \cdot f_{m,d}} = \frac{40.96 \text{ MPa}}{1 \cdot 14.22 \text{ MPa}} = 2.88 > 1 = 1 \text{ NO ✗}$$

$$\left( \frac{\sigma_{m,y,d}}{k_{\text{crit}} \cdot f_{m,d}} \right)^2 + \frac{\sigma_{c,0,d}}{k_{c,z} \cdot f_{c,0,d}} = \left( \frac{40.96 \text{ MPa}}{1 \cdot 14.22 \text{ MPa}} \right)^2 + \frac{0 \text{ MPa}}{0.173 \cdot 12.74 \text{ MPa}} = 8.3 > 1 = 1 \text{ NO ✗}$$