

THE TREE AND THE FOREST

Lior Ben-Gai
December 2019



WHAT'S NEXT?

You are here



Recursion

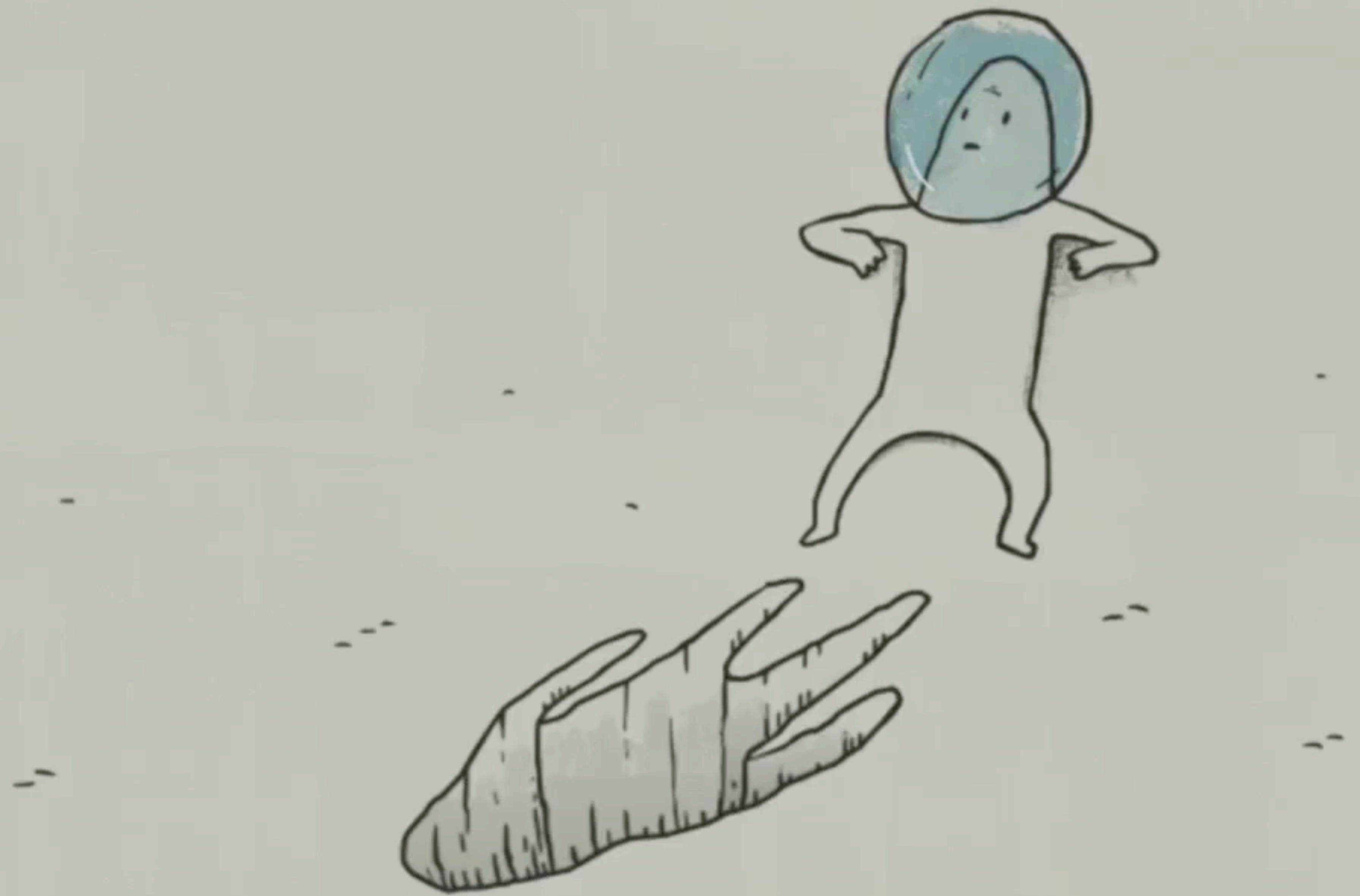
Data structures

Raster graphics

3D graphics and vectors

Intro to HTML

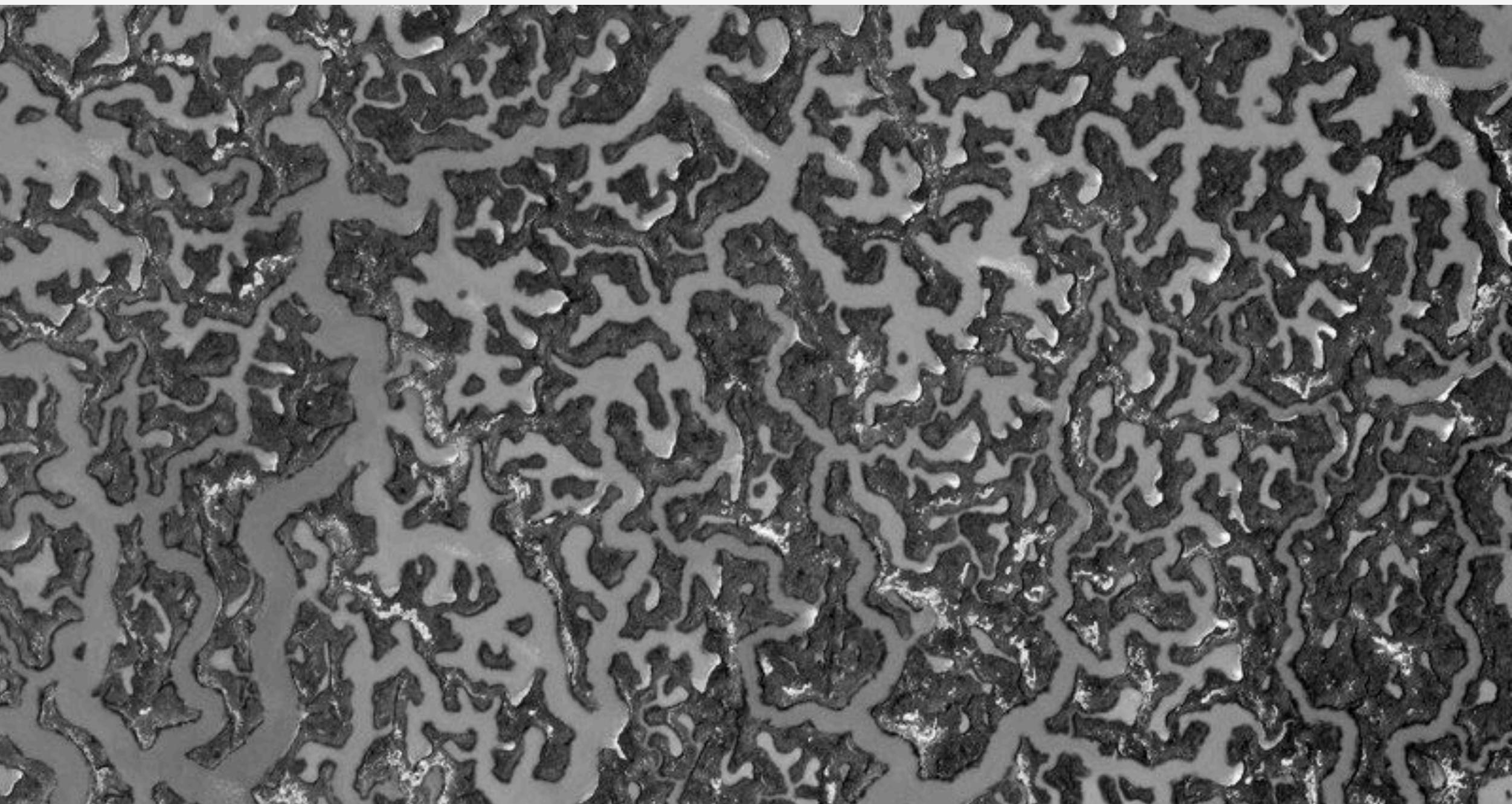
conclusion and submission



UMBRA

Malcolm Sutherland

<https://vimeo.com/14844291>

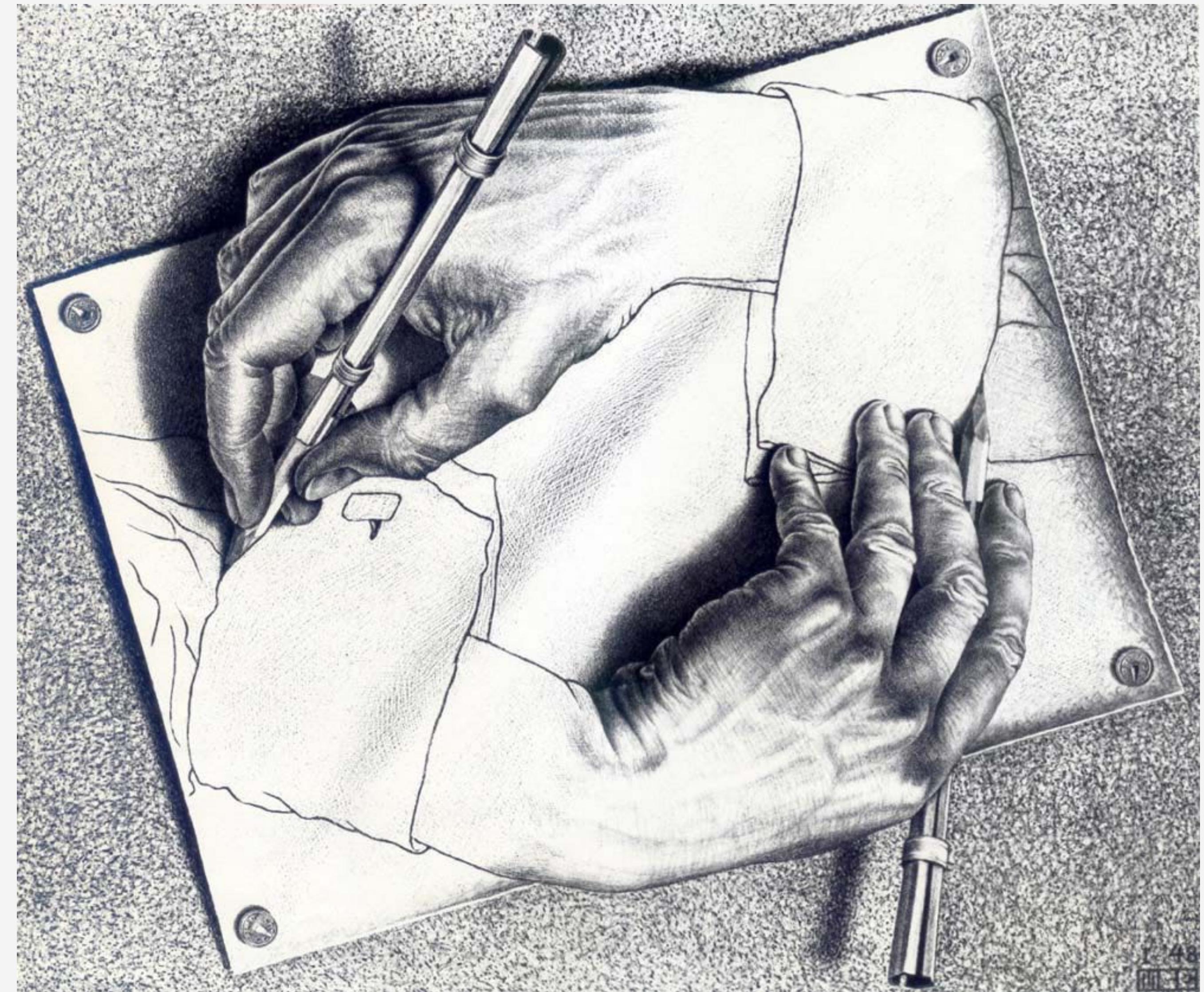


BIG



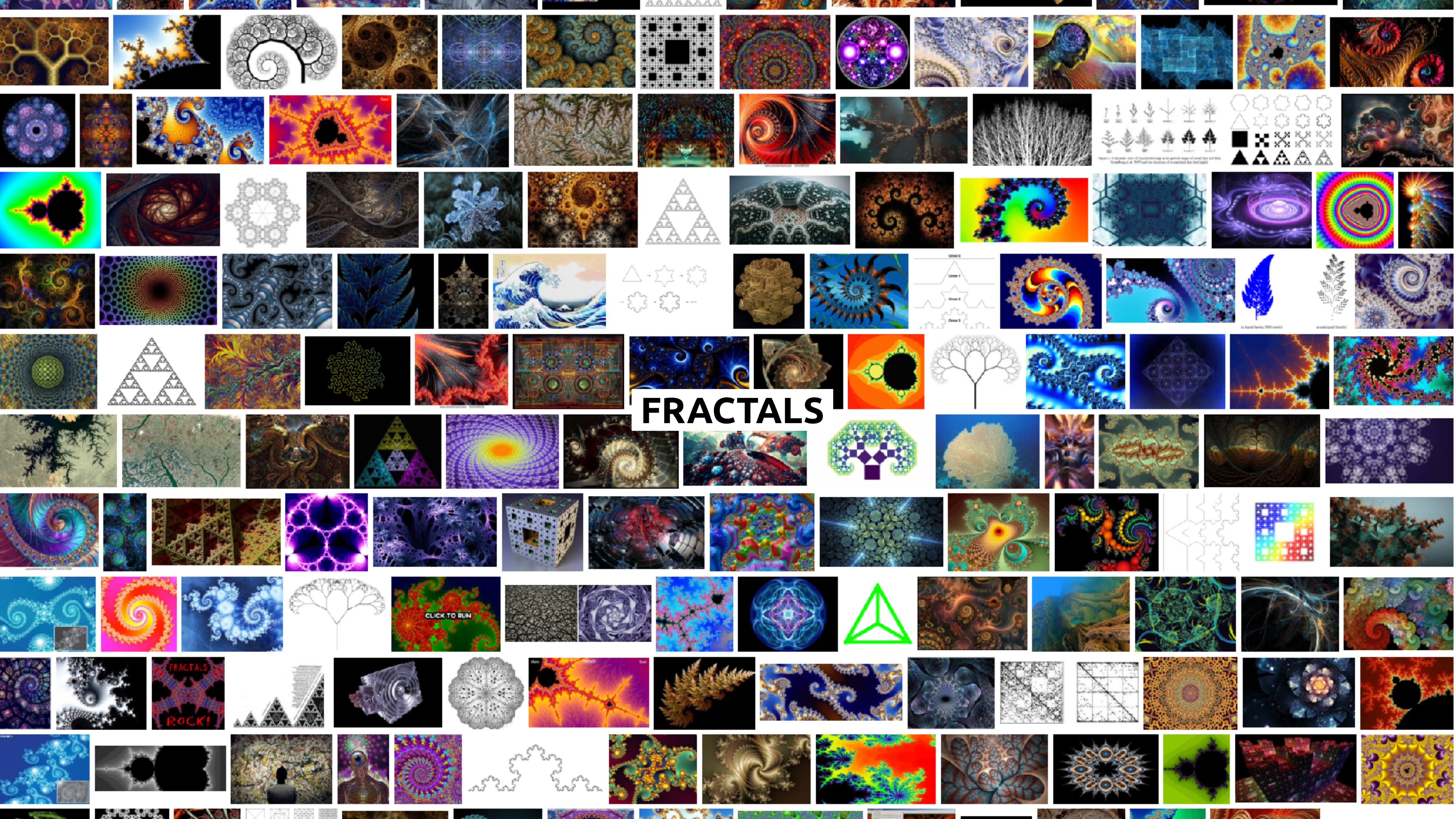
small

SELF-REFERENCE



M.C. Escher
Drawing Hands 1948





FRACTALS

Fractal-like patterns occur widely in nature, in phenomena as diverse as clouds, [river