

# Verifying Concurrent Turing Machines

Soonho Kong

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June 4, 2012

Internship Started  
working with Arie and Sagar

June 4, 2012

Topic:

“Time-bounded Analysis of Real-time Systems”

June 4, 2012

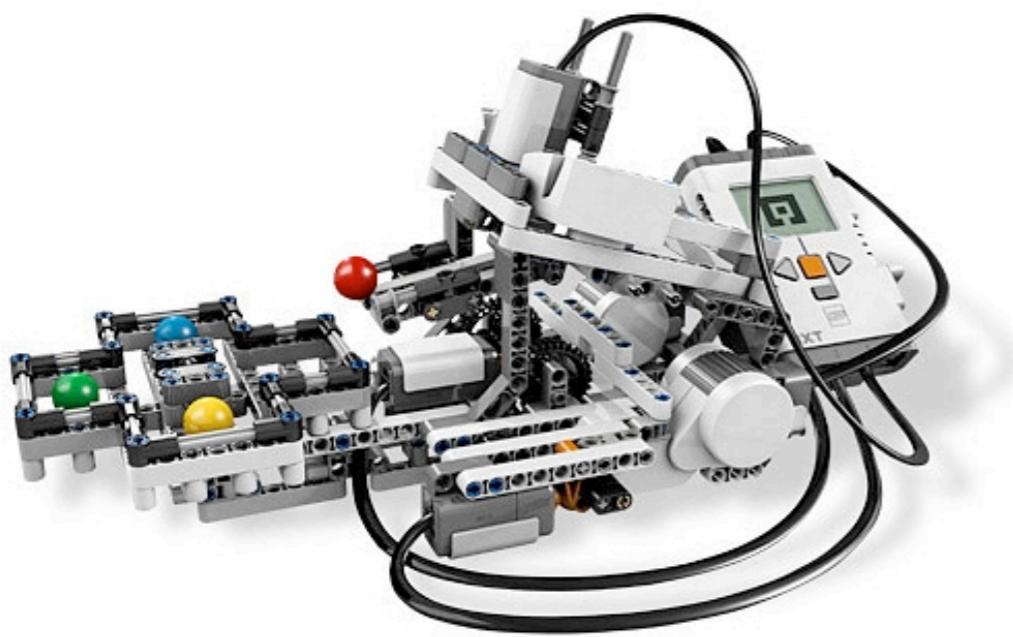
Verification of  
“Concurrent, Periodic, Real-time Embedded System”

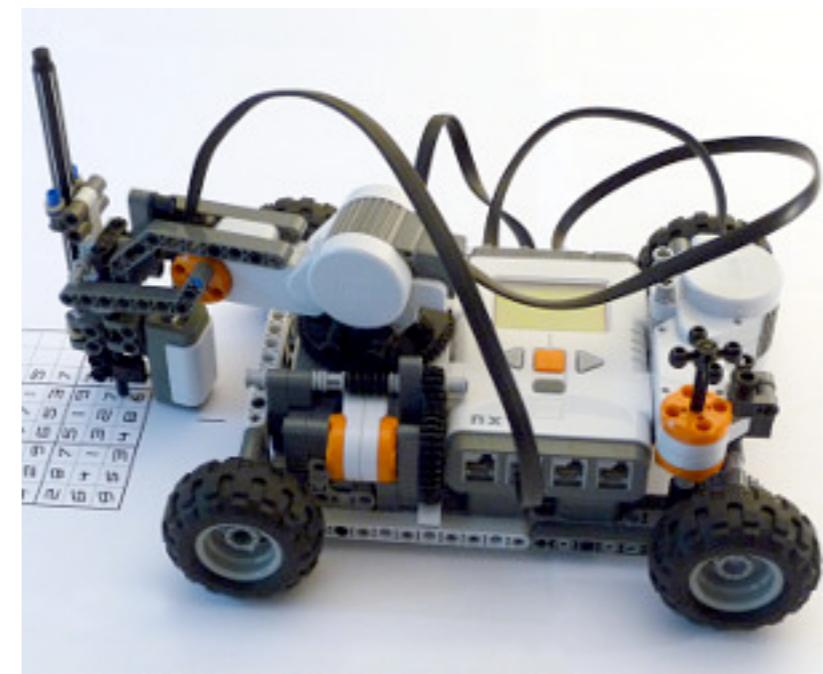
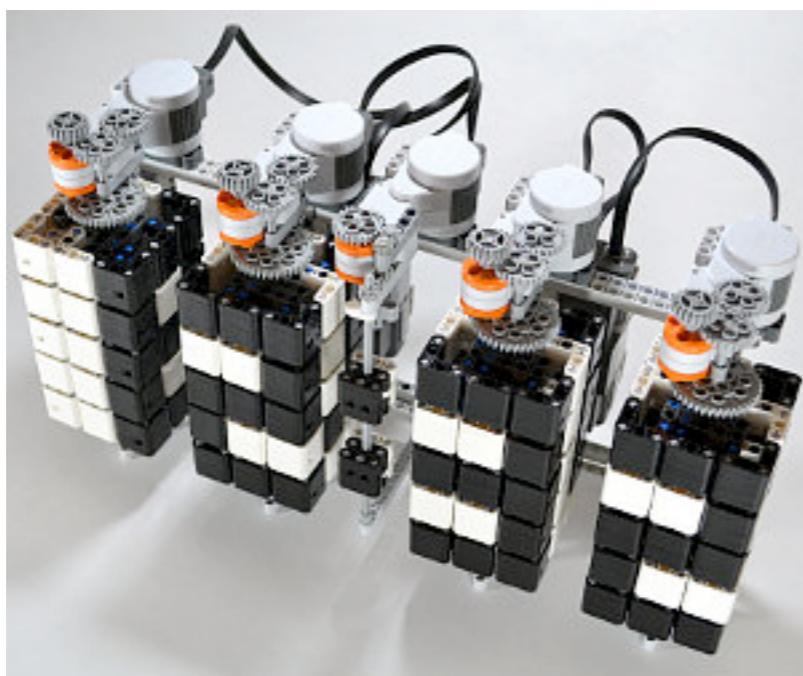
# June 5, 2012



We need more examples of concurrent systems.  
Can you make one with  
LEGO MINDSTORMS?







