

Exercise 3

This exercise session consists of Scala programming exercises.

Higher Order Functions Basics

Implement the methods described in the file: `higherOrderFunc.scala`.

Exercises From Last Week OPTIONAL

Revisit the exercises from last week and think about how you could use higher-order functions to solve the problems.

Hint: `map`, `flatMap`, `pack`, `span` and `foldLeft` are relevant.

Binary Search Trees (Dictionaries)

Background Information

A binary tree is either empty or it is composed of a root element and two successors, which are binary trees themselves.

A basic initial implementation of a binary tree is available in this project. Go to the `binarytree.scala` file and look at the following description of the implementation:

An `End` is equivalent to an empty tree. A `Branch` has a value, and two descendant trees.

A tree with only a root node would be `Node(4)` and an empty tree would be `End`.

Implementation: `addNode`

Write a function to add an element to a binary search tree.

```
scala> End.addNode(2)
res0: Node[Int] = T(2 . .)
```

```
scala> res0.addNode(3)
res1: Node[Int] = T(2 . T(3 . .))
```

```
scala> res1.addNode(0)
res2: Node[Int] = T(2 T(0 . .) T(3 . .))
```

Hint: The abstract definition of `addNode` in `Tree` should be:

```
def addNode(x: Int, tree: BinaryTree): BinaryTree
```

Implementation: isBinarySearchTree

Write a function to check if the given BinaryTree is a binary search tree. The function should have the following definition:

```
def isBinarySearchTree(bt: BinaryTree): Boolean
```

The exercise is adapted from P57 at <http://aperiodic.net/phil/scala/s-99/>.

Group the elements of a set into disjoint subsets

Create a new file and implement P27 from <http://aperiodic.net/phil/scala/s-99/> as described in the following.

Hint: You need to solve P26 before doing P27.

a)

In how many ways can a group of 9 people work in 3 disjoint subgroups of 2, 3 and 4 persons? Write a function that generates all the possibilities. Example:

```
group3(List("Aldo", "Beat",
            "Carla", "David",
            "Evi", "Flip",
            "Gary", "Hugo",
            "Ida"))
res0: List[List[List[String]]] =
  List(List(
    List(Aldo, Beat),
    List(Carla, David),
    List(Evi, Flip, Gary, Hugo, Ida)), ...
```

b)

Generalize the above predicate in a way that we can specify a list of group sizes and the predicate will return a list of groups.

Example:

```
group(
  List(2, 2, 5),
  List("Aldo", "Beat",
        "Carla", "David",
        "Evi", "Flip",
        "Gary", "Hugo",
```

```
        "Ida"))
res0:
  List[List[List[String]]] =
    List(List(
      List(Aldo, Beat),
      List(Carla, David),
      List(Evi, Flip, Gary, Hugo, Ida)), ...
```

Note that we do not want permutations of the group members; i.e. ((Aldo, Beat), ...) is the same solution as ((Beat, Aldo), ...). However, we make a difference between ((Aldo, Beat), (Carla, David), ...) and ((Carla, David), (Aldo, Beat), ...).

You may find more about this combinatorial problem in a good book on discrete mathematics under the term "multinomial coefficients".

Gray Code

Create a new file and implement P49 from <http://aperiodic.net/phil/scala/s-99/> as described in the following.

An n-bit Gray code is a sequence of n-bit strings constructed according to certain rules. For example, n = 1: C(1) = ("0", "1"). n = 2: C(2) = ("00", "01", "11", "10"). n = 3: C(3) = ("000", "001", "011", "010", "110", "111", "101", "100"). Find out the construction rules and write a function to generate Gray codes.

For instance:

```
gray(3)
res0 List[String] = List(000, 001, 011, 010, 110, 111, 101, 100)
```

See if you can use memoization to make the function more efficient.