networks](#), [geologic fault lines](#), [mountains](#), [coastlines](#),^[38] [animal coloration](#), [snow flakes](#),^[39] [crystals](#),^[40] [blood vessel branching](#),^[41] and [ocean waves](#).^[42]



Leaf of cow parsley,
Anthriscus sylvestris, is
2- or 3-pinnate, not
infinite



Fractal spirals:
Romanesco broccoli
showing self-similar form



[Angelica](#) flowerhead, a
sphere made of spheres
(self-similar)



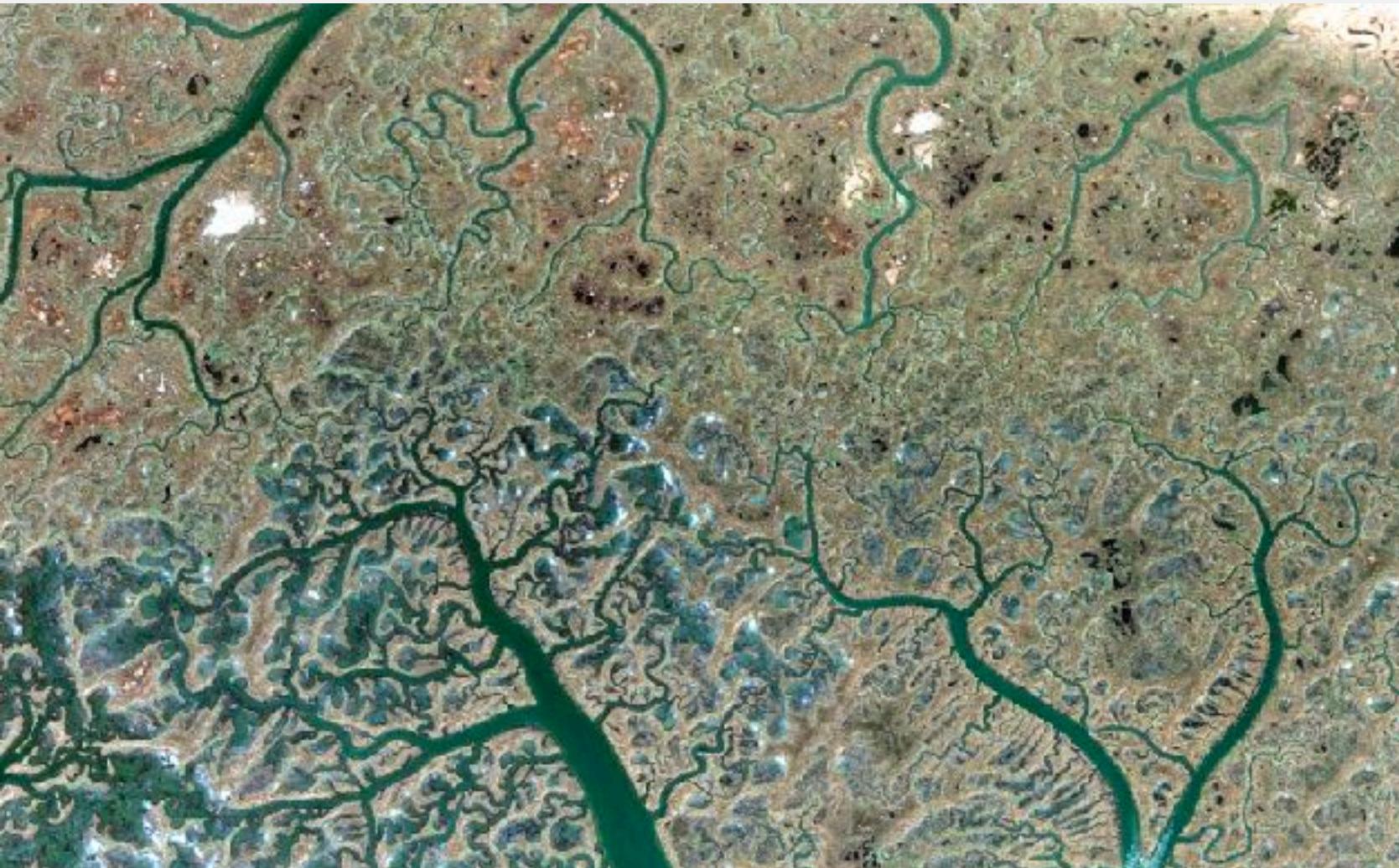
Trees: [Lichtenberg](#)
[figure](#): high voltage
dielectric breakdown in
an acrylic polymer block

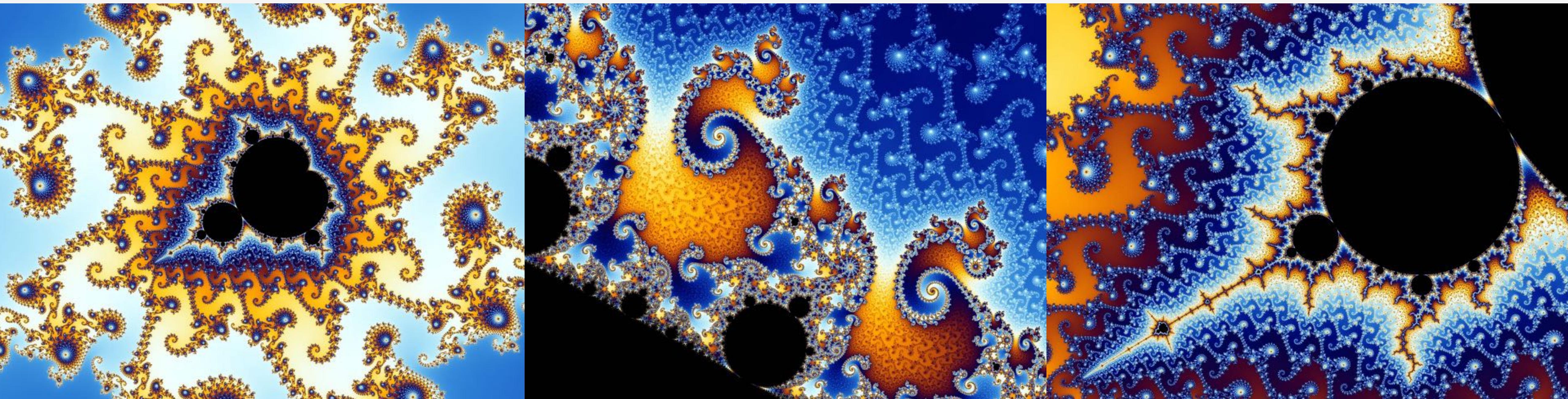


Trees: [dendritic](#) copper
crystals (in microscope)



<http://paulbourke.net/fractals/googleearth/>





MANDELBROT SET

Benoît Mandelbrot

$$z_{\text{new}} = z_{\text{old}}^2 + C$$
The diagram shows the iterative formula for generating the Mandelbrot set. It features a large circle with arrows indicating the iteration process: z_{new} is calculated from z_{old} by squaring it and adding a constant C . To the right, there is a small inset image showing a portion of the Mandelbrot set with specific points labeled 1 and 2, and red lines connecting them to the main formula diagram.

