# Artificial intelligence - Project 2 - Propositional Logic and Predicates -

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## 1 PROBLEM 1: Black Friday

## 1.1 Clues of the problem

Five friends are side by side drinking juice and talking about the deals they got during the Black Friday sales. Follow the clues to find out who bought the laptop.

#### Clues:

- 1. The man drinking the Orange juice is exactly to the right of the man who got the 70 % discount.
- 2. Keith is 45 years old.
- 3. The man who bought the TV is exactly to the left of the man wearing the Red shirt.
- 4. At the third position is the man who got the 50 % discount.
- 5. Keith is next to the man wearing the White shirt.
- 6. The 25-year-old man is somewhere between the 35-year-old man and the 40-year-old man, in that order.
- 7. The man drinking Apple juice bought the Smartphone.
- 8. The 30-year-old man is exactly to the left of the man that bought the Beard trimmer.
- 9. Sean is the youngest.
- 10. The man that got the 40% discount is exactly to the right of the man who bought the Beard trimmer.
- 11. Keith is next to the 35-year-old man.
- 12. Eugene is 40 years old.
- 13. Sean is wearing the Black shirt.
- 14. At the fourth position is the man who got the biggest discount.
- 15. Dustin got 60% off.
- 16. The man drinking the Lemon juice is exactly to the right of the man drinking the Grape juice.
- 17. Keith bought a Game console.
- 18. The man who got the 80% discount is exactly to the left of the man who is wearing the Blue shirt.
- 19. The man drinking Grape juice bought the Beard trimmer.
- 20. The man wearing the Black shirt is somewhere to the right of Keith.
- 21. The man that bought the Smartphone is next to the man wearing the Black shirt.

## 1.2 Code implementation and solution

This sub-section is dedicated to showcasing your own solution that you came up with for solving the above question. One has to put here any **code** that has been used for solving the above task, along with **comments** that explain every design decision made. To reference the code, please make use of the *code lines number*. Additionally, complete this sub-section with any **command configurations** that you may have used during the implementation or testing process (please fill in *just the arguments*).

#### Code:

```
% Saved by Prover9-Mace4 Version 0.5, December 2007.
   set(ignore_option_dependencies). % GUI handles dependencies
3
   if(Prover9). % Options for Prover9
     assign(max_seconds, 60).
   end_if.
   if (Mace4).
                 % Options for Mace4
     assign(max_seconds, 60).
10
   end_if.
11
12
   formulas(assumptions).
13
   %5 friends drinking juice
```

```
16
   differentFrom(man1,man2).
17
   differentFrom(man1,man3).
18
   differentFrom(man1,man4).
   differentFrom(man1,man5).
20
21
   differentFrom(man2,man3).
22
   differentFrom(man2,man4).
   differentFrom(man2,man5).
24
   differentFrom(man3,man4).
26
   differentFrom(man3,man5).
28
   differentFrom(man4,man5).
29
30
   differentFrom(x,y) -> differentFrom(y,x).
31
32
   %rightTo(x,y) - y is exactly to the right of x
33
34
   rightTo(man1,man2).
35
   rightTo(man2,man3).
   rightTo(man3,man4).
37
   rightTo(man4,man5).
39
   -rightTo(man1,man1).
   -rightTo(man1,man3).
41
    -rightTo(man1,man4).
    -rightTo(man1,man5).
43
44
   -rightTo(man2,man1).
45
   -rightTo(man2,man2).
46
    -rightTo(man2,man4).
47
   -rightTo(man2,man5).
48
49
   -rightTo(man3,man1).
50
    -rightTo(man3,man2).
51
   -rightTo(man3,man3).
52
    -rightTo(man3,man5).
54
   -rightTo(man4,man1).
   -rightTo(man4,man2).
56
   -rightTo(man4,man3).
    -rightTo(man4,man4).
58
   -rightTo(man5,man1).
60
    -rightTo(man5,man2).
    -rightTo(man5,man3).
62
   -rightTo(man5,man4).
63
    -rightTo(man5,man5).
65
   % \operatorname{leftTo}(x,y) - y \text{ is exactly to the left of } x
   rightTo(y,x) <-> leftTo(x,y).
67
   %nextTo(x,y) - y is to the left or to the right of x
```

```
rightTo(x,y) \mid leftTo(x,y) <-> nextTo(x,y).
70
71
    %somewhereRight(x,y) - y is somewhere to the right of x
72
    somewhereRight(man1,man2).
74
    somewhereRight(man1,man3).
    somewhereRight(man1,man4).
76
    somewhereRight(man1,man5).
78
    somewhereRight(man2,man3).
    somewhereRight(man2,man4).
80
    somewhereRight(man2,man5).
81
82
    somewhereRight(man3,man4).
83
    somewhereRight(man3,man5).
85
    somewhereRight(man4,man5).
87
    -somewhereRight(man1,man1).
89
    -somewhereRight(man2,man1).
90
    -somewhereRight(man2,man2).
91
    -somewhereRight(man3,man1).
93
    -somewhereRight(man3,man2).
    -somewhereRight(man3,man3).
95
    -somewhereRight(man4,man1).
97
    -somewhereRight(man4,man2).
    -somewhereRight(man4,man3).
    -somewhereRight(man4,man4).
100
101
    -somewhereRight(man5,man1).
102
    -somewhereRight(man5,man2).
103
    -somewhereRight(man5,man3).
104
    -somewhereRight(man5,man4).
105
    -somewhereRight(man5,man5).
106
    %somewhereLeft(x,y) - y is somewhere to the left of x
108
    somewhereRight(y,x) <-> somewhereLeft(x,y).
110
    %somewhereInBetween (x,y,z) - y is somwhere in between x and z, x is to the left of y and z is to the r
    somewhereLeft(y,x) & somewhereRight(y,z) <-> somewhereInBetween (x,y,z).
112
113
    %the colors of the men's t-shirts
114
    black(x) \mid blue(x) \mid green(x) \mid red(x) \mid white(x).
116
    %the name of the men
117
    dustin(x) \mid eugene(x) \mid hank(x) \mid keith(x) \mid sean(x).
118
119
    %the products purchased
120
    beardtrimmer(x) | gameconsole(x) | laptop(x) | smartphone(x) | tv(x).
121
122
    %the discounts
```

```
fortyp(x) \mid fiftyp(x) \mid sixtyp(x) \mid seventyp(x) \mid eightyp(x).
124
125
126
    twentyfivey(x) \mid thirtyy(x) \mid thirtyfivey(x) \mid fortyy(x) \mid fortyfivey(x).
128
    %the juices men drink
    apple(x) \mid cranberry(x) \mid grape(x) \mid lemon(x) \mid orange(x).
130
    %each man has a different colored t-shirt
132
    black(x) & black(y) -> -differentFrom(x,y).
    blue(x) & blue(y) -> -differentFrom(x,y).
134
    green(x) & green(y) -> -differentFrom(x,y).
    red(x) & red(y) -> -differentFrom(x,y).
    white(x) & white(y) \rightarrow -differentFrom(x,y).
137
    %each man has a different age
139
    dustin(x) & dustin(y) -> -differentFrom(x,y).
    eugene(x) & eugene(y) -> -differentFrom(x,y).
141
    hank(x) & hank(y) -> -differentFrom(x,y).
142
    keith(x) & keith(y) -> -differentFrom(x,y).
143
    sean(x) & sean(y) -> -differentFrom(x,y).
145
    %each man has purchased a different item
    beardtrimmer(x) & beardtrimmer(y) \rightarrow -differentFrom(x,y).
147
    gameconsole(x) & gameconsole(y) -> -differentFrom(x,y).
    laptop(x) & laptop(y) \rightarrow -differentFrom(x,y).
149
    smartphone(x) \& smartphone(y) \rightarrow -differentFrom(x,y).
    tv(x) & tv(y) \rightarrow -differentFrom(x,y).
151
152
    %each man has a different discount
153
    fortyp(x) & fortyp(y) -> -differentFrom(x,y).
    fiftyp(x) & fiftyp(y) -> -differentFrom(x,y).
    sixtyp(x) & sixtyp(y) \rightarrow -differentFrom(x,y).
156
    seventyp(x) & seventyp(y) -> -differentFrom(x,y).
    eightyp(x) & eightyp(y) -> -differentFrom(x,y).
158
159
    %each man has a different age
160
    twentyfivey(x) & twentyfivey(y) -> -differentFrom(x,y).
161
    thirtyy(x) & thirtyy(y) -> -differentFrom(x,y).
162
    thirtyfivey(x) & thirtyfivey(y) -> -differentFrom(x,y).
    fortyy(x) & fortyy(y) -> -differentFrom(x,y).
164
    fortyfivey(x) & fortyfivey(y) -> -differentFrom(x,y).
166
    %each man is drinking a different juice
    apple(x) & apple(y) -> -differentFrom(x,y).
168
    cranberry(x) & cranberry(y) -> -differentFrom(x,y).
    grape(x) & grape(y) -> -differentFrom(x,y).
    lemon(x) \& lemon(y) \rightarrow -differentFrom(x,y).
171
    orange(x) & orange(y) -> -differentFrom(x,y).
172
173
    %Clues
174
175
    %1. The man drinking the Orange juice is exactly to the right of the man who got the 70 discount
176
    rightTo(x,y) \leftarrow orange(y) \& seventyp(x).
```

```
178
    %2. Keith is 45 years old
179
    keith(x) <-> fortyfivey(x).
180
    %3. The man who bought the TV is exactly to the left of the man wearing the Red shirt.
182
    leftTo(x,y) \leftarrow tv(y) \& red(x).
184
    %4.At the third position is the man who got the 50% discount
    fiftyp(man3).
186
187
    %5. Keith is next to the man wearing the White shirt.
188
    nextTo(x,y) \leftarrow keith(x) \& white(y).
189
190
    %6. The 25-year-old man is somewhere between the 35-year-old man and the 40-year-old man, in that order
191
    somewhereInBetween(x,y,z) \leftarrow thirtyfivey(x) \& twentyfivey(y) \& fortyy(z).
192
193
    %7. The man drinking Apple juice bought the Smartphone.
    apple(x) <-> smartphone(x).
195
    %8. The 30-year-old man is exactly to the left of the man that bought the Beard trimmer.
197
    leftTo(x,y) <- beardtrimmer(x) & thirtyy(y) .</pre>
198
199
    %9. Sean is the youngest.
    sean(x) <-> twentyfivey(x).
201
202
    \%10. The man that got the 40\% discount is exactly to the right of the man who bought the Beard trimmer.
203
    rightTo(x,y) <- beardtrimmer(x) & fortyp(y) .</pre>
204
205
    %11. Keith is next to the 35-year-old man.
206
    nextTo(x,y) <- keith(x) & thirtyfivey(y).</pre>
207
208
    %12. Eugene is 40 years old.
209
    eugene(x) <-> fortyy(x).
210
    %13. Sean is wearing the Black shirt.
212
    sean(x) \iff black(x).
213
214
    %14. At the fourth position is the man who got the biggest discount.
    eightyp(man4).
216
217
    %15. Dustin got 60% off.
218
    dustin(x) <-> sixtyp(x).
220
    %16. The man drinking the Lemon juice is exactly to the right of the man drinking the Grape juice
    rightTo(x,y) <- lemon(y) & grape(x) .
222
    %17. Keith bought a Game console
224
    keith(x) <-> gameconsole(x).
225
226
    %18. The man who got the 80% discount is exactly to the left of the man who is wearing the Blue shirt.
227
    leftTo(x,y) <- blue(x) & eightyp(y).</pre>
228
229
    %19. The man drinking Grape juice bought the Beard trimmer.
230
    grape(x) <-> beardtrimmer(x).
231
```

```
232
    %20. The man wearing the Black shirt is somewhere to the right of Keith.
233
    somewhereRight(x,y) <- black(y) & keith(x).
234
    %21. The man that bought the Smartphone is next to the man wearing the Black shirt.
236
    nextTo(x,y) \leftarrow smartphone(x) \& black(y).
237
238
    end_of_list.
239
240
    formulas(goals).
241
242
    end_of_list.
243
```

