DATA AND MODELING INSIGHTS FOR LIFE EXPECTANCY PREDICTORS

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ABSTRACT. Life expectancy is a critical measure of societal well-being, reflecting health outcomes, socioeconomic development, and quality of life. Our research investigates the question, "What are the most significant factors that influence life expectancy across countries?" We employed linear regression, feature importance analysis, and Principal Component Analysis, to identify key predictors of life expectancy. Our analysis revealed that socioeconomic variables, such as income composition and years of schooling, along with health factors, are strong predictors of life expectancy.

1. Research question and overview of the data

Our research seeks to identify key factors influencing life expectancy across countries, focusing on differences between developed and developing nations. Life expectancy reflects health outcomes and quality of life, and understanding its drivers can help allocate resources and guide interventions. Previous studies have successfully employed neural networks to predict life expectancy [1]. Other studies [14] have shown that life expectancy has generally improved worldwide, though significant disparities persist between developed and developing nations despite the overall positive trend. By analyzing trends separately for these groups, we aim to uncover factors that explain this disparity, which neural networks may miss due to their lack of interpretability.

The dataset, provided by the World Health Organization, includes global life expectancy data alongside socioeconomic, health, and demographic variables, covering 182 countries from 2000 to 2015. Although it has missing entries and some out-of-range values, the dataset offers valuable insights once cleaned.

We hypothesize that socioeconomic factors like income and education will be the strongest predictors, followed by health variables such as immunization rates and access to healthcare. By using interpretable machine learning techniques, we aim to quantify these factors and examine their impact on global health outcomes, with a focus on disparities between developed and developing nations to inform interventions.

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2. Data Cleaning / Feature Engineering

In our data cleaning process, we aimed to preserve relevant information while minimizing excessive imputation by dropping countries with substantial missing data, sourcing reliable replacements and using linear interpolation and KNN for imputation. The dataset did not include data for South Sudan, so we dropped the country entirely. Most columns contained float values, requiring only the "Status" column—indicating whether a country is "Developed" or "Developing"—to be converted to a binary format. The population, BMI, under-5 mortality, and infant deaths, columns had large portions of data falling outside reasonable ranges and were entirely replaced with more reliable data. Scattered missing values including GDP were filled using supplementary data from the internet. For any remaining nulls after applying linear interpolation, we referenced data from other years for the same country to fill gaps where possible. When this approach was insufficient, we employed KNN imputation, which identifies similar instances in the dataset based on feature similarity to estimate missing values. These extensive replacements raised questions about the original dataset's quality, akin to the Ship of Theseus paradox.

Using our existing data, we engineered features like population density, population growth, and a health coverage index to enhance the dataset. We transformed our BMI and income features into categorical columns (e.g., underweight, overweight) for clearer trends. It was challenging to find reliable data that aligned with the scope of our dataset, so our new features are primarily derived from readily available sources. To be more specific, we incorporated features from OurWorldInData [13], such as a human rights index, a democracy index, and suicide rates to provide additional contextual information.

3. Data Visualization and Basic Analysis

To identify key factors influencing life expectancy, we used a multi-step approach combining data visualization, feature importance analysis, principal component analysis (PCA), and multiple linear regression. Our goal was to identify significant predictors and evaluate model effectiveness. The dataset, including health-related and socioeconomic variables like HIV/AIDS prevalence, income composition, and education, is well-suited for this analysis. We chose multiple linear regression because many features show linear relationships, and the model offers clear interpretability of how individual predictors affect life expectancy, in contrast to more complex models.

We started with exploratory data analysis and feature importance analysis using Random Forest to identify key predictors of life expectancy, excluding

¹Missing or unreasonable values in "Population," "Under-five Deaths," and "Life Expectancy" were supplemented with data from OurWorldInData. For "GDP", missing values were filled using data from data.worldbank.org, with additional values for Venezuela [16] and North Korea [7]. All sources are reputable and widely recognized.

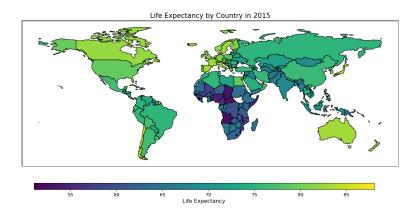


FIGURE 1. Average life expectancy per country in 2015. To observe changes in life expectancy from 2000 to 2015, click here.

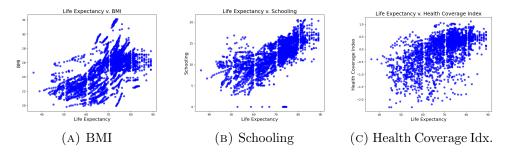


FIGURE 2. Several features in our dataset exhibit linear trends, as shown in the following examples above.

highly correlated factors like adult mortality and infant deaths. We applied PCA to reduce dimensionality and capture data variance. Multiple linear regression showed strong positive correlations between income composition, HIV/AIDS, high income, human rights, schooling, and life expectancy. Despite low Variance Inflation Factor (VIF) scores, we detected potential multicollinearity, which we addressed using Ridge Regression to penalize large coefficients and reduce its impact.

4. Learning Algorithms and In-depth Analysis

We applied a multiple linear regression model to three country groups: all countries, developing countries, and developed countries. The overall model had an R-squared of 0.807, indicating a good fit, though the Mean Absolute Error (3.10 years) and Root Mean Squared Error (4.33 years) suggest predictions deviate by several years, likely due to unmeasured variables. Key predictors included HIV/AIDS and BMI (negative impact) and income composition, schooling, and human rights (positive impact; see Table 1).

Feature importance analysis confirmed HIV/AIDS and income composition as critical factors, while variables like agricultural employment had minimal influence.

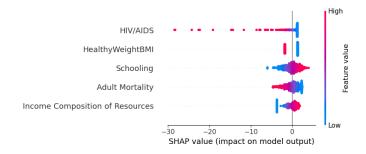


FIGURE 3. We use SHAP analysis, a feature importance technique, to visualize model predictions, where blue indicates factors that lower life expectancy, red indicates factors that increase it, and purple highlights overlapping contributions.

Variable	All Countries	Developing	Developed
Alcohol	0.0563***	0.0243**	-0.1221**
Diphtheria Immunizations	0.0555*	0.0561*	0.0226**
HIV/AIDS Deaths	-0.6456*	-0.6426*	4.5072*
Income Composition of Resources	6.4301*	4.5853*	21.8626*
High Income	1.7282*	2.2670*	0.1993
Healthy Weight BMI	-4.6401*	-5.4095*	3.0085*
Thinness 1-19 Years	-0.0515	-0.0013	-1.3058*
Human Rights	2.4229*	1.8488*	17.4744**
Suicide Rate	-0.1553*	-0.1397*	-0.1162*
Schooling	0.6419*	0.5793*	-0.0160
\mathbb{R}^2	0.807	0.763	0.613

TABLE 1. Regression Coefficients by Country Type. To analyze statistical significance, we use the following scale for the p-stat: *p<0.01, **p<0.05, ***p<0.1

For developing countries, percentage expenditure and high income had a stronger impact on life expectancy than in developed countries, where thinness showed a stronger correlation. Notably, the developing countries dataset (2400 rows) is significantly larger than the developed countries dataset (512 rows), which may affect result significance and explain the lower R-squared for developed countries.

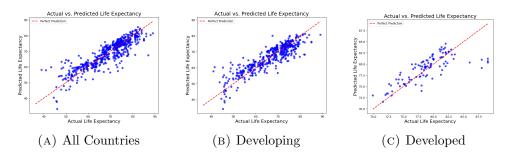


FIGURE 4. Actual vs. predicted life expectancy by country type.

5. ETHICAL IMPLICATIONS AND CONCLUSIONS

Having demonstrated our model's capabilities, we address ethical considerations. The WHO data is public and poses no privacy risks, making it a valuable tool for charities and nonprofits in resource allocation. However, using a simple algorithm for aid distribution could have unintended consequences, such as discouraging struggling nations from improving living conditions to maintain aid eligibility or prompting governments to prioritize short-term gains over long-term development. Life expectancy should not be the sole metric; we recommend complementing this model with additional factors like political stability, economic conditions, and conflict to avoid conflating correlation with causation.

Our project identified key factors influencing life expectancy, revealing that HIV/AIDS deaths negatively impact it, while income composition and schooling are strong positive predictors. Early-life mortality is strongly correlated with life expectancy, highlighting the importance of health interventions and education. We found notable differences between developed and developing countries: in developing countries, factors like expenditure and income had more influence, while in developed countries, thinness was more strongly correlated. Linear regression and PCA provided valuable insights, though unexplained variance suggests the need for additional factors. Future work will explore non-linear models and external data to deepen our understanding of life expectancy across different socioeconomic contexts.

References

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Import libraries and tools

```
import numpy as np
import pandas as pd
from sklearn.impute import KNNImputer
```

Data Cleaning

Load Raw Data

```
# Load raw data
df = pd.read_csv("LifeExpectancyRaw.csv")
```

Drop Rows

```
# Drop rows where life expectancy is missing (10 countries where the
country only has one year of data)
df = df.dropna(subset=['Life expectancy '])

# Drop South Sudan due to large portion of missing data
df = df[df['Country'] != 'South Sudan']
```

Convert Columns to Binary

```
# Convert status column to binary
df['Status'].replace({'Developed': 1, 'Developing': 0}, inplace=True)
```

