

# CS 422: Project 2 Write-up

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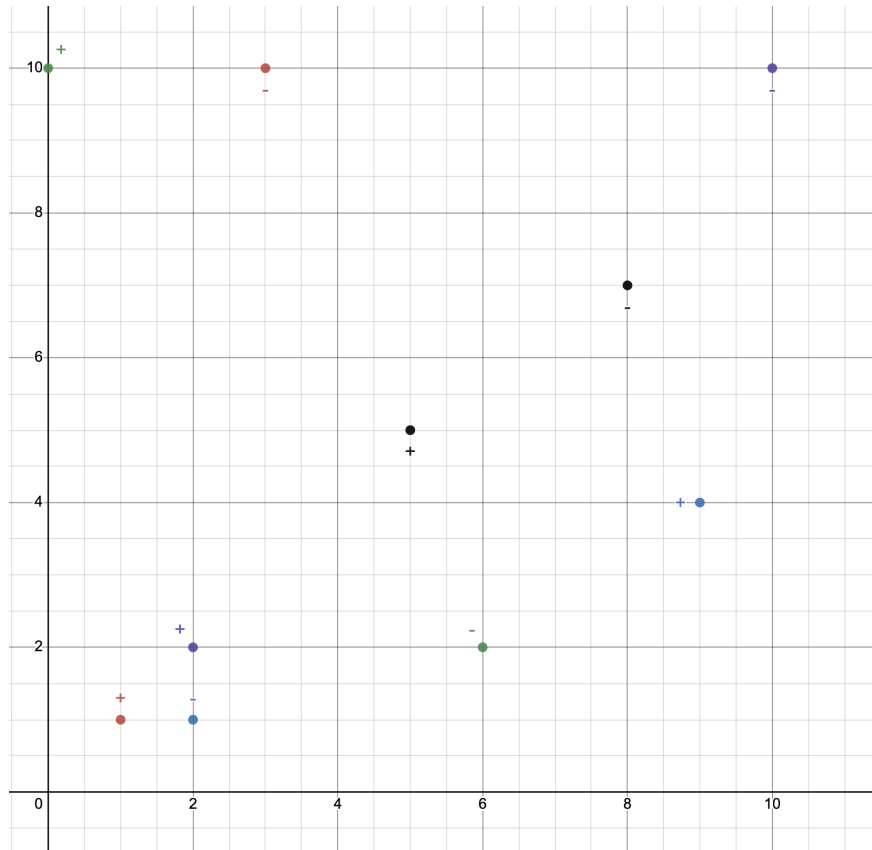
This is the link of my write-up: <https://www.overleaf.com/read/cbknfnfjvqff>.

## 1 Nearest Neighbors Implementation

Using the training data provided in "nearest neighbors 1.csv," my algorithm would classify the test points with  $K=1$ ,  $K=3$ , and  $K=5$  as follows:

Test points	$K = 1$	$K = 3$	$K = 5$
(1, 1, 1)	1	1	1
(2, 1, -1)	-1	1	1
(0, 10, 1)	1	1	1
(10, 10, -1)	-1	-1	-1
(5, 5, 1)	1	-1	1
(3, 10, -1)	-1	1	-1
(9, 4, 1)	1	-1	-1
(6, 2, -1)	-1	1	1
(2, 2, 1)	1	1	1
(8, 7, -1)	-1	-1	-1

The best  $K$  value for the training data above is difficult to say. Based on accuracies, we know that  $K = 1$  has an accuracy of 10/10,  $K = 3$  has an accuracy of 5/10, and  $K = 5$  has an accuracy of 7/10. However,  $K = 1$  would be overfitting. There's really not much of a large scale pattern in the points, either, and the difference in accuracy between  $K = 3$  and  $K = 5$  might just be luck.  $K = 5$  might be a bit underfitting, so perhaps  $K = 3$  would be better.



## 2 Clustering Implementation

The training data in "clustering 2.csv" with  $K=2$  and  $K=3$  result in some of the following KMeans.

It seems as if using KMeans on  $K = 2$  seems to have larger variance in its cluster centers than KMeans on  $K = 3$ , suggesting that the structure of "clustering2.csv" has a more distinct structure as three clusters than as two clusters.

