

Brief history of causal inference, 80's

- James Robins discovered - and solved - some important problems with longitudinal studies, from a causal inference perspective
 - Marginal Structural Models (MSMs)**
 - Structural Nested Models (SNMs)**



Brief history of causal inference, 90's

- Judea Pearl developed **Directed Acyclic Graphs (DAGs)**
 - Simplify interpretation and communication in causal inference
 - Useful for covariate selection in observational studies



Outline

Motivating example

DAG terminology

Covariate selection in DAGs

Motivating example, revisited

Potential problems

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Motivating example, revisited

Potential problems

Statistical association

- Research question: does smoking during pregnancy (SDP) cause malformations in newborns?
- For a large number of pregnancies, we collect data on both exposure and outcome
- Suppose that we observe an inverse statistical association between SDP and malformations ($RR = 0.8$)
- *Can we then say that SDP protects against malformations?*

A possible non-causal explanation

- Young mothers smoke more often than old mothers
- Young mothers have smaller risk for malformations in their babies, than old mothers
- Hence, smokers are more likely to be young, and for this reason less likely to have babies with malformations, than non-smokers
 - Even in the absence of a causal effect

Confounding

- Mothers age is a potential 'confounder' that may induce non-causal associations between SDP and malformations
 - There are several definitions of the term 'confounder' in the literature - more later
- *How can we eliminate the influence of confounders?*

Randomization

- By randomizing the exposure, we guarantee that there are no systematic differences between exposed and unexposed
 - Same distribution of age, sex, ethnicity, genes etc
- In an ideal randomized controlled trial (RCT) there is no confounding
 - Observed statistical associations can be given causal interpretations
- *Any problems?*

Problems with randomized trials

- Unethical
- Expensive
- Unpractical
- Non-compliance
- Non-blinding
- etc

Adjusting for potential confounders in the analysis

- Suppose that we stratify the sample on age
 - Each stratum contains women of similar age
- Each stratum is analyzed separately
- Within-stratum associations can not be attributed to different age distribution between exposed and unexposed
- The confounding influence of age is eliminated
- *Any problems?*

Problems with confounder adjustment

- We can only adjust for confounders that
 - we are aware of
 - we have measured
- Often many potential confounders are unknown to the investigator, and/or difficult/expensive to measure
 - e.g. genetics, lifestyle factors

Technical note

- There are several methods for confounding adjustments, which are often combined
 - stratification
 - matching
 - standardization
 - propensity scores
 - regression modeling
 - inverse probability weighting
 - etc
- For realistic sample sizes, these methods have different pros and cons
- For HUGE samples, they are equivalent
- We use the term ‘adjusting’ generically, for any of the methods

Motivating example revisited

- Suppose that we have measured five covariates:
 - the mothers age at conception
 - the mothers socioeconomic status/education level at conception
 - the mothers diet during pregnancy
 - indicator of whether there is a family history of birth defects
 - indicator of whether the baby was liveborn or stillborn
- Which of these are 'true' confounders, i.e. which should we adjust for?

The need for covariate selection

- One strategy would be to adjust for all measured covariates
- This strategy may not be optimal, because
 - **some covariates may not be confounders, and may increase bias if adjusted for**
 - more covariates requires a bigger model, with a higher potential for bias due to model misspecification
 - some covariates may be prone to measurement errors, and may therefore lead to bias
 - some covariates may reduce statistical power/efficiency when adjusted for
- Therefore, it is often desirable to adjust for a subset of covariates

Traditional covariate selection strategies

- Adjust for covariates that are selected in a stepwise regression procedure
- Adjust for covariates that change the point estimate of interest with more than 10%
- Adjust for covariates that
 - are associated with the exposure, and
 - are conditionally associated with the outcome, given the exposure, and
 - are not in the causal pathway between exposure and outcome

Problems with traditional strategies

- They rely on statistical analyses of observed data, rather than *a priori* knowledge about causal structures
 - require that data is already collected, and cannot not be used at the design stage
- They may select non-confounders, which may increase bias if adjusted for

