

## MATH 102: HOMEWORK 4

DUE DATE: THURSDAY, OCT 24

Note that you need to turn in L<sup>A</sup>T<sub>E</sub>X version of this homework.

*Problem 1.* In class on Oct 8, we discussed about inflation and present value. In short, if someone gives you  $F$  amount of dollars every year and the inflation rate is  $r$ , then the present value of  $N$  year of this fixed income would be

$$PV = F + \frac{F}{1+r} + \cdots + \frac{F}{(1+r)^N}.$$

- (1) Use induction to prove that after  $N$  year,

$$PV = F \left( \frac{1 + r - \frac{1}{(1+r)^N}}{r} \right)$$

- (2) Apply this to the situation when  $F = \$1$  and  $r = 5\%$  (I made a mistake in class about this)
- (3) What happen if you were to live forever? How much would you buy a stock if it pays you \$1 per year from now to eternity?