## **Explanation:**

• For solving this logic puzzle I created the following predicates:

The predicate differentFrom(x,y), expresses the idea that the men are distinct from one another. The "differentFrom" relation is symmetrical.

The predicate rightTo(x,y), expresses the fact that the y is exactly to the right of x for every pair of men.

The predicate leftTo(x,y), expresses the fact that the y is exactly to the left of x for every pair of men. The predicate leftTo(x,y), expresses the fact that the x is either to the left of y or to the right, this predicate was created using the rightTo and leftTo predicates.

The predicate somewhere Right(x,y), expresses the fact that the y is somewhere to the right of x for every pair of men.

The predicate somewhere Left(x,y), expresses the fact that the y is somewhere to the right of x for every pair of men.

The predicate somewhereInBetween(x,y,z), expresses the fact that the y is somewhere in between x and z, x being somewhere to the left of y and z somewhere to the right of y. The predicates black(x), blue(x), green(x), red(x), white(x) are used to define the colors of the men's t-shirts.

The predicates dustin(x), eugene(x), hank(x), keith(x), sean(x) are used to define the names of the men.

The predicates beardtrimmer(x), gameconsole(x), laptop(x), smartphone(x), tv(x) are used to define the product each man purchased.

The predicates fortyp(x), fiftyp(x), sixtyp(x), seventyp(x), eightyp(x) are used to define the discounts. The predicates twentyfivey(x), thirtyfivey(x), thirtyfivey(x), fortyy(x), fortyfivey(x) are used to define the age of each man.

The predicates apple(x), cranberry(x), grape(x), lemon(x), orange(x) are used to define the juice each man is drinking.

We know that each man has a different colored t-shirt, a different name, has purchased a different product with a different discount, has a different age and is drinking a different juice, so I stated that using the predicate different From and the predicates created for each attribute of the men, with statements like black(x) & black(y) -> -different From (x,y).

