

MATH 310: Mathematical Statistics (brief notes)

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Disclaimer

This is class notes for Mathematical Statistics at Fublbright University Vietnam. I claim no originality in this work as it is mostly taken from the reference books. However, all errors and typos are solely mine.

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1.2 Inequalities

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1.4 Central Limit Theorem

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Linear Least Squares

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