Directed Acyclic Graphs

- Directed Acyclic Graphs (DAGs) can be used to overcome the problems with traditional covariate selection strategies
- A DAG is a graphical representation of underlying causal structures
- DAGs for covariate selection:
 - encode our *a priori* causal knowledge/beliefs into a DAG
 - apply simple graphical rules to determine what covariates to adjust for

Outline

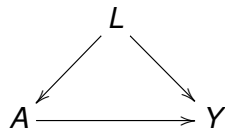
Motivating example

DAG terminology

Covariate selection in DAGs

Motivating example, revisited

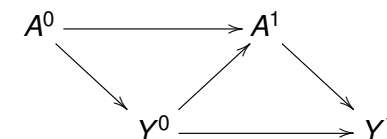
A simple DAG



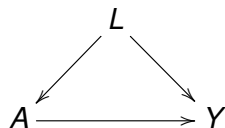
- Each arrow represents a causal influence
- The graph is
 - Directed, since each connection between two variables consists of an arrow
 - Acyclic, since the graph contains no directed cycles
- Formal connection to potential outcomes/counterfactuals through non-parametric structural equations
 - beyond the scope of this course

A note on acyclicity

- We impose acyclicity since a variable can't cause itself
 - e.g. my BMI today has no effect on my BMI today
- Observed variables are often snapshots of time varying processes
 - e.g. my BMI today certainly affects my BMI tomorrow
- Time varying processes can be depicted by explicitly adding one 'realization' of each variable per time unit
 - more later



Underlying assumptions



- Assumptions are encoded by the direction of arrows
 - the arrow from A to Y means that A may affect Y , but not the other way around

Underlying assumptions, cont'd



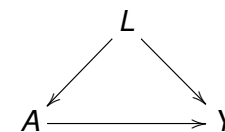
- Assumptions are encoded by the absence of arrows
 - the presence of an arrow from A to Y means that A may or may not affect Y
 - the absence of an arrow from A to Y means that A does not affect Y

Underlying assumptions, cont'd



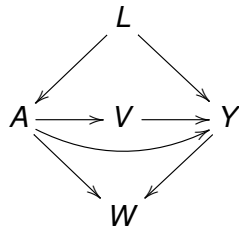
- Assumptions are encoded by the absence of common causes
 - the presence of L means that A and Y may or may not have common causes
 - the absence of L means that A and Y do not have any common causes

Ancestors and descendants



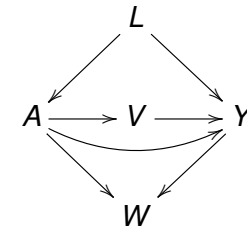
- The ancestors of a variable V are all other variables that affect V , either directly or indirectly
 - L is the single ancestor of A
- The descendants of a variable V are all other variables that are affected by V , either directly or indirectly
 - Y is the single descendent of A

Paths



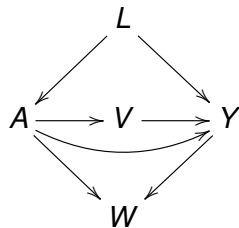
- A path is a route between two variables, not necessarily following the direction of arrows
- Which are the paths between A and Y?

Solution



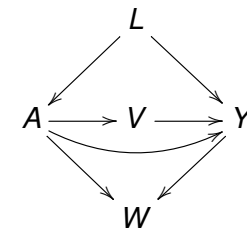
- Four paths between A and Y:
 - $A \rightarrow Y$
 - $A \rightarrow V \rightarrow Y$
 - $A \leftarrow L \rightarrow Y$
 - $A \rightarrow W \leftarrow Y$

Causal paths



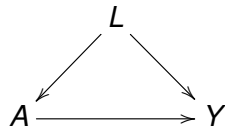
- A causal path is a route between two variables, **following the direction of arrows**
 - the causal paths from A to Y mediate the causal effect of A on Y, the non-causal paths do not
- Which are the causal paths between A and Y?