# ALAN TURING YEAR

2012



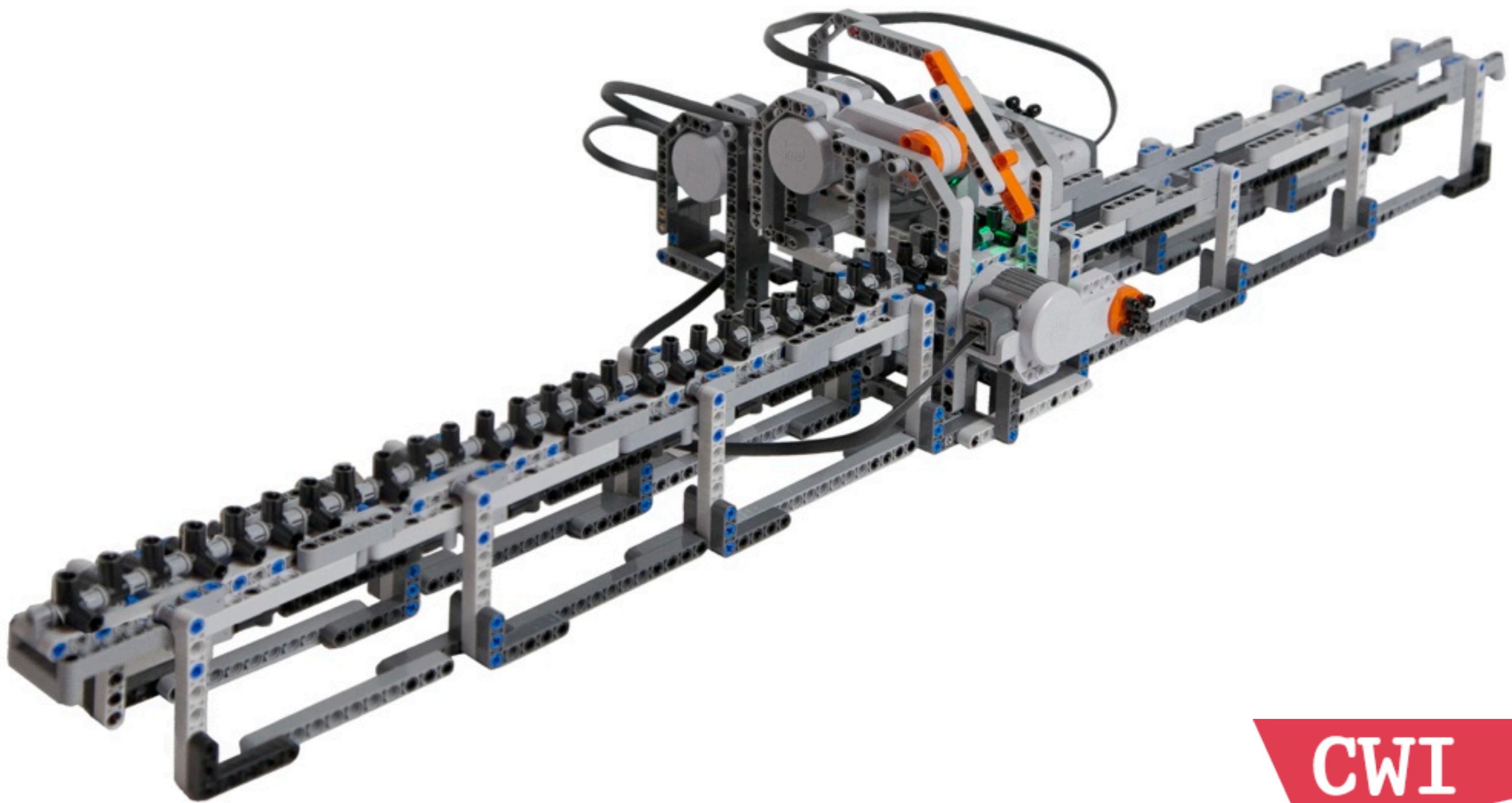
ALAN TURING YEAR



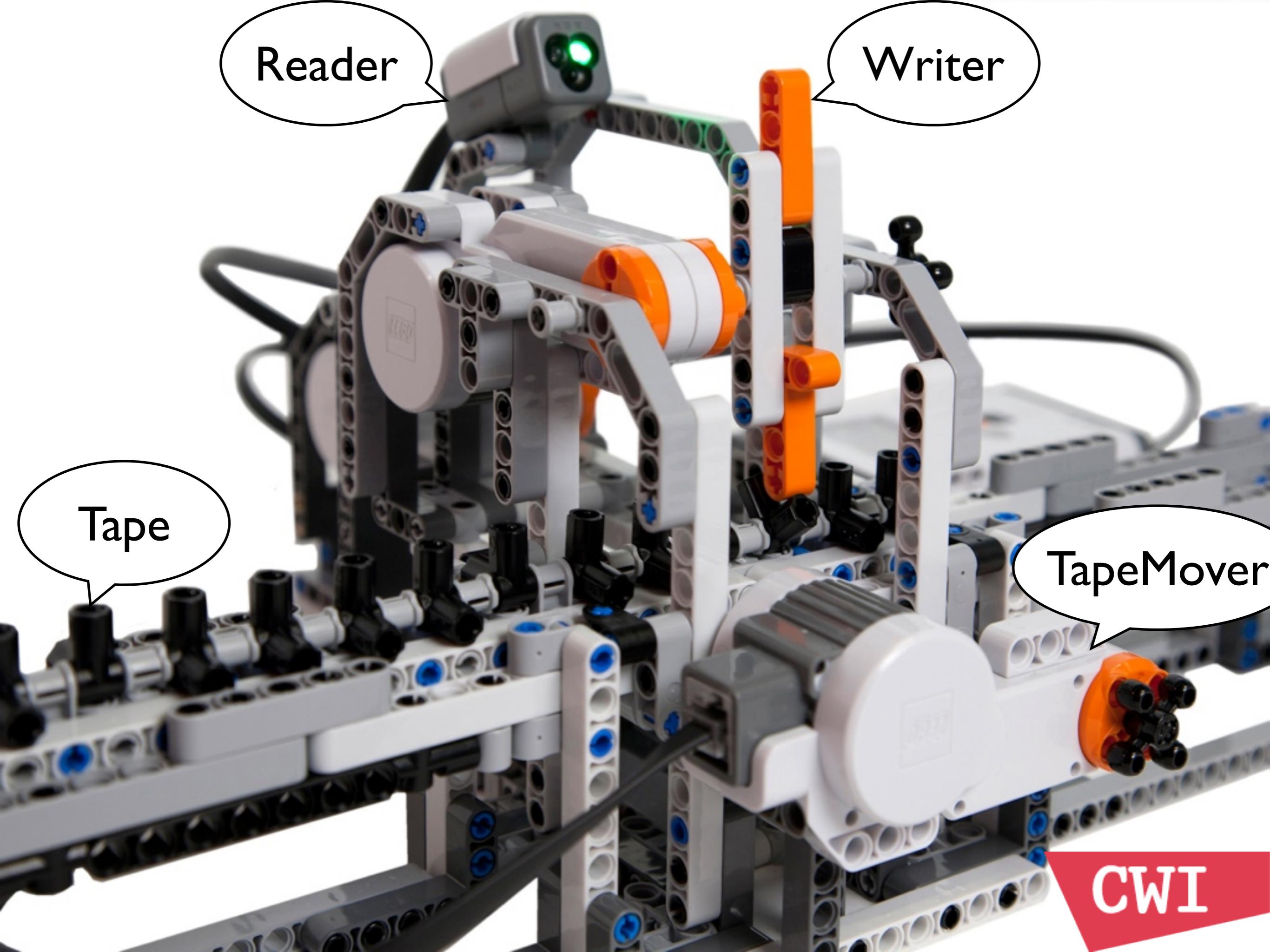
2012

LEGO Turing Machine?