Manually Insert Data

```
# Manually insert population
pop df = pd.read csv("population-and-demography.csv")
# Rename values and columns for merging
pop_df['Entity'] = pop_df['Entity'].replace({
    'Bolivia': 'Bolivia (Plurinational State of)',
    'Brunei': 'Brunei Darussalam',
    "Cote d'Ivoire": "Côte d'Ivoire",
    'Cape Verde': 'Cabo Verde',
    'Democratic Republic of Congo': 'Democratic Republic of the
Congo',
    'North Korea': "Democratic People's Republic of Korea",
    'Iran': 'Iran (Islamic Republic of)',
    'South Korea': 'Republic of Korea',
    'Laos': "Lao People's Democratic Republic",
    'Micronesia (country)': 'Micronesia (Federated States of)',
    'Moldova': 'Republic of Moldova',
    'North Macedonia': 'The former Yugoslav republic of Macedonia',
```

```
'Tanzania': 'United Republic of Tanzania',
    'United Kingdom': 'United Kingdom of Great Britain and Northern
Ireland',
    'United States': 'United States of America',
    'Venezuela': 'Venezuela (Bolivarian Republic of)',
    'Vietnam': 'Viet Nam',
    'Russia': 'Russian Federation',
    'Eswatini': 'Swaziland',
    'Syria': 'Syrian Arab Republic',
    'East Timor': 'Timor-Leste'
})
pop df = pop df.rename(columns={
    'Entity': 'Country',
    "Population - Sex: all - Age: all - Variant: estimates":
"Population"})
# Merge df with pop df on Country and Year
df = df.merge(pop_df[['Country', 'Year', 'Population']],
on=['Country', 'Year'], how='left', suffixes=('', ' pop df'))
# Fill missing values in df's Population column with values from
pop df
df['Population'] = df['Population pop df']
# Drop the additional Population column from pop df after filling in
missing values
df = df.drop(columns=['Population pop df'])
# Load measles data
measles df = pd.read csv('MeaslesCoverage.csv', encoding='latin1')
# Replace original values with NaN
df['Measles '] = np.nan
# Merge df with measles df on 'Country' and 'Year'
measles df = measles df.rename(columns={'NAME': 'Country', 'YEAR':
'Year'})
merged df = df.merge(measles df[['Country', 'Year', 'COVERAGE']],
on=['Country', 'Year'], how='left')
# Fill NaN values in the 'Measles' column with corresponding
'COVERAGE' values from measles df
df['Measles '] = merged df['Measles '].fillna(merged df['COVERAGE'])
# Replace values in 'Measles' column that fall outside the expected
percentage range with NaN
df.loc[df['Measles '] > 100, 'Measles '] = np.nan
```

```
# Manually insert under-five deaths
mortality df = pd.read csv("child-mortality.csv")
# Rename values and columns for merging
mortality df['Entity'] = mortality df['Entity'].replace({
    'Bolivia': 'Bolivia (Plurinational State of)',
    'Brunei': 'Brunei Darussalam',
    "Cote d'Ivoire": "Côte d'Ivoire",
    'Cape Verde': 'Cabo Verde',
    'Democratic Republic of Congo': 'Democratic Republic of the
Congo',
    'North Korea': "Democratic People's Republic of Korea",
    'Iran': 'Iran (Islamic Republic of)',
    'South Korea': 'Republic of Korea',
    'Laos': "Lao People's Democratic Republic",
    'Micronesia (country)': 'Micronesia (Federated States of)',
    'Moldova': 'Republic of Moldova',
    'North Macedonia': 'The former Yugoslav republic of Macedonia',
    'Tanzania': 'United Republic of Tanzania',
    'United Kingdom': 'United Kingdom of Great Britain and Northern
Ireland',
    'United States': 'United States of America',
    'Venezuela': 'Venezuela (Bolivarian Republic of)',
    'Vietnam': 'Viet Nam',
    'Russia': 'Russian Federation',
    'Eswatini': 'Swaziland',
    'Syria': 'Syrian Arab Republic',
    'East Timor': 'Timor-Leste'
})
mortality df = mortality df.rename(columns={
    'Entity': 'Country',
    'Under-five mortality rate': 'under-five deaths '})
# Merge df with pop df on Country and Year
df = df.merge(mortality_df[['Country', 'Year', 'under-five deaths ']],
on=['Country', 'Year'], how='left', suffixes=('', ' mortality df'))
# Replace under-five deaths with values from mortality df
df['under-five deaths '] = df['under-five deaths '].astype(float) #
Make columns the same dtype to avoid errors
df['under-five deaths '] = df['under-five deaths mortality df'] * 10
# Adjust from percentage to rate per 1000
# Drop the additional column from mortality df after filling in values
df = df.drop(columns=['under-five deaths mortality df'])
# Manually insert GDP data
gdp_df = pd.read_csv("GDP.csv", skiprows=4)
gdp_df.drop(columns=['Country Code', 'Indicator Code', '1960', '1961',
```

```
'1962', '1963', '1964', '1965', '1966', '1967', '1968',
'1969', '1970', '1971', '1972', '1973', '1974', '1975', '1976',
'1977',
'1978', '1979', '1980', '1981', '1982', '1983', '1984', '1985',
'1986',
'1987', '1988', '1989', '1990', '1991', '1992', '1993', '1994',
'1995',
unnecessary columns
# Rename column names to match our data
gdp df['Country Name'] = gdp df['Country Name'].replace({
    'Bahamas, The': 'Bahamas',
    'Bolivia': 'Bolivia (Plurinational State of)',
    "Cote d'Ivoire": "Côte d'Ivoire",
    'Congo, Dem. Rep.': 'Democratic Republic of the Congo',
    'Congo, Rep.':'Congo',
    'Egypt, Arab Rep.': 'Egypt',
    'Gambia, The': "Gambia",
    'Iran, Islamic Rep.': 'Iran (Islamic Republic of)',
    'Korea, Dem. People\'s Rep.':"Democratic People's Republic of
Korea",
    'Korea, Rep.': 'Republic of Korea',
    'Kyrgyz Republic': 'Kyrgyzstan',
    "Lao PDR": "Lao People's Democratic Republic",
    'Micronesia, Fed. Sts.': 'Micronesia (Federated States of)',
    'Moldova': 'Republic of Moldova',
    'North Macedonia': 'The former Yugoslav republic of Macedonia',
    'Slovak Republic': 'Slovakia',
    'St. Lucia': 'Saint Lucia',
    'St. Vincent and the Grenadines': 'Saint Vincent and the
Grenadines',
    'Tanzania': 'United Republic of Tanzania',
    'United Kingdom': 'United Kingdom of Great Britain and Northern
Ireland',
    'United States': 'United States of America',
    'Venezuela, RB': 'Venezuela (Bolivarian Republic of)',
    'Vietnam': 'Viet Nam',
    'Yemen, Rep.': 'Yemen'
})
# Turn year columns into seperate rows
qdp df = pd.melt(gdp df,
                   id vars=['Country Name', 'Indicator Name'],
                   var name='Year',
                   value name='GDP')
# Change year to int to be able to merge
```

```
gdp df['Year'] = gdp df['Year'].astype(int)
# Merge df with gdp df on 'Country' and 'Year'
gdp_df_merged = df.merge(gdp df[['Country Name', 'Year', 'GDP']],
left on=['Country', 'Year'],
                         right on=['Country Name', 'Year'],
                         how='left'
                         suffixes=('', ' new'))
# Add Venezuela data
years = list(range(2000, 2016))
gdp ven = [11.9e3, 12.1e3, 10.8e3, 9.83e3, 11.4e3, 12.4e3, 13.4e3,
14.4e3, 14.9e3, 14.2e3, 13.8e3, 14.2e3, 14.7e3, 14.7e3, 1.4e4, 14.1e3]
venezuela gdp = pd.DataFrame({
    'Country': 'Venezuela (Bolivarian Republic of)',
    'Year': years,
    'GDP v': gdp ven
})
# Add North Korea data
gdp nk = [10.61e9, 11.02e9, 10.91e9, 11.05e9, 11.17e9, 13.03e9,
13.76e9, 14.37e9, 13.34e9, 12.04e9, 13.95e9, 15.69e9, 15.91e9,
16.57e9, 17.4e9, 16.28e9]
nk gdp = pd.DataFrame({
    'Country': "Democratic People's Republic of Korea",
    'Year':years,
    'GDP nk':gdp nk
})
# Merge GDP data back into the main DataFrame on Country and Year
qdp df merged = qdp df merged.merge(venezuela qdp, on=['Country',
'Year'], how='outer')
gdp df merged = gdp df merged.merge(nk gdp, on=['Country', 'Year'],
how='outer')
# Fill missing GDP values
gdp_df_merged['GDP'] =
gdp df merged['GDP'].fillna(gdp df merged['GDP new'])
gdp df merged['GDP'] =
gdp df merged['GDP'].fillna(gdp df merged['GDP v'])
qdp df merqed['GDP'] =
gdp df merged['GDP'].fillna(gdp df merged['GDP nk']/gdp df merged['Pop
ulation'l)
# Drop joined columns after filling in missing values
df = gdp df merged.drop(columns=['Country Name', 'GDP v', 'GDP new',
'GDP_nk'])
# Manually insert infant mortality
infant df = pd.read csv("infant-mortality.csv")
```

```
# Rename values and columns for merging
infant df['Entity'] = infant df['Entity'].replace({
    'Bolivia': 'Bolivia (Plurinational State of)',
    'Brunei': 'Brunei Darussalam',
    "Cote d'Ivoire": "Côte d'Ivoire",
    'Cape Verde': 'Cabo Verde',
    'Democratic Republic of Congo': 'Democratic Republic of the
Congo',
    'North Korea': "Democratic People's Republic of Korea",
    'Iran': 'Iran (Islamic Republic of)',
    'South Korea': 'Republic of Korea',
    'Laos': "Lao People's Democratic Republic",
    'Micronesia (country)': 'Micronesia (Federated States of)',
    'Moldova': 'Republic of Moldova',
    'North Macedonia': 'The former Yugoslav republic of Macedonia',
    'Tanzania': 'United Republic of Tanzania'.
    'United Kingdom': 'United Kingdom of Great Britain and Northern
Ireland',
    'United States': 'United States of America',
    'Venezuela': 'Venezuela (Bolivarian Republic of)',
    'Vietnam': 'Viet Nam',
    'Russia': 'Russian Federation'.
    'Eswatini': 'Swaziland',
    'Syria': 'Syrian Arab Republic',
    'East Timor': 'Timor-Leste'
infant df = infant df.rename(columns={'Entity': 'Country'})
# Merge df with pop df on Country and Year
df = df.merge(infant_df[['Country', 'Year', 'infant deaths']],
on=['Country', 'Year'], how='left', suffixes=('', '_infant_df'))
# Replace infant deaths with values from infant df
df['infant deaths'] = df['infant deaths infant df'] * 10 # Adjust from
percentage to rate per 1000
# Drop the additional column from infant df after filling in values
df = df.drop(columns=['infant deaths infant df'])
```

Forward/Backward Fill and Linear Interpolation by Country

```
def fill_missing_values(group, col):
    # Interpolate values for years 2001-2014
    group.loc[(group['Year'] > 2000) & (group['Year'] < 2015), col] =
group[col].interpolate(method='linear')

# For year 2000, fill with the next year's value if available
    group.loc[group['Year'] == 2000, col] = group.loc[group['Year'] ==
2000, col].fillna(group.loc[group['Year'] == 2001, col])</pre>
```

```
# For year 2015, fill with the previous year's value if available
group.loc[group['Year'] == 2015, col] = group.loc[group['Year'] ==
2015, col].fillna(group.loc[group['Year'] == 2014, col])

return group

# Fill missing values by interpolation
start_col, end_col = df.columns.get_loc('Status'),
df.columns.get_loc('Schooling')
for col in df.columns[start_col:end_col + 1]:
    df = df.groupby('Country', group_keys=False).apply(lambda group:
fill_missing_values(group, col))
    df = df.reset_index(drop=True)
```

Fix Values that Fall Outside the Reasonable Range

```
# Replace values outside the reasonable adult mortality range with NaN
df.loc[~df['Adult Mortality'].between(1, 500), 'Adult Mortality'] =
np.nan
# Load sample data
fixed df = pd.read csv("LifeExpectancyCleanSample.csv")
# Rename columns in fixed df
fixed df['Country'] = fixed df['Country'].replace({'Bahamas,
The: 'Bahamas', 'Bolivia': 'Bolivia (Plurinational State of)'
        "Cote d'Ivoire": "Côte d'Ivoire", 'Congo, Rep.': 'Congo',
"Egypt, Arab Rep.": "Egypt",
        'Gambia, The':'Gambia', 'Iran, Islamic Rep.':'Iran (Islamic
Republic of)', 'Kyrgyz Republic':'Kyrgyzstan',
        "Lao PDR": "Lao People's Democratic Republic", 'Micronesia,
Fed. Sts.': 'Micronesia (Federated States of)',
        'Moldova': 'Republic of Moldova', 'St. Lucia': 'Saint Lucia',
"Congo, Dem. Rep.": "Democratic Republic of the Congo",
        'St. Vincent and the Grenadines': 'Saint Vincent and the
Grenadines', 'Slovak Republic': 'Slovakia',
        'Eswatini':'Swaziland', 'North Macedonia':'The former Yugoslav
republic of Macedonia',
        'Turkiye':'Turkey', 'United Kingdom':'United Kingdom of Great
Britain and Northern Ireland',
        'Tanzania': 'United Republic of Tanzania', 'United
States': 'United States of America',
        'Venezuela, RB': 'Venezuela (Bolivarian Republic of)',
'Vietnam':'Viet Nam', 'Yemen, Rep.':'Yemen'})
# Replace BMI values with BMI values from fixed df
df.rename(columns={' BMI ': 'BMI'}, inplace=True)
df = df.merge(fixed_df[['Country', 'Year', 'BMI']], on=['Country',
'Year'], how='left', suffixes=('', '_new'))
```

```
df['BMI'] = df['BMI_new'].combine_first(df['BMI'])
df.drop(columns=['BMI_new'], inplace=True)

# For countries not found in fixed_df, we drop the BMI values in our
df to impute by knn
df.loc[df['Country'].isin(["Democratic People's Republic of Korea",
'Republic of Korea', 'Sudan']), 'BMI'] = np.nan

# Replace 0 values in 'Total expenditure' with NaN
df['percentage expenditure'] = df['percentage expenditure'].replace(0,
np.nan)
```