$$K = 2$$

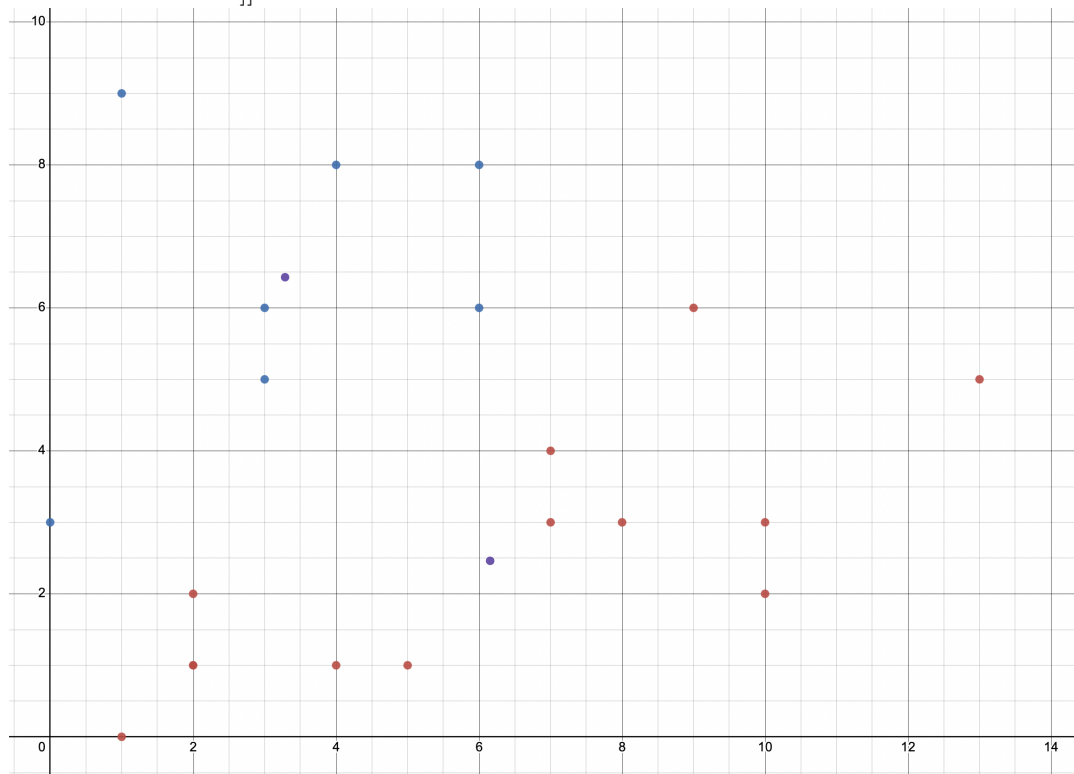
```
KMeans: [[3.28571429 6.42857143] [6.15384615 2.46153846]]
KMeans: [[2.45454545 3.36363636] [8.44444444 4.44444444]]
KMeans: [[8.44444444 4.44444444] [2.45454545 3.36363636]]
KMeans: [[8. 4.8] [2.3 2.9]]
KMeans: [[5.46153846 2.23076923] [4.57142857 6.85714286]]
```

$$K = 3$$

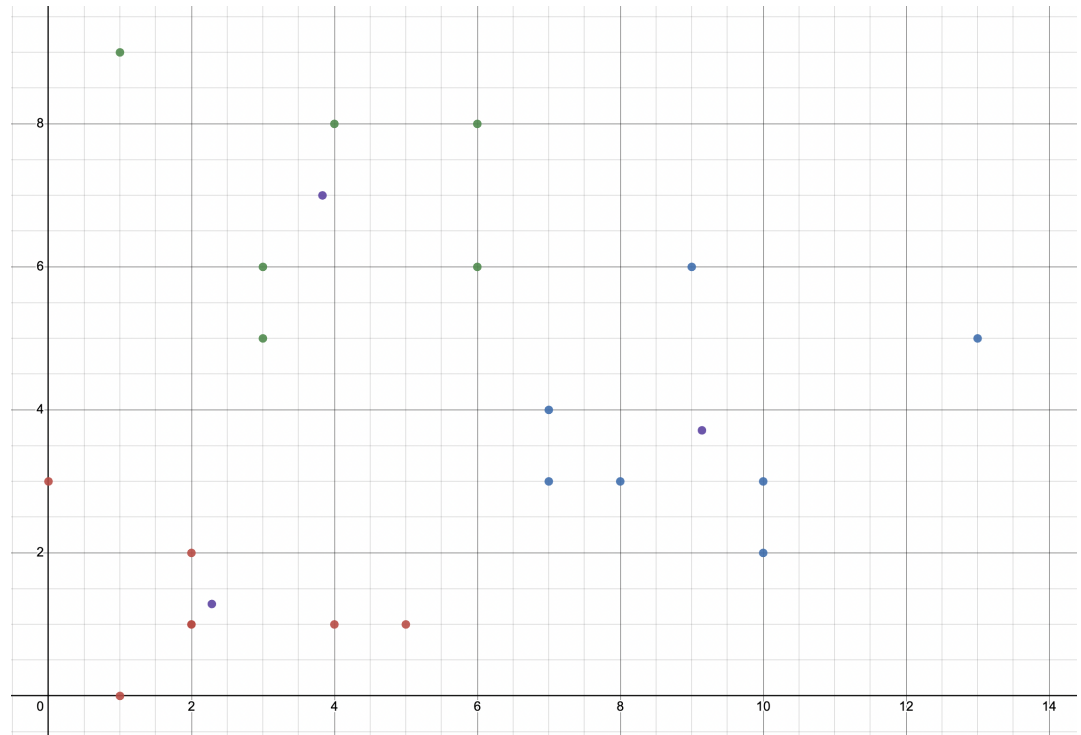
KMeans: [[2.28571429 1.28571429] [9.14285714 3.71428571] [3.83333333 7. ]]  
KMeans: [[9.14285714 3.71428571] [3.83333333 7. ] [2.28571429 1.28571429]]  
KMeans: [[3.83333333 7. ] [9.14285714 3.71428571] [2.28571429 1.28571429]]  
KMeans: [[9.14285714 3.71428571] [3.83333333 7. ] [2.28571429 1.28571429]]  
KMeans: [[10.5 4. ] [ 2. 3.88888889] [ 6.14285714 3.71428571]]  
KMeans: [[13. 5. ] [ 2.45454545 3.36363636] [ 7.875 4.375 ]]  
KMeans: [[11. 3.33333333] [ 6.71428571 5.42857143] [ 2.3 2.9 ]]  
KMeans: [[2.28571429 1.28571429] [3.83333333 7. ] [9.14285714 3.71428571]]

### Graphing

A graph of the clusters with  $K = 2$  and centers at [[3.28571429 6.42857143]  
[6.15384615 2.46153846]]:



A graph of the clusters with  $K = 3$  and centers at [[2.28571429 1.28571429]  
[9.14285714 3.71428571] [3.83333333 7. ]]:



### 3 Perceptron Implementation

My perceptron resulting from training on the dataset provided in "perceptron 2.csv" yield  $w = \langle 2, 4 \rangle$  and  $b = 2$ . Below, the decision boundary is plotted along with the dataset.

