Specification

We define a class named DirectedGraph representing a directed graph.

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The class DirectedGraph will provide the following methods:
     _{init} (vertices : int = 0, edges : int = 0)
           Constructs a graph.
     number of vertices()
           Returns the number of vertices.
     number_of_predecessors(vertex : int)
           Returns the number of predecessors of a given vertex.
     number_of_successors(vertex : int)
           Returns the number of successors of a given vertex.
     number of edges()
           Returns the number of edges.
     vertices_iterator()
           Yields every vertex (as an int) in the graph
     predecessors iterator(vertex : int)
           Yields every predecessor (as an int) of a given vertex
     successors iterator(vertex : int)
           Yields every successor (as an int) of a given vertex.
     edges_iterator()
           Yields every edge (as a tuple (vertex1, vertex2, cost)) in the
graph.
     is_vertex(vertex : int)
           Returns True if the vertex exists, False otherwise
     is edge(vertex1: int, vertex2: int)
           Returns True if the edge vertex1 – vertex2 exists, False
otherwise.
     edge_cost(vertex1 : int, vertex2 : int)
           Returns the cost of the edge vertex1 – vertex2.
           If the edge doesn't exist, it raises an error.
     set_edge_cost(vertex1 : int, vertex2 : int, new_cost : int)
           Sets the cost of the edge vertex1 – vertex2 to new_cost.
           If the edge doesn't exist, it raises an error.
     add_vertex(vertex : int)
           Adds a vertex to the graph.
           If the vertex already exists, it raises an error.
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add_edge(vertex1 : int, vertex2 : int, cost : int = 0)
    Adds an edge to the graph.
    If the edge already exists, it raises an error.
    If one of the vertices does not exist, an error is raised.
remove_vertex(vertex : int)
    Removes a vertex.
    If the vertex doesn't exist, it raises an error.
remove_edge(vertex1: int, vertex2 : int)
    Removes an edge.
    If the edge doesn't exist, it raises an error.
copy()
    Returns a copy of the graph
```

Implementation

The implementation uses a set of integers to store the vertices, two dictionaries of (key, values) as (integers, sets) for storing the predecessors and successors and a dictionary of (key, values) as (pair of integers, integer) for storing the edges.