KNN

```
# Store the 'Country' column temporarily in order to perform KNN on
Numeric Data
country_col = df['Country']
df = df.drop(columns=['Country'])

# Apply KNN Imputer for Remaining NaN Values
knn_imputer = KNNImputer(n_neighbors=2)
df = pd.DataFrame(knn_imputer.fit_transform(df), columns=df.columns)

# Re-add 'Country' to the DataFrame
df['Country'] = country_col.values
```

Formatting

```
# Strip columns of leading and trailing whitespace
df.columns = df.columns.str.strip()
# Rename columns to create consistent capitalization
df.rename(columns={'Life expectancy':'Life Expectancy', 'infant
deaths':'Infant Deaths', 'percentage expenditure':'Percentage
Expenditure',
                   'under-five deaths':'Under-five Deaths', 'Total
expenditure': 'Total Expenditure', 'thinness 1-19 years': 'Thinness 1-
19 Years',
                   'thinness 5-9 years': 'Thinness 5-9 Years', 'Income
composition of resources': 'Income Composition of Resources'},
inplace=True)
# Sort by countries
cols = ['Country'] + [col for col in df.columns if col != 'Country']
df = df[cols]
df = df.sort values(by=['Country', 'Year'])
# Rename lengthy country names
df['Country'] = df['Country'].replace({'Bolivia (Plurinational State
of)': 'Bolivia', "Côte d'Ivoire": "Cote d'Ivoire", 'Democratic Republic
```

Assertions

```
assert df.duplicated().sum() == 0, "The DataFrame contains duplicate
assert df.isnull().sum().sum() == 0, "There are null values in the
DataFrame."
assert df.groupby('Country')['Year'].apply(lambda x: set(range(2000,
2016)).issubset(x)).all(), "Not all countries have entries for each
year from 2000 to 2015."
assert df['Life Expectancy'].between(35, 100).all(), "Life expectancy
values are out of the specified range"
assert df['Adult Mortality'].between(1, 500).all(), "Adult mortality
values are out of the specified range"
assert df['Infant Deaths'].between(1, 500).all(), "Infant mortality
values are out of the specified range"
assert df['Alcohol'].between(0, 18).all(), "Alcohol consumption values
are out of the specified range"
assert df['Percentage Expenditure'].between(0, 30000).all(),
"Percentage expenditure values are out of the specified range"
assert df['Hepatitis B'].between(0, 100).all(), "Hepatitis B values
are out of the specified range"
assert df['Measles'].between(0, 100).all(), "Measles values are out of
the specified range"
assert df['BMI'].between(18, 33).all(), "BMI values are out of the
specified range"
assert df['Under-five Deaths'].between(1, 1000).all(), "Under-five
mortality values are out of the specified range"
assert df['Polio'].between(0, 100).all(), "Polio values are out of the
specified range"
assert df['Total Expenditure'].between(0, 30000).all(), "Total
expenditure values are out of the specified range"
assert df['Diphtheria'].between(0, 100).all(), "Diptheria values are
out of the specified range"
assert df['HIV/AIDS'].between(0, 300).all(), "HIV/AIDS values are out
of the specified range"
assert df['GDP'].between(0, 300000).all(), "GDP values are out of the
```

```
specified range"
assert df['Population'].between(100, 2000000000).all(), "Population
values are out of the specified range"
assert df['Thinness 1-19 Years'].between(0, 60).all(), "Thinness (1-
19) values are out of the specified range"
assert df['Thinness 5-9 Years'].between(0, 60).all(), "Thinness (5-9)
values are out of the specified range"
assert df['Income Composition of Resources'].between(0, 1).all(),
"Income composition resources values are out of the specified range"
assert df['Schooling'].between(0, 25).all(), "Schooling values are out of the specified range"
```

Export Clean Data to CSV

```
df.to_csv('LifeExpectancyDraft.csv', index=False)
```

Feature Engineering

```
# Read in cleaned data
df = pd.read_csv('LifeExpectancyDraft.csv')
```

Population Density

```
# Load Area Data
area_df = pd.read_csv('LandAreakm.csv')

# Rename Columns for clarity
area_df = area_df.rename(columns={'Entity': 'Country', 'Land area (sq. km)': 'Area'})

# Add 'Area' Column to df
area_df = area_df.groupby('Country', as_index=False).agg({'Area': 'first'})
df = df.merge(area_df[['Country', 'Area']], on='Country', how='left')

# Drop Duplicate Rows
df = df.drop_duplicates()

# Create Population Density Column
df['PopulationDensity'] = df['Population'] / df['Area']

# Remove Area Column
df = df.drop('Area', axis=1)
```

Population Growth Rate

```
# Load population data
pop_df = pd.read_csv('population-and-demography.csv')
```

```
# rename population column
pop df.rename(columns={'Population - Sex: all - Age: all - Variant:
estimates': 'Population 1999'}, inplace=True)
pop df['Entity'] = pop df['Entity'].replace({
    'Brunei': 'Brunei Darussalam',
    'Cape Verde': 'Cabo Verde',
    'Democratic Republic of Congo': 'DR of the Congo',
    'Laos': "Lao People's DR",
    'Micronesia (country)': 'Micronesia',
    'Moldova': 'Republic of Moldova',
    'Tanzania': 'United Republic of Tanzania',
    'Eswatini': 'Swaziland',
    'Saint Vincent and the Grenadines': 'St Vincent and the
Grenadines'.
    'South Korea': 'Republic of Korea',
    'Syria': 'Syrian Arab Republic',
    'East Timor': 'Timor-Leste'
})
# Calculate population growth rate
df["Population Growth Rate"] = (
    df.groupby("Country")["Population"]
    .apply(lambda x: x.diff() / x.shift()).reset index(level=0,
drop=True)
# Filter datasets for years 1999 and 2000
df 1999 = pop df[pop df["Year"] == 1999]
df 2000 = df[df["Year"] == 2000]
# Manually insert North Korea Population data
nk row = pd.DataFrame({"Entity": ["Democratic People's Republic of
Korea"], "Code": ["CODE"], "Year": [1999], "Population 1999":
[23204498]})
df 1999 = pd.concat([df 1999, nk row], ignore index=True)
# Merge the 2000 data with the 1999 poopulation data
df_merged = pd.merge(df_2000, df_1999, left_on="Country",
right_on="Entity", suffixes=("_2000", "_1999"))
# Calculate the population growth rate for the year 2000
df merged["Population Growth Rate"] = (
    (df merged["Population"] - df merged["Population 1999"])
    / df merged["Population 1999"]
)
# Create dictionary of population growth rates
growth rate dict = dict(zip(df merged["Country"],
df merged["Population Growth Rate"]))
```

```
# Add the Growth Rate from 2000 into the main df
df.loc[df["Year"] == 2000, "Population Growth Rate"] =
df.loc[df["Country"].map(growth_rate_dict).notna(),
"Country"].map(growth_rate_dict)
```

BMI Classification

```
# Create columns for each BMI classification based on the BMI range
df['UnderweightBMI'] = (df['BMI'] < 18.5).astype(int)
df['HealthyWeightBMI'] = ((df['BMI'] >= 18.5) & (df['BMI'] <
25)).astype(int)
df['OverweightBMI'] = ((df['BMI'] >= 25) & (df['BMI'] <
30)).astype(int)
df['ObesityBMI'] = (df['BMI'] >= 30).astype(int)
```

Income Classification

```
# Low-income economies: GNI per capita of $1,135 or less
# Lower-middle-income economies: GNI per capita between $1,136 and
$4,465
# Upper-middle-income economies: GNI per capita between $4,466 and
$13,845
# High-income economies: GNI per capita of $13,846 or more
df['LowIncome'] = (df['GDP'] < 1136).astype(int)
df['LowerMiddleIncome'] = ((df['GDP'] >= 1136) & (df['GDP'] <
4466)).astype(int)
df['UpperMiddleIncome'] = ((df['GDP'] >= 4466) & (df['GDP'] <
13846)).astype(int)
df['HighIncome'] = (df['GDP'] >= 13846).astype(int)
```

Health Coverage Index

- Positive index means above average
- Negative index means below average
- Zero index means exactly average

```
# Reverse necessary columns so a higher number means better health
for col in ['Measles', 'HIV/AIDS', 'Thinness 1-19 Years', 'Thinness 5-
9 Years']:
    df[f'{col}_adjusted'] = df[col].max() - df[col]

# Standardize all columns using z-score normalization
for col in ['Hepatitis B', 'Polio', 'Diphtheria', 'Measles_adjusted',
    'HIV/AIDS_adjusted', 'Thinness 1-19 Years_adjusted', 'Thinness 5-9
Years_adjusted']:
    df[f'{col}_z'] = (df[col] - df[col].mean()) / df[col].std()

# Combine into a health index by taking the weighted mean of z-scores
z_cols = [f'{col}_z' for col in ['Hepatitis B', 'Polio', 'Diphtheria',
```

```
'Measles adjusted', 'HIV/AIDS adjusted', 'Thinness 1-19
Years adjusted', 'Thinness 5-9 Years adjusted']]
weights = {
    'Hepatitis B z': 0.2,
    'Polio z': 0.2,
    'Diphtheria_z': 0.2,
    'Measles adjusted z': 0.15,
    'HIV/AIDS adjusted z': 0.1,
    'Thinness 1-19 Years adjusted z': 0.075,
    'Thinness 5-9 Years adjusted z': 0.075,
}
# Normalize weights
total weight = sum(weights.values())
weights = {k: v / total weight for k, v in weights.items()}
# Calculate the health index (handles missing data)
df['Health Coverage Index'] = df[z cols].apply(
    lambda row: np.average(
        row.dropna(),
        weights=[weights[col] for col in row.index if col in weights]
    ) if not row.isnull().all() else np.nan,
    axis=1
)
# Drop unnecessary rows
df = df.drop(columns={'Measles adjusted',
       'HIV/AIDS_adjusted', 'Thinness 1-19 Years adjusted',
       'Thinness 5-9 Years_adjusted', 'Hepatitis B_z', 'Polio_z',
       'Diphtheria z', 'Measles adjusted z', 'HIV/AIDS adjusted z',
       'Thinness 1-19 Years adjusted z', 'Thinness 5-9
Years adjusted z'})
```

Human Rights

```
rights_df = pd.read_csv('human-rights-index-vdem.csv')
# Rename Columns for clarity
rights_df = rights_df.rename(columns={'Entity': 'Country'})
# Create the 'Human Rights' column in df using the mapping
rights_mapping = rights_df.set_index(['Country', 'Year'])['Civil
liberties index (best estimate, aggregate: average)'].to_dict()
df['Human Rights'] = df.apply(lambda row:
rights_mapping.get((row['Country'], row['Year']), None), axis=1)
```

