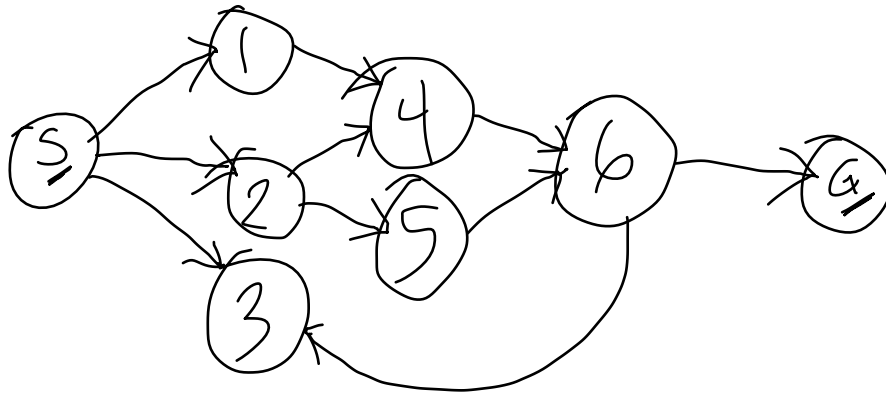
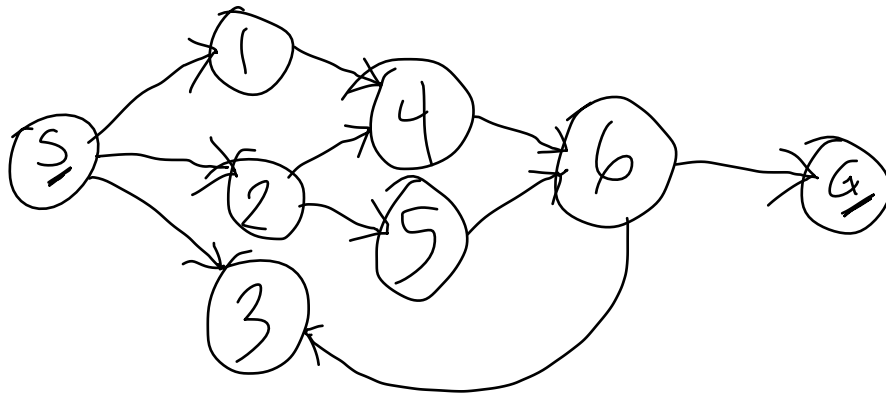


Let's remember BFS.



Draw the search tree



# Define Search Properties

1. Completeness

2. Optimality

3. Time Complexity

4. Space Complexity

# Breadth-First Properties

Completeness?

Optimality?

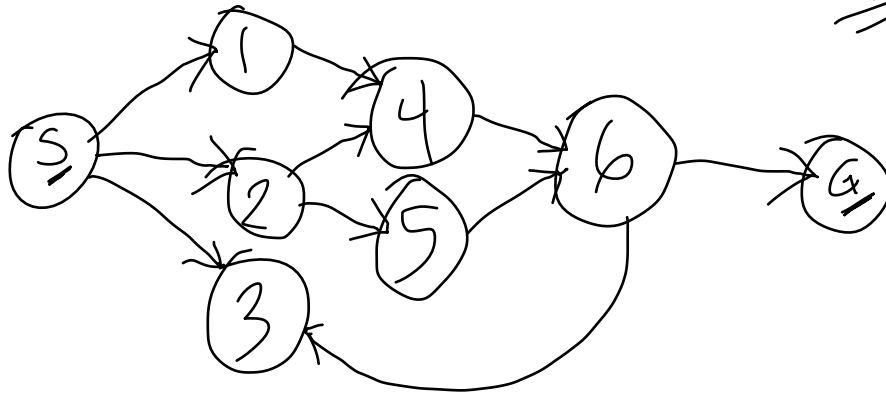
Record your answer here: <https://forms.gle/2krMifrptgaEDYyw9>

What is the Time Complexity?

What is the Space Complexity?

