100 numpy exercises

1. Import the numpy package under the name np $(\bigstar \stackrel{\wedge}{\cancel{\sim}} \stackrel{\wedge}{\cancel{\sim}})$

```
In [1]: import numpy as np
```

2. Print the numpy version and the configuration (★☆☆)

```
In [7]: print(np. version )
        print(np.show_config())
        1.21.5
        blas_mkl_info:
            libraries = ['mkl_rt', 'pthread']
            library dirs = ['/Users/roatny/opt/anaconda3/lib']
            define macros = [('SCIPY MKL H', None), ('HAVE CBLAS', None)]
            include dirs = ['/Users/roatny/opt/anaconda3/include']
        blas_opt_info:
            libraries = ['mkl_rt', 'pthread']
            library_dirs = ['/Users/roatny/opt/anaconda3/lib']
            define_macros = [('SCIPY_MKL_H', None), ('HAVE_CBLAS', None)]
            include dirs = ['/Users/roatny/opt/anaconda3/include']
        lapack mkl info:
            libraries = ['mkl_rt', 'pthread']
            library_dirs = ['/Users/roatny/opt/anaconda3/lib']
            define_macros = [('SCIPY_MKL_H', None), ('HAVE_CBLAS', None)]
            include dirs = ['/Users/roatny/opt/anaconda3/include']
        lapack opt info:
            libraries = ['mkl_rt', 'pthread']
            library_dirs = ['/Users/roatny/opt/anaconda3/lib']
            define_macros = [('SCIPY_MKL_H', None), ('HAVE_CBLAS', None)]
            include_dirs = ['/Users/roatny/opt/anaconda3/include']
        Supported SIMD extensions in this NumPy install:
            baseline = SSE,SSE2,SSE3
            found = SSSE3.SSE41.POPCNT.SSE42
            not found = AVX,F16C,FMA3,AVX2,AVX512F,AVX512CD,AVX512 KNL,AVX
        512 SKX, AVX512 CLX, AVX512 CNL, AVX512 ICL
        None
```

3. Create a null vector of size 10 (★☆☆)

```
In [8]:
    null=np.zeros(10)
    print(null)
```

[0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]

4. How to find the memory size of any array (★☆☆)

```
In [9]: x = np.array([100, 20, 34])
print("Memory size of the array:",x.size)
```

Memory size of the array: 3

5. How to get the documentation of the numpy add function from the command line? $(\bigstar \stackrel{\wedge}{\swarrow} \stackrel{\wedge}{\swarrow})$

```
In [10]: np.info(np.add) #Why?
```

add(x1, x2, /, out=None, *, where=True, casting='same_kind', order ='K', dtype=None, subok=True[, signature, extobj])

Add arguments element-wise.

Parameters

x1, x2 : array_like

The arrays to be added.

If ``x1.shape != x2.shape``, they must be broadcastable to a c
ommon

shape (which becomes the shape of the output).

out : ndarray, None, or tuple of ndarray and None, optional

A location into which the result is stored. If provided, it must have

a shape that the inputs broadcast to. If not provided or None,

a freshly—allocated array is returned. A tuple (possible only as a

keyword argument) must have length equal to the number of outputs.

where : array_like, optional

This condition is broadcast over the input. At locations where the

condition is True, the `out` array will be set to the ufunc re sult.

Elsewhere, the `out` array will retain its original value. Note that if an uninitialized `out` array is created via the d

```
efault
   ``out=None``, locations within it where the condition is False
    remain uninitialized.
**kwarqs
    For other keyword-only arguments, see the
    :ref:`ufunc docs <ufuncs.kwargs>`.
Returns
add : ndarray or scalar
   The sum of `x1` and `x2`, element-wise.
    This is a scalar if both `x1` and `x2` are scalars.
Notes
Equivalent to x1 + x2 in terms of array broadcasting.
Examples
>>> np.add(1.0, 4.0)
5.0
>>> x1 = np.arange(9.0).reshape((3, 3))
>>> x2 = np.arange(3.0)
>>> np.add(x1, x2)
array([[ 0., 2., 4.],
       [ 3., 5., 7.],
[ 6., 8., 10.]])
The ``+`` operator can be used as a shorthand for ``np.add`` on nd
arrays.
>>> x1 = np.arange(9.0).reshape((3, 3))
>>> x2 = np.arange(3.0)
>>> x1 + x2
array([[ 0., 2., 4.],
       [3., 5., 7.],
       [ 6., 8., 10.]])
```

6. Create a null vector of size 10 but the fifth value which is 1 (★☆☆)

```
In [11]: a=np.zeros(10)
a[4]=1
a
Out[11]: array([0., 0., 0., 0., 1., 0., 0., 0., 0., 0.])
```

7. Create a vector with values ranging from 10 to 49 (★☆☆)

```
In [14]: b=np.arange(10,49)
b
Out[14]: array([10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24,
```

Out[14]: array([10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48])

8. Reverse a vector (first element becomes last) (★☆☆)

```
In [15]: print(b[::-1])
     [48 47 46 45 44 43 42 41 40 39 38 37 36 35 34 33 32 31 30 29 28 27
     26 25
      24 23 22 21 20 19 18 17 16 15 14 13 12 11 10]
```

9. Create a 3x3 matrix with values ranging from 0 to 8 (★☆☆)

```
In [21]: c =np.arange(0,9).reshape(3,3)
    print(c)

[[0 1 2]
      [3 4 5]
      [6 7 8]]
```

10. Find indices of non-zero elements from [1,2,0,0,4,0] (★☆☆)

```
In [24]: d1=[1,2,0,0,4,0]
    d2=[]
    for i in range(len(d1)):
        if d1[i]!=0:
            d2.append(i)
        print(d2)
        [0, 1, 4]
```

11. Create a 3x3 identity matrix (★☆☆)

12. Create a 3x3x3 array with random values (★☆☆)

13. Create a 10x10 array with random values and find the minimum and maximum values (★☆☆)

```
In [41]: g=np.random.random((10,10))
Out[41]: array([[0.90005705, 0.98328121, 0.62492011, 0.5548771 , 0.15823363
                 0.45346475, 0.78492157, 0.63039117, 0.62585446, 0.74783865
         ],
                [0.10541635, 0.65169988, 0.63391122, 0.08704064, 0.06833723
                 0.18896972, 0.78591857, 0.71903419, 0.36682912, 0.60941882
         ],
                [0.01620981, 0.13648657, 0.30303598, 0.05032591, 0.15526704
                 0.0935427 , 0.43038619, 0.86181424, 0.00410034, 0.32979194
         ],
                [0.56925352, 0.17392608, 0.68759999, 0.12550366, 0.09906728
                 0.15756249, 0.00977323, 0.6652983, 0.82467368, 0.89527452
         ],
                [0.58717968, 0.27050513, 0.44464497, 0.65575782, 0.2633674
                 0.97541926, 0.91973792, 0.39358055, 0.54347658, 0.43969733
         ],
                 [0.96967941, 0.98316041, 0.55209943, 0.15309357, 0.35142155
                 0.72455887, 0.89746538, 0.31718343, 0.20153086, 0.6506147
         ],
                [0.34783547, 0.64027027, 0.14562874, 0.07793643, 0.59874019
                 0.40576042, 0.90147811, 0.76538156, 0.32340242, 0.25710718
         ],
                 [0.98121789, 0.07974413, 0.88416242, 0.68318328, 0.24519343
                 0.11250313, 0.07314364, 0.01931734, 0.04764178, 0.526018
         ],
                 [0.49835323, 0.12524231, 0.11738205, 0.76565308, 0.21122262
                 0.96658682, 0.21328417, 0.83383692, 0.48285392, 0.91807776
         ],
                [0.3507424 , 0.40167599, 0.9339651 , 0.2851172 , 0.02406186
                 0.2898851 , 0.06123243, 0.60298135, 0.09045495, 0.50594052
         ]])
In [42]: |q.min()
Out[42]: 0.004100338073978249
In [43]: q.max()
Out [43]: 0.9832812110467951
```

