

(1)  $A \rightarrow C \rightarrow Y$

Y	C	A	
0	0	0	0.08
0	0	1	0.04
0	1	0	0.06
0	1	1	0.08
1	0	0	0.12
1	0	1	0.06
1	1	0	0.24
1	1	1	0.32

$$P(A)=0.5 \quad P(C|Y)=0.8 \quad P(C|\sim Y)=0.6$$

$$P(Y|A)=0.8 \quad P(Y|\sim A)=0.6$$

$$P(Y|C,A) = \frac{0.32}{0.4} = 0.8$$

$$P(Y|C) = \frac{0.56}{0.7} = 0.8$$

$$P(C|Y,A) = \frac{0.32}{0.38} \approx 0.84$$

$$P(C|Y) = \frac{0.56}{0.74} \approx 0.75$$

(2)  $A \rightarrow Y \rightarrow C$

Y	C	A	
0	0	0	0.09
0	0	1	0.105
0	1	0	0.21
0	1	1	0.245
1	0	0	0.08
1	0	1	0.06
1	1	0	0.12
1	1	1	0.09

$$P(A)=0.5 \quad P(Y|A)=0.3 \quad P(Y|\sim A)=0.4$$

$$P(C|Y)=0.6 \quad P(C|\sim Y)=0.7$$

$$P(C|YA) = \frac{0.09}{0.15} = 0.6$$

$$P(C|Y) = \frac{0.21}{0.35} = 0.6$$

$$P(Y|C,A) = \frac{0.09}{0.335} \approx 0.27$$

$$P(Y|C) = \frac{0.21}{0.665} \approx 0.31$$