



## Homework assignment No. 06

Due October 11, 2018

Before beginning the assignment, use `git pull` to get the latest version of our Inviwo repository. Run CMake and compile once more. The files `topology.h/cpp` and `integrator.h/cpp` contain additional comments and instructions.

### Task 6.1: Topology of 2D Vector Fields

15 P

Load a 2D vector field and visualize its topological skeleton, i.e., its critical points and separatrices. You can use the workspace `topology.inv`. The assignment comes with several data sets for testing. See Figure 1 for examples. In particular, implement the following features:

- (a) Extraction of the critical points. This means to find the location of all critical points in the data set. Show them as thick points.  
*Hint: The VolumeRAM contains the data points. To find critical points, you can use the domain decomposition & change-of-sign test from the lecture.* (10 P)
- (b) Classification of the critical points. This means to determine the type of each critical point. The colors are given in the `ColorsCP` array, you can access them by the corresponding `TypeCP` enum value.  
*Hint: The Interpolator class has a function `sampleJacobian()` to compute the Jacobian at a given location. In `util/gradient.h` you find the function `eigenAnalysis()` to compute eigenvalues and eigenvectors.* (3 P)
- (c) Compute the separatrices. This means to integrate four stream lines from each saddle into the direction of the eigenvectors. Show them as lines in Inviwo. (2 P)

### Task 6.2: Analytical Fields

5 P

Load the `topology_analytical.inv` workspace. You can fill in a formula that is then sampled on a grid/volume.

- (a) Create a vector field formula that has a center at position  $(5, -3)$ . (1 P)
- (b) Make up a vector field formula that has a saddle at position  $(-2, 7)$ . (1 P)
- (c) Make up a vector field formula that has both the center from a) and the saddle from b). (1 P)
- (d) Visualize the scalar field topology of the field  $\sin(x) + \cos(y)$  in the range  $[-10, 10] \times [-10, 10]$ . (2 P)

### Task 6.3: (Extra Task) Additional structures

3 Extra Points

Another structure of vector field topology that was discussed in the lecture are *boundary switch points*. Find boundary switch points as seeds, integrate their separatrices and add them to the image.

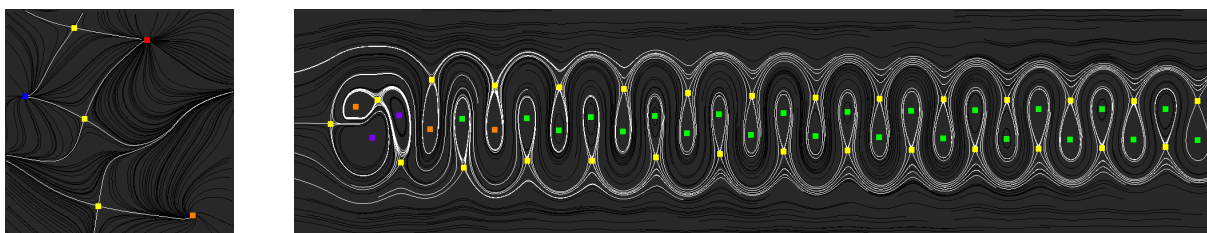


Figure 1: Topological skeletons of different data sets. The noise data set is a good reference. The distinction between foci and centers is dependent on a threshold, so your implementation might create slightly different classifications for the cylinder data sets.