In [46]: h=np.random.random((30))

14. Create a random vector of size 30 and find the mean value (★☆☆)

```
Out[46]: array([0.21640756, 0.9306141 , 0.35624436, 0.3351772 , 0.44661212,
                0.38907482, 0.64706016, 0.11199821, 0.04123379, 0.57979128,
                 0.8755312 , 0.17077043, 0.3808254 , 0.22471358, 0.09363036,
                0.02129857, 0.62565545, 0.93539476, 0.05718409, 0.15040503,
                 0.92437644, 0.3619423 , 0.23287199, 0.83635233, 0.13457537,
                0.64506826, 0.00543304, 0.9375695 , 0.88485084, 0.61266722]
         )
In [47]: |h.mean()
Out[47]: 0.4388443253745781
         15. Create a 2d array with 1 on the border and 0 inside (★☆☆)
In [50]: |i| = np.ones((10,10))
         i[1:-1,1:-1]=0
         i
Out[50]: array([[1., 1., 1., 1., 1., 1., 1., 1., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
                 [1., 0., 0., 0., 0., 0., 0., 0., 0., 1.],
```

16. How to add a border (filled with 0's) around an existing array? (★☆☆)

[1., 0., 0., 0., 0., 0., 0., 0., 0., 1.], [1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])

17. What is the result of the following expression? ($\bigstar \stackrel{\wedge}{\swarrow} \stackrel{\wedge}{\swarrow}$)

```
0 * np.nan
np.nan == np.nan
np.inf > np.nan
np.nan - np.nan
np.nan in set([np.nan])
0.3 == 3 * 0.1
```

```
In [52]: 0 * np.nan
    np.nan == np.nan
    np.inf > np.nan
    np.nan - np.nan
    np.nan in set([np.nan])
    0.3 == 3 * 0.1
```

Out[52]: False

18. Create a 5x5 matrix with values 1,2,3,4 just below the diagonal (★☆☆)

```
http://localhost:8888/notebooks/Desktop/ICT%20Master%20Appli...%20Project%20Management/Roatny_MDAS_Numpy_Assignment.ipynb#
```

[0, 0, 3, 0, 0], [0, 0, 0, 4, 0]])

19. Create a 8x8 matrix and fill it with a checkerboard pattern (★☆☆)

20. Consider a (6,7,8) shape array, what is the index (x,y,z) of the 100th element? $(\bigstar \stackrel{\wedge}{\times} \stackrel{\wedge}{\times})$

21. Create a checkerboard 8x8 matrix using the tile function (★☆☆)

```
In [58]: array= np.array([[0,1], [1,0]])
m = np.tile(array,(4,4))
print (m)

[[0 1 0 1 0 1 0 1 0 1]
        [1 0 1 0 1 0 1 0]
        [0 1 0 1 0 1 0 1]
        [1 0 1 0 1 0 1 0]
        [0 1 0 1 0 1 0 1]
        [1 0 1 0 1 0 1 0]
        [0 1 0 1 0 1 0 1]
        [1 0 1 0 1 0 1 0 1]
        [1 0 1 0 1 0 1 0 1]
        [1 0 1 0 1 0 1 0]
```

22. Normalize a 5x5 random matrix (★☆☆)

23. Create a custom dtype that describes a color as four unsigned bytes (RGBA) $(\bigstar \stackrel{\wedge}{\not\sim} \stackrel{\wedge}{\not\sim})$

/var/folders/cj/m_37th0926n097rrzhpj0n1h0000gn/T/ipykernel_1285/14 89744843.py:1: FutureWarning: Passing (type, 1) or '1type' as a sy nonym of type is deprecated; in a future version of numpy, it will be understood as (type, (1,)) / '(1,)type'. color = np.dtype([("r", np.ubyte, 1),

```
Out[61]: dtype([('r', 'u1'), ('g', 'u1'), ('b', 'u1'), ('a', 'u1')])
```

24. Multiply a 5x3 matrix by a 3x2 matrix (real matrix product) (★☆☆)

25. Given a 1D array, negate all elements which are between 3 and 8, in place. (★☆☆)

26. What is the output of the following script? ($\bigstar \Leftrightarrow \Leftrightarrow$)

```
# Author: Jake VanderPlas
print(sum(range(5),-1))
from numpy import *
print(sum(range(5),-1))
```

```
In [65]: print(sum(range(5),-1))
from numpy import *
print(sum(range(5),-1))
```

9 10

27. Consider an integer vector Z, which of these expressions are legal? $(\bigstar \stackrel{\wedge}{\times} \stackrel{\wedge}{\times})$

```
Z**Z
2 << Z >>> 2
Z <- Z
1j*Z
Z/1/1
Z<Z>Z
```

```
In [70]: Z**Z
2 << Z >>> 2
Z <- Z
1j*Z
Z/1/1
Z<Z>Z
```

NameError: name 'Z' is not defined

28. What are the result of the following expressions? ($\bigstar \Leftrightarrow \Leftrightarrow$)

```
np.array(0) / np.array(0)
np.array(0) // np.array(0)
np.array([np.nan]).astype(int).astype(float)
```

/var/folders/cj/m_37th0926n097rrzhpj0n1h0000gn/T/ipykernel_1285/54
8293649.py:1: RuntimeWarning: invalid value encountered in true_di
vide
 np.array(0) / np.array(0)
/var/folders/cj/m_37th0926n097rrzhpj0n1h0000gn/T/ipykernel_1285/54

8293649.py:2: RuntimeWarning: divide by zero encountered in floor_

divide
 np.array(0) // np.array(0)

Out[71]: array([-9.22337204e+18])

29. How to round away from zero a float array ? (★☆☆)

```
In [72]:

r = np.random.uniform(-10,+10,10)
print (np.copysign(np.ceil(np.abs(r)), r))

[-4. 6. 10. 9. 8. 8. 1. 9. 5. -7.]
```

30. How to find common values between two arrays? (★☆☆)

```
In [73]: s1 = np.random.randint(0,10,10)
s2 = np.random.randint(0,10,10)
print(np.intersect1d(s1,s2))

[0 1 7 8]
```

31. How to ignore all numpy warnings (not recommended)? (★☆☆)

```
In [76]: defaults = np.seterr(all="ignore")
t = np.ones(1) / 0

_ = np.seterr(**defaults)
```

Out[76]: array([inf])

32. Is the following expressions true? (★☆☆)

```
np.sqrt(-1) == np.emath.sqrt(-1)
```

33. How to get the dates of yesterday, today and tomorrow? (★☆☆)

```
yesterday = np.datetime64('today', 'D') - np.timedelta64(1, 'D')
today = np.datetime64('today', 'D')
tomorrow = np.datetime64('today', 'D') + np.timedelta64(1, 'D')
```