Solution



- Two causal paths from A to Y:
 - $A \rightarrow Y$
 - $A \rightarrow V \rightarrow Y$

Blocking of paths



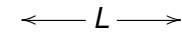
- Paths (both causal and non-causal) are either open or blocked, according to two rules

Rule 1

- A path is blocked if somewhere along the path there is a variable L that sits in a 'chain'



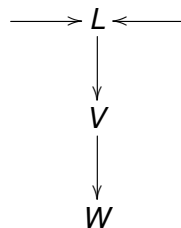
or in a 'fork'



and we have adjusted for L

Rule 2

- A path is blocked if somewhere along the path there is a variable L that sits in an 'inverted fork'



and we have **not** adjusted for L , or any of its descendents

Once blocked stays blocked



- Adjusting for V blocks the path from A to W (rule 1)
- Adjusting for W leaves the path open (rule 2)
- Adjusting for both V and W blocks the path

Outline

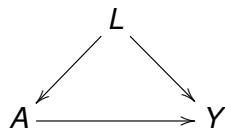
Motivating example

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Covariate selection in DAGs

Motivating example, revisited

Example

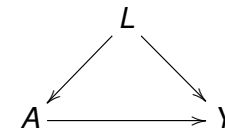


- Suppose that the DAG above depicts the true causal structure
- We want to test whether there is a causal effect of A on Y
 - i.e. does the causal path $A \rightarrow Y$ exist?
- *Adjust or not adjust for L ?*

Relation between 'blocking' and independence

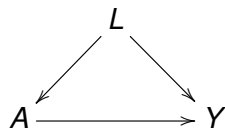
- If all paths between A and Y are blocked, then A and Y are independent
- Conversely: if there is an association between A and Y , then there is at least one open path between A and Y

Heuristic argument



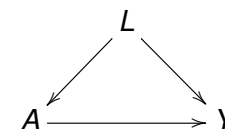
- A = smoking, Y = malformations, L = age
- Young mothers smoke more often, but their babies have smaller risk for malformations, than old mothers
- Hence, smokers are more likely to be young, and for this reason less likely to have babies with malformations, than non-smokers
- Thus, by not adjusting for age, we may observe an inverse association between smoking and malformations, even in the absence of a causal effect

Formal solution



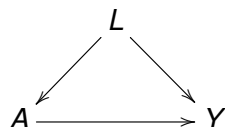
- Suppose that we don't adjust for L , and that we observe an association between A and Y
- There are two explanations for this association:
 - the causal path $A \rightarrow Y$
 - the open non-causal path $A \leftarrow L \rightarrow Y$ (Rule 1)
- Hence, an unadjusted association between A and Y does not prove that the causal path $A \rightarrow Y$ exists

Formal solution, cont'd



- Suppose that we adjust for L
 - we block the non-causal path $A \leftarrow L \rightarrow Y$ (Rule 1)
- Suppose that we observe an association between A and Y
 - this can only be explained by the causal path $A \rightarrow Y$
- Hence, an adjusted association between A and Y proves that there is a causal effect of A on Y

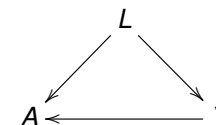
Conclusion



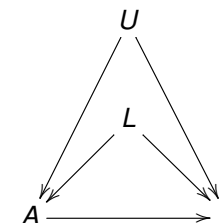
- If the aim is to test for a causal effect of A on Y , then we should adjust for L

Remark

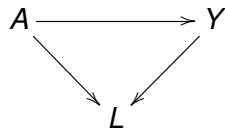
- Adjusting for L does not give a causal effect if the DAG is incorrect, e.g. if
 - Y causes A



- there are additional common causes of A and Y

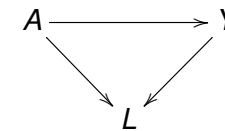


Example



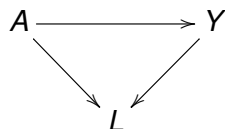
- Suppose that the DAG above depicts the true causal structure
- We want to test whether there is a causal effect of A on Y
 - i.e. does the causal path $A \rightarrow Y$ exist?
- *Adjust or not adjust for L ?*

Heuristic argument



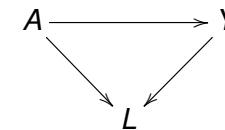
- A = smoking, Y = malformations, L = birth status (live/stillborn)
- Smoking and malformations increase the risk for stillbirth
- Consider the group of woman who has stillbirths: **what caused the stillbirths?**