# A Turing Machine built using



CWI



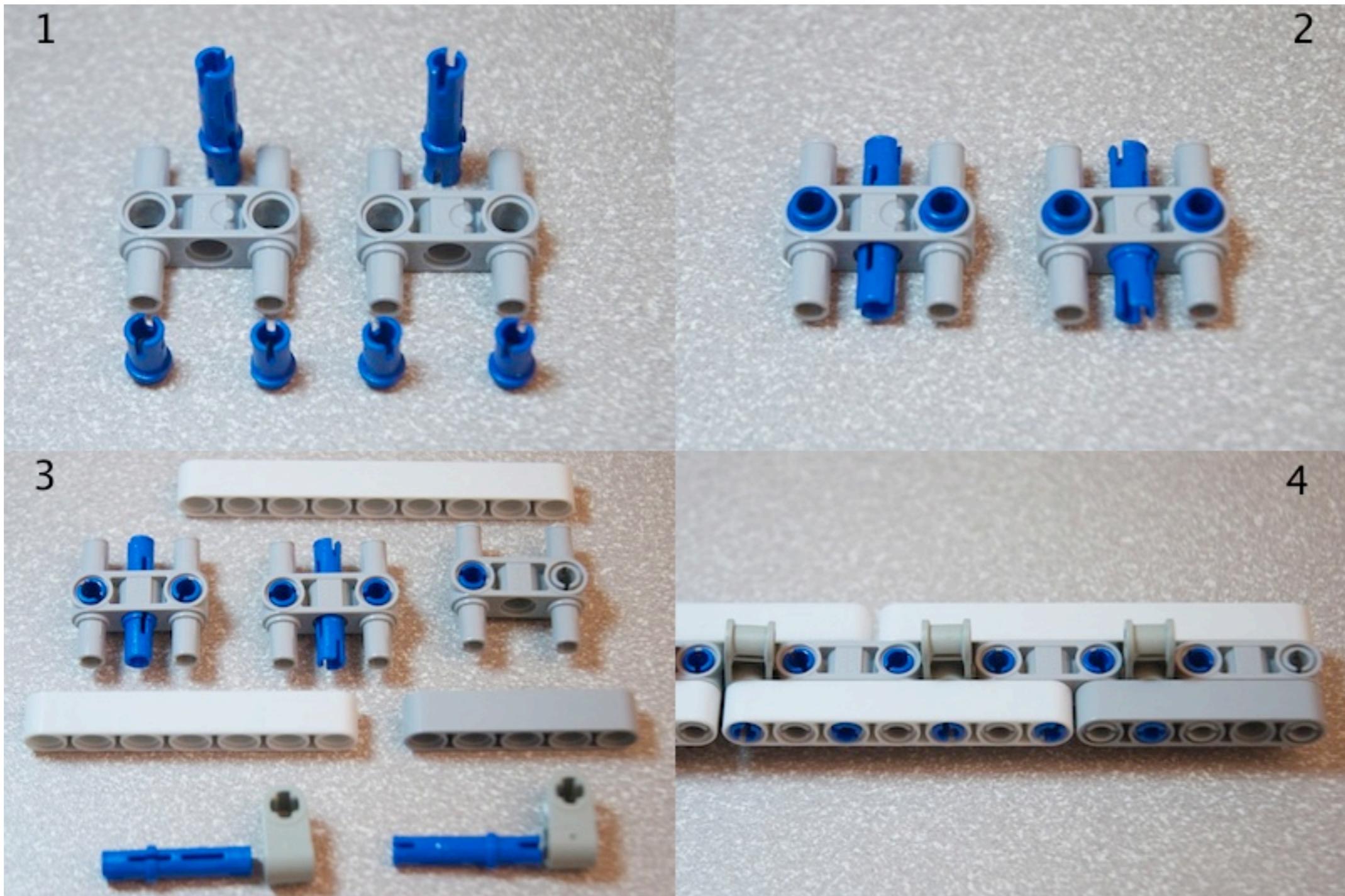
CWI

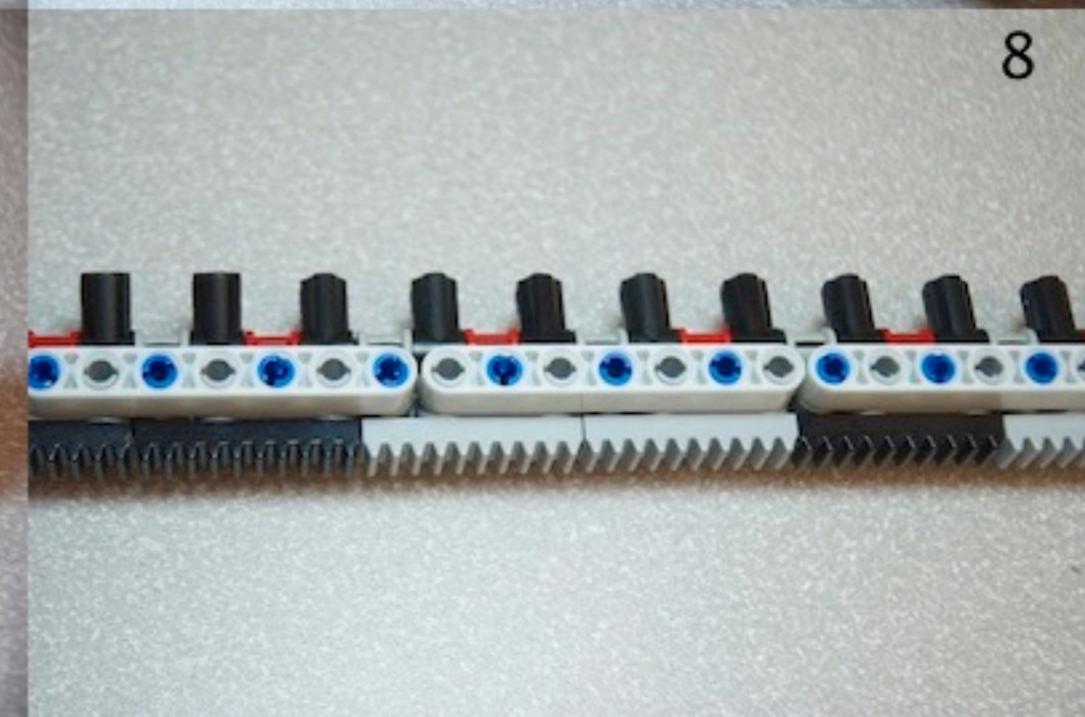