34. How to get all the dates corresponding to the month of July 2016? (★★☆)

```
In [79]: u = np.arange('2016-07', '2016-08', dtype='datetime64[D]')
    print(u)

['2016-07-01' '2016-07-02' '2016-07-03' '2016-07-04' '2016-07-05'
    '2016-07-06' '2016-07-07' '2016-07-08' '2016-07-09' '2016-07-10'
    '2016-07-11' '2016-07-12' '2016-07-13' '2016-07-14' '2016-07-15'
    '2016-07-16' '2016-07-17' '2016-07-18' '2016-07-19' '2016-07-20'
    '2016-07-21' '2016-07-22' '2016-07-23' '2016-07-24' '2016-07-25'
    '2016-07-26' '2016-07-27' '2016-07-28' '2016-07-29' '2016-07-30'
    '2016-07-31']
```

35. How to compute ((A+B)*(-A/2)) in place (without copy)? ($\bigstar \bigstar \updownarrow$)

36. Extract the integer part of a random array of positive numbers using 4 different methods ($\bigstar \bigstar \Leftrightarrow$)

```
In [82]: z = np.random.uniform(0,10,10)

print (z- z%1)
print (np.floor(z))
print (np.ceil(z)-1)
print (z.astype(int))
[0. 6. 4. 9. 6. 5. 8. 2. 1. 4.]
[0. 6. 4. 9. 6. 5. 8. 2. 1. 4.]
[0. 6. 4. 9. 6. 5. 8. 2. 1. 4.]
[0. 6. 4. 9. 6. 5. 8. 2. 1. 4.]
[0. 6. 4. 9. 6. 5. 8. 2. 1. 4.]
```

37. Create a 5x5 matrix with row values ranging from 0 to 4 (★★☆)

```
In [83]: A = np.zeros((5,5))
A += np.arange(5)
print(A)

[[0. 1. 2. 3. 4.]
       [0. 1. 2. 3. 4.]
       [0. 1. 2. 3. 4.]
       [0. 1. 2. 3. 4.]
       [0. 1. 2. 3. 4.]]
```

38. Consider a generator function that generates 10 integers and use it to build an array ($\bigstar \diamondsuit \diamondsuit$)

```
In [84]: def generate():
        for x in range(10):
            yield x
B = np.fromiter(generate(),dtype=float,count=-1)
        print(B)

[0. 1. 2. 3. 4. 5. 6. 7. 8. 9.]
```

39. Create a vector of size 10 with values ranging from 0 to 1, both excluded $(\bigstar \bigstar \diamondsuit)$

```
In [85]: C = np.linspace(0,1,11,endpoint=False)[1:]
    print(C)
[0.09090909 0.18181818 0.27272727 0.36363636 0.45454545 0.54545455
```

40. Create a random vector of size 10 and sort it (★★☆)

0.63636364 0.72727273 0.81818182 0.90909091]

```
In [86]: D = np.random.random(10)
D.sort()
print(D)
```

[0.07073528 0.09213961 0.1740076 0.3511049 0.49282776 0.54447535 0.54858057 0.78595241 0.80182775 0.96082067]

41. How to sum a small array faster than np.sum? ($\bigstar \bigstar \diamondsuit$)

```
In [87]: E = np.arange(10)
np.add.reduce(E)
```

Out[87]: 45

42. Consider two random array A and B, check if they are equal $(\bigstar \bigstar)$

```
In [88]: F = np.random.randint(0,2,5)
G = np.random.randint(0,2,5)

# Assuming identical shape of the arrays and a tolerance for the colequal = np.allclose(F,G)
print(equal)

# Checking both the shape and the element values, no tolerance (valequal = np.array_equal(F,G)
print(equal)
```

False False

43. Make an array immutable (read-only) (★★☆)

```
In [90]: H = np.zeros(10)
H.flags.writeable = False
H[0] =1
```

```
ValueError
all last)
/var/folders/cj/m_37th0926n097rrzhpj0n1h0000gn/T/ipykernel_1285/33
58469309.py in <module>
          1 H = np.zeros(10)
          2 H.flags.writeable = False
----> 3 H[0] =1
```

ValueError: assignment destination is read-only

44. Consider a random 10x2 matrix representing cartesian coordinates, convert them to polar coordinates ($\bigstar \bigstar \diamondsuit$)

```
In [91]: Z = np.random.random((10,2))
X,Y = Z[:,0], Z[:,1]
R = np.sqrt(X**2+Y**2)
T = np.arctan2(Y,X)
print(R)
print(T)
```

[1.26617288 1.06735756 0.76156466 1.02911027 0.98644419 0.95277227 0.52599805 0.89303859 0.57637303 0.72953261] [0.78830904 1.18269249 1.36306527 0.53022826 0.53643567 1.36229739 1.45061017 0.33495232 1.33862223 0.99957451]

45. Create random vector of size 10 and replace the maximum value by 0 (★★☆)

[0. 0.89868593 0.331076 0.40759222 0.50564007 0.88842885 0.64825794 0.79051618 0.2235078 0.91180214]

46. Create a structured array with x and y coordinates covering the [0,1]x[0,1] area $(\bigstar \bigstar \dot{x})$

```
In [93]: J = np.zeros((5,5), [('x',float),('y',float)])
         J['x'], J['y'] = np.meshgrid(np.linspace(0,1,5),
                                     np.linspace(0,1,5))
         print(J)
                     ) (0.25, 0. ) (0.5, 0. ) (0.75, 0. ) (1.
         [[(0.
                                                                         )
                . 0.
          [(0.
                , 0.25) (0.25, 0.25) (0.5, 0.25) (0.75, 0.25) (1. , 0.25)
                , 0.5 ) (0.25, 0.5 ) (0.5 , 0.5 ) (0.75, 0.5 ) (1. , 0.5 )
          [(0.
          [(0.
                (0.75) (0.25, 0.75) (0.5, 0.75) (0.75, 0.75) (1., 0.75)
                , 1. ) (0.25, 1. ) (0.5 , 1. ) (0.75, 1. ) (1. , 1. )
          [(0.
         11
```

47. Given two arrays, X and Y, construct the Cauchy matrix C (Cij =1/(xi - yj)) (★★☆)

```
In [94]: X = np.arange(8)
Y = X + 0.5
C = 1.0 / np.subtract.outer(X, Y)
print(np.linalg.det(C))
```

3638.1636371179666

48. Print the minimum and maximum representable value for each numpy scalar type $(\bigstar \bigstar \diamondsuit)$

```
In [95]: | for dtype in [np.int8, np.int32, np.int64]:
            print(np.iinfo(dtype).min)
            print(np.iinfo(dtype).max)
         for dtype in [np.float32, np.float64]:
            print(np.finfo(dtype).min)
            print(np.finfo(dtype).max)
            print(np.finfo(dtype).eps)
         -128
         127
         -2147483648
         2147483647
         -9223372036854775808
         9223372036854775807
         -3.4028235e+38
         3.4028235e+38
         1.1920929e-07
         -1.7976931348623157e+308
         1.7976931348623157e+308
         2.220446049250313e-16
```

49. How to print all the values of an array? $(\star \star \Rightarrow \Rightarrow)$

```
In [ ]: np.set_printoptions(threshold=np.nan)
Z = np.zeros((25,25))
print(Z)
```

50. How to find the closest value (to a given scalar) in a vector? ($\star\star$

```
In [100]: Z = np.arange(100)
v = np.random.uniform(0,100)
index = (np.abs(Z-v)).argmin()
print(Z[index])
```

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51. Create a structured array representing a position (x,y) and a color (r,g,b) $(\bigstar \bigstar \Leftrightarrow)$