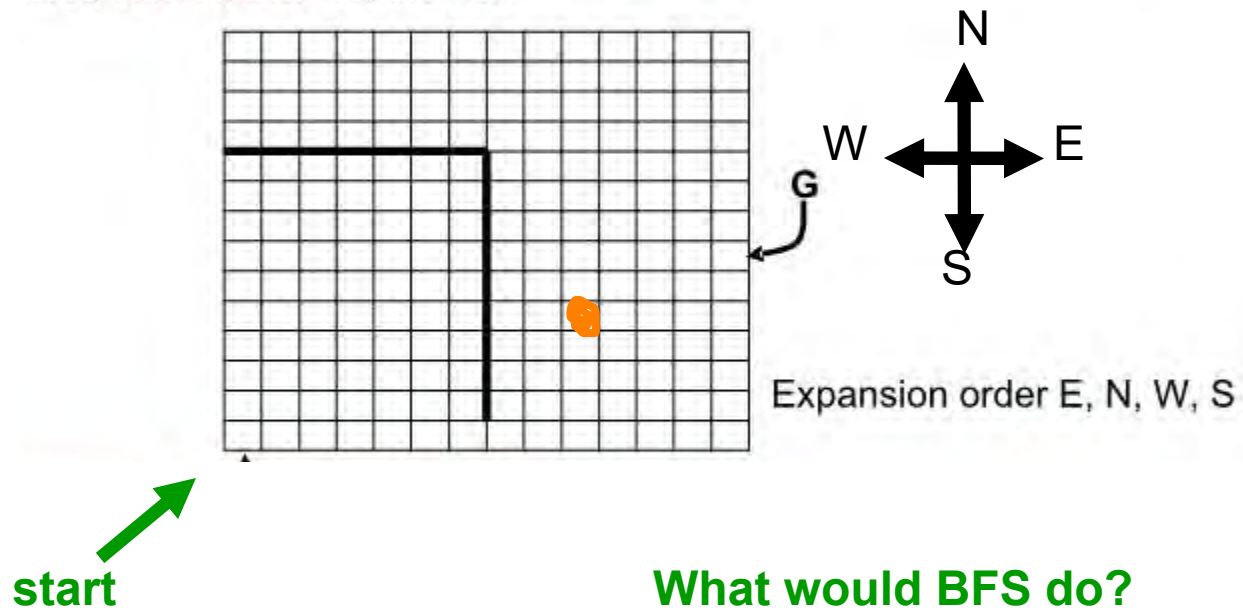
Record your answer here: <https://forms.gle/2krMifrptgaEDYyw9>

Let's search the same graph  
with Depth First Search



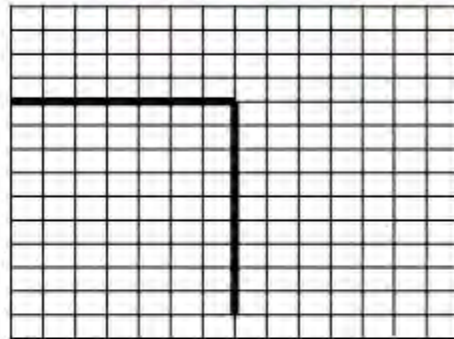
## Maze example

Imagine states are cells in a maze, you can move N, E, S, W. What would **plain DFS** do, assuming it always expanded the E successor first, then N, then W, then S?

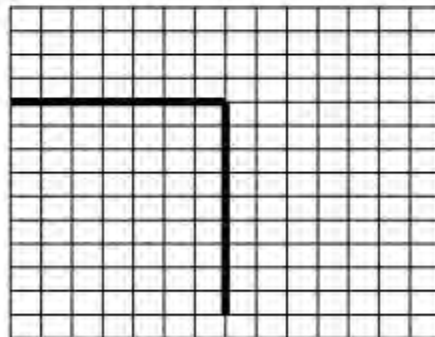


Record your answer here: <https://forms.gle/2PFoGVQG9Yiu95hV6>

## Two other DFS examples



Order: N, E, S, W?



Order: N, E, S, W  
with loops prevented





# Depth-First Properties

Complete?

Optimal?

# Depth-First Properties

Time Complexity?

Space Complexity?

# Depth Limited Search

```
DLS (Frontier, Successors, Goal?) /* Call with Frontier = {<START>} */
```

```
    WHILE (Frontier not EMPTY) {
```

```
        n= select first node from Frontier
```

```
        Curr = terminal state of n
```

```
        If(Goal?(Curr)) return n
```

```
        If Depth(n) < D //Don't add successors if Depth(n) = D!!
```

```
            Frontier= (Frontier- {n}) U Successors(Curr)
```

```
        Else
```

```
            Frontier= Frontier- {n}
```

```
            CutOffOccured = TRUE.
```

```
    }
```

```
    return FAIL
```

# Iterative Deepening Search

- Solve the problems of depth-first and breadth-first by extending depth limited search.
- Starting at depth limit  $L = 0$ , we iteratively increase the depth limit, performing a depth limited search for each depth limit.
- Stop if a solution is found, or if the depth limited search failed without cutting off any nodes because of the depth limit.
  - If no nodes were cut off, the search examined all paths in the state space and found no solution  $\rightarrow$  no solution exists.

