```
Algorithm 1: Splay Function
      Input: root: node, key: int
       Output: The root node after splaying
    1 Function splay(root, key):
           if root is null or root's key is equal to the given key then
    \mathbf{2}
    3
            return root;
           key\_value \leftarrow key;
    4
    5
           if root's key is greater than key_value then
               if root has no left child then
    6
                   return root;
               if root's left child's key is greater than key_value then
    8
                    root \rightarrow left \rightarrow left \leftarrow splay(root \rightarrow left \rightarrow left, key);
    9
                    root \leftarrow rightRotate(root);
  10
                else if root's left child's key is less than key_value then
  11
                    root \rightarrow left \rightarrow right \leftarrow splay(root \rightarrow left \rightarrow right, key);
  12
                    if root's left right child exists then
   13
                     root \rightarrow left \leftarrow leftRotate(root \rightarrow left);
   14
               return (root \rightarrow left\ exists)? rightRotate(root):root
  15
    16
                else
                    if root has no right child then
    17
                     | return root;
    18
                    if root's right child's key is greater than key_value then
    19
                         root \rightarrow right \rightarrow left \leftarrow splay(root \rightarrow right \rightarrow left, key);
    20
    21
                         if root's right left child exists then
                             root \rightarrow right \leftarrow rightRotate(root \rightarrow right);
    22
                    else if root's right child's key is less than key_value then
    23
                         root \rightarrow right \rightarrow right \leftarrow splay(root \rightarrow right \rightarrow right, key);
    24
                         root \leftarrow leftRotate(root);
    25
                    return (root→right exists)? leftRotate(root):root
    26
27
```

## Algorithm 2: Insert Function

```
Data: root: node, key: int
    Result: Root node after insertion and splay operation
 1 Function insert(root, key):
 \mathbf{2}
        parent \leftarrow NULL;
 3
        temp \leftarrow root;
 4
        while temp is not NULL do
 5
            parent \leftarrow temp;
 6
            if temp \rightarrow key < key then
 7
             | temp \leftarrow temp\rightarrowright;
 8
            else if temp \rightarrow key < key then
             | temp \leftarrow temp\rightarrowleft;
 9
            else
10
                return splay(root, key);
11
12
        insertNode \leftarrow createnode(key);
13
        if parent is NULL then
         | \quad root \leftarrow insertNode;
14
        else if parent \rightarrow key < key then
15
         | parent\rightarrowright \leftarrow insertNode;
16
17
        else
18
         | parent\rightarrowleft \leftarrow insertNode;
        return splay(root, key);
19
```

```
Algorithm 3: Deletenode Function
```

```
Data: root: node, key: int
    Result: Root node after deletion and splay operation
 1 Function deletenode (root, key):
 \mathbf{2}
         temp \leftarrow find(root, key);
 3
         if temp is NULL then
 4
             return root;
         if temp \rightarrow left is NULL then
 \mathbf{5}
 6
             root \leftarrow temp \rightarrow right;
 7
             free(temp);
 8
         else if temp \rightarrow right is NULL then
 9
             root \leftarrow temp \rightarrow left;
10
             free(temp);
         else
11
12
             maxleft \leftarrow findMaxleft(temp);
13
             maxleft \rightarrow right \leftarrow temp \rightarrow right;
             maxleft \rightarrow left \leftarrow temp \rightarrow left;
14
15
             root \leftarrow maxleft;
16
             free(temp);
17
         return root;
```

## Algorithm 4: FindMaxleft Function

```
Data: root: node
    Result: Node with maximum left value
 1 Function findMaxleft(root):
 \mathbf{2}
          temp \leftarrow root \rightarrow left;
 3
          P \leftarrow NULL;
 4
          while temp \rightarrow right do
 \mathbf{5}
              P \leftarrow \text{temp};
 6
              temp \leftarrow temp \rightarrow right;
 7
          if P is NULL then
              root \rightarrow left \leftarrow temp \rightarrow left;
 8
 9
              return temp;
          P \rightarrow right \leftarrow temp \rightarrow left;
10
11
          return temp;
```

## Algorithm 5: Find Function Data: root: node, key: int Result: Root node after splay operation 1 Function find(root, key): $\mathbf{2}$ $temp \leftarrow root;$ 3 $\mathbf{while} \ \mathit{temp} \ \mathit{is} \ \mathit{not} \ \mathit{NULL} \ \mathbf{do}$ 4 if $temp \rightarrow key < key$ then $\mathbf{5}$ | temp $\leftarrow$ temp $\rightarrow$ right; 6 else if $temp \rightarrow key > key$ then | temp $\leftarrow$ temp $\rightarrow$ left; 7 8 ${f else}$ 9 **10** $\mathbf{if} \ \mathit{temp} \ \mathit{is} \ \mathit{NULL} \ \mathbf{then}$ 11 Output: Not found; 12 $return \ root;$ **13 return** splay(root, key);