52. Consider a random vector with shape (100,2) representing coordinates, find point by point distances ($\bigstar \star \dot{\chi}$)

```
In [102]: Z = np.random.random((10,2))
          X,Y = np.atleast_2d(Z[:,0], Z[:,1])
          D = np.sqrt((X-X.T)**2 + (Y-Y.T)**2)
          print(D)
          # Much faster with scipy
          import scipy
          # Thanks Gavin Heverly-Coulson (#issue 1)
          import scipy.spatial
          Z = np.random.random((10,2))
          D = scipy.spatial.distance.cdist(Z,Z)
          print(D)
          [[0.
                       0.45574237 0.71065675 0.5532571 0.37305855 0.5832279
            0.09648755 0.22007657 0.4296158 0.22956487]
           [0.45574237 0.
                                 0.25671212 0.32311608 0.67454655 0.8271582
            0.51773205 0.47437548 0.10209215 0.48001645]
           [0.71065675 0.25671212 0.
                                            0.38625712 0.91617241 1.0073706
            0.76672147 0.69898085 0.29632386 0.702737431
           [0.5532571 0.32311608 0.38625712 0.
                                                       0.88337931 0.6452834
            0.56118623 0.42825599 0.2298198 0.42714353]
```

```
[0.37305855 0.67454655 0.91617241 0.88337931 0.
                                                         0.9179338
  0.43678669 0.59118398 0.70036168 0.60032696]
 [0.58322797 0.82715823 1.00737063 0.64528342 0.91793386 0.
  0.49408561 0.39201172 0.73667296 0.38281314]
 [0.09648755 0.51773205 0.76672147 0.56118623 0.43678669 0.4940856
1
            0.16551707 0.47521292 0.17317005]
 [0.22007657 0.47437548 0.69898085 0.42825599 0.59118398 0.3920117
 0.16551707 0.
                       0.40374093 0.009856971
 [0.4296158 0.10209215 0.29632386 0.2298198 0.70036168 0.7366729
6
  0.47521292 0.40374093 0.
                                  0.407967531
 [0.22956487 0.48001645 0.70273743 0.42714353 0.60032696 0.3828131
  0.17317005 0.00985697 0.40796753 0.
                                            11
[[0.
            0.57028851 0.69491963 0.58108204 0.35937161 0.4822617
3
  0.30437074 0.69547421 0.19932133 0.309884461
 [0.57028851 0.
                       0.49856277 0.6117666 0.92829177 0.6272497
  0.31932044 0.82667247 0.69975511 0.27778885]
 [0.69491963 0.49856277 0.
                                  1.04266412 1.00091598 1.0134583
  0.65423162 0.42740365 0.8910471 0.46174516
 [0.58108204 0.6117666 1.04266412 0.
                                              0.77829784 0.1257814
  0.39759519 1.21822043 0.50829251 0.59590401]
 [0.35937161 0.92829177 1.00091598 0.77829784 0.
                                                         0.6541189
  0.63995068 0.86390395 0.27832238 0.66807487]
 [0.48226173 0.62724978 1.01345837 0.12578145 0.65411896 0.
  0.35947152 1.14744485 0.38782859 0.55394261
 [0.30437074 0.31932044 0.65423162 0.39759519 0.63995068 0.3594715
2
  0.
            0.82988234 0.38841133 0.19858491]
 [0.69547421 0.82667247 0.42740365 1.21822043 0.86390395 1.1474448
  0.82988234 0.
                       0.88112098 0.64500481]
 [0.19932133 0.69975511 0.8910471 0.50829251 0.27832238 0.3878285
  0.38841133 0.88112098 0.
                                  0.474691451
 [0.30988446 0.27778885 0.46174516 0.59590401 0.66807487 0.5539426
1
  0.19858491 0.64500481 0.47469145 0.
                                             ]]
```

53. How to convert a float (32 bits) array into an integer (32 bits) in place?

```
In [103]: Z = np.arange(10, dtype=np.int32)
Z = Z.astype(np.float32, copy=False)
print(Z)
```

[0. 1. 2. 3. 4. 5. 6. 7. 8. 9.]

54. How to read the following file? $(\bigstar \bigstar \diamondsuit)$

```
1, 2, 3, 4, 5
6, , , 7, 8
, , 9,10,11
```

```
[[ 1 2 3 4 5]
[ 6 -1 -1 7 8]
[-1 -1 9 10 11]]
```

/var/folders/cj/m_37th0926n097rrzhpj0n1h0000gn/T/ipykernel_1285/12 71915251.py:7: DeprecationWarning: `np.int` is a deprecated alias for the builtin `int`. To silence this warning, use `int` by itsel f. Doing this will not modify any behavior and is safe. When repla cing `np.int`, you may wish to use e.g. `np.int64` or `np.int32` t o specify the precision. If you wish to review your current use, c heck the release note link for additional information.

Deprecated in NumPy 1.20; for more details and guidance: https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations (https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations)

Z = np.genfromtxt(s, delimiter=",", dtype=np.int)

55. What is the equivalent of enumerate for numpy arrays? ($\bigstar \star \updownarrow$)

```
(0, 0) 0
(0, 1) 1
(0, 2) 2
(1, 0) 3
(1, 1) 4
(1, 2) 5
(2, 0) 6
(2, 1) 7
(2, 2) 8
(0, 0) 0
(0, 1) 1
(0, 2) 2
(1, 0) 3
(1, 1) 4
(1, 2) 5
(2, 0) 6
(2, 1) 7
(2, 2) 8
```

56. Generate a generic 2D Gaussian-like array (★★☆)

```
In [4]: Z = np.arange(9).reshape(3,3)
        for index, value in np.ndenumerate(Z):
            print(index, value)
        for index in np.ndindex(Z.shape):
            print(index, Z[index])
        (0, 0) 0
        (0, 1) 1
        (0, 2) 2
        (1, 0) 3
        (1, 1) 4
        (1, 2) 5
        (2, 0) 6
        (2, 1) 7
        (2, 2) 8
        (0, 0) 0
        (0, 1) 1
        (0, 2) 2
        (1, 0) 3
        (1, 1) 4
        (1, 2) 5
        (2, 0) 6
        (2, 1) 7
        (2, 2) 8
```

57. How to randomly place p elements in a 2D array? (★★☆)

58. Subtract the mean of each row of a matrix ($\star\star$)

```
In [7]:
        X = np.random.rand(5, 10)
        # Recent versions of numpy
        Y = X - X.mean(axis=1, keepdims=True)
        # Older versions of numpy
        Y = X - X.mean(axis=1).reshape(-1, 1)
        print(Y)
        \lceil -0.40459155 \quad 0.20833087 \quad -0.11312464 \quad -0.22090915 \quad 0.03904833 \quad -0.0
        8105609
           0.061333451
         [-0.3181533
                       0.37084311 -0.24625812
                                               0.06504
                                                           0.38515546 - 0.3
        2173493
           0.15294926 0.03859459 -0.54766357
                                               0.421227491
         [-0.07047032 0.46348719 -0.06872773
                                               0.18831735 - 0.09063542 - 0.1
        1750908
          -0.32166971 -0.02904471 -0.02019143
                                               0.066443851
         [-0.37076738 0.15068995 0.46966491
                                               0.46233958 -0.2445305
                                                                       0.4
        3542208
          -0.10439545 -0.25732393 -0.32267347 -0.21842578
         [-0.59261501 0.05993769 0.01968782
                                               0.03289092 0.39717162
                                                                       0.2
        1174831
          -0.5212097 -0.22806755 0.23308934 0.38736656]]
```

