13. [15 marks] [Causation Questions]

The table below shows the data collected from 12 individuals. The goal of the study was to estimate the effect of daily low-dose aspirin (T=1) on the risk of heart disease (Y=1). The table also shows the values of the potential outcomes that would have been observed given treatment Y_1 and no treatment Y_0 . Recall also that a treatment effect depends on these potential outcomes and is defined by $P(Y_1) - P(Y_0)$.

| ID | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|-------|---|---|---|---|---|---|---|---|---|----|----|----|
| T | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| Y | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 |
| Y_0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| Y_1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 |

- 14. [2 marks] Are the populations of individuals who were treated and those who were not treated exchangeable? Explain.
- 15. [3 marks] Suppose that you are given the first three rows of the table above, i.e. ID, T, and Y, but not the potential outcomes Y_0 and Y_1 . In this case, might it be possible for the true treatment effect to be negative? If yes, provide viable values for Y_0 and Y_1 that will make for a treatment effect that is negative. If not, write the value that corresponds with the smallest possible treatment effect next to the table below.

| ID | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|-------|---|---|---|---|---|---|---|---|---|----|----|----|
| Y_0 | | | | | | | | | | | | |
| Y_1 | | | | | | | | | | | | |

16. [3 marks] Might it be possible for the treatment effect to be 1? If yes, provide viable values for Y_0 and Y_1 that will make for a treatment effect of 1. If not, write the value that corresponds with the largest possible treatment effect next to the table below.

| ID | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|-------|---|---|---|---|---|---|---|---|---|----|----|----|
| Y_0 | | | | | | | | | | | | |
| Y_1 | | | | | | | | | | | | |

17. [1 mark] Based on your analysis above, can you confidently suggest one takes aspirin to reduce the risk of heart disease?