#### Mace4 solution:

```
interpretation( 5, [number = 1,seconds = 0], [
    function(man1, [0]),
    function(man2, [1]),
    function(man3, [2]),
    function(man4, [3]),
    function(man5, [4]),
    relation(apple(_), [0,0,1,0,0]),
    relation(beardtrimmer(_), [0,0,0,1,0]),
    relation(black(_), [0,0,0,1,0]),
```

```
relation(blue(_), [0,0,0,0,1]),
10
        relation(cranberry(_), [1,0,0,0,0]),
11
        relation(dustin(_), [0,1,0,0,0]),
12
        relation(eightyp(_), [0,0,0,1,0]),
        relation(eugene(_), [0,0,0,0,1]),
14
        relation(fiftyp(_), [0,0,1,0,0]),
        relation(fortyfivey(_), [1,0,0,0,0]),
16
        relation(fortyp(_), [0,0,0,0,1]),
        relation(fortyy(_), [0,0,0,0,1]),
18
        relation(gameconsole(_), [1,0,0,0,0]),
        relation(grape(_), [0,0,0,1,0]),
20
        relation(green(_), [1,0,0,0,0]),
21
        relation(hank(_), [0,0,1,0,0]),
22
        relation(keith(_), [1,0,0,0,0]),
23
        relation(laptop(_), [0,0,0,0,1]),
24
        relation(lemon(_), [0,0,0,0,1]),
25
        relation(orange(_), [0,1,0,0,0]),
26
        relation(red(_), [0,0,1,0,0]),
27
        relation(sean(_), [0,0,0,1,0]),
28
        relation(seventyp(\underline{\phantom{a}}), [1,0,0,0,0]),
29
        relation(sixtyp(_), [0,1,0,0,0]),
30
        relation(smartphone(_), [0,0,1,0,0]),
31
        relation(thirtyfivey(_), [0,1,0,0,0]),
        relation(thirtyy(_), [0,0,1,0,0]),
33
        relation(tv(_), [0,1,0,0,0]),
        relation(twentyfivey(_), [0,0,0,1,0]),
35
        relation(white(_), [0,1,0,0,0]),
        relation(differentFrom(_,_), [
37
            0,1,1,1,1,
38
            1,0,1,1,1,
39
            1,1,0,1,1,
40
            1,1,1,0,1,
41
            1,1,1,1,0]),
42
        relation(leftTo(_,_), [
43
            0.0.0.0.0.
44
            1,0,0,0,0,
45
            0,1,0,0,0,
46
            0,0,1,0,0,
            0,0,0,1,0]),
48
        relation(nextTo(_,_), [
49
            0,1,0,0,0,
50
            1,0,1,0,0,
            0,1,0,1,0,
52
            0,0,1,0,1,
53
            0,0,0,1,0]),
54
        relation(rightTo(_,_), [
55
            0,1,0,0,0,
56
            0,0,1,0,0,
57
            0,0,0,1,0,
            0,0,0,0,1,
59
            0,0,0,0,0]),
        relation(somewhereLeft(_,_), [
61
            0,0,0,0,0,
62
            1,0,0,0,0,
63
```

```
1,1,0,0,0,
64
       1,1,1,0,0,
65
       1,1,1,1,0]),
66
    relation(somewhereRight(_,_), [
       0,1,1,1,1,
68
       0,0,1,1,1,
69
       0,0,0,1,1,
70
       0,0,0,0,1,
       0,0,0,0,0]),
72
    73
```

## Solution:



Figure 1: The solution of the logic puzzle

## 1.3 References

https://www.brainzilla.com/logic/zebra/black-friday/

## 2 PROBLEM 2: New York Beauty Salon

## 2.1 Clues of the problem

The New You Beauty Salon has a number of different hair colorings scheduled today. Using only the clues below, match each customer to her stylist, and determine the time of her appointment and the hair color dve she has chosen.

#### Clues:

- 1. The costumer that chose midnight blue is sometime before Georgia.
- 2. Susie's costumer has her appointment 4 hours after Tammie's client.
- 3. Whitney's costumer has her appointment 4 hours before Blanche.
- 4. Yvonne's costumer has her appointment sometime after the client that chose warm Mocha.
- 5. Yvonne's costumer, the client that chose honey blonde and Georgia are three different costumers.
- 6.Of Blanche and Rhonda's costumer one has the 4 pm appointment and the other one chose jet black.
- 7. The client tat chose jet black is either Opal's or Susie's client.
- 8.Georgia isn't helped by Rhonda.
- 9. Kelly doesn't have the 11 am appointment.
- 10. Of Opal's costumer and the client that chose vivacious red one has the 3pm appointment and the other one is Flora.
- 11. Alison , the costumer that chose brown sable, Susie's costumer, the costumer that chose honey blonde, the client that chose the 2pm appointment and Victoria 's customer are all different.
- 12. The costumer that chose honey blonde has her appointment 1 hour after the client that chose vivacious red.
- 13.Kelly didn't choose honey blonde.
- 14. Alison didn't choose deep copper.
- 15. Cristina doesn't have the 3pm appointment.

## 2.2 Code implementation and solution

This sub-section is dedicated to showcasing your own solution that you came up with for solving the above question. One has to put here any **code** that has been used for solving the above task, along with **comments** that explain every design decision made. To reference the code, please make use of the *code lines number*. Additionally, complete this sub-section with any **command configurations** that you may have used during the implementation or testing process (please fill in *just the arguments*).