10^{-0}



L-SYSTEMS

<https://en.wikipedia.org/wiki/L-system>

Example 4: Koch curve [edit]

A variant of the Koch curve which uses only right angles.

```
variables : F
constants : + -
start : F
rules : (F → F+F-F-F+F)
```

Here, F means "draw forward", + means "turn left 90°", and – means "turn right 90°" (see [turtle graphics](#)).

$$n = 0;$$

F

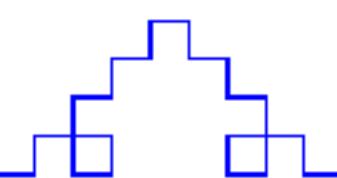
$$n = 1:$$

F+F-F-F+F



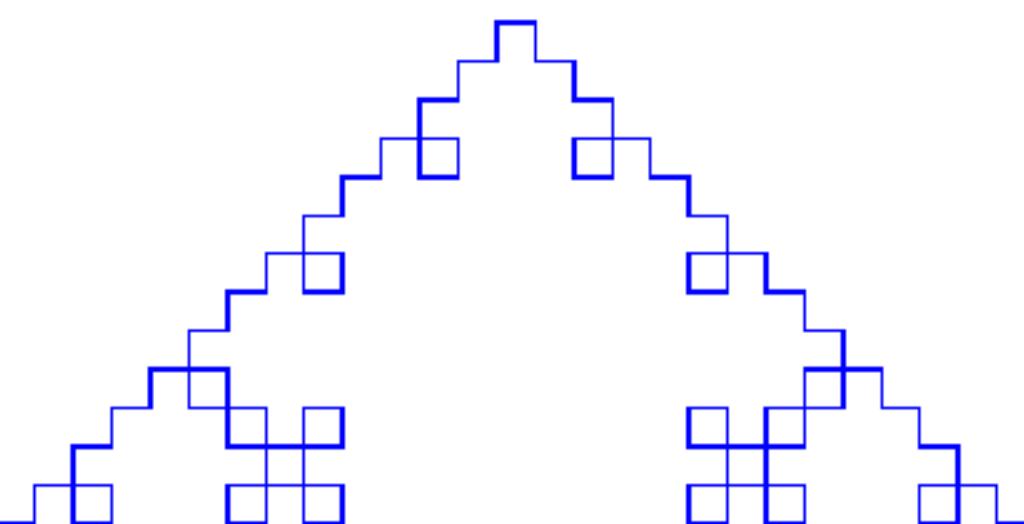
$$n = 2$$

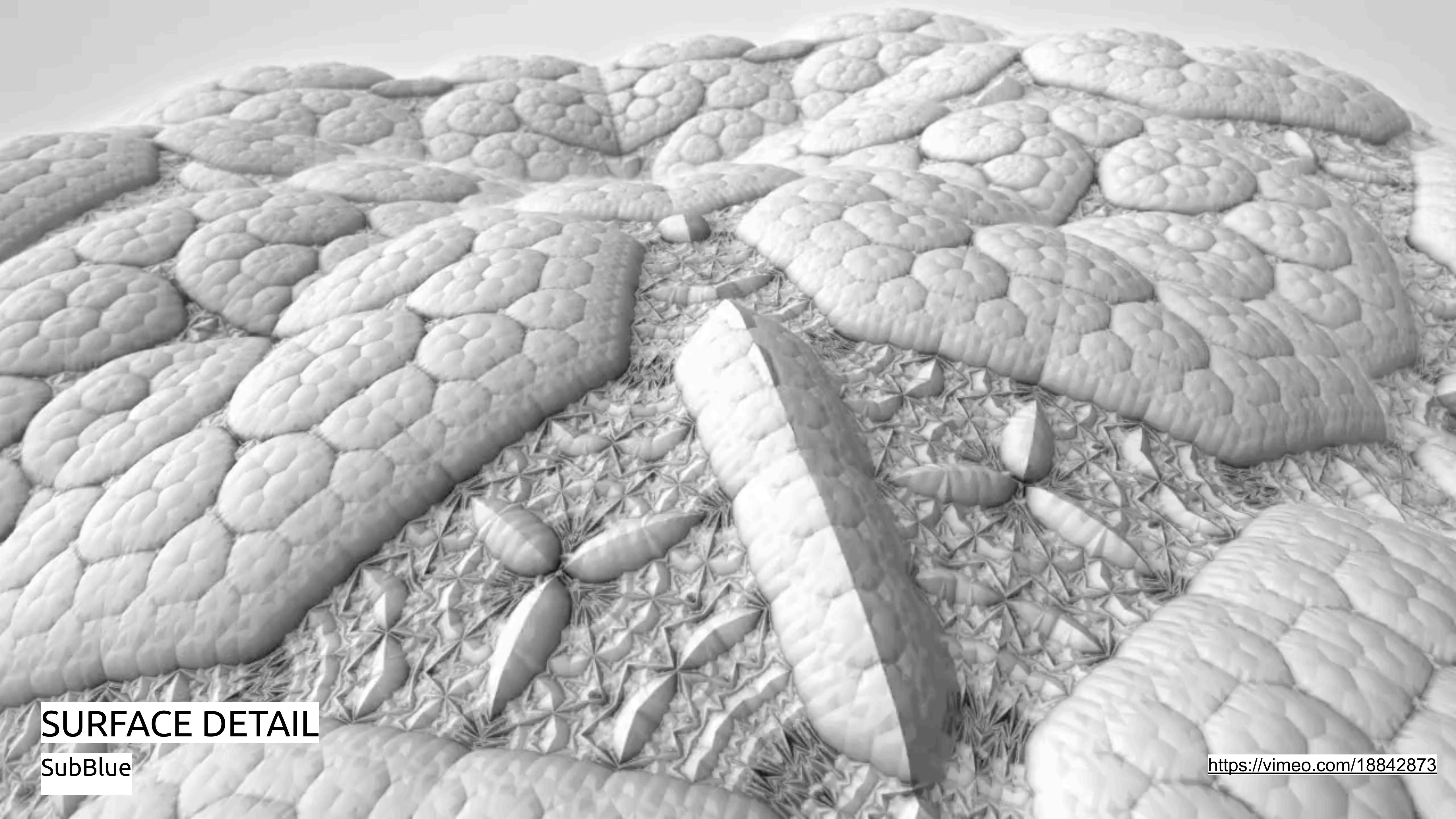
$$F+F-F-F+F + F+F-F-F+F - F+F-F-F+F - F+F-F-F+F + F+F-F-F+F$$



$$n = 3:$$

$F+F-F-F+F+F-F-F+F-F+F-F+F-F+F-F+F-F+F-F+F-F+F+F+F-F-F+F+$
 $F+F-F-F+F+F+F-F-F+F-F+F-F+F-F+F-F+F-F+F-F+F-F+F-F+F-F+F-$
 $F+F-F-F+F+F+F-F-F+F-F+F-F+F-F+F-F+F-F+F+F+F-F+F-F+F-$
 $F+F-F-F+F+F+F-F-F+F-F+F-F+F-F+F-F+F-F+F+F+F-F-F+F+F+$
 $F+F-F-F+F+F+F-F-F+F-F+F-F+F-F+F-F+F-F+F+F+F-F-F+F$





SURFACE DETAIL

SubBlue

<https://vimeo.com/18842873>

localhost:3004/lab.html#/scene/1873

Demo 4

The main view shows a complex 3D scene of a city with numerous skyscrapers and a river. The interface includes a sidebar with 'Account' and 'Settings' buttons, and sections for 'Scenes', 'Explore', 'Renders', and 'Help'. A timeline at the bottom indicates the scene starts at 00:00:00 and ends at 00:00:16s, with a segment labeled 'SEGMENT 01' highlighted in yellow.

