WORKSHEET 7

MATH 101

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Useful definitions:

- (1) $\tan x = \frac{\sin x}{\cos x}$ (2) $\cot x = \frac{\cos x}{\sin x}$ (3) $\csc x = \frac{1}{\sin x}$ (4) $\sec x = \frac{1}{\cos x}$

(1) Show the chain rule: Question 1.

$$\frac{d}{dx}f(g(x)) = f'(g(x))g'(x).$$

(2) Apply the chain rule to show the quotient rule:

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x)g(x) - f(x)g'(x)}{g(x)^2}$$

(3) Apply the above rules when

$$f(x) = x^3 - \pi x$$

and

$$g(x) = \frac{1}{x^2 + 3}$$

Question 2. For this part, you should review https://openstax.org/books/calculus-volume-1/pages/2-3-the-limit-laws for the limits $\lim_{\theta \to 0} \frac{\sin \theta}{\theta} = 1$ and $\lim_{\theta \to 0} \frac{\cos \theta - 1}{\theta} = 0$. Show that

(1)
$$(\sin x)' = \cos x$$

($Hint: \sin(x+y) = \sin x \cos y + \sin y \cos x$)

(2)
$$(\cos x)' = -\sin x$$

($Hint: \cos(x+y) = \cos x \cos y - \sin x \sin y$)

Question 3. Use all the rules above to find

(1)
$$(\cot x)'$$

(2)
$$(\tan x)'$$

$$(3) (\csc x)'$$

$$(4) (\sec x)'$$