

CALCULUS

MINI EXAM 1 FIRST SECTION

NAME: _____

ID: _____

SCORE: _____ / 80

RULES:

- You have 30 minutes to complete the exam.
- There are 3 questions and 80 points in total.
- You can use a non-graphing calculator.
- If you need to go to the restroom, please turn in your cellphone before.

Date: October 11, 2024.

Problem 1 (30 points). (1) (10 points) State the mean value theorem (you can use your own words)

(2) (20 points) Show that the equation $\ln(x) - \sin x = 0$ has a solution between 1 and 100.

Problem 2 (30 points). Do the limits below exist? Give reason.

$$(1) \lim_{x \rightarrow \pi/2} \left(x - \frac{\pi}{2} \right) \cos \left(\frac{1}{x - \pi/2} \right)$$

$$(2) \lim_{x \rightarrow e} \frac{e^2 - x}{x - e}$$

$$(3) \lim_{x \rightarrow 2} \frac{x^2 - 5}{x - 2}$$

Problem 3 (20 points). Consider

$$f(x) = \begin{cases} ke^x, & x < 0 \\ 2 \cos x + \sin x, & x \geqslant 0. \end{cases}$$

Find k to make $f(x)$ continuous at $x = 0$.