STRUCTURE

Mandalay type: Type 1

Basics

- Folding: Scale 2.7778
- Rotation
- Elements: Offset x 1.40741
- Translate: Offset y -0.66667
- Transform: Offset z -0.22222
- Instancing: Radius 0.2222
- Clipping: Bounding radius 1.481
- Complexity: Mandelbrot/Julia 0.000

Edit

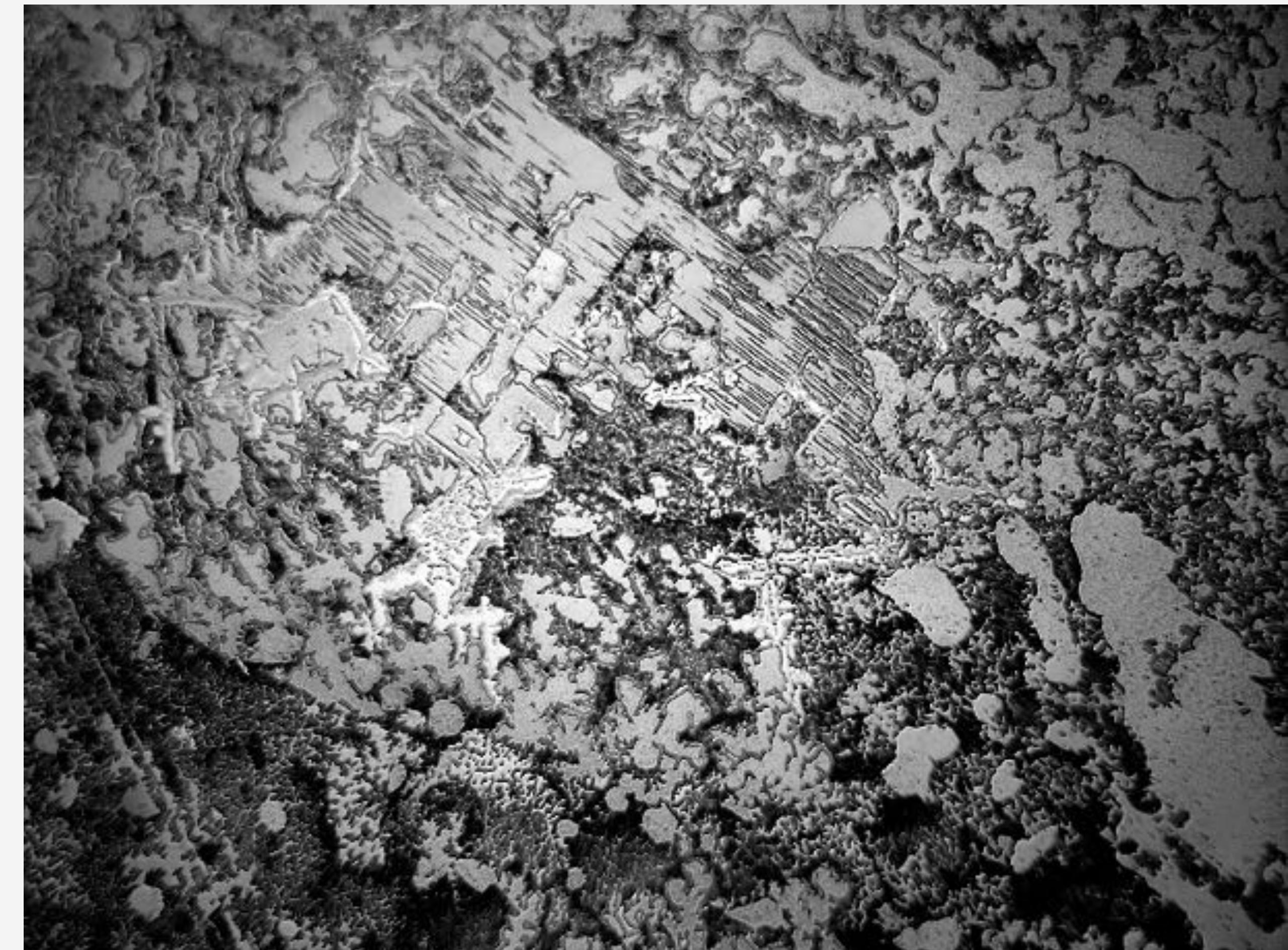
