

Chapter 1

Axioms

1. $\mathbb{C} \supset \mathbb{R}$

The set of complex numbrs are a proper superset of all real numbers.

2. $\forall s \in \mathbb{C} (s = a + ib \wedge i = \sqrt{-1} \wedge a \in \mathbb{R} \wedge b \in \mathbb{R})$

It is true that for all numbers s in the set \mathbb{C} that $i = \sqrt{-1}$ and that a is a real number and that b is a real number.

3. $\forall s \in \mathbb{C} (\text{Re}(s) = a \wedge \text{Im}(s) = b)$

The function Re applied to any complex number s will return the real part a , and the function Im will return the imaginary part b .

4. $ib \in s \perp a \in s$

All values b exists in a dimension perpendicular to \mathbb{R} . All values in \mathbb{C} exists in a plane, where one axis is the real coordinate and the imaginary component of s is regarded as occupying another coordinate axis in a cartesian coordinate system.

5. $\exists s \in \mathbb{C} (s = 0 \wedge s = 0 + 0i)$

There exists an elemment s in \mathbb{C} such that s is null and the meaning of this is that $a = 0$ and $b = 0$. This is called the null element.

6. $\exists s \in \mathbb{C} (s = 1 \wedge s = 1 + 0i)$

There exists an element s in \mathbb{C} such that s is 1 and the meaning of this is that $a = 1$ and $b = 0$. This is