

1. **Separated but not sufficient:**

Gender is independent of hyperlipidemia given age, but gender is not independent of age given hyperlipidemia

- **A:** Gender
- **C:** Hyperlipidemia
- **Y:** Age

SEPERATED	SUFFICIENT
$P(\text{ag: } \sim 60 \mid \text{hl: YES, gd: Male}) = 0.39557$	$P(\text{hl: YES} \mid \text{ag: } \sim 60, \text{gd: Male}) = 0.51168$
$P(\text{ag: } \sim 60 \mid \text{hl: YES}) = 0.39557$	$P(\text{hl: YES} \mid \text{ag: } \sim 60) = 0.47549$
$P(\text{ag: } \sim 40 \mid \text{hl: YES, gd: Male}) = 0.35546$	$P(\text{hl: NO} \mid \text{ag: } \sim 60, \text{gd: Male}) = 0.48832$
$P(\text{ag: } \sim 40 \mid \text{hl: YES}) = 0.35546$	$P(\text{hl: NO} \mid \text{ag: } \sim 60) = 0.52451$
$P(\text{ag: } < 40 \mid \text{hl: YES, gd: Male}) = 0.24897$	$P(\text{hl: YES} \mid \text{ag: } \sim 60, \text{gd: Female}) = 0.43458$
$P(\text{ag: } < 40 \mid \text{hl: YES}) = 0.24897$	$P(\text{hl: YES} \mid \text{ag: } \sim 60) = 0.47549$
$P(\text{ag: } \sim 60 \mid \text{hl: YES, gd: Female}) = 0.39557$	$P(\text{hl: NO} \mid \text{ag: } \sim 60, \text{gd: Female}) = 0.56542$
$P(\text{ag: } \sim 60 \mid \text{hl: YES}) = 0.39557$	$P(\text{hl: NO} \mid \text{ag: } \sim 60) = 0.52451$
$P(\text{ag: } \sim 40 \mid \text{hl: YES, gd: Female}) = 0.35546$	$P(\text{hl: YES} \mid \text{ag: } \sim 40, \text{gd: Male}) = 0.46432$
$P(\text{ag: } \sim 40 \mid \text{hl: YES}) = 0.35546$	$P(\text{hl: YES} \mid \text{ag: } \sim 40) = 0.42854$
$P(\text{ag: } < 40 \mid \text{hl: YES, gd: Female}) = 0.24897$	$P(\text{hl: NO} \mid \text{ag: } \sim 40, \text{gd: Male}) = 0.53568$
$P(\text{ag: } < 40 \mid \text{hl: YES}) = 0.24897$	$P(\text{hl: NO} \mid \text{ag: } \sim 40) = 0.57146$
$P(\text{ag: } \sim 60 \mid \text{hl: NO, gd: Male}) = 0.29712$	$P(\text{hl: YES} \mid \text{ag: } \sim 40, \text{gd: Female}) = 0.38867$
$P(\text{ag: } \sim 60 \mid \text{hl: NO}) = 0.29712$	$P(\text{hl: YES} \mid \text{ag: } \sim 40) = 0.42854$
$P(\text{ag: } \sim 40 \mid \text{hl: NO, gd: Male}) = 0.32275$	$P(\text{hl: NO} \mid \text{ag: } \sim 40, \text{gd: Female}) = 0.61133$
$P(\text{ag: } \sim 40 \mid \text{hl: NO}) = 0.32275$	$P(\text{hl: NO} \mid \text{ag: } \sim 40) = 0.57146$
$P(\text{ag: } < 40 \mid \text{hl: NO, gd: Male}) = 0.38014$	$P(\text{hl: YES} \mid \text{ag: } < 40, \text{gd: Male}) = 0.34014$
$P(\text{ag: } < 40 \mid \text{hl: NO}) = 0.38014$	$P(\text{hl: YES} \mid \text{ag: } < 40) = 0.30842$
$P(\text{ag: } \sim 60 \mid \text{hl: NO, gd: Female}) = 0.29712$	$P(\text{hl: NO} \mid \text{ag: } < 40, \text{gd: Male}) = 0.65986$
$P(\text{ag: } \sim 60 \mid \text{hl: NO}) = 0.29712$	$P(\text{hl: NO} \mid \text{ag: } < 40) = 0.69158$
$P(\text{ag: } \sim 40 \mid \text{hl: NO, gd: Female}) = 0.32275$	$P(\text{hl: YES} \mid \text{ag: } < 40, \text{gd: Female}) = 0.27436$
$P(\text{ag: } \sim 40 \mid \text{hl: NO}) = 0.32275$	$P(\text{hl: YES} \mid \text{ag: } < 40) = 0.30842$
$P(\text{ag: } < 40 \mid \text{hl: NO, gd: Female}) = 0.38014$	$P(\text{hl: NO} \mid \text{ag: } < 40, \text{gd: Female}) = 0.72564$
$P(\text{ag: } < 40 \mid \text{hl: NO}) = 0.38014$	$P(\text{hl: NO} \mid \text{ag: } < 40) = 0.69158$