Mandalay

MEMDOTS

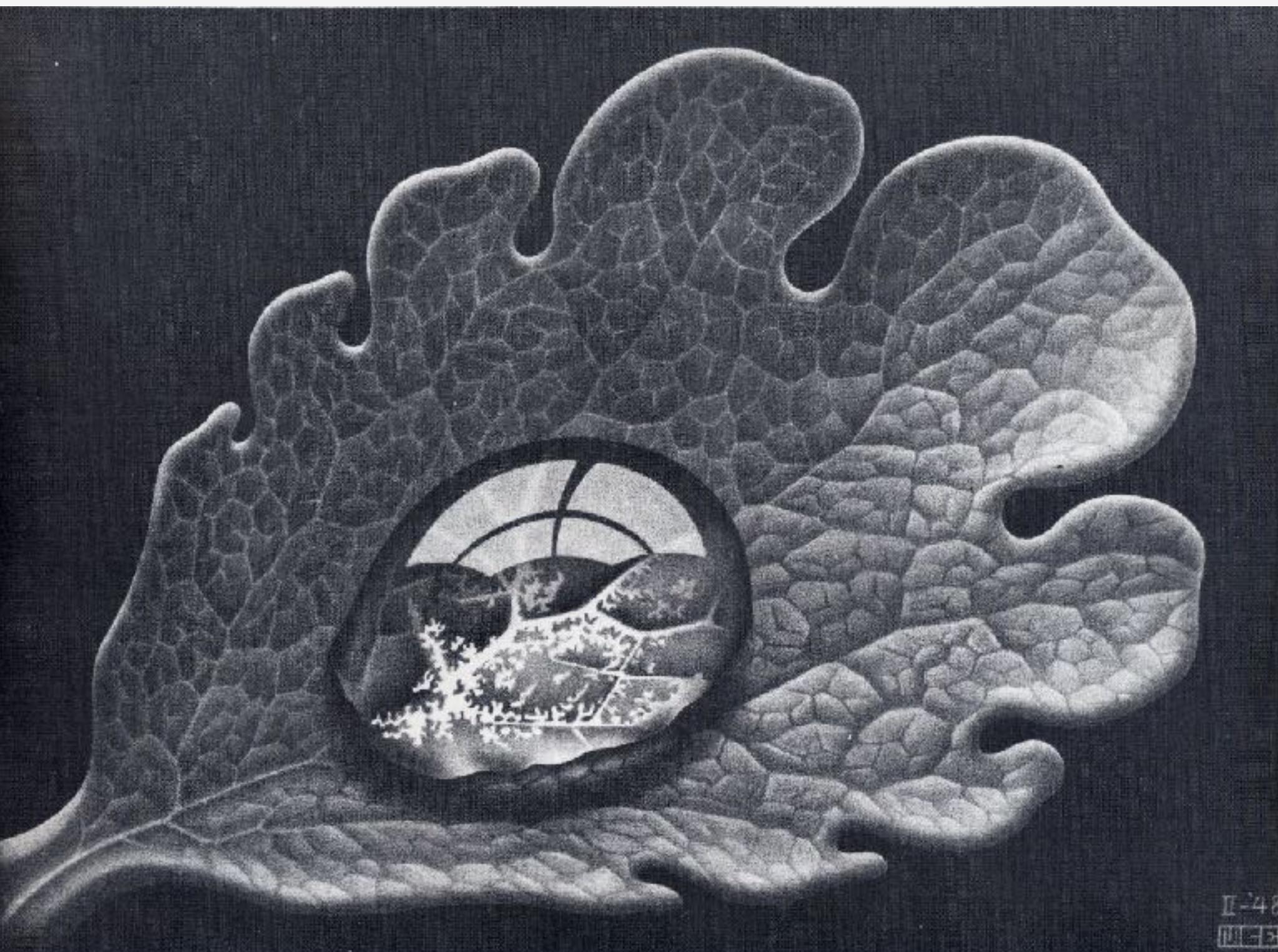
<https://vimeo.com/126664436>



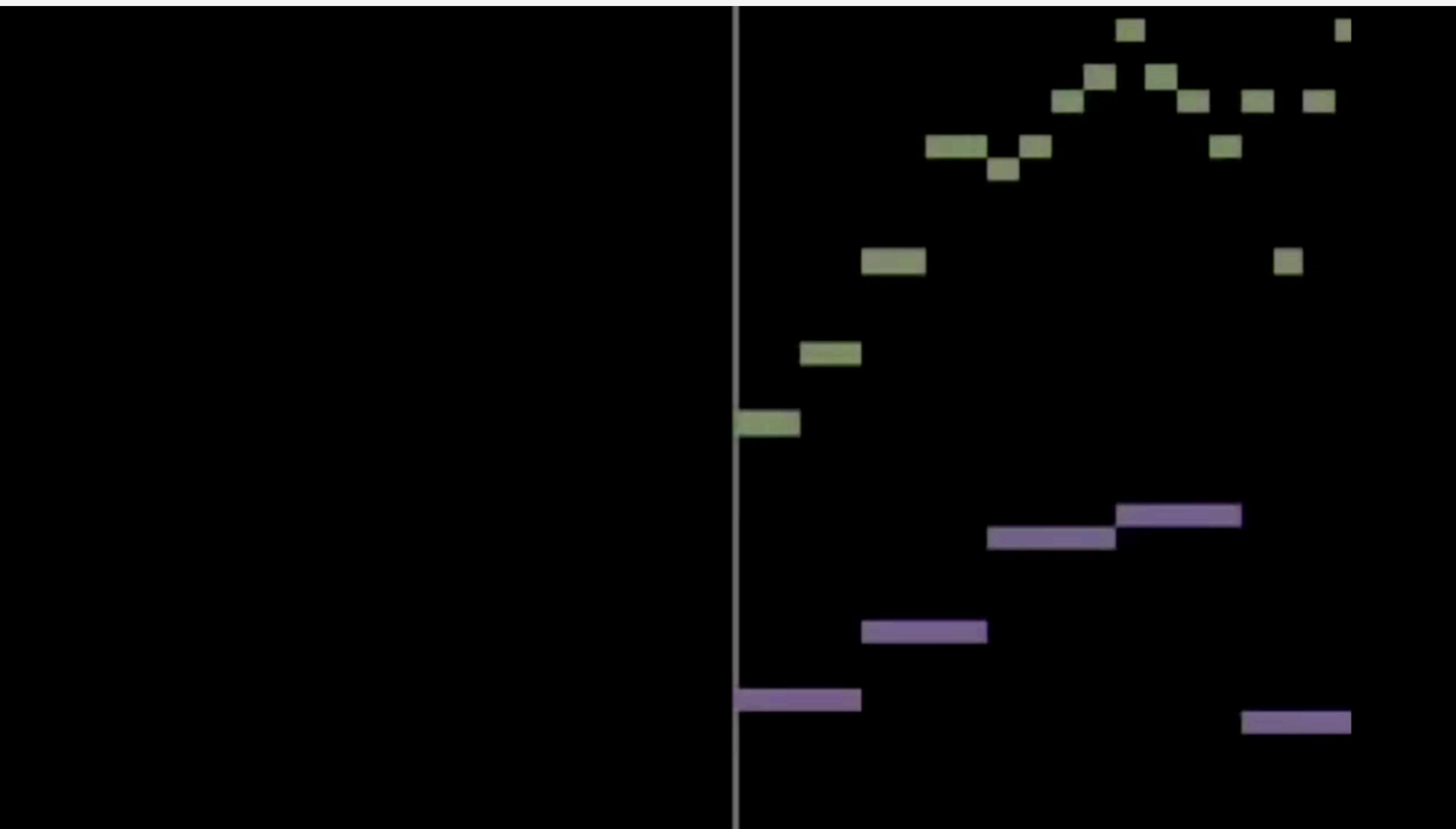
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small



M.C. ESCHER



J.S BACH

https://www.youtube.com/watch?v=beNUq_v1fB8

"This mathematical theorem cannot be proved using math"