59. How to sort an array by the nth column? $(\star \star \Rightarrow)$

```
In [8]: Z = np.random.randint(0,10,(3,3))
    print(Z)
    print(Z[Z[:,1].argsort()])

[[3 4 6]
      [5 6 3]
      [9 5 1]]
[[3 4 6]
      [9 5 1]
      [5 6 3]]
```

60. How to tell if a given 2D array has null columns? $(\bigstar \bigstar)$

```
In [9]: Z = np.random.randint(0,3,(3,10))
print((~Z.any(axis=0)).any())
```

True

61. Find the nearest value from a given value in an array (★★☆)

```
In [10]: Z = np.random.uniform(0,1,10)
z = 0.5
m = Z.flat[np.abs(Z - z).argmin()]
print(m)
```

0.3416144101832661

62. Considering two arrays with shape (1,3) and (3,1), how to compute their sum using an iterator? $(\bigstar \bigstar)$

63. Create an array class that has a name attribute (★★☆)

```
In [12]:
    class NamedArray(np.ndarray):
        def __new__(cls, array, name="no name"):
            obj = np.asarray(array).view(cls)
            obj.name = name
            return obj
        def __array_finalize__(self, obj):
            if obj is None: return
            self.info = getattr(obj, 'name', "no name")

Z = NamedArray(np.arange(10), "range_10")
        print (Z.name)
```

range_10

64. Consider a given vector, how to add 1 to each element indexed by a second vector (be careful with repeated indices)? $(\bigstar \star \star)$

```
In [13]: Z = np.ones(10)
I = np.random.randint(0,len(Z),20)
Z += np.bincount(I, minlength=len(Z))
print(Z)

# Another solution
# Author: Bartosz Telenczuk
np.add.at(Z, I, 1)
print(Z)

[1. 3. 3. 4. 5. 1. 3. 2. 5. 3.]
[1. 5. 5. 7. 9. 1. 5. 3. 9. 5.]
```

65. How to accumulate elements of a vector (X) to an array (F) based on an index list (I)? $(\pm \star \pm)$

```
In [14]: X = [1,2,3,4,5,6]
I = [1,3,9,3,4,1]
F = np.bincount(I,X)
print(F)

[0, 7, 0, 6, 5, 0, 0, 0, 3,]
```

66. Considering a (w,h,3) image of (dtype=ubyte), compute the number of unique colors (★★☆)

```
In [15]: w,h = 16,16
I = np.random.randint(0,2,(h,w,3)).astype(np.ubyte)
F = I[...,0]*256*256 + I[...,1]*256 +I[...,2]
n = len(np.unique(F))
print(np.unique(I))
[0 1]
```

67. Considering a four dimensions array, how to get sum over the last two axis at once? $(\bigstar \bigstar \bigstar)$

```
In [16]: A = np.random.randint(0,10,(3,4,3,4))
# solution by passing a tuple of axes (introduced in numpy 1.7.0)
sum = A.sum(axis=(-2,-1))
print(sum)
# solution by flattening the last two dimensions into one
# (useful for functions that don't accept tuples for axis argument)
sum = A.reshape(A.shape[:-2] + (-1,)).sum(axis=-1)
print(sum)

[[55 53 70 53]
[63 56 55 63]
[47 56 44 54]]
[[55 53 70 53]
[63 56 55 63]
[47 56 44 54]]
```

68. Considering a one-dimensional vector D, how to compute means of subsets of D using a vector S of same size describing subset indices? $(\bigstar \bigstar \bigstar)$

```
In [17]:
         D = np.random.uniform(0,1,100)
         S = np.random.randint(0,10,100)
         D_sums = np.bincount(S, weights=D)
         D counts = np.bincount(S)
         D_means = D_sums / D_counts
         print(D means)
         # Pandas solution as a reference due to more intuitive code
         import pandas as pd
         print(pd.Series(D).groupby(S).mean())
          [0.57146854 0.60286441 0.40416054 0.42371912 0.4494612 0.60707258
          0.37493685 0.50487551 0.39462024 0.38841574]
               0.571469
         1
               0.602864
         2
              0.404161
              0.423719
         3
         4
              0.449461
         5
              0.607073
         6
              0.374937
         7
              0.504876
         8
              0.394620
         9
               0.388416
         dtype: float64
```

69. How to get the diagonal of a dot product? ($\star\star$

```
In [18]:
    A = np.random.uniform(0,1,(5,5))
    B = np.random.uniform(0,1,(5,5))

# Slow version
    np.diag(np.dot(A, B))

# Fast version
    np.sum(A * B.T, axis=1)

# Faster version
    np.einsum("ij,ji->i", A, B)

Out[18]: array([2.53885442, 0.70691255, 0.59769867, 1.27727734, 1.17424763])
```

70. Consider the vector [1, 2, 3, 4, 5], how to build a new vector with 3 consecutive zeros interleaved between each value? ($\bigstar \bigstar \bigstar$)

```
In [19]:
    Z = np.array([1,2,3,4,5])
    nz = 3
    Z0 = np.zeros(len(Z) + (len(Z)-1)*(nz))
    Z0[::nz+1] = Z
    print(Z0)
    [1. 0. 0. 0. 2. 0. 0. 0. 3. 0. 0. 0. 4. 0. 0. 0. 5.]
```

71. Consider an array of dimension (5,5,3), how to mulitply it by an array with dimensions (5,5)? $(\star\star\star)$

```
In [20]: A = np.ones((5,5,3))
          B = 2*np.ones((5,5))
          print(A * B[:,:,None])
          [[2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]]
           [[2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]]
           [[2, 2, 2, 1]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.1]
           [[2, 2, 2, ]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]]
           [[2, 2, 2, 1]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]
            [2. 2. 2.]]]
```

72. How to swap two rows of an array? $(\bigstar \bigstar \bigstar)$

```
In [21]: A = np.arange(25).reshape(5,5)
A[[0,1]] = A[[1,0]]
print(A)

[[ 5  6  7  8   9]
      [ 0  1  2  3   4]
      [10 11 12 13 14]
      [15  16  17  18  19]
      [20  21  22  23  24]]
```

73. Consider a set of 10 triplets describing 10 triangles (with shared vertices), find the set of unique line segments composing all the triangles ($\bigstar \bigstar \bigstar$)

```
In [22]: faces = np.random.randint(0,100,(10,3))
    F = np.roll(faces.repeat(2,axis=1),-1,axis=1)
    F = F.reshape(len(F)*3,2)
    F = np.sort(F,axis=1)
    G = F.view( dtype=[('p0',F.dtype),('p1',F.dtype)] )
    G = np.unique(G)
    print(G)

    [( 4, 22) ( 4, 80) ( 6, 24) ( 6, 68) ( 8, 73) ( 8, 82) ( 8, 83) ( 8, 91)
        (10, 21) (10, 32) (10, 54) (10, 80) (21, 32) (22, 80) (24, 68) (3 6, 84)
        (36, 85) (40, 48) (40, 73) (48, 73) (51, 78) (51, 82) (54, 80) (7 3, 82)
        (75, 93) (75, 99) (78, 82) (83, 91) (84, 85) (93, 99)]
```

74. Given a sorted array C that corresponds to a bincount, how to produce an array A such that np.bincount(A) == \mathbb{C} ? ($\bigstar \star \star$)

```
In [23]: C = np.bincount([1,1,2,3,4,4,6])
A = np.repeat(np.arange(len(C)), C)
print(A)

[1 1 2 3 4 4 6]
```