#### Code:

```
% Saved by Prover9-Mace4 Version 0.5, December 2007.
   set(ignore_option_dependencies). % GUI handles dependencies
   if(Prover9). % Options for Prover9
5
     assign(max_seconds, 60).
   end_if.
   if (Mace4).
                 % Options for Mace4
9
     assign(max_seconds, 60).
10
   end_if.
11
12
   formulas(assumptions).
13
14
   differentFrom(time11,time12).
15
   differentFrom(time11,time13).
16
   differentFrom(time11,time14).
```

```
differentFrom(time11,time15).
   differentFrom(time11,time16).
19
   differentFrom(time11,time17).
20
   differentFrom(time12,time13).
22
   differentFrom(time12,time14).
23
   differentFrom(time12.time15).
24
   differentFrom(time12,time16).
   differentFrom(time12,time17).
26
   differentFrom(time13,time14).
28
   differentFrom(time13,time15).
   differentFrom(time13,time16).
30
   differentFrom(time13,time17).
31
32
   differentFrom(time14,time15).
33
   differentFrom(time14,time16).
34
   differentFrom(time14,time17).
35
36
   differentFrom(time15,time16).
37
   differentFrom(time15,time16).
38
39
   differentFrom(time16,time17).
41
   differentFrom(x,y) -> differentFrom(y,x).
43
   %sometimeBefore(x,y) - y is sometime before x
44
45
    sometimeBefore(time12,time11).
46
47
    sometimeBefore(time13,time12).
48
    sometimeBefore(time13,time11).
49
50
   sometimeBefore(time14,time12).
   sometimeBefore(time14,time11).
52
   sometimeBefore(time14,time13).
53
54
   sometimeBefore(time15,time14).
    sometimeBefore(time15,time13).
56
   sometimeBefore(time15,time12).
   sometimeBefore(time15,time11).
58
   sometimeBefore(time16,time15).
60
   sometimeBefore(time16,time14).
   sometimeBefore(time16,time13).
62
   sometimeBefore(time16,time12).
    sometimeBefore(time16,time11).
64
65
   sometimeBefore(time17,time16).
66
   sometimeBefore(time17,time15).
67
   sometimeBefore(time17,time14).
   sometimeBefore(time17,time13).
69
   sometimeBefore(time17,time12).
70
   sometimeBefore(time17,time11).
```

```
72
    -sometimeBefore(time17,time17).
73
74
    -sometimeBefore(time16,time17).
    -sometimeBefore(time16,time16).
76
    -sometimeBefore(time15,time17).
78
    -sometimeBefore(time15,time16).
    -sometimeBefore(time15,time15).
80
    -sometimeBefore(time14,time17).
82
    -sometimeBefore(time14,time16).
    -sometimeBefore(time14,time15).
84
    -sometimeBefore(time14,time14).
85
    -sometimeBefore(time13,time13).
87
    -sometimeBefore(time13,time14).
    -sometimeBefore(time13,time15).
89
    -sometimeBefore(time13,time16).
    -sometimeBefore(time13,time17).
91
92
    -sometimeBefore(time12,time12).
93
    -sometimeBefore(time12,time13).
    -sometimeBefore(time12,time14).
95
    -sometimeBefore(time12,time15).
    -sometimeBefore(time12.time16).
97
    -sometimeBefore(time12,time17).
99
    -sometimeBefore(time11,time11).
100
    -sometimeBefore(time11,time12).
101
    -sometimeBefore(time11,time13).
102
    -sometimeBefore(time11,time14).
103
    -sometimeBefore(time11,time15).
104
    -sometimeBefore(time11,time16).
    -sometimeBefore(time11,time17).
106
107
    %sometimeAfter(x,y) - y is sometime after x
108
    sometimeBefore(y,x) <-> sometimeAfter(x,y).
109
110
    %fourAfter(x,y) - y is exactly four hours after x
112
    fourAfter(time11,time15).
    fourAfter(time12,time16).
114
    fourAfter(time13,time17).
116
    -fourAfter(time11,time11).
    -fourAfter(time11,time12).
118
    -fourAfter(time11,time13).
119
    -fourAfter(time11,time14).
120
    -fourAfter(time11,time16).
121
    -fourAfter(time11,time17).
122
123
    -fourAfter(time12,time11).
124
    -fourAfter(time12,time12).
```

```
-fourAfter(time12,time13).
126
    -fourAfter(time12,time14).
127
    -fourAfter(time12,time15).
128
    -fourAfter(time12,time17).
130
    -fourAfter(time13,time11).
    -fourAfter(time13,time12).
132
    -fourAfter(time13,time13).
    -fourAfter(time13,time14).
134
    -fourAfter(time13,time15).
    -fourAfter(time13,time16).
136
137
    -fourAfter(time14,time11).
138
139
    -fourAfter(time14, time12).
    -fourAfter(time14,time13).
140
    -fourAfter(time14, time14).
141
    -fourAfter(time14,time15).
    -fourAfter(time14,time16).
143
    -fourAfter(time14,time17).
144
145
    -fourAfter(time15,time11).
    -fourAfter(time15,time12).
147
    -fourAfter(time15,time13).
    -fourAfter(time15,time14).
149
    -fourAfter(time15, time15).
    -fourAfter(time15,time16).
151
    -fourAfter(time15,time17).
153
    -fourAfter(time16,time11).
154
    -fourAfter(time16,time12).
155
    -fourAfter(time16,time13).
156
    -fourAfter(time16,time14).
157
    -fourAfter(time16,time15).
158
    -fourAfter(time16,time16).
    -fourAfter(time16,time17).
160
161
    -fourAfter(time17, time11).
162
    -fourAfter(time17,time12).
    -fourAfter(time17,time13).
164
    -fourAfter(time17,time14).
    -fourAfter(time17,time15).
166
    -fourAfter(time17, time16).
    -fourAfter(time17,time17).
168
169
    %fourBefore(x,y)(x,y) - y is exactly four hours before x
170
    fourAfter(y,x) <-> fourBefore(x,y).
172
    %oneAfter(x,y) - y is exactly one hour after x
173
174
    oneAfter(time11,time12).
175
    oneAfter(time12,time13).
    oneAfter(time13, time14).
177
    oneAfter(time14,time15).
178
    oneAfter(time15, time16).
```

```
oneAfter(time16,time17).
180
181
    -oneAfter(time11, time11).
182
    -oneAfter(time11,time14).
    -oneAfter(time11,time13).
184
    -oneAfter(time11,time15).
    -oneAfter(time11.time16).
186
    -oneAfter(time11,time17).
188
    -oneAfter(time12,time11).
    -oneAfter(time12,time12).
190
    -oneAfter(time12,time14).
191
    -oneAfter(time12,time15).
192
    -oneAfter(time12,time16).
193
    -oneAfter(time12,time17).
194
195
    -oneAfter(time13,time11).
    -oneAfter(time13,time12).
197
    -oneAfter(time13,time13).
    -oneAfter(time13,time15).
199
    -oneAfter(time13,time16).
    -oneAfter(time13,time17).
201
    -oneAfter(time14.time11).
203
    -oneAfter(time14,time12).
    -oneAfter(time14,time13).
205
    -oneAfter(time14,time14).
    -oneAfter(time14,time16).
207
    -oneAfter(time14,time17).
208
209
    -oneAfter(time15,time11).
210
    -oneAfter(time15,time12).
211
    -oneAfter(time15,time13).
212
    -oneAfter(time15,time14).
    -oneAfter(time15,time15).
214
    -oneAfter(time15,time17).
215
216
    -oneAfter(time16,time11).
    -oneAfter(time16,time12).
218
    -oneAfter(time16,time13).
    -oneAfter(time16,time14).
220
    -oneAfter(time16,time15).
    -oneAfter(time16, time16).
222
    -oneAfter(time17,time11).
224
    -oneAfter(time17,time12).
    -oneAfter(time17,time13).
226
    -oneAfter(time17,time14).
227
    -oneAfter(time17,time15).
    -oneAfter(time17,time16).
229
    -oneAfter(time17,time17).
230
231
    %the names of the costumers
232
    alison(x) \mid blanche(x) \mid cristina(x) \mid flora(x) \mid georgia(x) \mid hope(x) \mid kelly(x).
```

```
234
    %the names of the stylists
235
    opal(x) | rohnda(x) | susie(x) | tammie(x) | victoria(x) | whitney(x) | yvonne(x).
236
    %the colors
238
    brownSable(x) | deepCopper(x) | honeyBlonde(x) | jetBlack(x) | midnightBlue(x) | vivaciousRed(x) | warmM
240
    %each costumer has an appointment at a different time
    alison(x) & alison(y) -> -differentFrom(x,y).
242
    blanche(x) & blanche(y) -> -differentFrom(x,y).
    cristina(x) & cristina(y) -> -differentFrom(x,y).
244
    flora(x) & flora(y) -> -differentFrom(x,y).
    georgia(x) & georgia(y) -> -differentFrom(x,y).
    hope(x) & hope(y) \rightarrow -differentFrom(x,y).
    kelly(x) & kelly(y) \rightarrow -differentFrom(x,y).
249
    %each stylist works at a different time
    opal(x) & opal(y) -> -differentFrom(x,y).
251
    rohnda(x) & rohnda(y) -> -differentFrom(x,y).
252
    susie(x) & susie(y) -> -differentFrom(x,y).
253
    tammie(x) & tammie(y) -> -differentFrom(x,y).
    victoria(x) & victoria(y) -> -differentFrom(x,y).
255
    whitney(x) & whitney(y) -> -differentFrom(x,y).
    yvonne(x) & yvonne(y) -> -differentFrom(x,y).
257
    %each stylist works at a different time
259
    brownSable(x) & brownSable(y) -> -differentFrom(x,y).
    deepCopper(x) & deepCopper(y) -> -differentFrom(x,y).
261
    honeyBlonde(x) & honeyBlonde(y) -> -differentFrom(x,y).
262
    jetBlack(x) & jetBlack(y) -> -differentFrom(x,y).
263
    midnightBlue(x) & midnightBlue(y) -> -differentFrom(x,y).
    vivaciousRed(x) & vivaciousRed(y) -> -differentFrom(x,y).
265
    warmMocha(x) & warmMocha(y) -> -differentFrom(x,y).
266
    %Clues
268
269
    1. The costumer that chose midnight blue is sometime before Georgia
270
    sometimeBefore(x,y) <- midnightBlue(y) & georgia(x) .</pre>
272
    %2. Susie's costumer has her appointment 4 hours after Tammie's client
    fourAfter(x,y) <- tammie(x) & susie(y).</pre>
274
    %3. Whitney's costumer has her appointment 4 hours before Blanche.
276
    fourBefore(x,y) <- whitney(y) & blanche(x).</pre>
278
    %4.Yvonne's costumer has her appointment sometime after the client that chose warm Mocha.
    sometimeAfter(x,y) <- yvonne(y) & warmMocha(x) .</pre>
280
281
    %5. Yvonne's costumer, the client that chose honey blonde and Georgia are three different costumers.
282
283
    yvonne(x) & honeyBlonde(y) -> differentFrom(x,y).
    yvonne(x) & georgia(y) -> differentFrom(x,y).
285
    honeyBlonde(x) & georgia(y) -> differentFrom(x,y).
286
287
```

```
%6.0f Blanche and Rhonda's costumer one has the 4 pm appointment and the other one chose jet black.
288
    (blanche(time16) &( rohnda(x)<-> jetBlack(x)))|(rohnda(time16) &( blanche(x)<-> jetBlack(x))).
289
290
    %7. The client tat chose jet black is either Opal's or Susie's client.
    (opal(x) <-> jetBlack(x))|(susie(x) <-> jetBlack(x)).
292
    %8. Georgia isn't helped by Rhonda.
294
    georgia(x) & rohnda(y) -> differentFrom(x,y).
296
    %9. Kelly doesn't have the 11 am appointment
297
    -kelly(time11).
298
299
    %10. Of Opal's costumer and the client that chose vivacious red one has the 3pm appointment and the other
300
301
    (opal(time15)\&(vivaciousRed(x)<->flora(x)))|(vivaciousRed(time15)\&(opal(x)<->flora(x))).
303
    %11. Alison , the costumer that chose brown sable, Susie's costumer, the costumer that chose honey blone
    %the client that chose the 2pm appointment and victoria's customere are all different
305
    -alison(time14).
307
    -brownSable(time14).
    -susie(time14).
309
    -honeyBlonde(time14).
    -victoria(time14).
311
    alison(x) & brownSable(y) -> differentFrom(x,y).
313
    alison(x) & susie(y) -> differentFrom(x,y).
    alison(x) & honeyBlonde(y) -> differentFrom(x,y).
315
    alison(x) & victoria(y) -> differentFrom(x,y).
316
317
    %brownSable(x) & susie(y) -> differentFrom(x,y). - this staement is false
318
    brownSable(x) & victoria(y) -> differentFrom(x,y).
319
320
    susie(x) & honeyBlonde(y) -> differentFrom(x,y).
322
    honeyBlonde(x) & victoria(y) -> differentFrom(x,y).
323
324
    %12. The costumer that chose honey blonde has her appointment 1 hour after the client that chose vivacion
    oneAfter(x,y) <- honeyBlonde(y) & vivaciousRed(x).
326
    %13. Kelly didn't choose honey blonde.
328
    kelly(x) & honeyBlonde(y) -> differentFrom(x,y).
329
330
    %14. Alison didn't choose deep copper.
331
    alison(x) & deepCopper(y) -> differentFrom(x,y).
332
    %15. Cristina doesn't have the 3pm appointment
334
    -cristina(time15).
335
336
    end_of_list.
337
338
    formulas(goals).
339
340
    end_of_list.
341
```