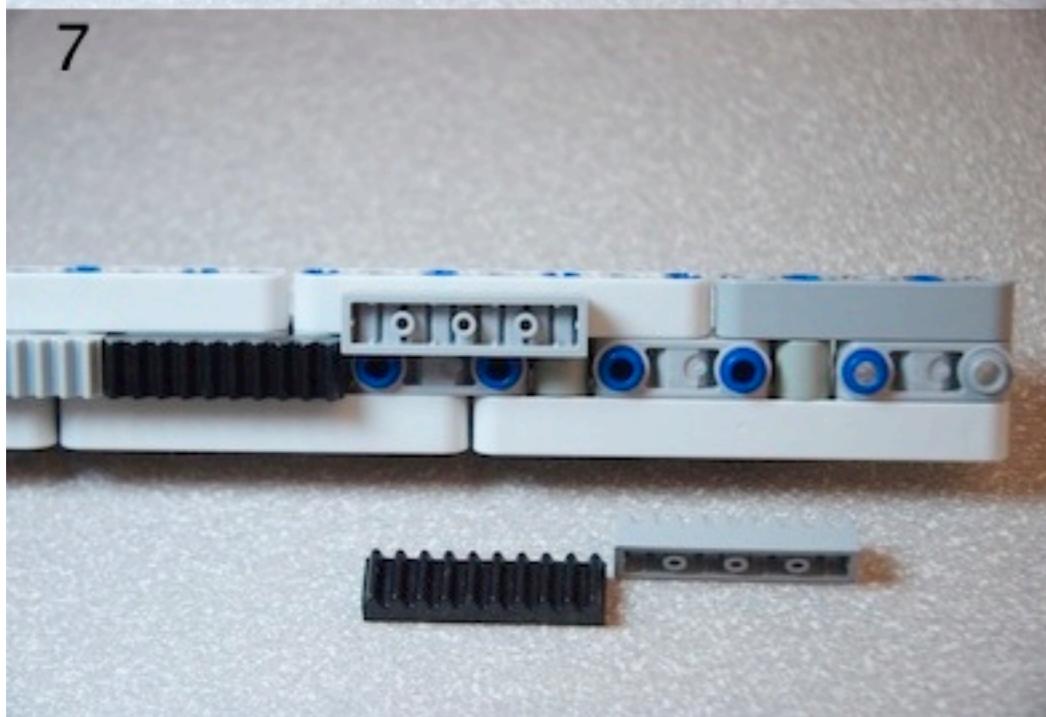
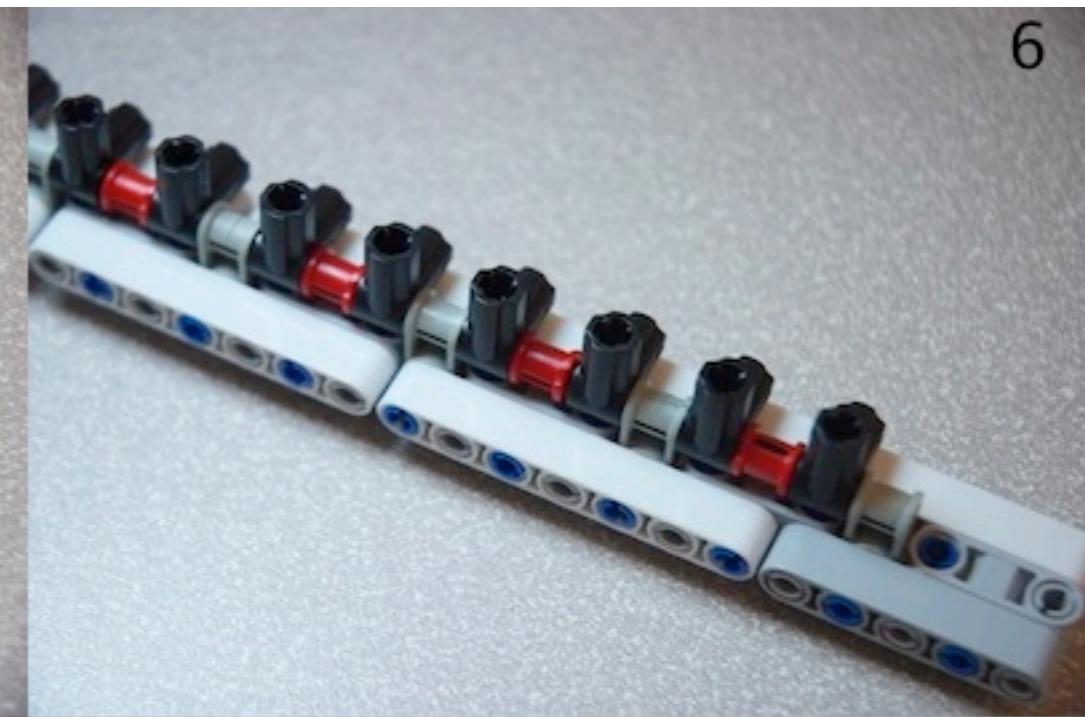
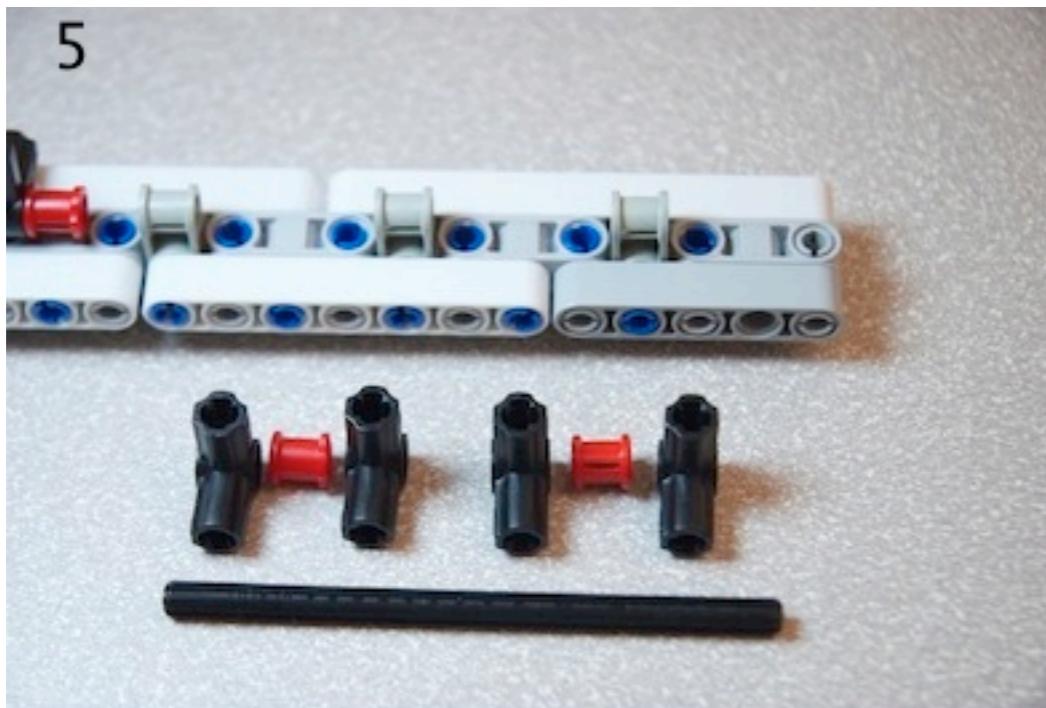
# June 9, 2012