Electoral Democracy

```
democracy_df = pd.read_csv('electoral-democracy-index.csv')
```

```
# Rename Columns for clarity
democracy_df = democracy_df.rename(columns={'Entity': 'Country'})
# Create 'Democracy' column
democracy_mapping = democracy_df.set_index(['Country', 'Year'])
['Electoral democracy index (best estimate, aggregate:
average)'].to_dict()
df['Democracy'] = df.apply(lambda row:
democracy_mapping.get((row['Country'], row['Year']), None), axis=1)
```

Armed Personnel

```
army_df = pd.read_csv('armed-forces-personnel-percent.csv')

# Rename Columns for clarity
army_df = army_df.rename(columns={'Entity': 'Country'})

# Create 'Army Personnel' column
army_mapping = army_df.set_index(['Country', 'Year'])['Armed forces
personnel (% of total population)'].to_dict()
df['Armed Personnel'] = df.apply(lambda row:
army_mapping.get((row['Country'], row['Year']), None), axis=1)
```

Suicide Rate

```
suicide_df = pd.read_csv('death-rate-from-suicides-gho.csv')

# Rename Columns for clarity
suicide_df = suicide_df.rename(columns={'Entity': 'Country'})

# Create 'Suicide Rate' column
suicide_mapping = suicide_df.set_index(['Country', 'Year'])['Age-standardized death rate from self-harm amongboth sexes'].to_dict()
df['Suicide Rate'] = df.apply(lambda row:
suicide_mapping.get((row['Country'], row['Year']), None), axis=1)
```

Agriculture Employment

```
agr_df = pd.read_csv('agriculture-value-added-per-worker-wdi.csv')

# Rename Columns for clarity
agr_df = agr_df.rename(columns={'Entity': 'Country'})

# Create 'Emigration' column
agr_mapping = agr_df.set_index(['Country', 'Year'])["Agriculture, forestry, and fishing, value added per worker (constant 2015
US$)"].to_dict()
df['Agriculture Employment'] = df.apply(lambda row:
agr_mapping.get((row['Country'], row['Year']), None), axis=1)
```

KNN

```
# Store the 'Country' column temporarily in order to perform KNN
country_col = df['Country']
df = df.drop(columns=['Country'])

# Apply KNN Imputer for Remaining NaN Values
knn_imputer = KNNImputer(n_neighbors=2)
df = pd.DataFrame(knn_imputer.fit_transform(df), columns=df.columns)

# Re-add 'Country' to the DataFrame
df['Country'] = country_col.values
df = df[['Country'] + [col for col in df.columns if col != 'Country']]
df.to_csv('LifeExpectancyClean.csv')
```

Import libraries and tools

```
import pandas as pd
import matplotlib.pyplot as plt
import shap
from sklearn.ensemble import RandomForestRegressor
from sklearn.model_selection import train_test_split
import geopandas as gpd
from matplotlib.patches import Rectangle
from matplotlib.colorbar import Colorbar
from matplotlib.colors import LogNorm, Normalize
from matplotlib.cm import ScalarMappable
import matplotlib.animation as animation
from matplotlib.ticker import FuncFormatter
```

World map

```
# Load Data
world = gpd.read_file("worldmap.gpkg")
df = pd.read csv('LifeExpectancyClean.csv', index col=0)
# Rename 'ADMIN' Column to 'Country'
world = world.rename(columns={'ADMIN': 'Country'})
# Rename Countries in World
world['Country'] = world['Country'].replace('The Bahamas', 'Bahamas')
world['Country'] = world['Country'].replace('Brunei', 'Brunei
Darussalam')
world['Country'] = world['Country'].replace('Democratic Republic of
the Congo', 'DR of the Congo')
world['Country'] = world['Country'].replace("North Korea", "Democratic
People's Republic of Korea")
world['Country'] = world['Country'].replace('Republic of the Congo',
'Congo')
world['Country'] = world['Country'].replace("Republic of Cote
D'Ivoire", "Cote d'Ivoire")
world['Country'] = world['Country'].replace('Laos', "Lao People's DR")
world['Country'] = world['Country'].replace('South Korea', 'Republic
of Korea')
world['Country'] = world['Country'].replace('Moldova', 'Republic of
Moldova')
world['Country'] = world['Country'].replace('Republic of Serbia',
'Serbia')
world['Country'] = world['Country'].replace('eSwatini', 'Swaziland')
world['Country'] = world['Country'].replace('Syria', 'Syrian Arab
Republic')
world['Country'] = world['Country'].replace('East Timor', 'Timor-
Leste')
world['Country'] = world['Country'].replace('United States of
```

```
America', 'United States')

# Merge World and Life Expectancy Data on 'Country'
combined = world.merge(df, on='Country', how='left')
```

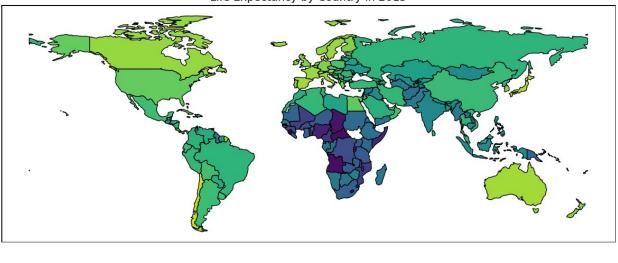
World map animation

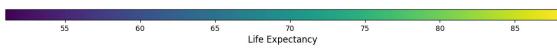
```
# Create figure and axis
fig, ax = plt.subplots(1, figsize=(10, 7))
# Normalize color scale for Life Expectancy
norm = Normalize(vmin=50, vmax=85) # Manually set min and max values
for the color scale
def update(date):
    ax.clear()
    # Filter the data for the current year
    merged = combined[combined['Year'] == date]
    # Plot the Life Expectancy by country
    merged.plot(column="Life Expectancy", cmap="viridis", ax=ax,
edgecolor="gray", norm=norm)
    # Plot the World Country Outlines
    world.boundary.plot(ax=ax, linewidth=1, color="black")
    # Add Year Label
    ax.text(0.02, 0.95, str(int(date)), transform=ax.transAxes,
fontsize=12,
            verticalalignment='top', bbox=dict(facecolor='white',
alpha=0.7)
    # Add Title
    ax.set title("Life Expectancy by Country from 2000-2015")
    ax.axis('off')
    # Add a black border around the plot
    rect = Rectangle(
        (0, 0), 1, 1, \text{ transform=ax.transAxes}, \# (x, y, width, height)
in normalized axes coordinates
        color='black',
        linewidth=2,
        fill=False
    ax.add patch(rect)
# Set up the colorbar
sm = ScalarMappable(norm=norm, cmap="viridis")
```

World Life Expectancy 2015

```
# Load and prepare data
df = pd.read csv('LifeExpectancyClean.csv', index col=0)
df = df[df['Year'] == 2015]
# Merge World and Life Expectancy Data on 'Country'
combined = world.merge(df, on='Country', how='left')
# Plot life expectancy data
fig, ax = plt.subplots(1, 1, figsize=(15, 10))
# Plot the data
combined.plot(
    column='Life Expectancy',
    cmap='viridis',
    legend=False,
    ax=ax,
    edgecolor='black'
)
# Turn off the axes
ax.axis('off')
# Add a black border around the plot
rect = Rectangle(
    (0, 0), 1, 1, transform=ax.transAxes, # (x, y, width, height) in
normalized axes coordinates
    color='black',
    linewidth=2,
```



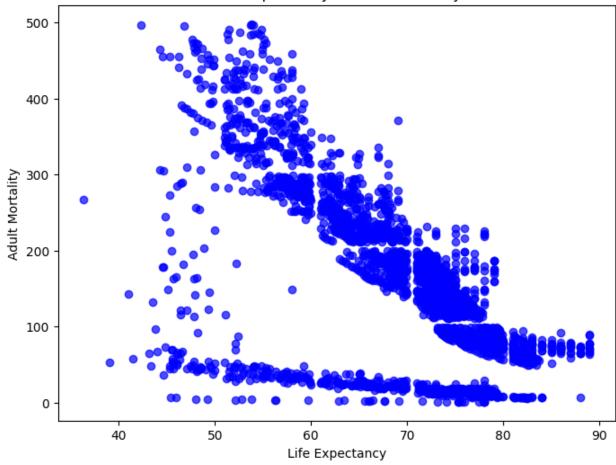




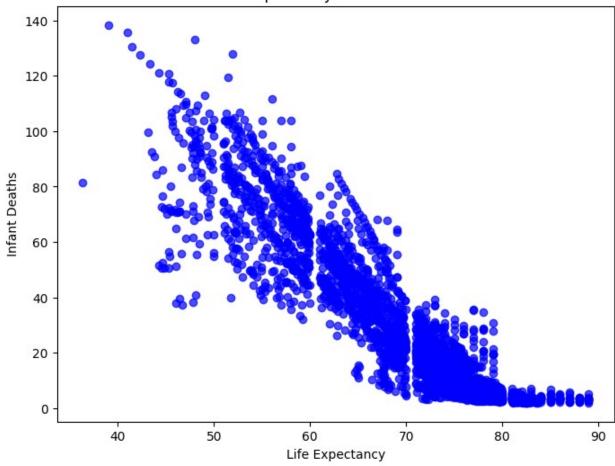
Scatter plots

```
'Thinness 5-9 Years',\
               'Income Composition of Resources', 'Schooling',
'PopulationDensity', 'Population Growth Rate',\
               'Health Coverage Index', 'Human Rights', 'Democracy',
'Armed Personnel', 'Suicide Rate',\
               'Agriculture Employment']
binary = ['UnderweightBMI', 'HealthyWeightBMI', 'OverweightBMI',
'ObesityBMI', 'LowIncome', 'LowerMiddleIncome',\
           'UpperMiddleIncome', 'HighIncome']
def scatter(feature):
    """ Plots a scatter plot of 'Life Expectancy' against a specified
feature.
    Parameters:
        feature (str): The name of the column from `df` to plot on the
y-axis.
    Returns:
       None. Displays the scatter plot.
    # Specify the features to plot
    x feature = 'Life Expectancy'
    y feature = feature
    # Scatter plot
    plt.figure(figsize=(8, 6))
    plt.scatter(df[x_feature], df[y_feature], color='blue', alpha=0.7)
    plt.title(f"{x feature} v. {y_feature}")
    plt.xlabel(x feature)
    plt.ylabel(y feature)
    plt.show()
for feature in continuous:
    scatter(feature)
```