#### **Explanation:**

• For solving this logic puzzle I created the following predicates:

The predicate differentFrom(x,y), expresses the idea that the time of the appointments are distinct from one another. The "differentFrom" relation is symmetrical.

The predicate sometime Before (x,y), express the fact that the appointment y is sometime before x, for each pair of appointments.

The predicate sometime After(x,y), expresses the fact that appointment y is sometime after x, for each pair of appointments.

The predicate fourAfter(x,y), expresses the fact that the appointment y is exactly 4 hours after x,for each pair of appointments.

The predicate fourBefore(x,y), express the fact that the appointment y is exactly 4 hours before x, for each pair of appointments.

The predicate oneAfter(x,y), express the fact that the appointment y is exactly one hour after x, for each pair of appointments.

The predicates alison(x), blanche(x), cristina(x), flora(x), georgia(x), hope(x), kelly(x) are used to define the names of the costumers.

The predicates opal(x), rohnda(x), susie(x), tammie(x), victoria(x), whitney(x), yvonne(x) are used to define the names of the stylists.

The predicates brownSable(x), deepCopper(x), honeyBlonde(x), jetBlack(x), midnightBlue(x), vivaciousRed(x), warmMocha(x) are used to define the color of hair dye each client chose.

We know that every hour there is a different stylist working on a different client's appointment that has chosen a different hair dye, so I stated that using the predicate differentFrom and the predicates created for each atribute of the men, whit staements like alison(x) & alison(y) -> -differentFrom(x,y). The predicate differentFrom(x,y) was also used for clues 5,8,11,13 and 14.

Clue 11 it's slightly mistaken. It states that Alison , the client that chose brown sable, Susie's costumer, the costumer that chose honey blonde, the client that has the 2pm appointment and Victoria 's costumer are all different, but the solution to the problem is that Susie dies her client's hair sable brown. If the statements of brownStable(x) are excluded the solution found by Mace4 isn't complete as it finds more possible options for the stylist Opal and none for Susie, same happens if the statements with susie(x) are excluded, so the only condition I excluded was that brownSable(x) & susie(x) -> -differentFrom(x,y) and with this condition excluded the program works properly.

