

Case 1: Separation holds but not sufficiency

\* these are made up numbers

A	C	Y	$P(A)$	$P(C)$	$P(Y)$	$P(C A)$	$P(A C)$	$P(A C,Y)$	$P(C A,Y)$
0	0	0	0.3	0.4	0.4	0.1	0.075	0.075	0.06
0	0	1	0.3	0.4	0.6	0.1	0.075	0.075	0.09
0	1	0	0.3	0.6	0.4	0.2	0.1	0.1	0.08
0	1	1	0.3	0.6	0.6	0.2	0.1	0.1	0.12
1	0	0	0.7	0.4	0.4	0.1	0.175	0.175	0.14
1	0	1	0.7	0.4	0.6	0.1	0.175	0.175	0.21
1	1	0	0.7	0.6	0.4	0.1	0.117	0.117	0.094
1	1	1	0.7	0.6	0.6	0.1	0.117	0.117	0.14

Highlighted with the same colour means that A is Separated From Y given C, so Separation holds. However, sufficiency does not hold Since  $P(C|A,Y) \neq P(C|A)$