Heuristic argument, cont'd



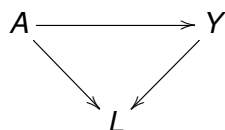
- For the non-smokers who had a stillbirth, smoking was obviously not the cause
 - perhaps malformations then?
- When smoking is ruled out as the cause of malformation, the likelihood of malformation increases
 - an inverse non-causal association between smoking and malformation!
- Thus, by adjusting for (e.g. stratifying on) birth status, we may observe an inverse association between smoking and malformations, even in the absence of a causal effect

Formal solution



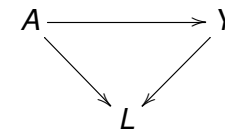
- Suppose that we adjust for L , and that we observe an association between A and Y
- There are two explanations for this association:
 - the causal path $A \rightarrow Y$
 - the open non-causal path $A \rightarrow L \leftarrow Y$ (Rule 2)
- Hence, an adjusted association between A and Y does not prove that the causal path $A \rightarrow Y$ exists

Formal solution, cont'd



- Suppose that we don't adjust for L
 - we block the non-causal path $A \rightarrow L \leftarrow Y$ (Rule 2)
- Suppose that we observe an association between A and Y
 - this can only be explained by the causal path $A \rightarrow Y$
- Hence, an unadjusted association between A and Y proves that there is a causal effect of A on Y

Conclusion

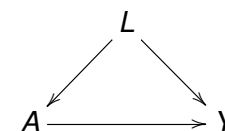


- If the aim is to test for a causal effect of A on Y , then we should not adjust for L

General strategy for covariate selection

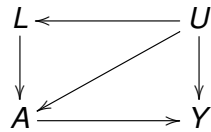
- We should adjust for those covariates that block non-causal paths between the exposure and the outcome
- We should not adjust for those covariates that open non-causal paths between the exposure and the outcome
- If we manage to block all non-causal paths, then any observed association must be due to a causal effect
- Thus, if all non-causal paths are blocked, then we have a valid test for causation

Confounding



- Common causes of the exposure and the outcome lead to non-causal paths
- We say that there is **confounding** if the exposure and the outcome have common causes

Confounder



- A **confounder** is a variable that blocks a non-causal path between the exposure and the outcome, if adjusted for
 - both L and U are confounders in the DAG above
- A (set of) variable(s) is **sufficient for confounding control** if the variable(s) blocks all non-causal paths
 - U is sufficient for confounding control, L is not

Outline

Motivating example

DAG terminology

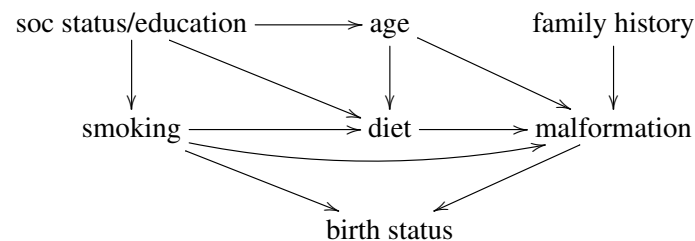
Covariate selection in DAGs

Motivating example, revisited

Potential problems

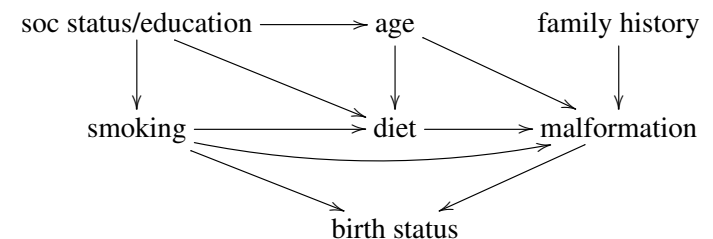
A possible DAG for the motivating example

- Suppose we agree that the causal structures for our data can be described by the DAG below



- Which assumptions are encoded in this DAG?
- Can these assumptions be tested?

Covariate selection



- Given the DAG, which covariates should we adjust for?
- Which covariates would be selected by the traditional strategies?