#### Mace4 solution:

```
interpretation( 7, [number = 1,seconds = 0], [
       function(time11, [0]),
2
       function(time12, [1]),
3
       function(time13, [2]),
       function(time14, [3]),
       function(time15, [4]),
       function(time16, [5]),
       function(time17, [6]),
       relation(alison(_), [0,0,0,0,0,1,0]),
9
       relation(blanche(_), [0,0,0,0,1,0,0]),
10
       relation(brownSable(_), [0,0,0,0,0,0,1]),
11
       relation(cristina(_), [0,0,1,0,0,0,0]),
12
       relation(deepCopper(_), [0,0,0,1,0,0,0]),
13
       relation(flora(_), [0,1,0,0,0,0,0]),
14
       relation(georgia(_), [0,0,0,0,0,0,1]),
15
       relation(honeyBlonde(_), [0,0,1,0,0,0,0]),
16
```

```
relation(hope(_), [1,0,0,0,0,0,0]),
17
        relation(jetBlack(_), [0,0,0,0,1,0,0]),
18
        relation(kelly(_), [0,0,0,1,0,0,0]),
19
        relation(midnightBlue(_), [0,0,0,0,0,1,0]),
        relation(opal(_), [0,0,0,0,1,0,0]),
21
        relation(rohnda(_), [0,0,0,0,0,1,0]),
22
        relation(susie(_), [0,0,0,0,0,0,1]),
23
        relation(tammie(_), [0,0,1,0,0,0,0]),
        relation(victoria(_), [0,1,0,0,0,0,0]),
25
        relation(vivaciousRed(_), [0,1,0,0,0,0,0]),
        relation(warmMocha(_), [1,0,0,0,0,0,0]),
27
        relation(whitney(_), [1,0,0,0,0,0,0]),
28
        relation(yvonne(_), [0,0,0,1,0,0,0]),
29
        relation(differentFrom(_,_), [
30
            0,1,1,1,1,1,1,
31
            1,0,1,1,1,1,1,
32
            1,1,0,1,1,1,1,
            1,1,1,0,1,1,1,
34
            1,1,1,1,0,1,0,
35
            1,1,1,1,1,0,1,
36
            1,1,1,1,0,1,0]),
37
        relation(fourAfter(_,_), [
38
            0,0,0,0,1,0,0,
            0,0,0,0,0,1,0,
40
            0,0,0,0,0,0,1,
            0,0,0,0,0,0,0,
42
            0,0,0,0,0,0,0,
43
            0,0,0,0,0,0,0,
44
            0,0,0,0,0,0,0]),
45
        relation(fourBefore(_,_), [
46
            0,0,0,0,0,0,0,
47
            0,0,0,0,0,0,0,
48
            0,0,0,0,0,0,0,
49
            0,0,0,0,0,0,0,
            1,0,0,0,0,0,0,
51
            0,1,0,0,0,0,0,
52
            0,0,1,0,0,0,0]),
53
        relation(oneAfter(_,_), [
            0,1,0,0,0,0,0,
55
            0,0,1,0,0,0,0,
            0,0,0,1,0,0,0,
57
            0,0,0,0,1,0,0,
            0,0,0,0,0,1,0,
59
            0,0,0,0,0,0,1,
60
            0,0,0,0,0,0,0]),
61
        relation(sometimeAfter(_,_), [
62
            0,1,1,1,1,1,1,
63
            0,0,1,1,1,1,1,
64
            0,0,0,1,1,1,1,
            0,0,0,0,1,1,1,
66
            0,0,0,0,0,1,1,
67
            0,0,0,0,0,0,1,
68
            0,0,0,0,0,0,0]),
69
        relation(sometimeBefore(_,_), [
70
```

```
71 0,0,0,0,0,0,0,
72 1,0,0,0,0,0,
73 1,1,0,0,0,0,
74 1,1,1,0,0,0,
75 1,1,1,1,1,0,0,
76 1,1,1,1,1,1,0])]).
```

Solution:



# **Answers**

This grid will auto-populate with all the true relationships you've created on the top 7 rows on the grid. Once this table is fully populated you will be able to submit your solution.

Times	Customers	Stylists	Colors
11:00am	Hope	Whitney	warm mocha
12:00pm	Flora	Victoria	vivacious red
1:00pm	Cristina	Tammie	honey blonde
2:00pm	Kelly	Yvonne	deep copper
3:00pm	Blanche	Opal	jet black
4:00pm	Alison	Rhonda	midnight blue
5:00pm	Georgia	Susie	brown sable
	Output it		

Figure 2: The solution of the logic puzzle

## 2.3 References

https://logic.puzzlebaron.com/play.php

## 3 PROBLEM 3: Blood Donation

## 3.1 Clues of the problem

Five women are side by side donating blood. Use logic and the clues to figure out their blood types. Clues:

- 1. The A+ donor is next to the B+ donor.
- 2.Brooke is at one of the ends.
- 3. The woman wearing the Black shirt is somewhere to the left of the 150 lb woman.
- 4. The Actress is next to the Chef.
- 5. Kathleen is 40 years old.
- 6. The Florist is somewhere to the right of the woman wearing the Purple shirt.
- 7. The oldest donor weighs 130 lb.
- 8. Brooke is next to Nichole.
- 9. The 35-year-old woman is exactly to the left of the 30-year-old woman.
- 10. The 120 lb donor is somewhere between the the O- donor and the 150 lb donor, in that order.
- 11. Kathleen is at one of the ends.
- 12. The woman wearing the Purple shirt is somewhere to the right of the woman wearing the Green shirt.
- 13. The B+ donor weighs 140 lb.
- 14. The youngest woman is next to the 30-year-old woman.
- 15. The woman considered universal recipient is exactly to the left of the A+ donor.
- 16. Meghan is somewhere to the right of the woman wearing the Purple shirt.
- 17. The woman wearing the Green shirt is somewhere between the Actress and the woman wearing the Red shirt, in that order.
- 18. At one of the ends is the 130 lb woman.
- 19. The universal donor is 35 years old.
- 20. The Florist is somewhere between the Actress and the Engineer, in that order.
- 21. The woman wearing the Blue shirt is somewhere to the left of the woman wearing the Red shirt.
- 22. The AB+ donor is next to the youngest woman.

## 3.2 Code implementation and solution

This sub-section is dedicated to showcasing your own solution that you came up with for solving the above question. One has to put here any **code** that has been used for solving the above task, along with **comments** that explain every design decision made. To reference the code, please make use of the *code lines number*. Additionally, complete this sub-section with any **command configurations** that you may have used during the implementation or testing process (please fill in *just the arguments*).