75. How to compute averages using a sliding window over an array? (★★★)

76. Consider a one-dimensional array Z, build a two-dimensional array whose first row is (Z[0],Z[1],Z[2]) and each subsequent row is shifted by 1 (last row should be (Z[-3],Z[-2],Z[-1]) (\bigstar

[7 8 9]]

```
In [25]: from numpy.lib import stride_tricks

def rolling(a, window):
    shape = (a.size - window + 1, window)
    strides = (a.itemsize, a.itemsize)
    return stride_tricks.as_strided(a, shape=shape, strides=strides

Z = rolling(np.arange(10), 3)
print(Z)

[[0 1 2]
  [1 2 3]
  [2 3 4]
  [3 4 5]
  [4 5 6]
  [5 6 7]
  [6 7 8]
```

77. How to negate a boolean, or to change the sign of a float inplace? $(\bigstar \bigstar \bigstar)$

In [26]: Z = np.random.randint(0,2,100)

```
np.logical not(Z, out=Z)
         Z = np.random.uniform(-1.0, 1.0, 100)
         np.negative(Z, out=Z)
Out[26]: array([ 0.3497504 , -0.3979124 , 0.13582173, 0.44657538,
                                                                     0.6957
         1546.
                 0.74750678, 0.69142115, -0.9056327, -0.94051209, -0.7827
         0662,
                 0.75072325, -0.1378537, -0.50240359, -0.23983862, 0.5425
         1255,
                -0.68801251, 0.29876285, -0.91887031, 0.78986207, -0.1546
         7315,
                -0.74501757, 0.04297443, 0.47587592, 0.57771489,
                                                                    0.8273
         1932,
                 0.23476873, 0.45941788, -0.51928372, -0.9266702,
                                                                    0.9742
         2173,
                 0.20294609, 0.99930156, -0.39814051, 0.26113002, -0.0445
         9141,
                -0.08265899, -0.86554058, 0.26216449, 0.21055264,
                                                                    0.9352
         5242,
                -0.38390414, -0.81326614, 0.86864029, -0.80876403, -0.3014
         1593,
                -0.14139024, -0.90190665, -0.94683187, -0.38874918,
                                                                    0.4188
         5534,
                -0.03536736, 0.30872982,
                                          0.88987136, 0.0861563,
                                                                    0.3715
         6055,
                -0.9301718 , -0.65574918,
                                          0.14198597, -0.98227561,
                                                                    0.9625
         2119,
                 0.90004964, 0.75517361,
                                          0.84218896, 0.37114059, -0.3877
         448 ,
                 0.88559001. 0.2760651. 0.09361562. 0.86786971. 0.6948
         5986,
                -0.19893208, -0.31311717,
                                          0.49581271, 0.75279381, -0.8065
         677 ,
                 0.01472876, -0.92101422, 0.95522871, -0.66887861, -0.4006
         4936,
                -0.25710423, -0.30294865, -0.61665386, -0.16228169, 0.8462
         9874.
                -0.36508614, 0.77920276, 0.91277102, 0.99224436, -0.8300
         5601,
                -0.16186958, -0.95255491, 0.80210863, 0.91917702, -0.0992
         0456,
                -0.20340782, -0.2487168, -0.29088956, 0.63109706, 0.4381
         45191)
```

78. Consider 2 sets of points P0,P1 describing lines (2d) and a point p, how to compute distance from p to each line i (P0[i],P1[i])? $(\bigstar \star \star)$

```
In [27]: def distance(P0, P1, p):
    T = P1 - P0
    L = (T**2).sum(axis=1)
    U = -((P0[:,0]-p[...,0])*T[:,0] + (P0[:,1]-p[...,1])*T[:,1]) /
    U = U.reshape(len(U),1)
    D = P0 + U*T - p
    return np.sqrt((D**2).sum(axis=1))

P0 = np.random.uniform(-10,10,(10,2))
    P1 = np.random.uniform(-10,10,(10,2))
    p = np.random.uniform(-10,10,(10,2))
    p = np.random.uniform(-10,10,(10,2))
    print(distance(P0, P1, p))
```

```
[ 2.75609682 13.16625876  0.47734244 11.89799392  7.44924655  8.52  266477  13.58367067  9.07258314  6.23717516  9.79416119]
```

79. Consider 2 sets of points P0,P1 describing lines (2d) and a set of points P, how to compute distance from each point j (P[j]) to each line i (P0[i],P1[i])? (★★★)

```
In [28]: P0 = np.random.uniform(-10, 10, (10,2))
         P1 = np.random.uniform(-10,10,(10,2))
         p = np.random.uniform(-10, 10, (10,2))
         print(np.array([distance(P0,P1,p_i) for p_i in p]))
         [[ 2.88602843 4.71728439
                                     8.82952128
                                                  1.63097634
                                                                           3.5
                                                              5.23119758
         3893427
            9.38288165
                         7.12863047
                                     0.32453436
                                                  1.773104831
           [15.41529823 11.57901067
                                     3.30721455
                                                  1.5861924
                                                              2.95997521 14.0
         6281563
            4.28412707
                         1.07990146 13.36592607 11.66165921]
           [16.24883565 12.22066272
                                     3.65609164
                                                  1.42326463
                                                              3.65580733 15.0
         3815535
                         1.77643945 13.77367572 12.09563496]
            3.71976195
          [ 8.56596738
                         3.31715399 5.62021585 6.27341995
                                                              6.83622718 11.2
         1038924
            0.9511647
                         4.94783381
                                     4.47995871
                                                  2.80719541
           [ 3.86791554
                         2.39264116
                                     2.12863313
                                                  2.92858494
                                                              5.72564889
                                                                           1.0
         6431812
           11.12075757
                         7.61575189
                                     7.16671986
                                                  5.123693951
           1.60542747
                         0.7480818
                                     2.87875128
                                                  3.6695826
                                                              7.92596928
                                                                           1.7
         507296
           12.97328803
                         9.81790641
                                     6.23974351
                                                  4.117508861
           [ 8.56139292
                         3.50809695
                                     5.22786241
                                                  5.6741333
                                                              6.20827979 10.8
         6922085
            0.30580496
                         4.32004644
                                     4.83782084
                                                  3.14884478]
           [ 3.19639135
                         6.76099181 12.61856145
                                                  7.12389437
                                                              0.30214956
                                                                           0.7
         8544552
                         1.59706723
                                                  5.127589141
            3.63228634
                                     3.16931706
                         6.84619193
          [ 8.25293133
                                     1.89229791
                                                  5.38859035
                                                              5.52485362
                                                                           4.3
         3375929
                         7.41033472 11.30795581
                                                  9.313822471
           11.71209773
          [14.95002389 13.06583501
                                    6.85311096
                                                  7.35441451 3.34988305 10.3
         3232087
           10.69264706
                        5.22879585 16.55478772 14.68342781]]
```