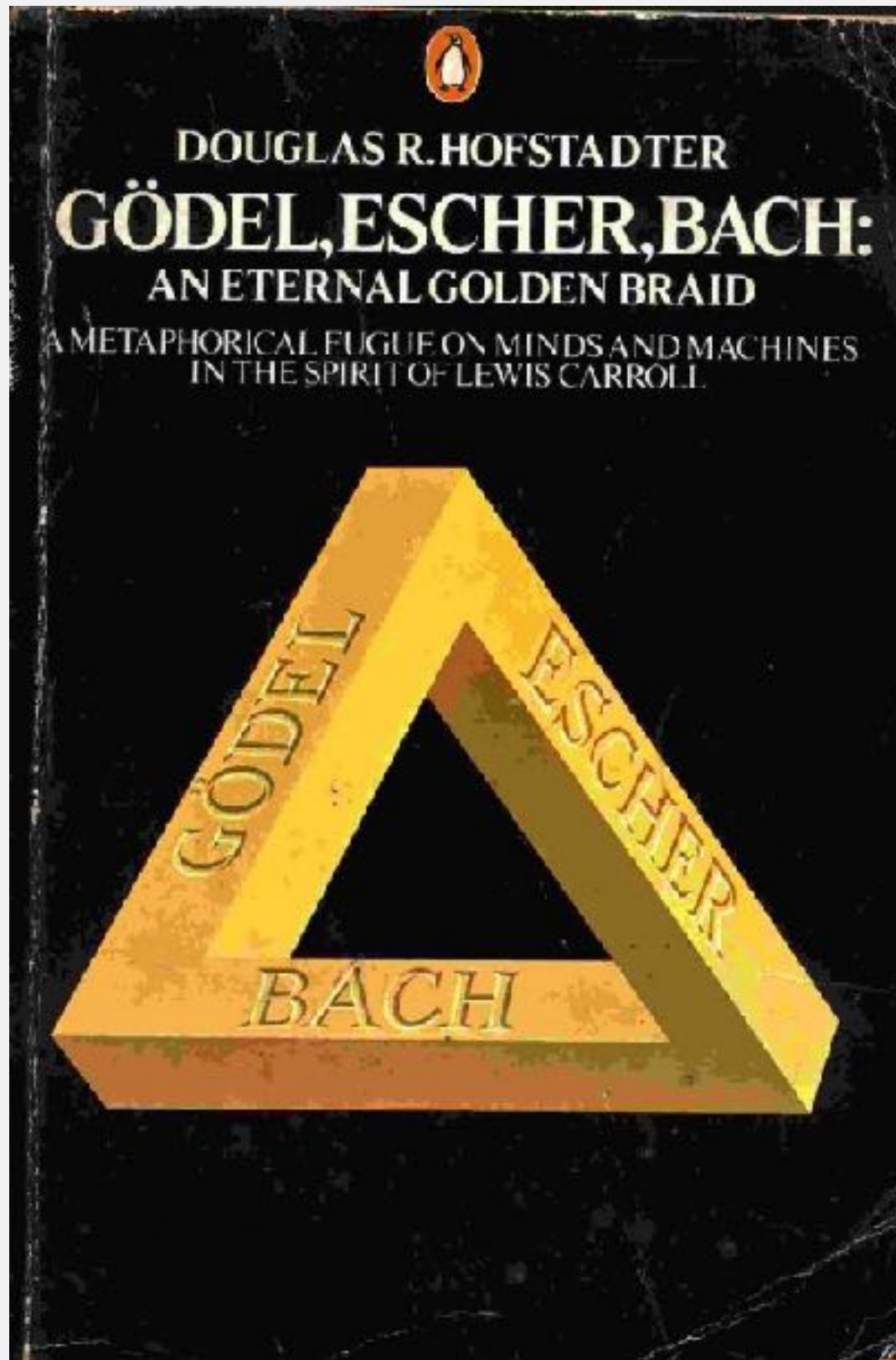
1. For a given (non-trivial) formal system, there will be statements that are true in that system, but which cannot be proved to be true inside the system.
2. If a system can be proved to be complete using its own logic, then there will be a theorem in the system that is contradictory.

Formal systems cannot be both consistent and complete

KURT GÖDEL

https://simple.wikipedia.org/wiki/G%C3%B6del%27s_incompleteness_theorems

https://en.wikipedia.org/wiki/G%C3%B6del%27s_incompleteness_theorems



(And, twice as quickly as the Meta-Genie did, this MetaMeta-Genie removes from the folds of his robe an object which looks just like the gold MetaLamp, except that it is made of ...)

. . .{GOD}

(... swirls back into the MetaMeta-Meta-Lamp, which the Meta-Meta-Genie then folds back into his robe, half as quickly as the Meta-Meta-Meta-Genie did.)

THE NATURE OF CODE

DANIEL SHIFFMAN

WELCOME
ACKNOWLEDGMENTS
DEDICATION
PREFACE
INTRODUCTION
1. VECTORS
2. FORCES
3. OSCILLATION
4. PARTICLE SYSTEMS
5. PHYSICS LIBRARIES
6. AUTONOMOUS AGENTS
7. CELLULAR AUTOMATA
8. FRACTALS
9. THE EVOLUTION OF CODE
10. NEURAL NETWORKS
FURTHER READING
INDEX

Chapter 8. Fractals

*"Pathological monsters! cried the terrified mathematician
Every one of them a splinter in my eye
I hate the Peano Space and the Koch Curve
I fear the Cantor Ternary Set
The Sierpinski Gasket makes me wanna cry
And a million miles away a butterfly flapped its wings
On a cold November day a man named Benoit Mandelbrot was born"*

— Jonathan Coulton, lyrics from "Mandelbrot Set"

Once upon a time, I took a course in high school called "Geometry." Perhaps you did too. You learned about shapes in one dimension, two dimensions, and maybe even three. What is the circumference of a circle? The area of a rectangle? The distance between a point and a line? Come to think of it, we've been studying geometry all along in this book, using vectors to describe the motion of bodies in Cartesian space. This sort of geometry is generally referred to as Euclidean geometry, after the Greek mathematician Euclid.

And for the second line:

```
line(x+len*2/3,y,x+len,y); becomes -----> cantor(x+len*2/3,y,len/3);
```

Show Row

Leaving us with:

```
void cantor(float x, float y, float len) {  
    line(x,y,x+len,y);  
  
    y += 20;  
  
    cantor(x,y,len/3);  
    cantor(x+len*2/3,y,len/3);  
}
```

Show Row

And since the `cantor()` function is called recursively, the same rule will be applied to the next lines and to the next and to the next as `cantor()` calls itself again and again! Now, don't go and run this code yet. We're missing that crucial element: an exit condition. We'll want to make sure we stop at some point—for example, if the length of the line ever is less than 1 pixel.



RESET PAUSE



TREES

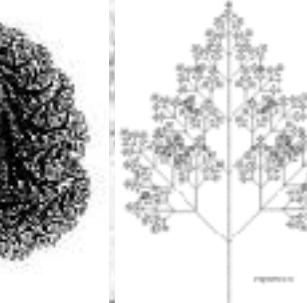
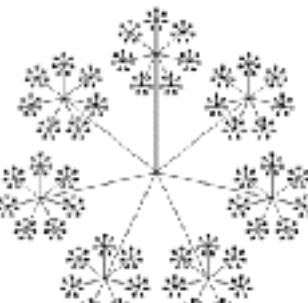
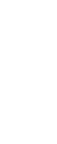
1

2

3

4

8



*“My life seemed to be a series of events and accidents.
Yet when I look back I see a pattern.”*

Benoît Mandelbrot

Honorable mention:



RECURSION

```
‐ for(var i = 0 ; i < 10; i++){  
    doSomething();  
}  
  
‐ function doSomething(){  
    //...  
}
```

```
‐ function doSomething(){  
    doSomethingElse();  
}  
  
‐ function doSomethingElse(){  
    //...  
}
```

```
‐ function doSomething(){  
    doSomething();  
}
```

Iteration

Composition

Recursion

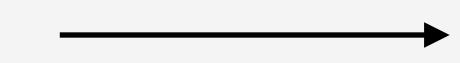
ANATOMY OF A RECURSIVE LOOP

outside call



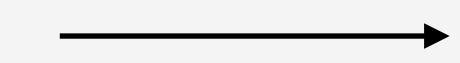
```
function draw() {  
    myRecursiveFunction(10);  
}
```

ending condition



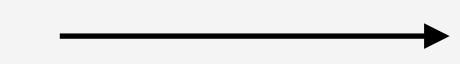
```
function myRecursiveFunction(param){  
    // always start at the end!  
    if(param < 1){  
        return;  
    }
```

do something



```
// ...
```

recurse



```
    myRecursiveFunction(param - 1);  
}
```

NATURE OF CODE

```
int factorial(int n) {  
    if (n == 1) {  
        return 1;  
    } else {  
        return n * factorial(n-1);  
    }  
}
```

[Show Raw](#)

It may look crazy, but it works. Here are the steps that happen when `factorial(4)` is called.