Outline

Motivating example

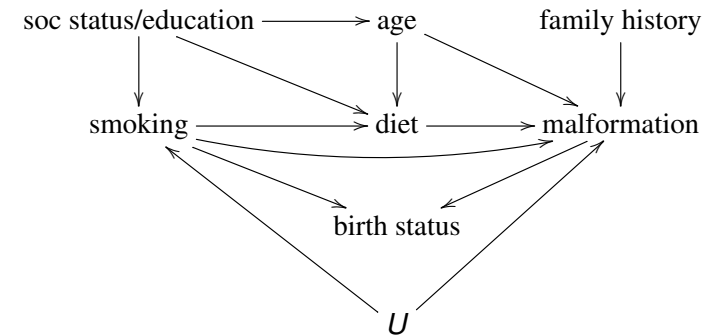
DAG terminology

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Potential problems

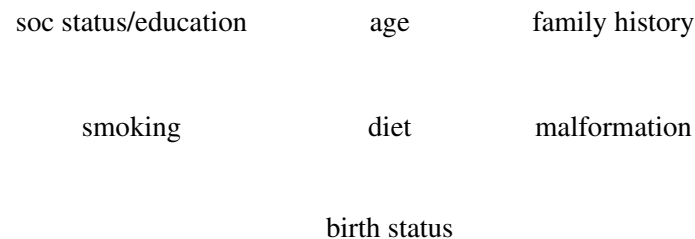
Unmeasured confounding



- Not a problem with DAGs, but with observational studies
- Try to reduce confounding bias as much as possible
 - i.e. block as many non-causal paths as possible

No *a priori* knowledge

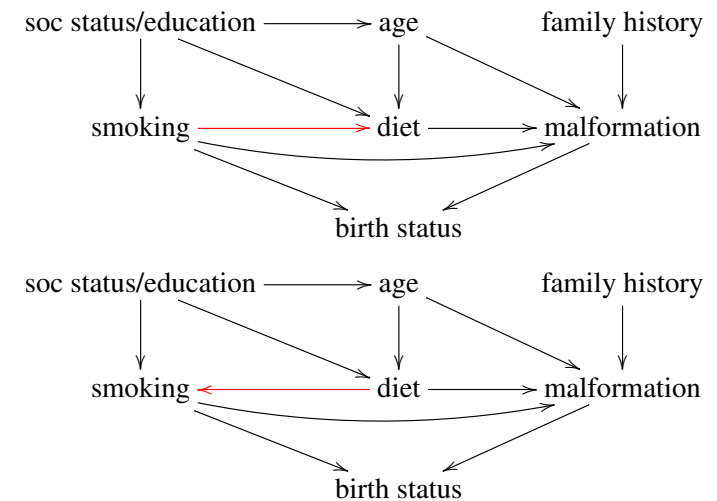
- Cannot construct a plausible DAG



- DAG-based covariate selection cannot be used, and we have to resort to traditional strategies
 - but be aware of the pitfalls

Weak *a priori* knowledge

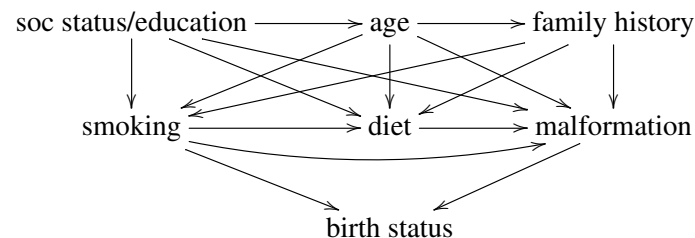
- Cannot settle with **one** plausible DAG



- Present all plausible DAGs, and the implied analyses

A complicated DAG

- No/little covariate reduction



- But remember that
 - more covariates requires a bigger model, with a higher potential for bias due to model misspecification
 - some covariates may be prone to measurement errors, and may therefore lead to bias
 - some covariates may reduce statistical power/efficiency when adjusted for
- It may sometimes be reasonable to exclude covariates with a weak 'confounding effect'

Summary

- Traditional covariate selection strategies
 - are difficult to apply at the design stage
 - may select non-confounders, which may increase bias if adjusted for
- DAGs can be used for covariate selection
 - encode our *a priori* causal knowledge/beliefs into a DAG
 - adjust for those covariates that block non-causal paths between the exposure and the outcome
- DAGs are not only tools for covariate selection
 - generally speaking, they are used to facilitate interpretation and communication in causal inference