80. Consider an arbitrary array, write a function that extract a subpart with a fixed shape and centered on a given element (pad with a fill value when necessary) $(\star\star\star$

```
In [30]: Z = np.random.randint(0,10,(10,10))
         shape = (5,5)
         fill = 0
         position = (1,1)
         R = np.ones(shape, dtype=Z.dtype)*fill
         P = np.array(list(position)).astype(int)
         Rs = np.array(list(R.shape)).astype(int)
         Zs = np.array(list(Z.shape)).astype(int)
         R start = np.zeros((len(shape),)).astype(int)
         R_stop = np.array(list(shape)).astype(int)
         Z_start = (P-Rs//2)
         Z \text{ stop} = (P+Rs//2)+Rs%2
         R_start = (R_start - np.minimum(Z_start,0)).tolist()
         Z start = (np.maximum(Z start,0)).tolist()
         R_{stop} = np.maximum(R_{start}, (R_{stop} - np.maximum(Z_{stop} - Zs, 0))).to
         Z_{stop} = (np.minimum(Z_{stop}, Z_{s})).tolist()
         r = [slice(start,stop) for start,stop in zip(R_start,R_stop)]
         z = [slice(start,stop) for start,stop in zip(Z start,Z stop)]
         R[r] = Z[z]
         print(Z)
         print(R)
```

```
[[9 5 8 9 1 0 6 2 6 3]
[7 1 3 8 5 5 8 9 0 7]
[3 9 1 3 9 3 8 0 6 3]
[4 4 0 0 0 7 1 8 5 9]
[2 0 6 5 2 8 0 6 9 0]
[9 4 9 8 8 5 9 9 3 4]
[8 1 8 9 2 6 7 1 1 7]
[0 0 7 5 5 3 0 3 1 3]
[4 5 4 6 3 5 0 8 2 6]
[8 4 1 9 3 5 1 0 1 3]]
[[0 0 0 0 0]
[0 9 5 8 9]
[0 7 1 3 8]
[0 3 9 1 3]
[0 4 4 0 0]]
```

/var/folders/cj/m_37th0926n097rrzhpj0n1h0000gn/T/ipykernel_1308/20 87351065.py:23: FutureWarning: Using a non-tuple sequence for mult idimensional indexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the future this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

```
R[r] = Z[z]
```

81. Consider an array Z = [1,2,3,4,5,6,7,8,9,10,11,12,13,14], how to generate an array R = [[1,2,3,4], [2,3,4,5], [3,4,5,6], ..., [11,12,13,14]]? ($\bigstar \star \star \star$)

```
In [31]: Z = np.arange(1,15,dtype=np.uint32)
         R = stride_tricks.as_strided(Z,(11,4),(4,4))
         print(R)
         [[1
               2
                     4]
               3 4 5]
          [ 2
          [ 3
               4 5
                    6]
          [ 4
               5 6
                     71
               6 7 8]
          [ 5
          6
               7 8 91
          [ 7
               8 9 10]
          [8 9 10 11]
          [ 9 10 11 12]
          [10 11 12 13]
          [11 12 13 14]]
```

82. Compute a matrix rank (★★★)

```
In [33]: Z = np.random.uniform(0,1,(10,10))
U, S, V = np.linalg.svd(Z) # Singular Value Decomposition
rank = np.sum(S > 1e-10)
print(rank)
```

10

83. How to find the most frequent value in an array?

```
In [34]: Z = np.random.randint(0,10,50)
print(np.bincount(Z).argmax())
```

4

84. Extract all the contiguous 3x3 blocks from a random 10x10 matrix $(\bigstar \bigstar \bigstar)$

```
In [35]: Z = np.random.randint(0,5,(10,10))
          n = 3
          i = 1 + (Z.shape[0]-3)
          j = 1 + (Z.shape[1]-3)
          C = stride_tricks.as_strided(Z, shape=(i, j, n, n), strides=Z.strid
          print(C)
             [4 2 3]
             [0 2 0]]]
           [[[2 2 0]
             [3 2 0]
             [1 \ 1 \ 1]
            [[2 0 1]
             [2 0 4]
             [1 1 3]]
            [[0 1 0]
             [0 \ 4 \ 2]
             [1 3 3]]
            [[1 0 2]
             [4 2 2]
             [3 3 0]]
```

85. Create a 2D array subclass such that Z[i,j] == Z[j,i] (★★★)

```
In [36]: class Symetric(np.ndarray):
    def __setitem__(self, index, value):
        i,j = index
            super(Symetric, self).__setitem__((i,j), value)
        super(Symetric, self).__setitem__((j,i), value)

def symetric(Z):
    return np.asarray(Z + Z.T - np.diag(Z.diagonal())).view(Symetri

S = symetric(np.random.randint(0,10,(5,5)))
S[2,3] = 42
print(S)

[[ 1    7    15    10    7]
[ 7    4    7    16    14]
[ 15    7    0    42    6]
[ 10    16    42    6    12]
[ 7    14    6    12    6]]
```

86. Consider a set of p matrices wich shape (n,n) and a set of p vectors with shape (n,1). How to compute the sum of the p matrix products at once? (result has shape (n,1)) $(\bigstar \star \star)$

```
In [37]: p, n = 10, 20
          M = np.ones((p,n,n))
          V = np.ones((p,n,1))
          S = np.tensordot(M, V, axes=[[0, 2], [0, 1]])
          print(S)
          [[200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]
           [200.]]
```

87. Consider a 16x16 array, how to get the block-sum (block size is 4x4)? $(\star\star\star)$

88. How to implement the Game of Life using numpy arrays? $(\star \star \star)$

```
In [41]: def iterate(Z):
              # Count neighbours
              N = (Z[0:-2,0:-2] + Z[0:-2,1:-1] + Z[0:-2,2:] +
                    Z[1:-1,0:-2]
                                                 + Z[1:-1,2:] +
                    Z[1:-1,0:-2] + Z[1:-1,2:] - Z[2: ,0:-2] + Z[2: ,1:-1] + Z[2: ,2:])
              # Apply rules
              birth = (N==3) & (Z[1:-1,1:-1]==0)
              survive = ((N==2) | (N==3)) & (Z[1:-1,1:-1]==1)
              Z[\ldots] = 0
              Z[1:-1,1:-1][birth | survive] = 1
               return Z
          Z = np.random.randint(0,2,(50,50))
          for i in range(100): Z = iterate(Z)
          print(Z)
          [[0 \ 0 \ 0 \ \dots \ 0 \ 0 \ 0]
           [0\ 0\ 0\ \dots\ 0\ 0\ 0]
           [0 0 0 ... 0 0 0]
```

89. How to get the n largest values of an array ($\star\star$

[0 0 0 ... 0 0 0] [0 0 0 ... 0 0 0] [0 0 0 ... 0 0 0]]

[9999 9998 9996 9997 9995]

```
In [42]: Z = np.arange(10000)
    np.random.shuffle(Z)
    n = 5

# Slow
    print (Z[np.argsort(Z)[-n:]])

# Fast
    print (Z[np.argpartition(-Z,n)[:n]])

[9995 9996 9997 9998 9999]
```

90. Given an arbitrary number of vectors, build the cartesian product (every combinations of every item) $(\bigstar \bigstar \bigstar)$

```
In [43]:

def cartesian(arrays):
    arrays = [np.asarray(a) for a in arrays]
    shape = (len(x) for x in arrays)

    ix = np.indices(shape, dtype=int)
    ix = ix.reshape(len(arrays), -1).T

    for n, arr in enumerate(arrays):
        ix[:, n] = arrays[n][ix[:, n]]

    return ix

print (cartesian(([1, 2, 3], [4, 5], [6, 7])))

[[1 4 6]
```

```
[1 4 6]

[1 4 7]

[1 5 6]

[1 5 7]

[2 4 6]

[2 5 6]

[2 5 7]

[3 4 6]

[3 5 6]

[3 5 7]
```

91. How to create a record array from a regular array? (★★★)

92. Consider a large vector Z, compute Z to the power of 3 using 3 different methods ($\bigstar \bigstar \bigstar$)

```
In [48]: x = np.random.rand(5e7)

%timeit np.power(x,3)
%timeit x*x*x
%timeit np.einsum('i,i,i->i',x,x,x)
```