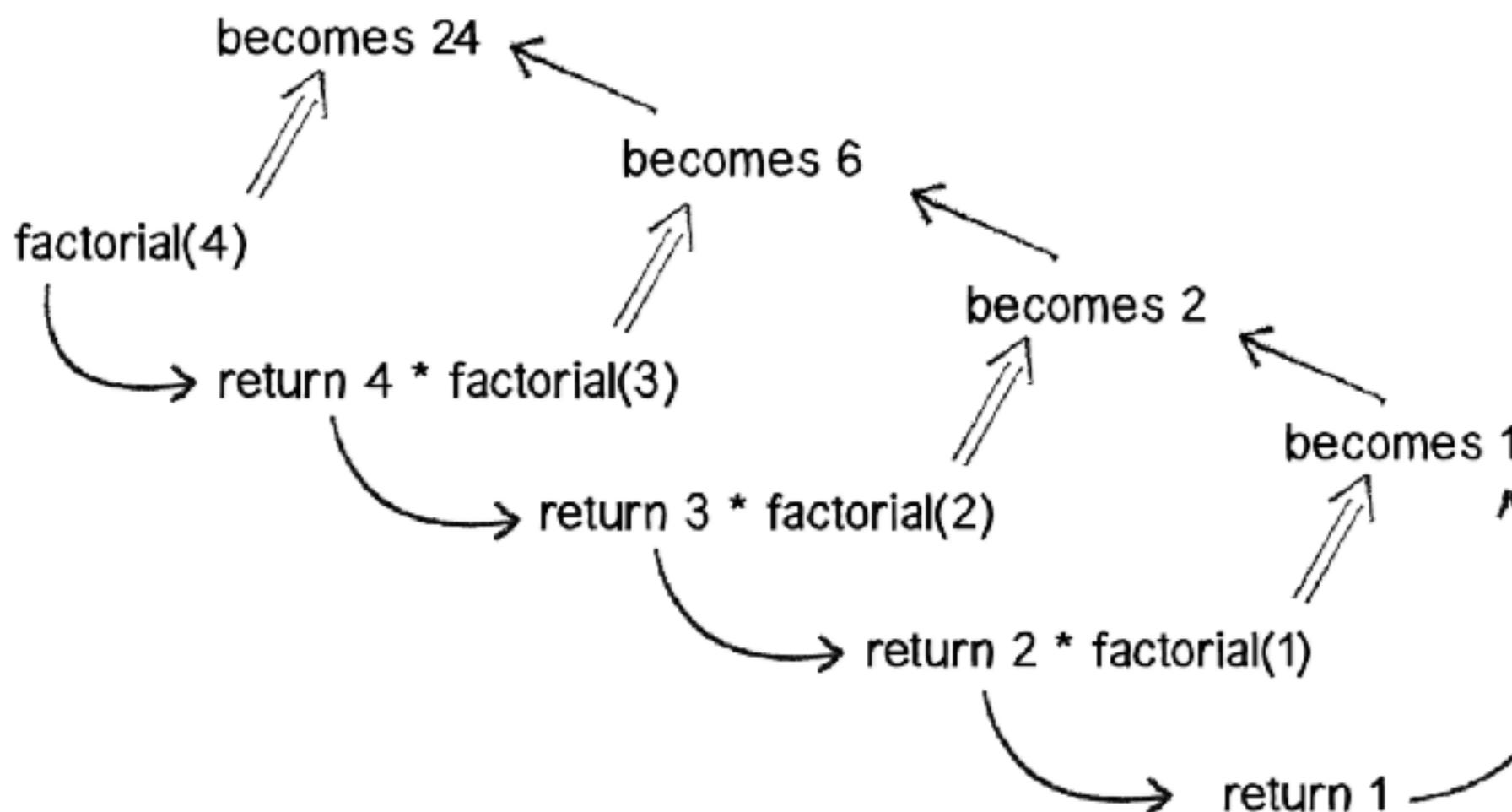
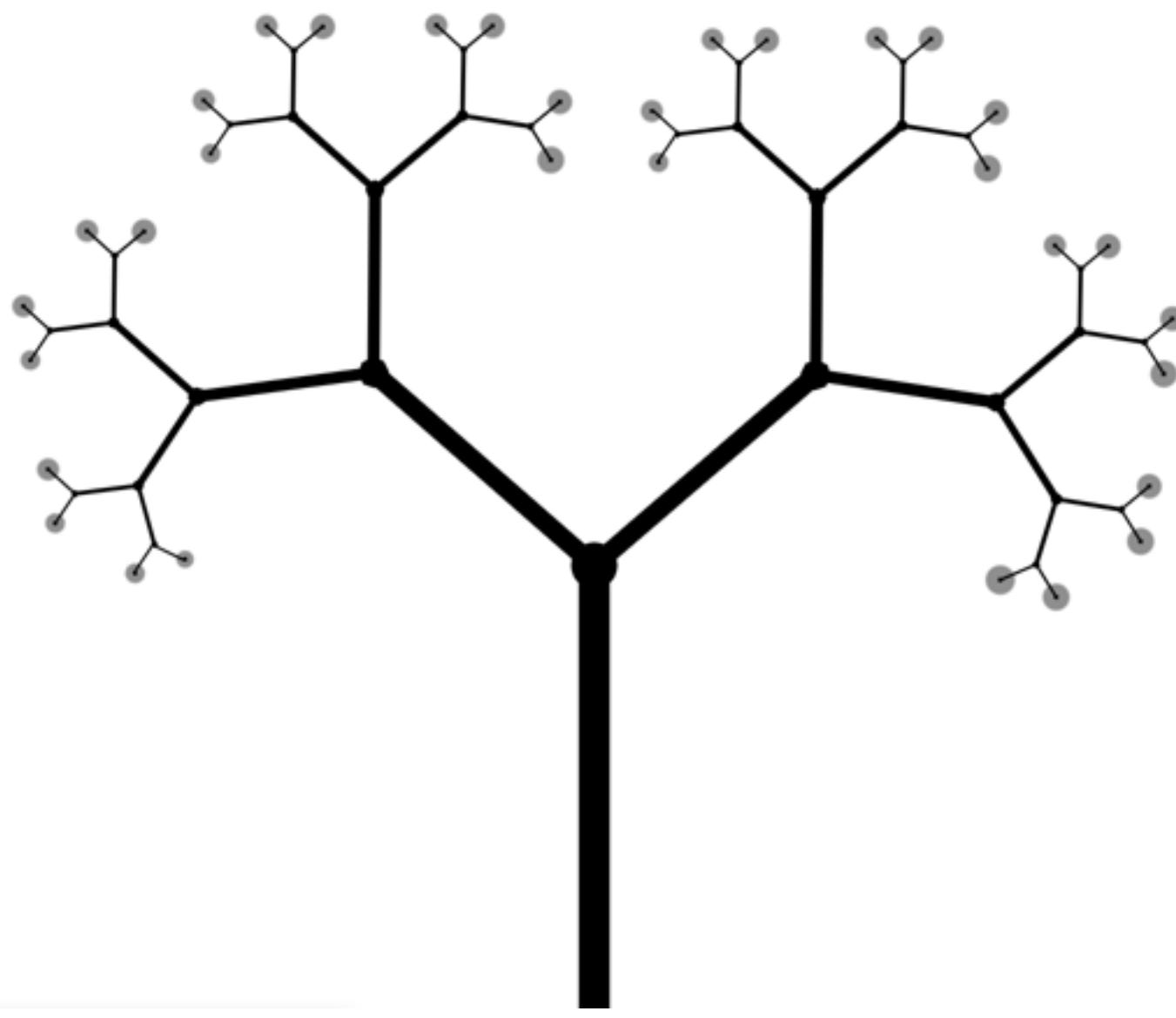


Figure 8.9



Let's create a tree



HOMEWORK #09

Create a Forest.