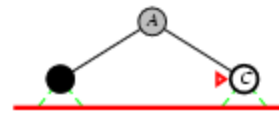
# Iterative Deepening Search

Limit = 0



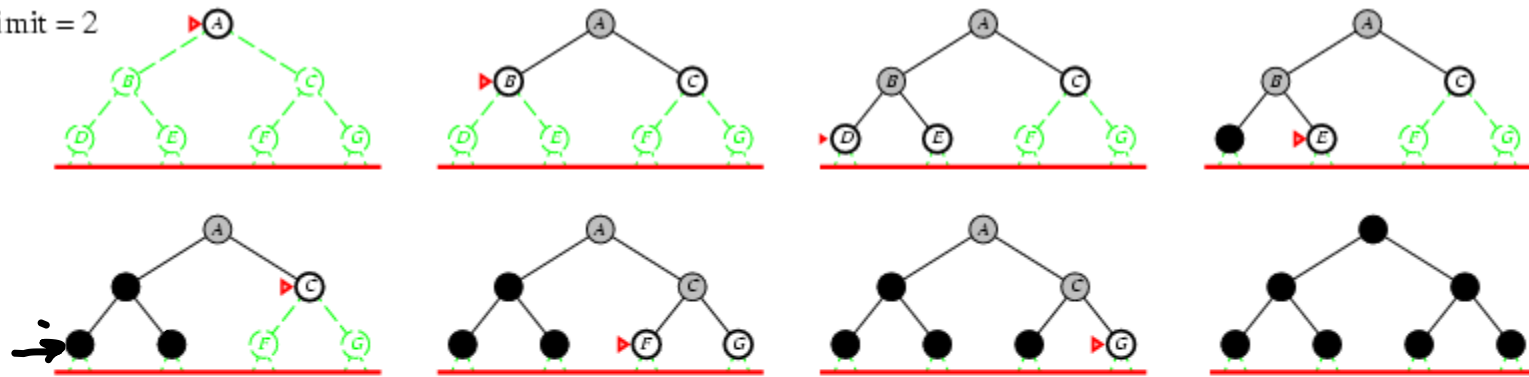
# Iterative Deepening Search

Limit = 1



# Iterative Deepening Search

Limit = 2



# Iterative Deepening Search

Completeness?

Optimality?

Space Complexity?



Iterative deepening complexity?

what's better? BFS or iterative deepening DFS?

# Path Checking

Recall that paths are commonly stored on the Frontier.

If  $n_k$  represents the path  $\langle s_0, s_1, \dots, s_k \rangle$  and we expand  $s_k$  to obtain child  $c$ , we have

$$\langle s_0, s_1, \dots, s_k, c \rangle$$

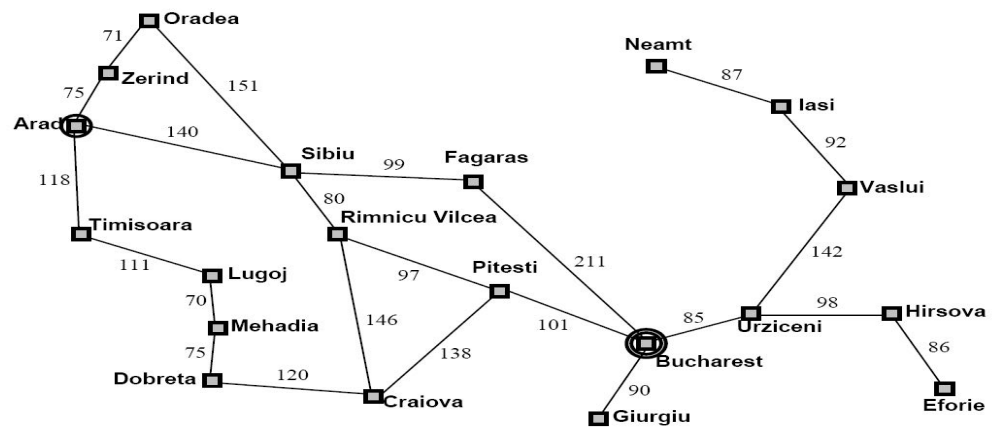
as the path to “ $c$ ”.

Path checking:

- Ensure that the state  $c$  is not equal to the state reached by any ancestor of  $c$  along this path.
- Paths are checked in isolation!

