## MATH 102: HOMEWORK 5

DUE DATE: TUES, NOV 14

Problem 1. Describe  $\mathbb{R} \times \mathbb{N}$  using set notation. What is a graphical representation of this set? (For this, make sure you know how to insert figures in LaTeX).

Problem 2. (1) Is the set  $([0,1] \cup [1,2]) \times ([2,3] \cup [3,4])$  the same with  $([0,1] \times [2,3]) \cup ([1,2] \times [3,4])$ ?

- (2) Let A, B, C, D be sets. What must be true for the relationship between  $(A \cup B) \times (C \cup D)$  and  $(A \times B) \cup (B \times D)$ ?
- (3) Prove your claim in (2).

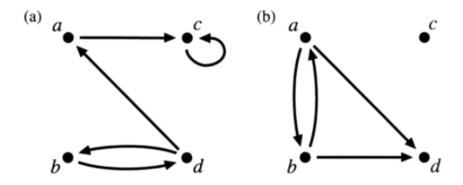
Problem 3. Prove that

- $(1) \ A \times (B \cap C) = (A \times B) \cap (A \times C)$
- $(2) (A \cap B) \times (C \cap D) = (A \times B) \cup (B \times D)$

Problem 4. Let R be a relation from A to B and S be a relation from B to C. We define the composition of relations  $S \circ R$  as follows

$$S \circ R = \{(a,c) \in A \times C \mid \exists b \in B, (a,b) \in R \land (b,c) \in S\}.$$

Consider the following graphs.



Let R be the relation in (a) and S be the relation in (b).

- (1) Write, in set notation,  $S \circ R$ .
- (2) Draw  $S \circ R$ .

Date: November 1, 2023.