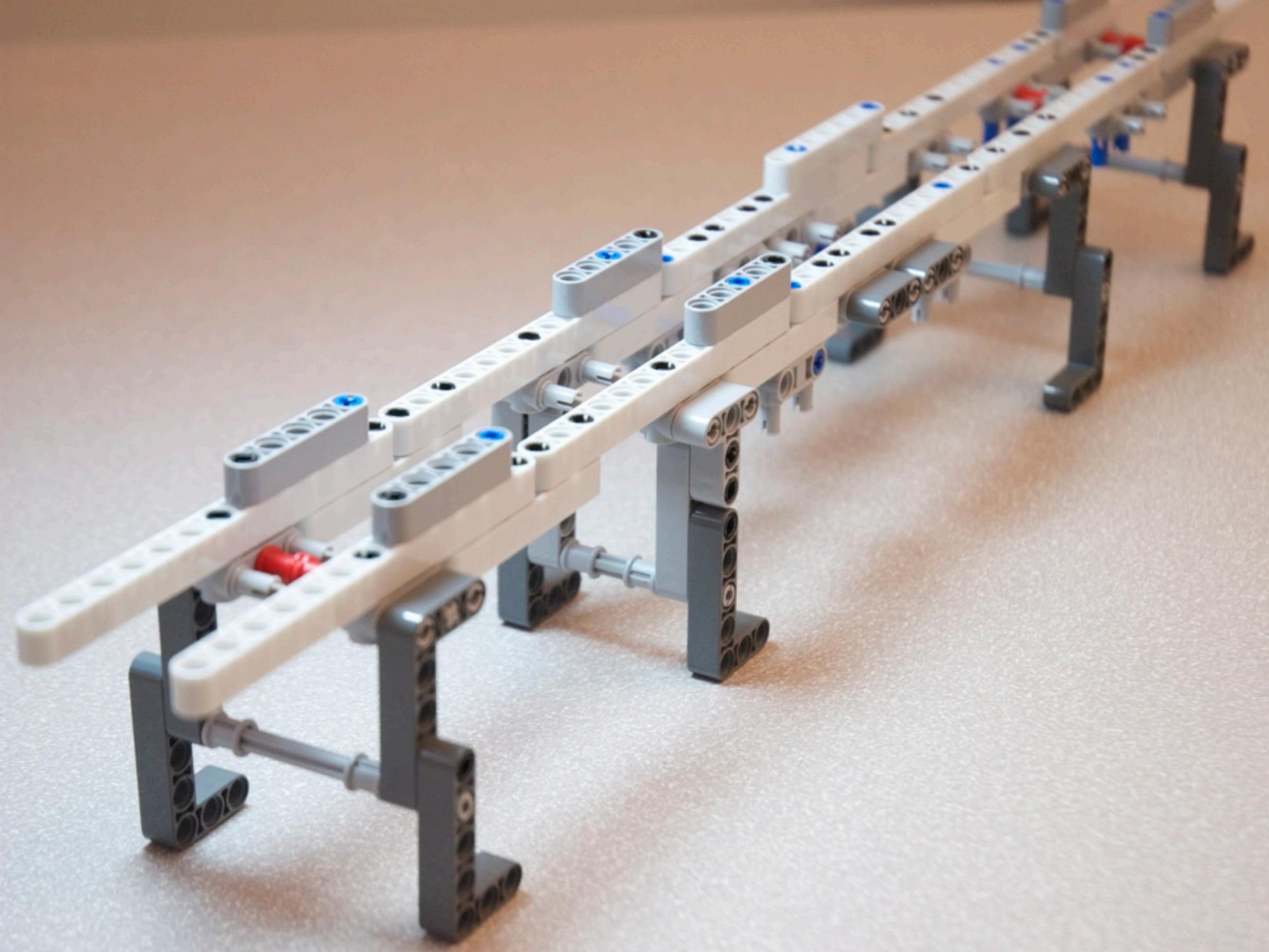


OK, Let's build one!









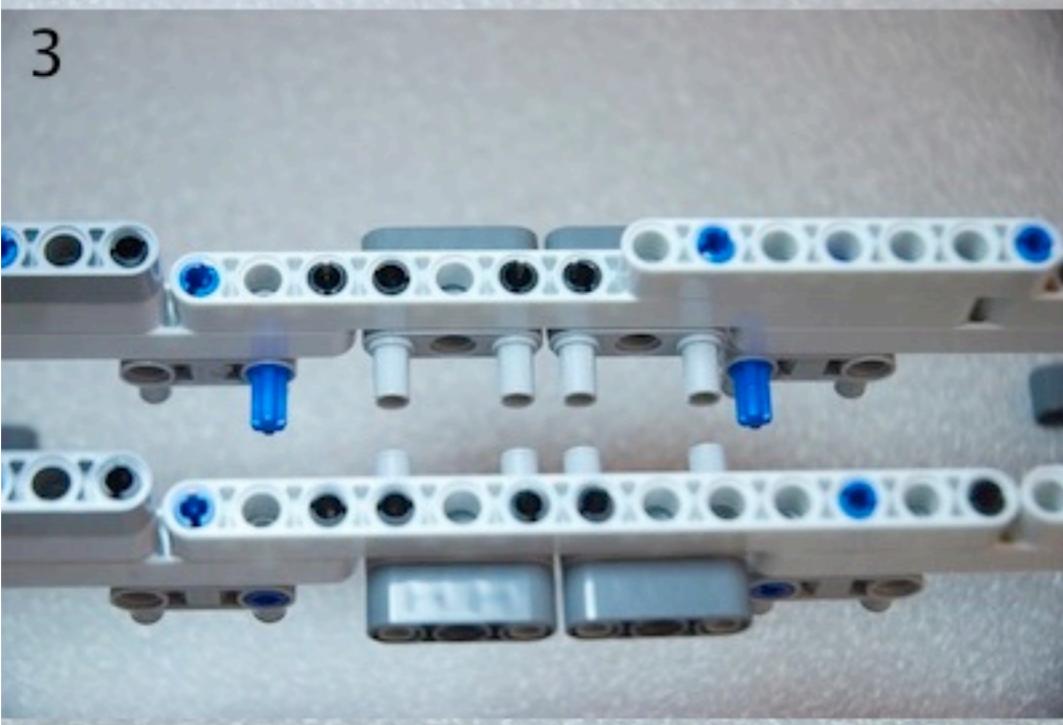
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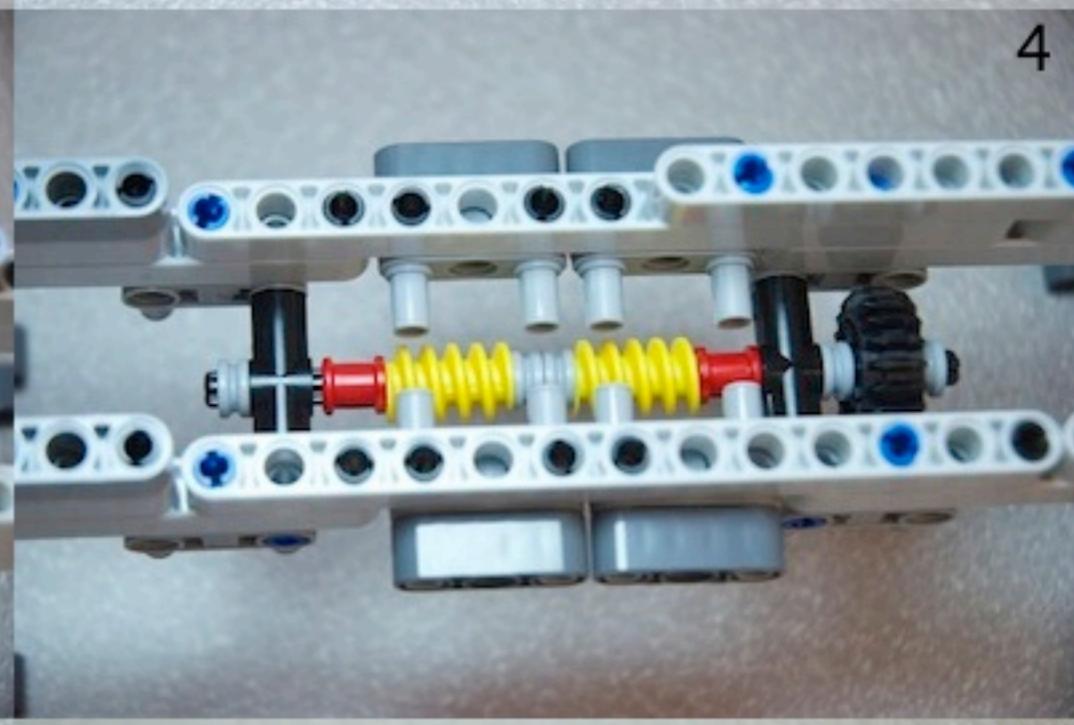
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3