2. Sufficient but not separated:

Gender is not independent of BMI given hyperlipidemia, but gender independent of hyperlipidemia given BMI

- **A:** Gender
- **C:** BMI
- **Y:** Hyperlipidemia

SEPERATED

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P(hl: YES | bmi: ~18.5, gd: Male) = 0.24111
P(hl: YES | bmi: ~18.5) = 0.21561

P(hl: NO | bmi: ~18.5, gd: Male) = 0.75889
P(hl: NO | bmi: ~18.5) = 0.78439

P(hl: YES | bmi: ~18.5, gd: Female) = 0.189
P(hl: YES | bmi: ~18.5) = 0.21561

P(hl: NO | bmi: ~18.5, gd: Female) = 0.811
P(hl: NO | bmi: ~18.5) = 0.78439

P(hl: YES | bmi: ~24.0, gd: Male) = 0.50474
P(hl: YES | bmi: ~24.0) = 0.46857

P(hl: NO | bmi: ~24.0, gd: Male) = 0.49526
P(hl: NO | bmi: ~24.0) = 0.53143

P(hl: YES | bmi: ~24.0, gd: Female) = 0.42777
P(hl: YES | bmi: ~24.0) = 0.46857

P(hl: NO | bmi: ~24.0, gd: Female) = 0.57223
P(hl: NO | bmi: ~24.0) = 0.53143

P(hl: YES | bmi: ~28.0, gd: Male) = 0.68373
P(hl: YES | bmi: ~28.0) = 0.65161

P(hl: NO | bmi: ~28.0, gd: Male) = 0.31627
P(hl: NO | bmi: ~28.0) = 0.34839

P(hl: YES | bmi: ~28.0, gd: Female) = 0.61326
P(hl: YES | bmi: ~28.0) = 0.65161

P(hl: NO | bmi: ~28.0, gd: Female) = 0.38674
P(hl: NO | bmi: ~28.0) = 0.34839

P(hl: YES | bmi: <18.5, gd: Male) = 0.10009
P(hl: YES | bmi: <18.5) = 0.08778

P(hl: NO | bmi: <18.5, gd: Male) = 0.89991
P(hl: NO | bmi: <18.5) = 0.91222

P(hl: YES | bmi: <18.5, gd: Female) = 0.07543
P(hl: YES | bmi: <18.5) = 0.08778

P(hl: NO | bmi: <18.5, gd: Female) = 0.92457
P(hl: NO | bmi: <18.5) = 0.91222
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SUFFICIENT

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P(bmi: ~18.5 | hl: YES, gd: Male) = 0.19853
P(bmi: ~18.5 | hl: YES) = 0.19853

P(bmi: ~24.0 | hl: YES, gd: Male) = 0.46963
P(bmi: ~24.0 | hl: YES) = 0.46963

P(bmi: ~28.0 | hl: YES, gd: Male) = 0.32815
P(bmi: ~28.0 | hl: YES) = 0.32815

P(bmi: <18.5 | hl: YES, gd: Male) = 0.00368
P(bmi: <18.5 | hl: YES) = 0.00368

P(bmi: ~18.5 | hl: YES, gd: Female) = 0.19853
P(bmi: ~18.5 | hl: YES) = 0.19853

P(bmi: ~24.0 | hl: YES, gd: Female) = 0.46963
P(bmi: ~24.0 | hl: YES) = 0.46963

P(bmi: ~28.0 | hl: YES, gd: Female) = 0.32815
P(bmi: ~28.0 | hl: YES) = 0.32815

P(bmi: <18.5 | hl: YES, gd: Female) = 0.00368
P(bmi: <18.5 | hl: YES) = 0.00368

P(bmi: ~18.5 | hl: NO, gd: Male) = 0.4918
P(bmi: ~18.5 | hl: NO) = 0.4918

P(bmi: ~24.0 | hl: NO, gd: Male) = 0.36267
P(bmi: ~24.0 | hl: NO) = 0.36267

P(bmi: ~28.0 | hl: NO, gd: Male) = 0.11946
P(bmi: ~28.0 | hl: NO) = 0.11946

P(bmi: <18.5 | hl: NO, gd: Male) = 0.02607
P(bmi: <18.5 | hl: NO) = 0.02607

P(bmi: ~18.5 | hl: NO, gd: Female) = 0.4918
P(bmi: ~18.5 | hl: NO) = 0.4918

P(bmi: ~24.0 | hl: NO, gd: Female) = 0.36267
P(bmi: ~24.0 | hl: NO) = 0.36267

P(bmi: ~28.0 | hl: NO, gd: Female) = 0.11946
P(bmi: ~28.0 | hl: NO) = 0.11946

P(bmi: <18.5 | hl: NO, gd: Female) = 0.02607
P(bmi: <18.5 | hl: NO) = 0.02607
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