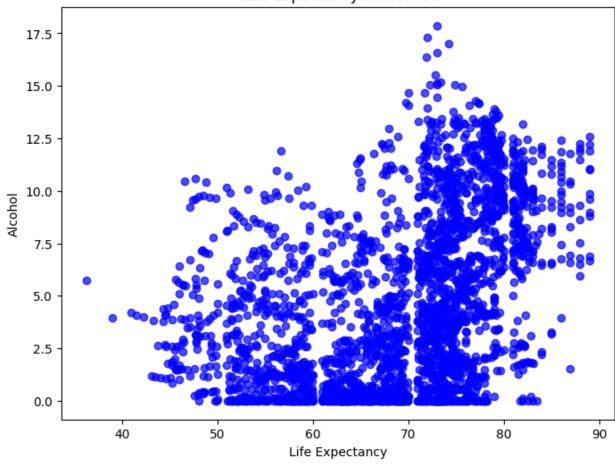
Life Expectancy v. Adult Mortality



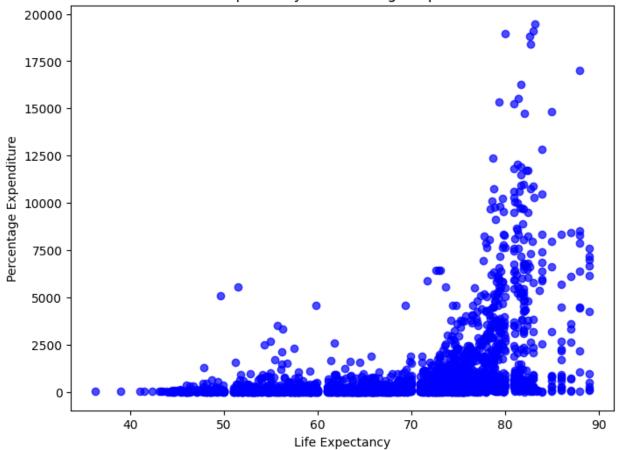
Life Expectancy v. Infant Deaths

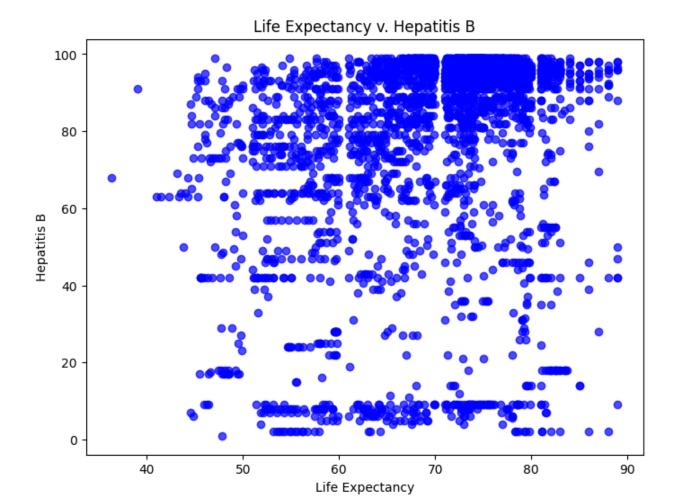


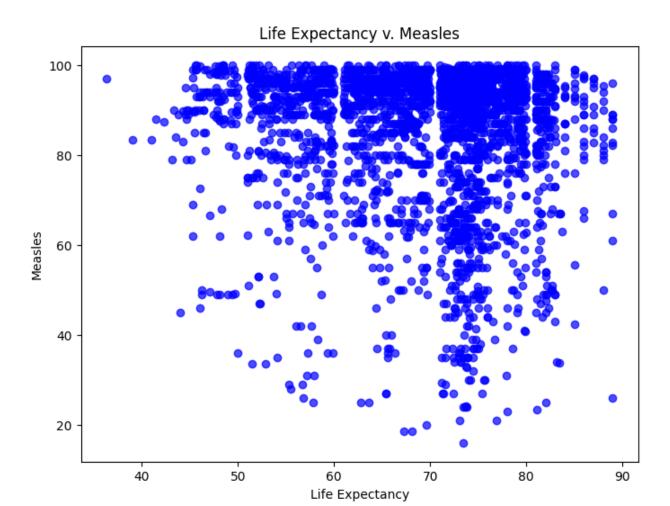




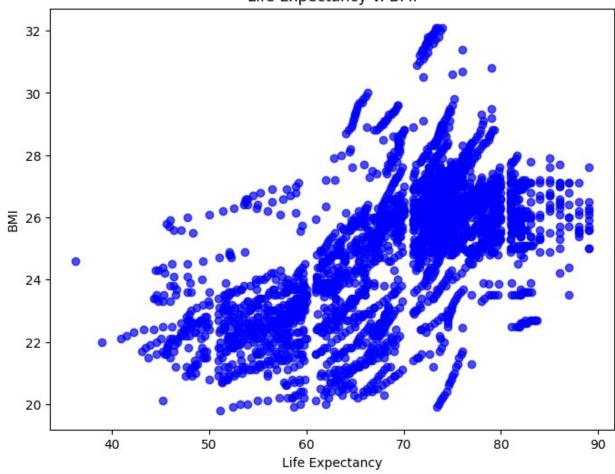
Life Expectancy v. Percentage Expenditure