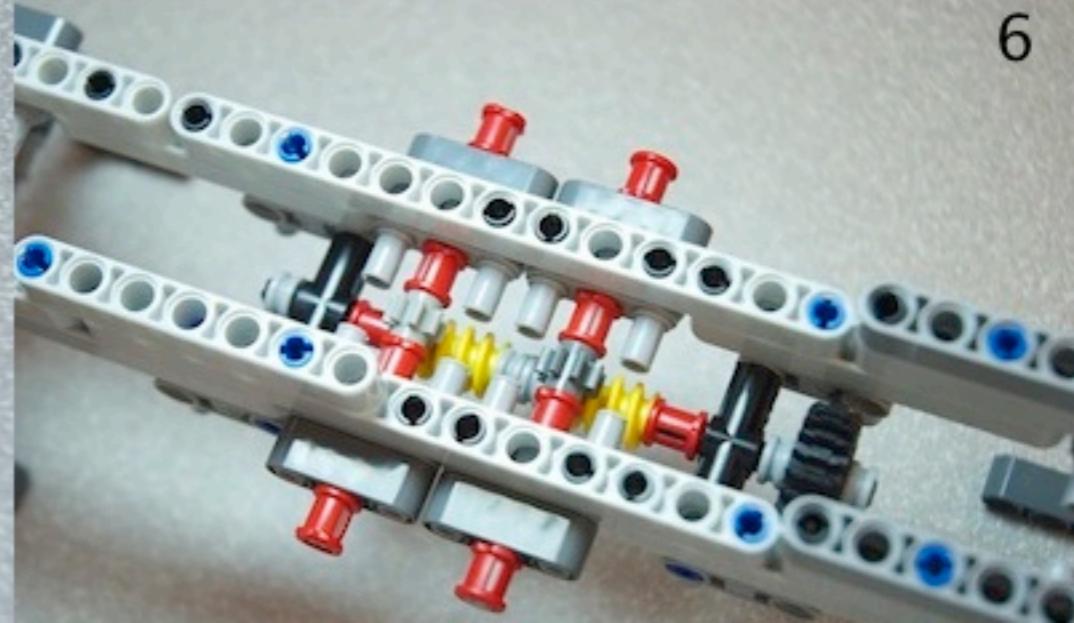
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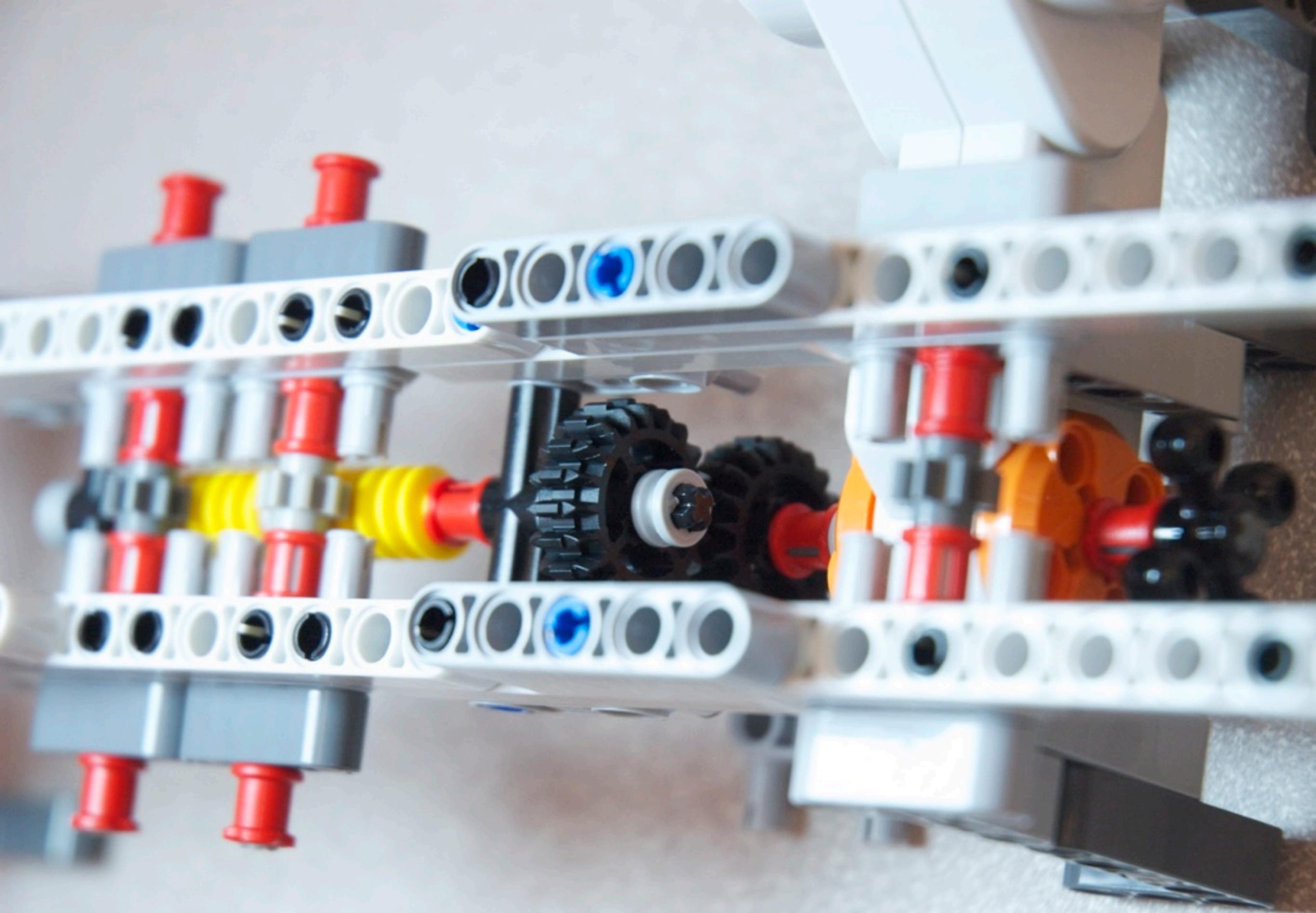