### Code:

```
% Saved by Prover9-Mace4 Version 0.5, December 2007.
2
   set(ignore_option_dependencies). % GUI handles dependencies
   if(Prover9). % Options for Prover9
     assign(max_seconds, 60).
6
   end_if.
   if(Mace4).
                 % Options for Mace4
     assign(max_seconds, 60).
10
   end_if.
11
12
   formulas(assumptions).
13
14
```

```
differentFrom(donnor1,donnor2).
          differentFrom(donnor1,donnor3).
          differentFrom(donnor1, donnor4).
17
          differentFrom(donnor1,donnor5).
19
          differentFrom(donnor2,donnor3).
          differentFrom(donnor2.donnor4).
21
          differentFrom(donnor2,donnor5).
23
          differentFrom(donnor3,donnor4).
          differentFrom(donnor3,donnor5).
25
26
          differentFrom(donnor4,donnor5).
27
28
          differentFrom(x,y) -> differentFrom(y,x).
29
30
          %rightTo(x,y) - y is exactly to the right of x
31
32
          rightTo(donnor1,donnor2).
33
          rightTo(donnor2,donnor3).
34
          rightTo(donnor3,donnor4).
          rightTo(donnor4,donnor5).
36
          -rightTo(donnor1,donnor1).
38
          -rightTo(donnor1,donnor3).
          -rightTo(donnor1,donnor4).
40
          -rightTo(donnor1,donnor5).
42
          -rightTo(donnor2,donnor1).
43
          -rightTo(donnor2,donnor2).
44
          -rightTo(donnor2,donnor4).
          -rightTo(donnor2,donnor5).
46
47
          -rightTo(donnor3,donnor1).
          -rightTo(donnor3,donnor2).
49
          -rightTo(donnor3,donnor3).
50
          -rightTo(donnor3,donnor5).
51
52
          -rightTo(donnor4,donnor1).
53
          -rightTo(donnor4,donnor2).
          -rightTo(donnor4,donnor3).
55
          -rightTo(donnor4,donnor4).
57
          -rightTo(donnor5,donnor1).
          -rightTo(donnor5,donnor2).
59
          -rightTo(donnor5,donnor3).
          -rightTo(donnor5,donnor4).
61
          -rightTo(donnor5,donnor5).
62
          \label{eq:leftTo} \mbox{\ensuremath{\texttt{X}}\xspace} = \mbox{\ensuremath{\texttt{Y}}\xspace} = \mbox{\ensuremath{\texttt{
64
          rightTo(y,x) <-> leftTo(x,y).
65
66
          %nextTo(x,y) - y is to the left or to the right of x
67
          rightTo(x,y) \mid leftTo(x,y) <-> nextTo(x,y).
```

```
69
    %somewhereRight(x,y) - y is somewhere to the right of x
70
71
    somewhereRight(donnor1,donnor2).
72
    somewhereRight(donnor1,donnor3).
73
    somewhereRight(donnor1,donnor4).
    somewhereRight(donnor1,donnor5).
75
    somewhereRight(donnor2,donnor3).
77
    somewhereRight(donnor2,donnor4).
    somewhereRight(donnor2,donnor5).
80
    somewhereRight(donnor3,donnor4).
81
    somewhereRight(donnor3,donnor5).
82
    somewhereRight(donnor4,donnor5).
84
    -somewhereRight(donnor1,donnor1).
86
    -somewhereRight(donnor2,donnor1).
88
    -somewhereRight(donnor2,donnor2).
89
90
    -somewhereRight(donnor3,donnor1).
    -somewhereRight(donnor3,donnor2).
92
    -somewhereRight(donnor3,donnor3).
94
    -somewhereRight(donnor4,donnor1).
    -somewhereRight(donnor4,donnor2).
96
    -somewhereRight(donnor4,donnor3).
97
    -somewhereRight(donnor4,donnor4).
98
99
    -somewhereRight(donnor5,donnor1).
100
    -somewhereRight(donnor5,donnor2).
101
    -somewhereRight(donnor5,donnor3).
102
    -somewhereRight(donnor5,donnor4).
103
    -somewhereRight(donnor5,donnor5).
104
105
    %somewhereLeft(x,y) - y is somewhere to the left of x
106
    somewhereRight(y,x) <-> somewhereLeft(x,y).
107
    %somewhereInBetween (x,y,z) - y is somwhere in between x and z, x is to the left of y and z is to the r
109
    somewhereLeft(y,x) & somewhereRight(y,z) <-> somewhereInBetween (x,y,z).
111
    %the colors of the donnors's t-shirts
    black(x) | blue(x) | green(x) | purple(x) | red(x).
113
    %the name of the donnors
115
    andrea(x) | brooke(x) | kathleen(x) | meghan(x) | nichole(x).
116
117
    %the blood type
118
    a(x) | ab(x) | bp(x) | bn(x) | o(x).
119
120
    %the weights
121
    w120(x) | w130(x) | w140(x) | w150(x) | w160(x).
```

```
123
    %the ages
124
     twentyfivey(x) | thirtyy(x) | thirtyfivey(x) | fortyy(x) | fortyfivey(x).
125
127
    actress(x) \mid chef(x) \mid engineer(x) \mid florist(x) \mid policewoman(x).
129
    %each donnor has a different colored t-shirt
    black(x) & black(y) -> -differentFrom(x,y).
131
    blue(x) & blue(y) \rightarrow -differentFrom(x,y).
    green(x) & green(y) -> -differentFrom(x,y).
133
    red(x) \& red(y) \rightarrow -differentFrom(x,y).
134
    purple(x) & purple(y) -> -differentFrom(x,y).
135
136
    %each donnor has a different name
137
     andrea(x) & andrea(y) -> -differentFrom(x,y).
138
    brooke(x) & brooke(y) -> -differentFrom(x,y).
    kathleen(x) & kathleen(y) -> -differentFrom(x,y).
140
    meghan(x) & meghan(y) -> -differentFrom(x,y).
141
    nichole(x) & nichole(y) -> -differentFrom(x,y).
142
    %each donnor has a different blood type
144
    a(x) \& a(y) \rightarrow -differentFrom(x,y).
    ab(x) \& ab(y) \rightarrow -differentFrom(x,y).
146
    bp(x) \& bp(y) \rightarrow -differentFrom(x,y).
    bn(x) \& bn(y) \rightarrow -differentFrom(x,y).
148
    o(x) & o(y) \rightarrow -differentFrom(x,y).
150
    %each donnoor has a different weight
151
    w120(x) & w120(y) \rightarrow -differentFrom(x,y).
152
    w130(x) \& w130(y) \rightarrow -differentFrom(x,y).
153
    w140(x) \& w140(y) \rightarrow -differentFrom(x,y).
154
    w150(x) \& w150(y) \rightarrow -differentFrom(x,y).
155
    w160(x) & w160(y) \rightarrow -differentFrom(x,y).
157
    %each donnor has a different age
158
    twentyfivey(x) & twentyfivey(y) \rightarrow -differentFrom(x,y).
159
    thirtyy(x) & thirtyy(y) -> -differentFrom(x,y).
    thirtyfivey(x) & thirtyfivey(y) -> -differentFrom(x,y).
161
    fortyy(x) & fortyy(y) -> -differentFrom(x,y).
    fortyfivey(x) & fortyfivey(y) \rightarrow -differentFrom(x,y).
163
    %each donnor has a different job
165
    actress(x) & actress(y) -> -differentFrom(x,y).
    chef(x) & chef(y) -> -differentFrom(x,y).
167
    engineer(x) & engineer(y) -> -differentFrom(x,y).
    florist(x) & florist(y) -> -differentFrom(x,y).
169
    policewoman(x) & policewoman(y) -> -differentFrom(x,y).
170
171
    %Clues
172
173
    %1. The A+ donor is next to the B+ donor.
174
    nextTo(x,y) \leftarrow a(x) \& bp(y).
175
```

176

```
%2.Brooke is at one of the ends.
    brooke(donnor1) | brooke(donnor5).
179
    %3. The woman wearing the Black shirt is somewhere to the left of the 150 lb woman.
    somewhereLeft(x,y) <- black(y) & w150(x).
181
    %4. The Actress is next to the Chef.
183
    nextTo(x,y) \leftarrow actress(y) & chef(x).
185
    %5. Kathleen is 40 years old.
186
    kathleen(x) <-> fortyy(x).
187
188
    %6. The Florist is somewhere to the right of the woman wearing the Purple shirt.
189
    somewhereRight(x,y) <- florist(y) & purple(x) .</pre>
190
    %7. The oldest donor weighs 130 lb.
192
    fortyfivey(x) <-> w130(x).
194
    %8. Brooke is next to Nichole.
195
    nextTo(x,y) <- brooke(x) & nichole(y) .</pre>
196
197
    %9. The 35-year-old woman is exactly to the left of the 30-year-old woman.
198
    leftTo(x,y) \leftarrow thirtyfivey(y) & thirtyy(x).
200
    %10. The 120 lb donor is somewhere between the the O-donor and the 150 lb donor, in that order.
    somewhereInBetween(x,y,z) \leftarrow o(x)& w120(y) & w150(z).
202
    %11. Kathleen is at one of the ends.
204
    kathleen(donnor1)|kathleen(donnor5).
205
206
    12. The woman wearing the Purple shirt is somewhere to the right of the woman wearing the Green shirt.
207
    somewhereRight(x,y) <- purple(y) & green(x) .</pre>
208
209
    %13. The B+ donor weighs 140 lb.
    bp(x) <-> w140(x).
211
212
    %14. The youngest woman is next to the 30-year-old woman.
213
    nextTo(x,y) <- twentyfivey(x) & thirtyy(y) .</pre>
215
    %15. The woman considered universal recipient is exactly to the left of the A+ donor.
    leftTo(x,y) \leftarrow a(x) \& ab(y).
217
    %16. Meghan is somewhere to the right of the woman wearing the Purple shirt.
219
    somewhereRight(x,y) <- meghan(y) & purple(x) .</pre>
221
    %17. The woman wearing the Green shirt is somewhere between the Actress and the woman wearing the Red sl
222
    somewhereInBetween(x,y,z) \leftarrow actress(x) \& green(y) \& red(z).
223
224
    %18. At one of the ends is the 130 lb woman.
    w130(donnor1) | w130(donnor5).
226
227
    %19. The universal donor is 35 years old.
228
    o(x) \iff thirtyfivey(x).
229
```