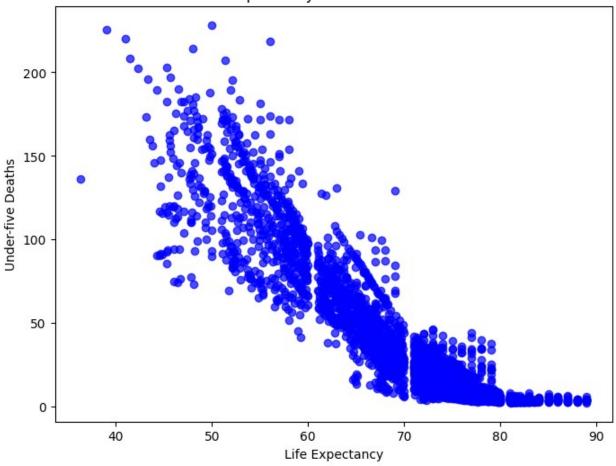


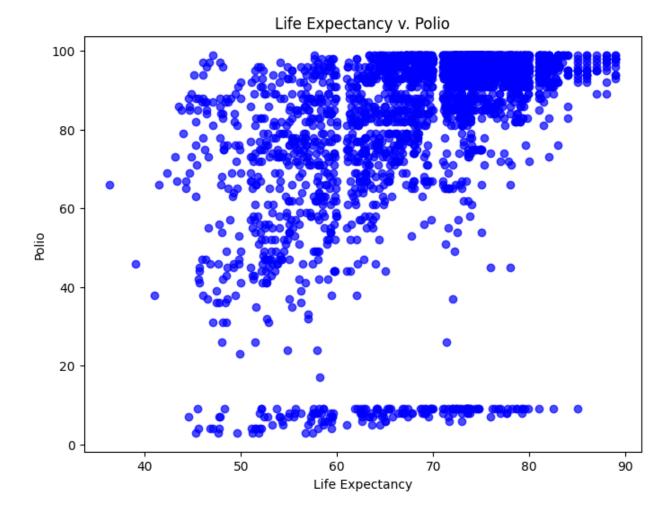


Life Expectancy v. BMI

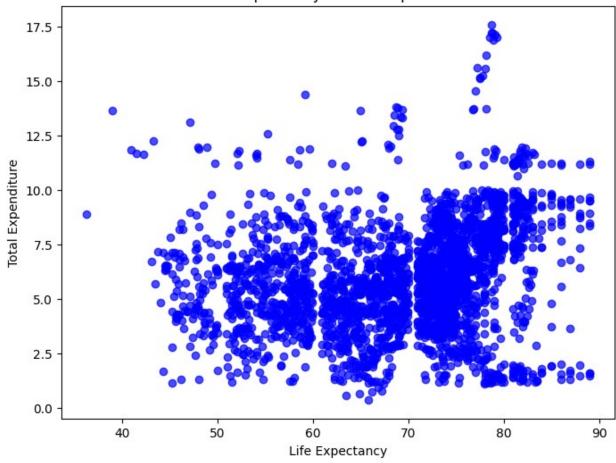


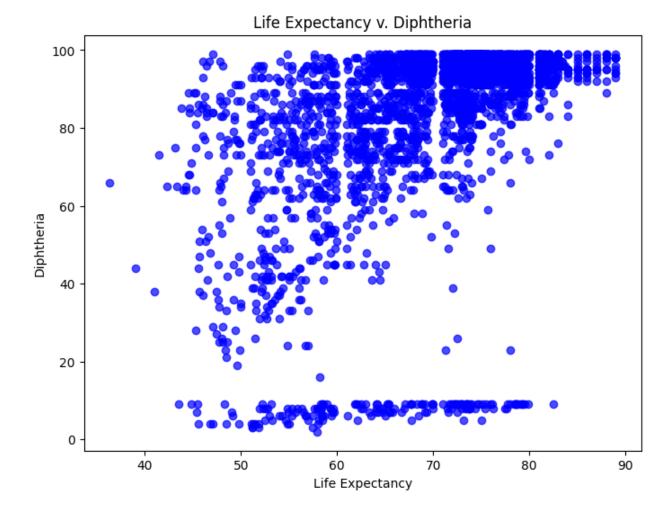
Life Expectancy v. Under-five Deaths



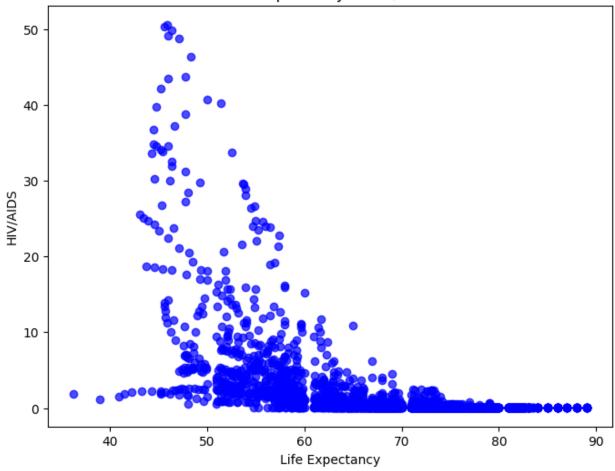


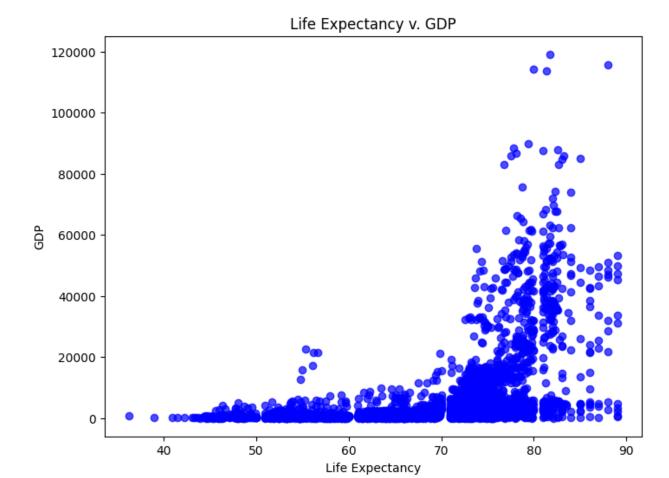
Life Expectancy v. Total Expenditure

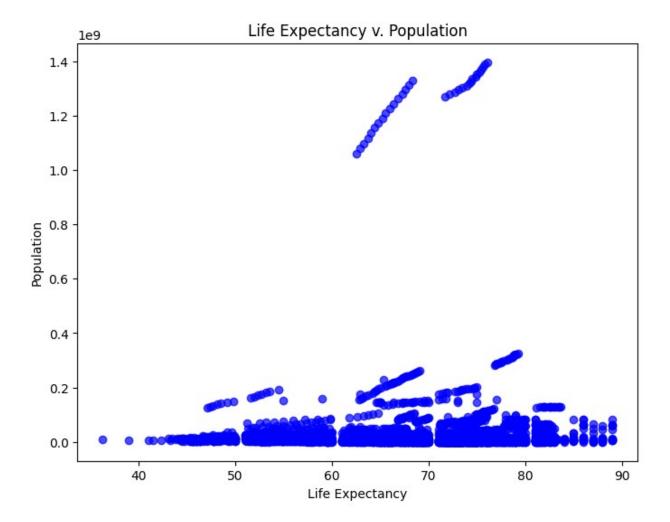




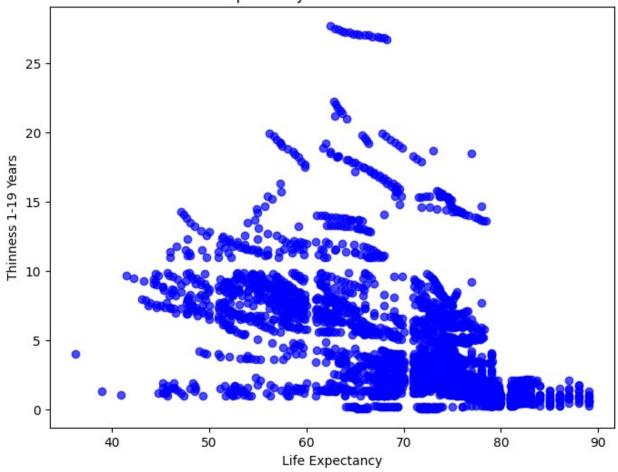
Life Expectancy v. HIV/AIDS

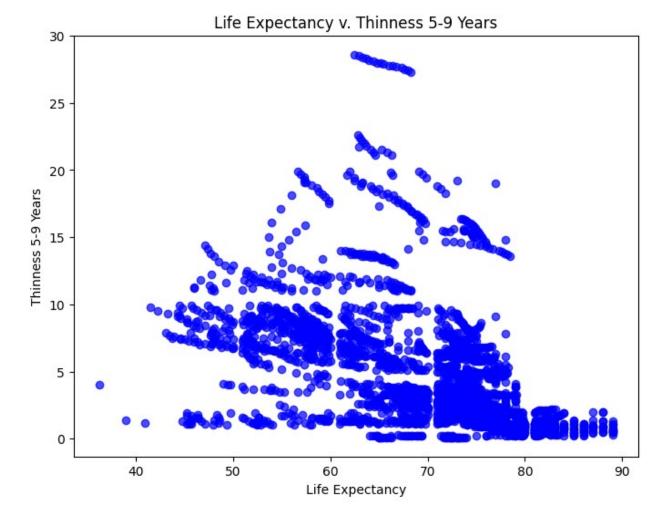




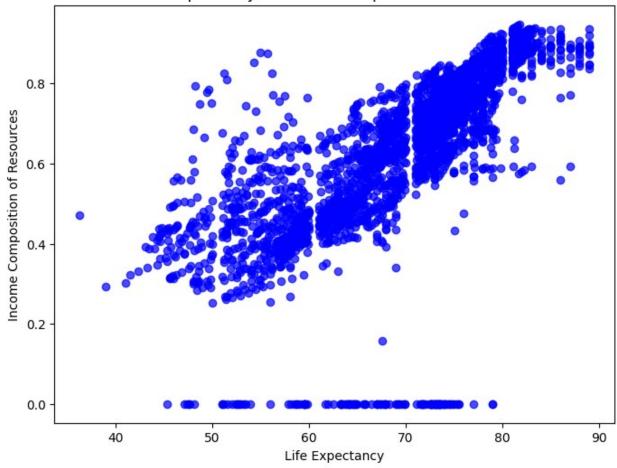


Life Expectancy v. Thinness 1-19 Years

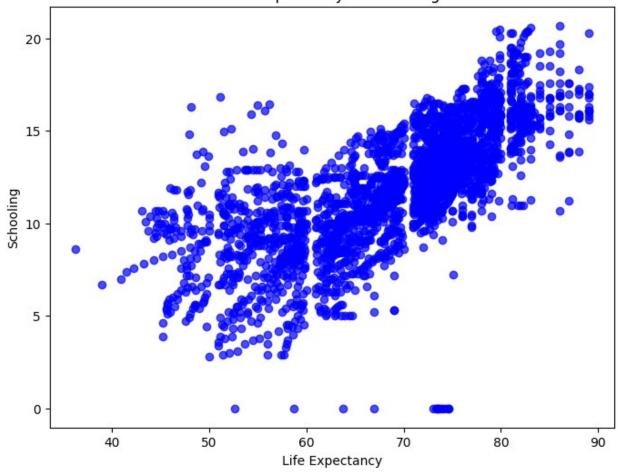




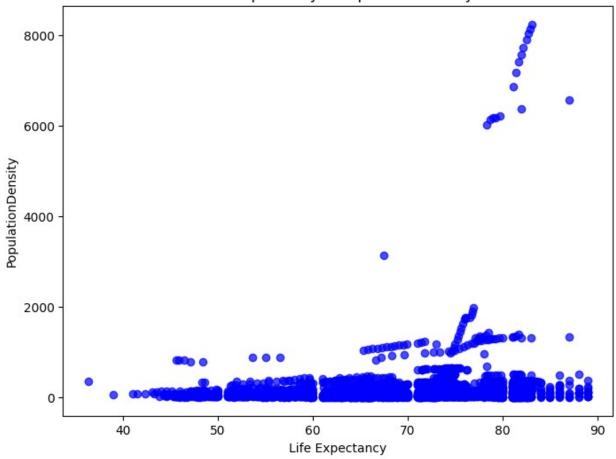
Life Expectancy v. Income Composition of Resources

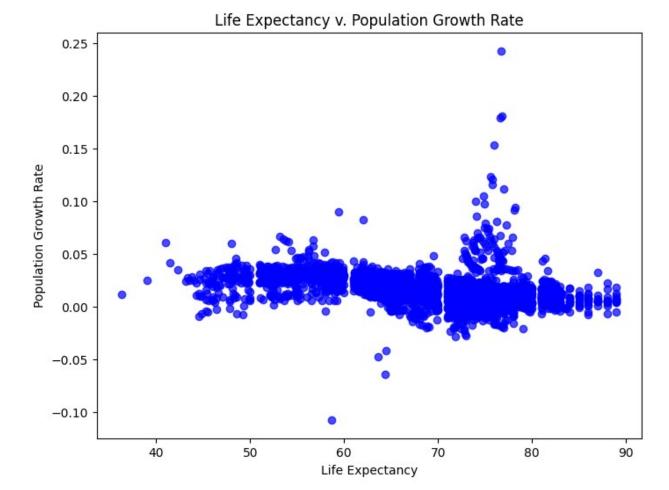


Life Expectancy v. Schooling

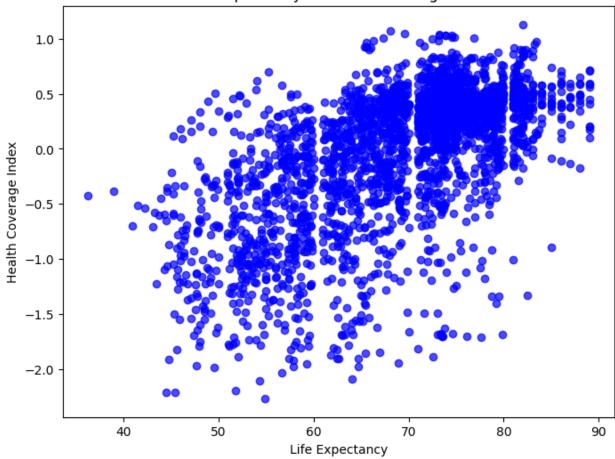


Life Expectancy v. PopulationDensity

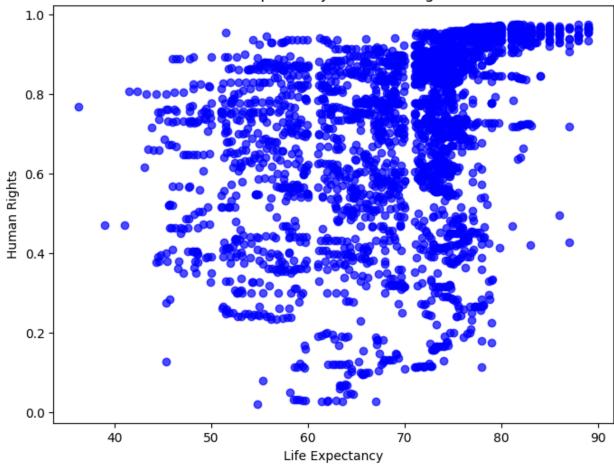




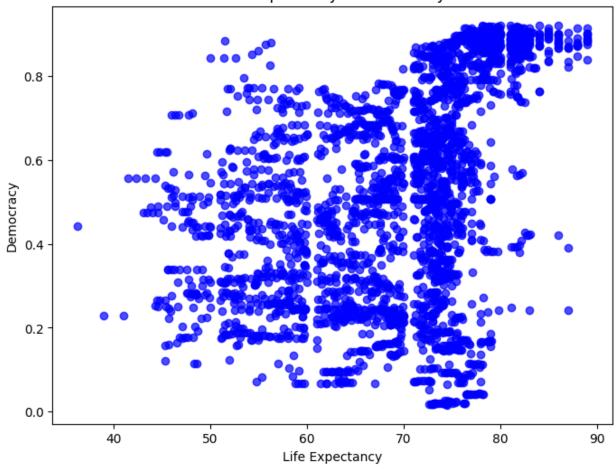
Life Expectancy v. Health Coverage Index