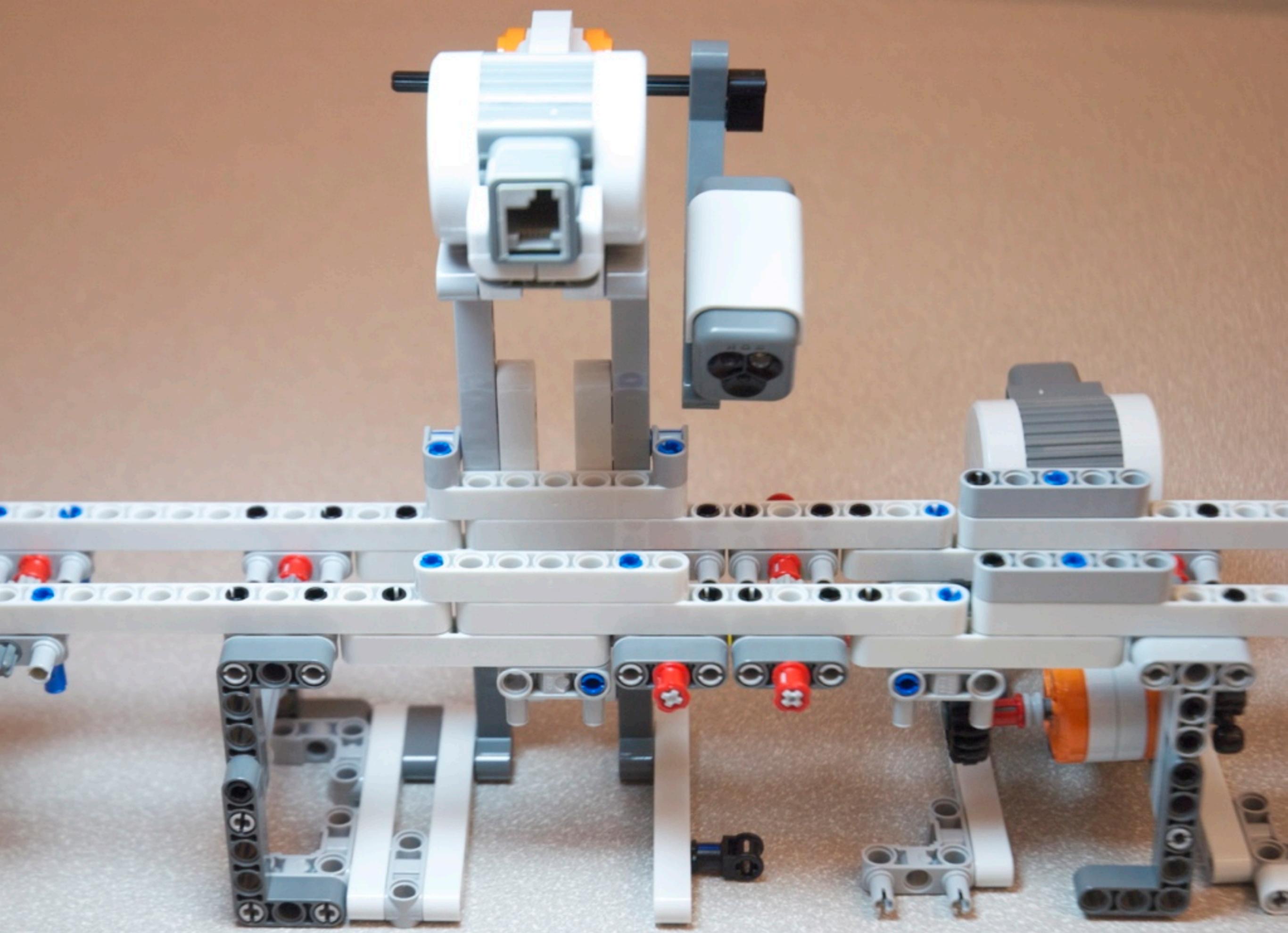
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6





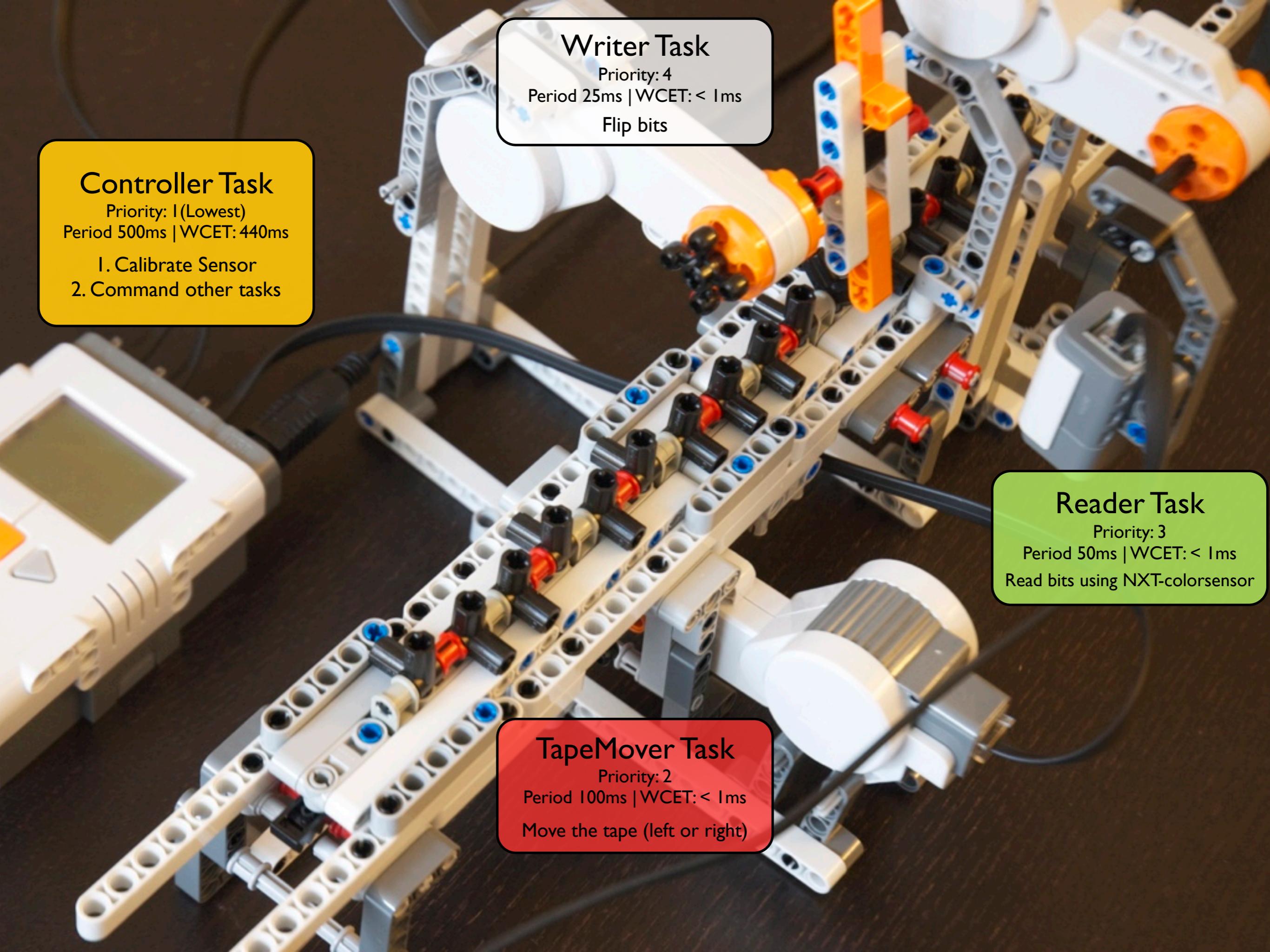






July 25, 2012  
Construction Completed!