230

```
%20. The Florist is somewhere between the Actress and the Engineer, in that order.
231
    somewhereInBetween(x,y,z) <-</pre>
                                       actress(x)& florist(y) & engineer(z) .
232
233
    %21. The woman wearing the Blue shirt is somewhere to the left of the woman wearing the Red shirt.
    somewhereLeft(x,y) <- blue(y) & red(x) .</pre>
235
236
    %22. The AB+ donor is next to the youngest woman.
237
    nextTo(x,y) \leftarrow ab(x) \& twentyfivey(y).
238
239
    end_of_list.
240
241
    formulas(goals).
242
243
    end_of_list.
244
```

#### **Explanation:**

• For solving this logic puzzle I created the following predicates:

The predicate differentFrom(x,y), express the idea that the donors are distinct from one another. The "differentFrom" relation is symmetrical.

The predicate rightTo(x,y), express the fact that the y is exactly to the right of x, for every pair of donors.

The predicate leftTo(x,y), express the fact that the y is exactly to the left of x, for every pair of donors. The predicate leftTo(x,y), express the fact that the x is eighter to the left of y or to the right, this predicate was created using the rightTo and leftTo predicates.

The predicate somewhere Right(x,y), express the fact that the y is somewhere to the right of x for every pair of donors.

The predicate somewhere Left(x,y), express the fact that the y is somewhere to the right of x for every pair of donors.

The predicate somewhere InBetween(x,y,z), express the fact that the y is somewhere in between x and z, x being somewhere to the left of y and z somewhere to the right of y. The predicates black(x), blue(x), green(x), purple(x), red(x) are used to define the colors of the donors 's t-shirts.

The predicates  $\operatorname{andrea}(x)$ ,  $\operatorname{brooke}(x)$ ,  $\operatorname{kathleen}(x)$ ,  $\operatorname{meghan}(x)$ ,  $\operatorname{nichole}(x)$  used to define the names of the donors.

The predicates a(x), ab(x), bp(x), bn(x), o(x) are used to define the blood types of the donors.

The predicates w120(x), w130(x), w140(x), w150(x), w160(x) are used to define the weight of each donor.

The predicates twenty fivey(x), thirtyfivey(x), fortyfivey(x), fortyfivey(x) are used to define the age of each donor.

The predicates actress(x), chef(x), engineer(x), florist(x), policewoman(x) are used to define the job of each donor.

We know that each donor has a different colored t-shirt, a different name, has a different blood type, a different weight, has a different age and has a different job , so I stated that using the predicate different From and the predicates created for each atribute of the men, with staements like black (x) & black(y) -> -different From(x,y).

#### Mace4 solution:

```
interpretation( 5, [number = 1,seconds = 1], [
   function(donnor1, [0]),
   function(donnor2, [1]),
   function(donnor3, [2]),
   function(donnor4, [3]),
   function(donnor5, [4]),
   relation(a(_), [0,0,0,1,0]),
```

```
relation(ab(_), [0,0,1,0,0]),
8
        relation(actress(_), [1,0,0,0,0]),
9
        relation(andrea(_), [0,0,1,0,0]),
10
        relation(black(_), [1,0,0,0,0]),
        relation(blue(_), [0,0,0,1,0]),
12
        relation(bn(_), [1,0,0,0,0]),
        relation(bp(_), [0,0,0,0,1]),
14
        relation(brooke(_), [1,0,0,0,0]),
        relation(chef(_), [0,1,0,0,0]),
16
        relation(engineer(_), [0,0,0,0,1]),
        relation(florist(_), [0,0,0,1,0]),
18
        relation(fortyfivey(_), [1,0,0,0,0]),
19
        relation(fortyy(_), [0,0,0,0,1]),
20
21
        relation(green(_), [0,1,0,0,0]),
        relation(kathleen(_), [0,0,0,0,1]),
22
        relation(meghan(_), [0,0,0,1,0]),
23
        relation(nichole(_), [0,1,0,0,0]),
24
        relation(o(_), [0,1,0,0,0]),
25
        relation(policewoman(_), [0,0,1,0,0]),
26
        relation(purple(_), [0,0,1,0,0]),
27
        relation(red(_), [0,0,0,0,1]),
28
        relation(thirtyfivey(_), [0,1,0,0,0]),
29
        relation(thirtyy(_), [0,0,1,0,0]),
        relation(twentyfivey(_), [0,0,0,1,0]),
31
        relation(w120(_), [0,0,1,0,0]),
        relation(w130(_), [1,0,0,0,0]),
33
        relation(w140(_), [0,0,0,0,1]),
        relation(w150(_), [0,0,0,1,0]),
35
        relation(w160(_), [0,1,0,0,0]),
36
        relation(differentFrom(_,_), [
37
            0,1,1,1,1,
38
            1,0,1,1,1,
39
            1,1,0,1,1,
40
            1,1,1,0,1,
            1,1,1,1,0]),
42
        relation(leftTo(_,_), [
43
            0,0,0,0,0,
44
            1,0,0,0,0,
            0,1,0,0,0,
46
            0,0,1,0,0,
            0,0,0,1,0]),
48
        relation(nextTo(_,_), [
49
            0,1,0,0,0,
50
            1,0,1,0,0,
51
            0,1,0,1,0,
52
            0,0,1,0,1,
53
            0,0,0,1,0]),
54
        relation(rightTo(_,_), [
55
            0,1,0,0,0,
            0,0,1,0,0,
57
            0,0,0,1,0,
            0,0,0,0,1,
59
            0,0,0,0,0]),
60
        relation(somewhereLeft(_,_), [
61
```

```
0,0,0,0,0,
62
        1,0,0,0,0,
63
        1,1,0,0,0,
64
        1,1,1,0,0,
        1,1,1,1,0]),
66
     relation(somewhereRight(_,_), [
67
       0,1,1,1,1,
68
       0,0,1,1,1,
69
       0,0,0,1,1,
70
        0,0,0,0,1,
71
       0,0,0,0,0]),
72
     73
```

## Solution:

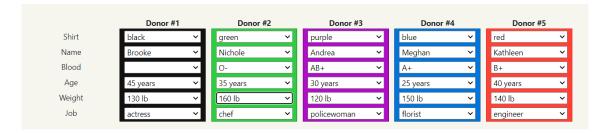


Figure 3: The solution of the logic puzzle

## 3.3 References

https://www.brainzilla.com/logic/zebra/blood-donation/