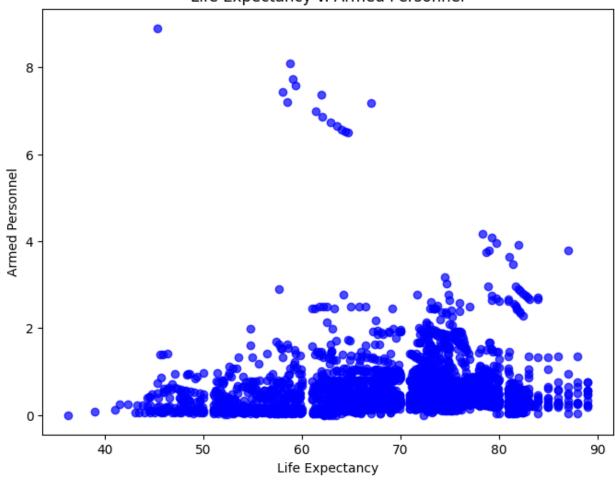
Life Expectancy v. Human Rights

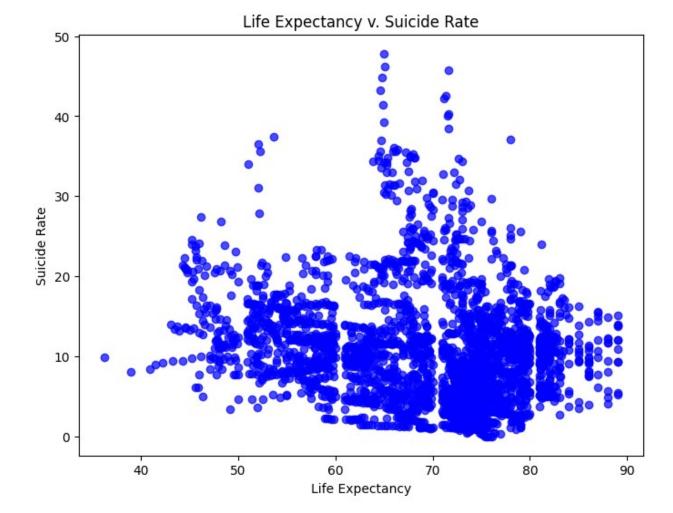


Life Expectancy v. Democracy

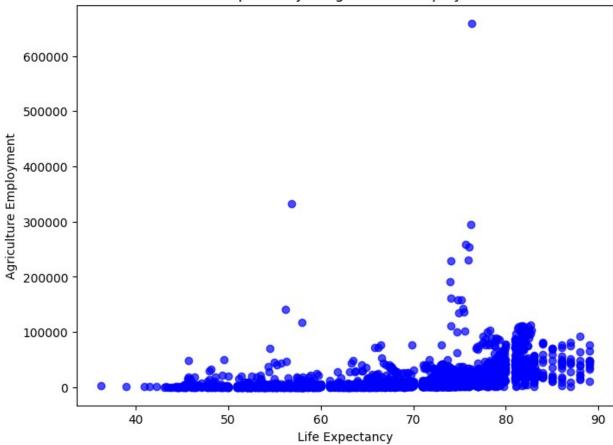


Life Expectancy v. Armed Personnel





Life Expectancy v. Agriculture Employment



SHAP

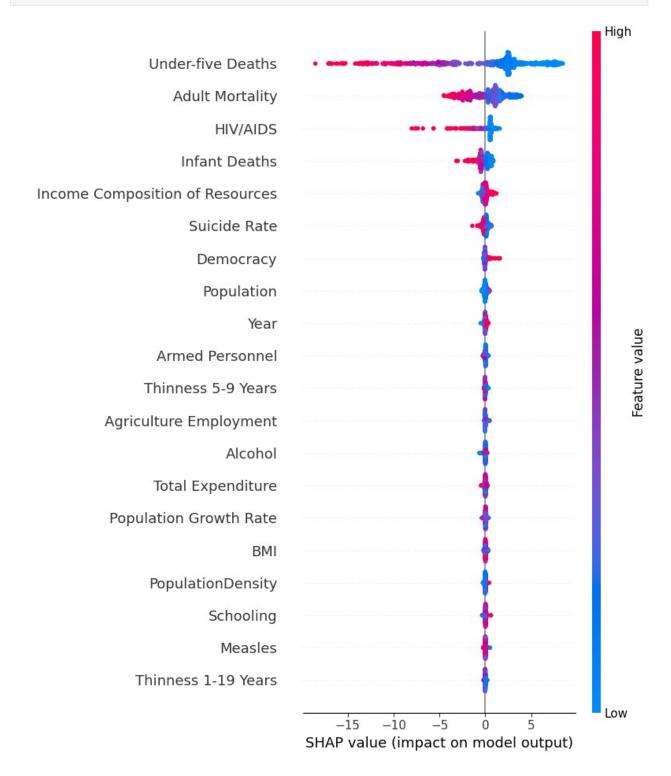
```
df = pd.read_csv('LifeExpectancyClean.csv', index_col=0)
df = df.drop(columns=['Country'])

# Identify target variable
X = df.drop(["Life Expectancy"], axis=1)
y = df["Life Expectancy"]

# Split the data
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)

# Train model
model = RandomForestRegressor()
model.fit(X_train, y_train)

# Explain the model predictions using SHAP
explainer = shap.Explainer(model, X_train) # TreeExplainer for tree-based models
shap_values = explainer(X_test)
```



Import libraries and tools

```
import numpy as np
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.ensemble import RandomForestRegressor
from sklearn.metrics import mean_absolute_error, mean_squared_error,
r2_score
import matplotlib.pyplot as plt
import seaborn as sns
from statsmodels.stats.outliers_influence import
variance_inflation_factor
import statsmodels.api as sm
from sklearn.decomposition import PCA
from sklearn.preprocessing import StandardScaler
from sklearn.linear_model import Ridge
```

Read in data

Multiple Linear Regression Model

```
def run_regression(X, y):
    """ Fits a Ridge regression model, evaluates its performance,
displays key metrics and OLS summary
    statistics, and creates a scatter plot of predicted vs. actual
values.

Parameters:
    X: Array of independent variables.
    y: Array of the dependent variable.
```

```
Returns:
       None. Prints model performance metrics and OLS summary.
    # Split the data
    X_train, X_test, y_train, y_test = train_test_split(X, y,
test_size=0.2, random state=42)
    # Initialize and fit Ridge regression model
    ridge model = Ridge(alpha=1.0) # You can adjust the alpha
(regularization strength)
    ridge model.fit(X train, y train)
    # Predictions
    y pred = ridge model.predict(X test)
    # Evaluate the model
    mae = mean_absolute_error(y_test, y_pred)
    mse = mean squared error(y test, y pred)
    r2 = r2_score(y_test, y_pred)
    print(f'MAE: {mae}')
    print(f'MSE: {mse}')
    print(f'RMSE: {np.sqrt(mse)}')
    print(f'R^2: {r2}')
    # Coefficients and intercept
    print("Intercept:", ridge_model.intercept_)
    print("Coefficients:", ridge model.coef )
    # Approximate p-values using statsmodels OLS
    ols_model = sm.OLS(y_train, X_train).fit()
    print(ols model.summary()) # Will show coefficients, p-values,
and more
    # Scatter plot of actual vs. predicted values
    plt.figure(figsize=(8, 6))
    plt.scatter(y_test, y_pred, color='blue', alpha=0.7)
    plt.plot([y.min(), y.max()], [y.min(), y.max()], 'r--', lw=2,
label='Perfect Prediction') # Diagonal line
    plt.xlabel('Actual Life Expectancy', fontsize=16)
    plt.ylabel('Predicted Life Expectancy', fontsize=16)
    plt.title('Actual vs. Predicted Life Expectancy', fontsize=18)
    plt.legend()
    plt.show()
# Prepare the data
X = df[cols] # Independent variables
y = df['Life Expectancy'] # Dependent variable
```

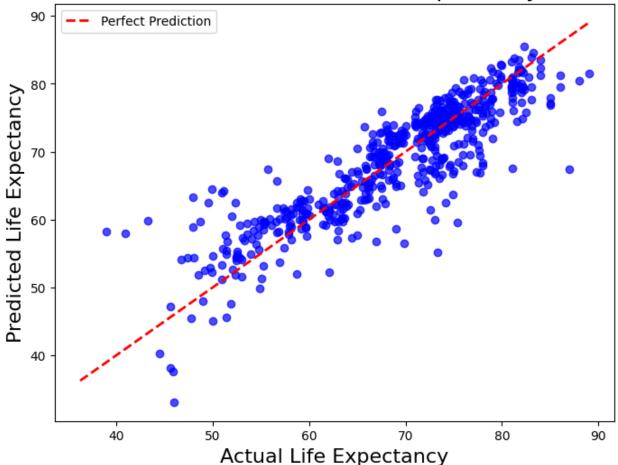
```
# Add constant to the independent variables (intercept term)
X = sm.add constant(X, has constant='add')
run regression(X, y)
/opt/homebrew/lib/python3.10/site-packages/sklearn/linear model/
ridge.py:216: LinAlgWarning: Ill-conditioned matrix (rcond=2.36694e-
20): result may not be accurate.
  return linalg.solve(A, Xy, assume a="pos", overwrite a=True).T
MAE: 3.1054546843671975
MSE: 18.952501388896334
RMSE: 4.3534470697249015
R^2: 0.7826229288375897
Intercept: 54.99665966279319
Coefficients: [ 0.00000000e+00 5.75096645e-02 2.42908311e-04
5.31951431e-02
 -6.46893141e-01 4.93424380e-09 1.44485344e-03 6.26262327e+00
  1.72102807e+00 -4.67156028e+00 -5.31598821e-02 2.41652161e+00
 -1.55709579e-01 1.00043000e-05 6.47107458e-011
                           OLS Regression Results
Dep. Variable: Life Expectancy
                                       R-squared:
0.806
Model:
                                 0LS
                                     Adj. R-squared:
0.805
Method:
                       Least Squares F-statistic:
686.2
                    Mon, 09 Dec 2024 Prob (F-statistic):
Date:
0.00
Time:
                            17:53:55 Log-Likelihood:
-6641.9
No. Observations:
                                2329
                                       AIC:
1.331e+04
Df Residuals:
                                2314
                                     BIC:
1.340e+04
Df Model:
                                  14
Covariance Type:
                           nonrobust
                                     coef std err t
          [0.025
P>|t|
                      0.975]
                                  54.9812 0.613
                                                        89.732
const
0.000
          53.780
                      56.183
```

Alcohol			0.0	565	0.030	1.916
0.055 Percentage	-0.001	0.114	0.0	002	6.06e-05	3.979
0.000	0.000	0.000	0.0	002	0.00e-05	3.979
Diphtheria		0.000	0.0	531	0.004	12.788
0.000	0.045	0.061	0.0	331	01001	12.700
HIV/AIDS		0.00=	-0.6	464	0.018	-34.969
0.000	-0.683	-0.610				
Population	1		4.923e	- 09	6.84e-10	7.195
0.000	3.58e-09	6.26e-09				
Population			0.0	014	0.000	9.212
0.000	0.001	0.002				
		of Resources	6.4	615	0.762	8.480
0.000	4.967	7.956				
HighIncome		2 200	1.7	2/0	0.337	5.126
0.000	1.066	2.388	4 C	052	0 262	17 000
HealthyWei	.gntBM1 -5.199	-4.171	-4.6	853	0.262	-17.880
Thinness 1			-0.0	510	0.027	-1.927
0.054	-0.105	0.001	-0.0	319	0.027	-1.927
Human Righ		0.001	2.4	4 75	0.467	5.236
0.000	1.531	3.364	211	175	01107	3.230
Suicide Ra		31301	-0.1	552	0.013	-11.747
0.000	-0.181	-0.129			0.000	
Agricultur	e Employm	nent	9.986e	-06	3.71e-06	2.694
	2.72e-06	1.73e-05				
Schooling			0.6	369	0.054	11.847
0.000	0.531	0.742				
	:======		======	====		
Omnibus:		1	41.498	Durk	oin-Watson:	
2.041		_		2011		
Prob(Omnib	ous):		0.000	Jaro	que-Bera (JB)):
608.018						
Skew:			0.023	Prob	o(JB):	
9.35e-133						
Kurtosis:			5.503	Cond	d. No.	
1.24e+09						
			======	====		
======						

Notoc:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.24e+09. This might indicate that there are
- strong multicollinearity or other numerical problems.





