

Q3

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Ex 1: Separated but not sufficient.

Let $A = \text{Gender}$, $C = \text{Diabetes}$, $Y = \text{Hyperlipidemia}$

Then $A \perp\!\!\!\perp C|Y$ but $A \not\perp\!\!\!\perp Y|C$.

The following is the joint probabilities table representing
 $P(\text{Hyperlipidemia}, \text{Diabetes}, \text{Gender})$

Hyperlipidemia	Diabetes	Gender	$P(\text{Hyperlipidemia}, \text{Diabetes}, \text{Gender})$
Yes	Yes	Male	$0.405 \times 0.646 \times 0.571 = 0.149$
Yes	Yes	Female	$0.405 \times 0.646 \times 0.429 = 0.112$
Yes	No	Male	$0.405 \times 0.354 \times 0.571 = 0.082$
Yes	No	Female	$0.405 \times 0.354 \times 0.429 = 0.062$
No	Yes	Male	$0.595 \times 0.385 \times 0.494 = 0.113$
No	Yes	Female	$0.595 \times 0.385 \times 0.506 = 0.116$
No	No	Male	$0.595 \times 0.615 \times 0.494 = 0.181$
No	No	Female	$0.595 \times 0.615 \times 0.506 = 0.185$

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Ex 2: Sufficient but not Separated.

Let $A = \text{Gender}$, $C = \text{Hyperlipidemia}$, $Y = \text{Central Obesity}$.

Then $A \perp\!\!\!\perp Y|C$, but $A \perp\!\!\!\perp C|Y$.

The following is the joint probabilities table representing:

$P(\text{Central Obesity}, \text{Hyperlipidemia}, \text{Gender})$

Central Obesity	Hyperlipidemia	Gender	$P(\text{Central Obesity}, \text{Hyperlipidemia}, \text{Gender})$
Yes	Yes	Male	$0.666 \times 0.479 \times 0.571 = 0.182$
Yes	Yes	Female	$0.666 \times 0.479 \times 0.429 = 0.137$
Yes	No	Male	$0.666 \times 0.521 \times 0.494 = 0.171$
Yes	No	Female	$0.666 \times 0.521 \times 0.506 = 0.176$
No	Yes	Male	$0.334 \times 0.258 \times 0.571 = 0.049$
No	Yes	Female	$0.334 \times 0.258 \times 0.429 = 0.037$
No	No	Male	$0.334 \times 0.742 \times 0.494 = 0.122$
No	No	Female	$0.334 \times 0.742 \times 0.506 = 0.125$