# Cycle Checking

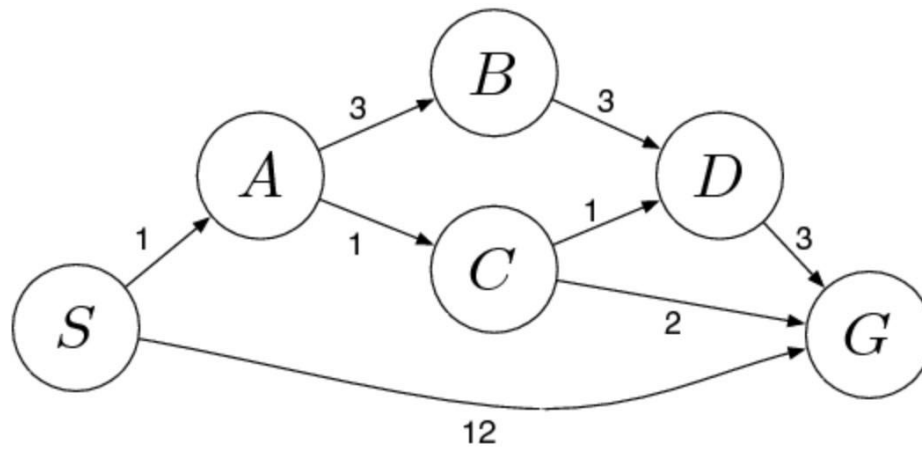
- Keep track of **all states** previously expanded during the search.
- When we expand  $n_k$  to obtain child  $c$ 
  - Ensure that  $c$  is not equal to **any** previously expanded state.
- This is called **cycle checking**, or **multiple path checking**.
- What happens when we utilize this technique with depth-first search?
  - **What happens to space complexity?**



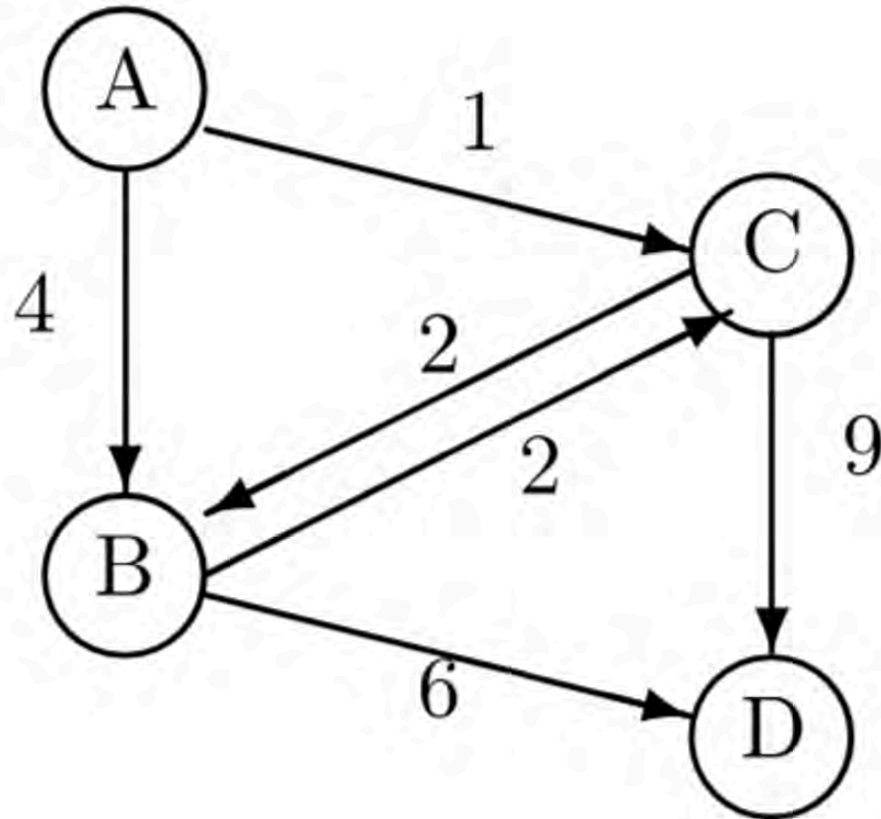
# Uniform-Cost Search

- Keeps **Frontier** ordered by **increasing cost of the path** (*know a good data structure for this?*)
- Always expand the **least cost path**.
- Identical to Breadth First Search if each action has the same cost

1. Illustrate the frontier at each iteration of Uniform Cost Search for a search from the start (S) to the goal (G) for the following problem:



# Problem!



$$h(A) = 8$$

$$h(B) = 3$$

$$h(C) = 7$$

$$h(D) = 0$$

START = A  
GOAL = D