93. Consider two arrays A and B of shape (8,3) and (2,2). How to find rows of A that contain elements of each row of B regardless of the order of the elements in B? $(\star\star\star)$

```
In [49]: A = np.random.randint(0,5,(8,3))
B = np.random.randint(0,5,(2,2))

C = (A[..., np.newaxis, np.newaxis] == B)
  rows = np.where(C.any((3,1)).all(1))[0]
  print(rows)
[0 3 7]
```

94. Considering a 10x3 matrix, extract rows with unequal values (e.g. [2,2,3]) (★★★)

```
In [50]: Z = np.random.randint(0,5,(10,3))
          print(Z)
          # solution for arrays of all dtypes (including string arrays and re
          E = np.all(Z[:,1:] == Z[:,:-1], axis=1)
          U = Z[\sim E]
          print(U)
          # soluiton for numerical arrays only, will work for any number of c
          U = Z[Z.max(axis=1) != Z.min(axis=1),:]
          print(U)
          [[3 0 1]
           [3 1 3]
           [3 2 0]
           [0 3 3]
           [0 \ 4 \ 4]
           [1 3 0]
           [4 1 3]
           [1 2 4]
           [2 0 1]
           [4 2 0]]
          [[3 0 1]
           [3 1 3]
           [3 2 0]
           [0 3 3]
           [0 \ 4 \ 4]
           [1 \ 3 \ 0]
           [4 1 3]
           [1 2 4]
           [2 0 1]
           [4 2 0]]
          [[3 0 1]
           [3 1 3]
           [3 2 0]
           [0 3 3]
           [0 \ 4 \ 4]
           [1 3 0]
           [4 1 3]
           [1 2 4]
           [2 0 1]
           [4 2 0]]
```

95. Convert a vector of ints into a matrix binary representation ($\star\star$

```
In [51]: I = np.array([0, 1, 2, 3, 15, 16, 32, 64, 128])
          B = ((I.reshape(-1,1) \& (2**np.arange(8))) != 0).astype(int)
          print(B[:,::-1])
         # Author: Daniel T. McDonald
          I = np.array([0, 1, 2, 3, 15, 16, 32, 64, 128], dtype=np.uint8)
          print(np.unpackbits(I[:, np.newaxis], axis=1))
          [[0 0 0 0 0 0 0]]
           [0 0 0 0 0 0 0 1]
           [0 0 0 0 0 0 1 0]
           [0 0 0 0 0 0 1 1]
           [0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1]
           [0 0 0 1 0 0 0 0]
           [0 0 1 0 0 0 0 0]
           [0 1 0 0 0 0 0 0]
           [1 0 0 0 0 0 0 0]]
          [[0 0 0 0 0 0 0 0]
           [0 0 0 0 0 0 0 1]
           [0 0 0 0 0 0 1 0]
           [0 0 0 0 0 0 1 1]
           [0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1]
           [0 0 0 1 0 0 0 0]
           [0 0 1 0 0 0 0 0]
           [0 1 0 0 0 0 0 0]
           [1 0 0 0 0 0 0 0]]
```

96. Given a two dimensional array, how to extract unique rows? (★★★)

```
In [52]: Z = np.random.randint(0,2,(6,3))
    T = np.ascontiguousarray(Z).view(np.dtype((np.void, Z.dtype.itemsiz
    _, idx = np.unique(T, return_index=True)
    uZ = Z[idx]
    print(uZ)

[[0 1 0]
    [0 1 1]
    [1 0 1]
    [1 1 0]
    [1 1 1]]
```

97. Considering 2 vectors A & B, write the einsum equivalent of inner, outer, sum, and mul function $(\star \star \star)$

```
In [53]: A = np.random.uniform(0,1,10)
         B = np.random.uniform(0.1.10)
         np.einsum('i->', A)
                                   # np.sum(A)
         np.einsum('i,i->i', A, B) # A * B
         np.einsum('i,i', A, B)
                                   # np.inner(A, B)
         np.einsum('i,j->ij', A, B)
                                       # np.outer(A, B)
Out[53]: array([[0.31276462, 0.30089477, 0.45198479, 0.40211532, 0.26163358
                 0.1003606 , 0.18592724, 0.25024273, 0.4183349 , 0.48905826
         ],
                 [0.10086815, 0.09704007, 0.14576736, 0.1296842 , 0.08437814
                 0.0323668 , 0.05996247, 0.08070453, 0.1349151 , 0.15772374
         ],
                 [0.26565585, 0.25557385, 0.38390661, 0.3415485 , 0.2222262
                 0.08524424, 0.15792278, 0.21255104, 0.35532508, 0.41539606
         ],
                [0.27287885, 0.26252272, 0.39434477, 0.35083497, 0.22826838
         ,
                 0.08756197, 0.1622166 , 0.21833015, 0.36498612, 0.42669039
         ],
                 [0.09325224, 0.08971319, 0.1347614 , 0.11989258, 0.07800729
                 0.02992299, 0.05543508, 0.07461105, 0.12472852, 0.14581503
         ],
                 [0.44942489, 0.4323686, 0.64947633, 0.57781674, 0.37595252
                 0.14421246, 0.26716682, 0.3595845 , 0.60112336, 0.70274879
         ],
                [0.13689038, 0.13169521, 0.19782408, 0.17599727, 0.11451142
                 0.04392569, 0.08137638, 0.10952589, 0.18309624, 0.21405034
         ],
                 [0.44501804, 0.428129 , 0.64310787, 0.57215094, 0.3722661
                 0.14279837, 0.26454711, 0.35605859, 0.59522902, 0.69585796
         ],
                 [0.03330262, 0.03203874, 0.04812654, 0.04281653, 0.02785828
                 0.01068622, 0.0197972 , 0.0266454 , 0.04454356, 0.05207406
         ],
                 [0.05833635, 0.05612241, 0.08430347, 0.0750019 , 0.04879947
                 0.0187191 , 0.03467885, 0.04667487, 0.07802715, 0.09121836
         ]])
```

98. Considering a path described by two vectors (X,Y), how to sample it using equidistant samples $(\bigstar \bigstar \bigstar)$?

```
In [55]: phi = np.arange(0, 10*np.pi, 0.1)
a = 1
x = a*phi*np.cos(phi)
y = a*phi*np.sin(phi)

dr = (np.diff(x)**2 + np.diff(y)**2)**.5 # segment lengths
r = np.zeros_like(x)
r[1:] = np.cumsum(dr) # integrate path
r_int = np.linspace(0, r.max(), 200) # regular spaced path
x_int = np.interp(r_int, r, x) # integrate path
y_int = np.interp(r_int, r, y)
```

99. Given an integer n and a 2D array X, select from X the rows which can be interpreted as draws from a multinomial distribution with n degrees, i.e., the rows which only contain integers and which sum to n. $(\star \star \star)$

100. Compute bootstrapped 95% confidence intervals for the mean of a 1D array X (i.e., resample the elements of an array with replacement N times, compute the mean of each sample, and then compute percentiles over the means). $(\star \star \star)$

```
In [57]: X = np.random.randn(100) # random 1D array
N = 1000 # number of bootstrap samples
idx = np.random.randint(0, X.size, (N, X.size))
means = X[idx].mean(axis=1)
confint = np.percentile(means, [2.5, 97.5])
print(confint)
```

[-0.22626447 0.16936667]