Test Multicollinearity and Correlation

VIF

```
def calculate_vif(X):
    """ Calculates the Variance Inflation Factor (VIF) for each
feature in the dataset
    to detect multicollinearity among independent variables.

Parameters:
    X : X : Array of independent variables.

Returns:
    None. Prints a DataFrame showing each feature's VIF value.

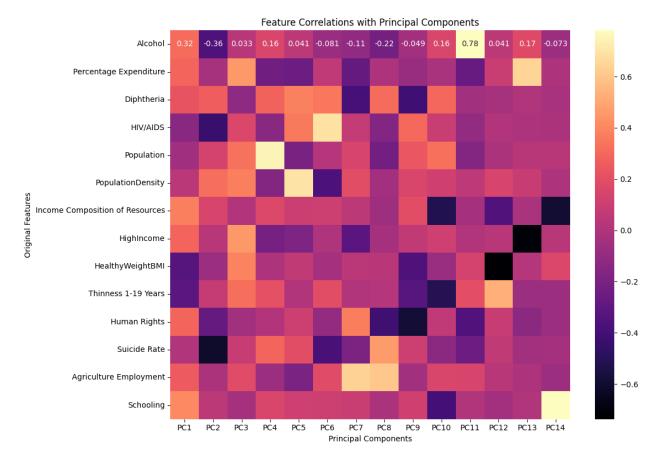
"""

# Calculate VIF for each independent variable
vif_data = pd.DataFrame()
vif_data['Variable'] = X.columns
vif_data['VIF'] = [variance_inflation_factor(X.values, i) for i in
```

```
range(X.shape[1])]
     print(vif data)
calculate vif(X)
                                  Variable
                                                      VIF
0
                                      const 50.664338
                Alcohol 1.844292
Percentage Expenditure 1.912356
1
2
3
                               Diphtheria 1.253468
4
                                  HIV/AIDS 1.140730
5
                               Population 1.115808
     PopulationDensity 1.091584 Income Composition of Resources 2.945715
6
7
8
                               HighIncome 1.991131
9
                        HealthyWeightBMI
                                                2.165912
                    Thinness 1-19 Years 1.841865
Human Rights 1.507866
Suicide Rate 1.149728
10
11
12
                Agriculture Employment 1.289851
Schooling 3.723695
13
14
```

PCA

```
def calculate pca():
    """ Performs Principal Component Analysis (PCA) on a set of
features, visualizes feature correlations
    with principal components, and prints the explained variance ratio
for each component.
    Returns:
        None. Displays a heatmap of feature-PC correlations and prints
the explained variance for each principal component.
    X_PCA = df[cols]
    # Standardize the data
    scaler = StandardScaler()
    X scaled = scaler.fit transform(X PCA)
    # Perform PCA
    pca = PCA()
    X_pca = pca.fit_transform(X_scaled)
    # Get the loadings
    loadings = pd.DataFrame(
        pca.components .T,
        columns = [f"PC{i+1}" for i in range(X pca.shape[1])],
        index=cols
```



```
PC1 explains 32.24% of the variance.
PC2 explains 9.89% of the variance.
PC3 explains 9.59% of the variance.
```

```
PC4 explains 7.83% of the variance.
PC5 explains 6.82% of the variance.
PC6 explains 5.74% of the variance.
PC7 explains 5.60% of the variance.
PC8 explains 5.09% of the variance.
PC9 explains 4.28% of the variance.
PC10 explains 3.84% of the variance.
PC11 explains 3.03% of the variance.
PC12 explains 2.42% of the variance.
PC13 explains 2.31% of the variance.
PC14 explains 1.30% of the variance.
```

Correlation Matrix

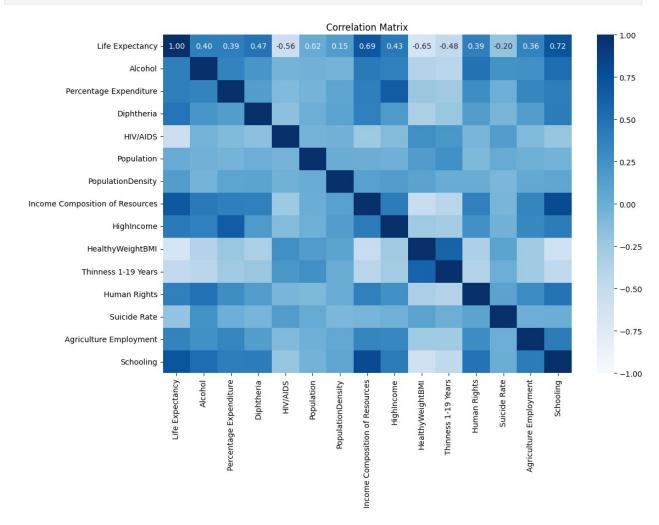
```
def calculate corr matrix():
    """Computes and visualizes the correlation matrix for a set of
features.
    Returns:
        None. Displays the correlation matrix and the heatmap
visualization.
    df corr = df[cols ext]
    # Compute the correlation matrix
    corr matrix = df corr.corr()
    # Display the correlation matrix
    display(corr matrix)
    # Visualize the correlation matrix using a heatmap
    plt.figure(figsize=(12, 8))
    sns.heatmap(corr_matrix, annot=True, cmap='Blues', vmin=-1,
vmax=1, fmt='.2f')
    plt.title("Correlation Matrix")
    plt.show()
calculate corr matrix()
                                 Life Expectancy Alcohol \
Life Expectancy
                                        1.000000 0.395782
Alcohol
                                        0.395782 1.000000
                                        0.392870 0.361026
Percentage Expenditure
Diphtheria
                                        0.470657 0.218709
HIV/AIDS
                                       -0.557549 -0.048415
Population
                                        0.020565 -0.024166
PopulationDensity
                                        0.149266 -0.047897
Income Composition of Resources
                                        0.690552 0.436655
HighIncome
                                        0.434693 0.389933
HealthyWeightBMI
                                       -0.652780 -0.389465
```

Thinness 1-19 Years Human Rights Suicide Rate Agriculture Employment Schooling	0.3861 -0.2020	40 -0.4187 59 0.4899 44 0.2344 05 0.2554 27 0.5268	27 07 98	
	Percentage Ex	nenditure	Diphtheria	
HIV/AIDS \	Tercentage Ex	penareare	Dipireneria	
Life Expectancy		0.392870	0.470657 -	
•		0.392070	0.4/003/ -	
0.557549				
Alcohol		0.361026	0.218709 -	
0.048415				
Percentage Expenditure		1.000000	0.147277 -	
0.106917				
Diphtheria		0.147277	1.000000 -	
		0.14/2//	1.000000 -	
0.160751		0 100017	0 100751	
HIV/AIDS		-0.106917	-0.160751	
1.000000				
Population		-0.046905	-0.000952 -	
0.049091				
PopulationDensity		0.085930	0.090455 -	
0.036280		0.00000	01030133	
Income Composition of Resources		0.396316	0.389195 -	
		0.390310	0.309193 -	
0.243533		0.660711	0 170001	
HighIncome		0.662711	0.178091 -	
0.131954				
HealthyWeightBMI		-0.225208	-0.336773	
0.265416				
Thinness 1-19 Years		-0.256365	-0.224631	
0.203049		0.20000	01221051	
Human Rights		0.281092	0.153014 -	
0.067349		0.201092	0.133014 -	
		0 000401	0.005000	
Suicide Rate		-0.008401	-0.065066	
0.154562				
Agriculture Employment		0.342013	0.142392 -	
0.105067				
Schooling		0.404376	0.409614 -	
0.217555				
	Population P	opulationD	ensity \	
Life Expectancy	0.020565		149266	
Alcohol	-0.024166		047897	
Percentage Expenditure	-0.046905		085930	
Diphtheria	-0.000952	0.	090455	
HIV/AIDS	-0.049091	-0.	036280	
Population	1.000000	0.	010537	
PopulationDensity	0.010537		000000	
Income Composition of Resources	0.004605		116358	
HighIncome	-0.022556		151868	
TI STITITE ONIC	0.022330	0.	131000	

HealthyWeightBMI Thinness 1-19 Years Human Rights Suicide Rate Agriculture Employment Schooling	0.156914 0.256959 -0.099423 0.028308 -0.022485 -0.043605	0.086919 0.012518 0.008503 -0.085217 0.044078 0.077303
	Income Compositio	n of Resources
HighIncome \ Life Expectancy 0.434693	1coc copcs1t1c	0.690552
Alcohol 0.389933		0.436655
Percentage Expenditure 0.662711		0.396316
Diphtheria		0.389195
0.178091 HIV/AIDS		-0.243533 -
0.131954		-0.243333 -
Population		0.004605 -
0.022556		
PopulationDensity		0.116358
0.151868		1 00000
Income Composition of Resources 0.420543		1.000000
HighIncome		0.420543
1.000000		
HealthyWeightBMI		-0.530666 -
0.253594		0.417060
Thinness 1-19 Years 0.288875		-0.417869 -
Human Rights		0.384839
0.250808		0.30.033
Suicide Rate		-0.067840 -
0.026974		
Agriculture Employment		0.350654
0.324867		0.704725
Schooling 0.416127		0.794735
0.410127		
	HealthyWeightBMI	Thinness 1-19 Years
\		
Life Expectancy	-0.652780	-0.476540
Alcohol	-0.389465	-0.418701
Percentage Expenditure	-0.225208	-0.256365
Diphtheria	-0.336773	-0.224631

HIV/AIDS	0.265416	0.203049
Population	0.156914	0.256959
PopulationDensity	0.086919	0.012518
Income Composition of Resources	-0.530666	-0.417869
HighIncome	-0.253594	-0.288875
HealthyWeightBMI	1.000000	0.599444
Thinness 1-19 Years	0.599444	1.000000
Human Rights	-0.338707	-0.388758
Suicide Rate	0.088899	-0.005964
Agriculture Employment	-0.263869	-0.271680
Schooling	-0.604840	-0.468108
Life Expectancy Alcohol Percentage Expenditure Diphtheria HIV/AIDS Population PopulationDensity Income Composition of Resources HighIncome HealthyWeightBMI Thinness 1-19 Years Human Rights Suicide Rate Agriculture Employment Schooling	Human Rights	14 07 01 66 62 08 17 40 74 99 64 17
Life Expectancy Alcohol Percentage Expenditure Diphtheria HIV/AIDS Population PopulationDensity Income Composition of Resources HighIncome	0.361705 0.255498 0.342013 0.142392 -0.105067	6chooling 0.717427 0.526801 0.404376 0.409614 0.217555 0.043605 0.077303 0.794735 0.416127

HealthyWeightBMI Thinness 1-19 Years Human Rights	-0.263869 -0.271680 0.284028	-0.604840 -0.468108 0.479620
Suicide Rate Agriculture Employment	-0.003705 1.000000	0.479020 0.003806 0.415885
Schooling	0.415885	1.000000



Feature Importance - Random Forest

```
def random_forest(X, y):
    """ Trains a Random Forest Regressor, evaluates feature
importance,
    and visualizes the most important features.

Parameters:
    X : Array of independent variables.
    y : Array of the dependent variable.

Returns:
```

```
None. Prints the feature importance table and displays the bar
plot of feature importance.
    # Split the data
    X_train, X_test, y_train, y_test = train_test_split(X, y,
test size=0.2, random state=42)
    # Initialize and train the Random Forest Regressor
    rf = RandomForestRegressor(n estimators=100, random state=42)
    rf.fit(X_train, y_train)
    # Predict on the test data
    y_pred = rf.predict(X_test)
    # Feature Importance
    feature importance = pd.DataFrame({
        'Feature': X.columns,
        'Importance': rf.feature importances
    }).sort values(by='Importance', ascending=False)
    print("\nFeature Importance:")
    print(feature importance)
    # Visualize Feature Importance
    plt.figure(figsize=(10, 8))
    sns.barplot(x='Importance', y='Feature', color='mediumblue',
data=feature importance)
    plt.title('Feature Importance for Predicting Life Expectancy')
    plt.show()
random forest(X, y)
Feature Importance:
                            Feature
                                     Importance
4
                           HIV/AIDS
                                        0.621173
7
    Income Composition of Resources
                                       0.207394
14
                          Schooling
                                       0.028217
12
                       Suicide Rate
                                       0.021548
6
                  PopulationDensity
                                       0.018420
9
                   HealthyWeightBMI
                                       0.015424
                Thinness 1-19 Years
10
                                       0.015423
5
                         Population
                                       0.014670
3
                         Diphtheria
                                       0.013067
11
                       Human Rights
                                       0.012430
1
                            Alcohol
                                       0.011083
13
             Agriculture Employment
                                       0.009423
2
             Percentage Expenditure
                                       0.005997
8
                         HighIncome
                                       0.005732
0
                              const
                                       0.000000
```