# Software Implementation



# DEMO

## Unary Addition

$$2 + 3 = ?$$

<http://www.youtube.com/watch?v=teDyd0d5M4o>

# Properties

Property 1: When a bit is being read, all the motors should **stop**.

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

Property 3: When tape moves, the writer motor and read motor should **stop**.

Property 4: When a bit is being read, the sensor should be on **Green** mode

Property 5: The sensor mode must be switched in **Controller Task**, not in Reader Task

# Properties

Property 1: When a bit is being read, all the motors should **stop**.

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

Property 3: When tape moves, the writer motor and read motor should **stop**.

Property 4: When a bit is being read, the sensor should be on **Green** mode

Property 5: The code below shows how properties 1 and 4 are checked in Reader Task

```
case READ_SENSOR:  
    if(!IR(need_to_run_nxtbg)) {  
  
        #ifdef VERIFICATION  
            /* Property 1: When a bit is being read,  
             all the motors should be stopped. */  
            /* PASSED with 4 hyper-periods */  
            assert(R(R_speed) == 0 && R(W_speed) == 0 && R(T_speed) == 0);  
  
            /* Property 4: When a bit is being read,  
             the sensor should be on Green mode */  
            assert(ecrobot_get_nxtcolorsensor_mode(COLOR_SENSOR) == NXT_LIGHTSENSOR_GREEN);  
        #endif  
        /* Read Sensor Value */  
        bg_nxtcolorsensor(false);  
        color = ecrobot_get_nxtcolorsensor_light(COLOR_SENSOR);  
        W(input, color < R(threshold) ? 1 : 0);  
    }  
}
```

# Properties

Property 1: When a bit is being read, all the motors should **stop**.

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

Property 3: When tape moves, the writer motor and read motor should **stop**.

Property 4: When a bit is being read, the tape motor and read motor should **stop** mode

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
     * motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Property 5: The sensor value is 0, not in Reader Task

# Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:  
    /* Check if we need to change the bit */  
    if(R(input) != R(output)) {  
        /* Check the header and move it back if necessary */  
        if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {  
            W(R_state, READ_MOVE_HEADER_BACKWARD);  
        }  
  
        /* Check the header and flip the bit if it is safe to do */  
        if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {  
            W(W_state, WRITE_FLIP);  
        }  
    } else {  
        /* Nothing to change for writer */  
        W(W_state, WRITE_IDLE);  
        C_state = C_MOVE;  
    }  
break;
```

Controller  
Task

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
     * motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Writer Task

# Properties

Property 2: When writer writes, the tape motor and read motor should **stop**.

Do we need to write?

```
case C_WRITE:  
  
    /* Check if we need to change the bit */  
    if(R(input) != R(output)) {  
        /* Check the header and move it back if necessary */  
        if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {  
            W(R_state, READ_MOVE_HEADER_BACKWARD);  
        }  
  
        /* Check the header and flip the bit if it is safe to do */  
        if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {  
            W(W_state, WRITE_FLIP);  
        }  
    } else {  
        /* Nothing to change for writer */  
        W(W_state, WRITE_IDLE);  
        C_state = C_MOVE;  
    }  
break;
```

Controller  
Task

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
     * motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Writer Task

# Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:  
    /* Check if we need to change the bit */  
    if(R(input) != R(output)) {  
        /* Check the header and move it back if necessary */  
        if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {  
            W(R_state, READ_MOVE_HEADER_BACKWARD);  
        }  
  
        /* Check the header and flip the bit if it is safe to do */  
        if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {  
            W(W_state, WRITE_FLIP);  
        }  
    } else {  
        /* Nothing to change for writer */  
        W(W_state, WRITE_IDLE);  
        C_state = C_MOVE;  
    }  
break;
```

Controller  
Task

If the READ header is up,  
Move it back  
to avoid collision!

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
    motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Writer Task

# Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:  
    /* Check if we need to change the bit */  
    if(R(input) != R(output)) {  
        /* Check the header and move it back if necessary */  
        if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {  
            W(R_state, READ_MOVE_HEADER_BACKWARD);  
        }  
  
        /* Check the header and flip the bit if it is safe to do */  
        if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {  
            W(W_state, WRITE_FLIP);  
        }  
    } else {  
        /* Nothing to change for writer */  
        W(W_state, WRITE_IDLE);  
        C_state = C_MOVE;  
    }  
break;
```

Controller Task

OK, it's safe to write!

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
     * motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Writer Task

# Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:  
    /* Check if we need to change the bit */  
    if(R(input) != R(output)) {  
        /* Check the header and move it back if necessary */  
        if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {  
            W(R_state, READ_MOVE_HEADER_BACKWARD);  
        }  
  
        /* Check the header and flip the bit if it is safe to do */  
        if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {  
            W(W_state, WRITE_FLIP);  
        }  
    } else {  
        /* Nothing to change for writer */  
        W(W_state, WRITE_IDLE);  
        C_state = C_MOVE;  
    }  
break;
```

Controller  
Task

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
     * motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Writer Task

NO!  
The position of READ header is in safe area ( $\leq 0$ ),  
however it's possible that it is **still moving!**

# Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:  
    /* Check if we need to change the bit */  
    if(R(input) != R(output)) {  
        /* Check the header and move it back if necessary */  
        if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {  
            W(R_state, READ_MOVE_HEADER_BACKWARD);  
        }  
  
        /* Check the header and flip the bit if it is safe to do */  
        if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {  
            W(W_state, WRITE_FLIP);  
        }  
    } else {  
        /* Nothing to change for writer */  
        W(W_state, WRITE_IDLE);  
        C_state = C_MOVE;  
    }  
    break;
```

Controller  
Task

```
case WRITE_FLIP:  
#ifdef VERIFICATION  
    /* Property 3: When writer flips a bit, the tape motor and read  
     * motor should be stopped. */  
  
    /* IT FAILS!! with BOUND 120 */  
    assert(R(T_speed) == 0 && R(R_speed) == 0);  
#endif
```

Writer Task

REKH(out tool) can find this bug within 2mins.

**DEMO**

**REKH & Counterexample**

<http://www.cs.cmu.edu/~soonhok/rekh-viz>

Thank you!