```
def lowest cost path(self, vertex1 : int, vertex2 : int):
114
              if not self.is vertex(vertex1):
115
                  raise VertexError("the vertex {} doesn't exist!".format(vertex1))
116
117
              if not self.is vertex(vertex2):
                  raise VertexError("the vertex {} doesn't exist!".format(vertex2))
118
              q = PriorityQueue()
119
              prev = {vertex: -1 for vertex in self.vertices iterator()}
120
              dist = {vertex: le7 for vertex in self.vertices iterator()}
121
              dist[vertex1] = 0
122
              q.put((dist[vertex1], vertex1))
123
              found = False
124
              while not q.empty() and not found:
125
126
                  (inutil, x) = q.qet()
                  if x == vertex2:
127
                      found = True
128
                  for y in self.successors iterator(x):
129
                      if dist[y] is le7 or dist[x] + self.edge cost(x, y) < dist[y]:
130
                          dist[y] = dist[x] + self.edge cost(x, y)
131
                          q.put((dist[y], y))
132
133
                          prev[y] = x
134
135
              if found is False:
                  raise WalkError("no walk between {} and {}.".format(vertex1, vertex2))
136
              return (dist[vertex2], prev)
137
```