

International Reserve Management under Rollover Crises

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The views expressed herein are those of the authors and not necessarily those of the Federal Reserve Bank of Minneapolis or the Federal Reserve System.

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To reduce the vulnerability to a debt crisis:

- Should the government reduce the debt or increase reserves?

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Answer unclear:

- Reserves provide liquidity
... but reducing debt may lower vulnerability more

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 - Sunspot shocks, deterministic income
- How should the government exit the 'crisis zone'?

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- If heavily indebted, optimal to initially reduce debt and keep zero reserves
- Once debt is reduced sufficiently, optimal to increase debt and accumulate reserves

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- Borrowing to accumulate reserves can reduce spreads

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 - **Borrowing to accumulate reserves helps exiting the crisis zone**
- **Hernandez (2019)**: numerical simulations w/ fundamental and sunspot shocks

Cole-Kehoe (2001); Corsetti-Dedola (2016); Aguiar-Amador (2020); Bianchi-Mondragon (2022); Bianchi and Sosa-Padilla (2023); Corsetti-Maeng (2023ab)

Model

Environment

- Discrete time, infinite horizon. Constant endowment: $y_t = y$
- Government trades two assets ...
 - short-term risk-free reserves, a
 - long-term defaultable debt, b
a bond issued in t promises to pay

$$\kappa [1, (1 - \delta), (1 - \delta)^2, \dots]$$

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- Risk-neutral deep pocket international investors:
 - Discount future flows at rate r , assume $\beta(1 + r) = 1$
- Markov equilibrium w/ Cole-Kehoe (2000) timing:
 - Borrowing at the beginning of the period
 - Settlement (repay/default) at the end

Preferences and resource constraint

- Preferences:

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - \phi d_t]$$

where $d_t = 0$ (1) denotes repayment (default)

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- If the government repays:

$$c_t = \underbrace{y + a_t - \kappa b_t}_{\text{resources avail.}} - \underbrace{\frac{a_{t+1}}{1+r}}_{\text{reserve purchases}} + \underbrace{q_t [b_{t+1} - (1-\delta)b_t]}_{\text{debt issuance}}$$

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- If the government defaults:

$$c_t = y + \textcolor{red}{a}_t - \frac{\textcolor{red}{a}_{t+1}}{1+r} \quad \text{Gov. saves on bond payments}$$

and faces permanent exclusion and utility loss ϕ

Recursive Government Problem

- State is $s \equiv (a, b, \zeta)$

ζ denotes an iid sunspot that coordinates the lenders

- The government chooses to repay or default

$$V(\textcolor{red}{a}, b, \zeta) = \max \{ V_R(\textcolor{red}{a}, b, \zeta), V_D(\textcolor{red}{a}) \}$$

If indifferent, assume repay

Value of Default

$$V_D(a) = \max_{a' \geq 0} \{u(c) - \phi + \beta V_D(a')\}$$

subject to

$$c \leq y + a - \frac{a'}{1+r}$$

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subject to

$$c \leq y + a - \frac{a'}{1+r}$$

- Given $\beta(1+r) = 1$, we have constant consumption

$$V_D(a) = \frac{u(y + (1-\beta)a) - \phi}{1-\beta}$$

Value of Repayment

Two cases, depending on whether the investors want to rollover the debt

If investors **want** to rollover:

$$V_R^+(a, b) = \max_{a' \geq 0, b'} \{u(c) + \beta \mathbb{E} V(a', b', s')\}$$

subject to

$$c = y + a - \frac{a'}{1+r} - \kappa b + q(a', b') (b' - (1-\delta)b)$$

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Bond price depends on the portfolio and reflects default prob:

$$q(a', b') = \frac{1}{1+r} \mathbb{E} [(1-d(s')) (\kappa + (1-\delta)q(a'', b'', s'))]$$

Value of Repayment

Two cases, depending on whether the investors want to rollover the debt

If investors **don't want** to rollover:

$$V_R^-(a, b) = \max_{a' \geq 0} \{ u(c) + \beta \mathbb{E} V(a', (1 - \delta)b, s') \}$$

subject to

$$c = y + a - \frac{a'}{1 + r} - \kappa b + q(a', b') (b' - (1 - \delta)b) \rightarrow 0$$

To pay debt, need to use reserves or cut consumption

Multiplicity of Equilibria

- Coordination failure may lead to self-fulfilling crises (Cole-Kehoe)

- If lenders expect...
 - ... repayment, then they rollover, and the govt repays
 - ... default, then they don't rollover, and the govt defaults

Characterization

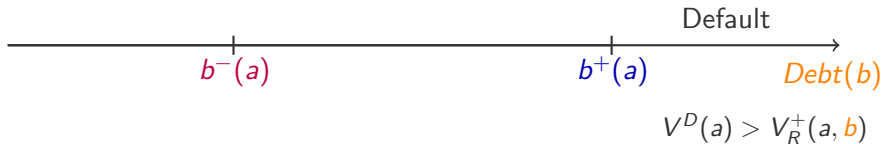
Default thresholds

For a given level of reserves, two thresholds



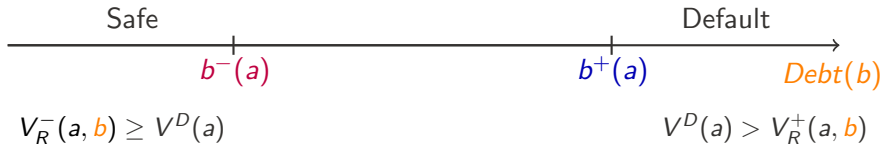
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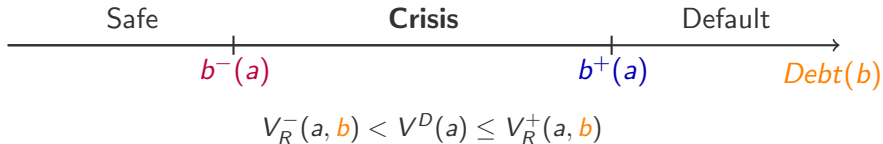
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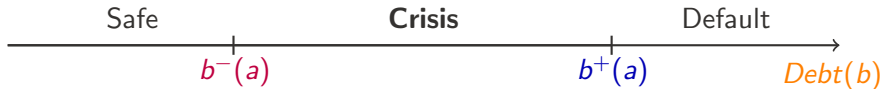
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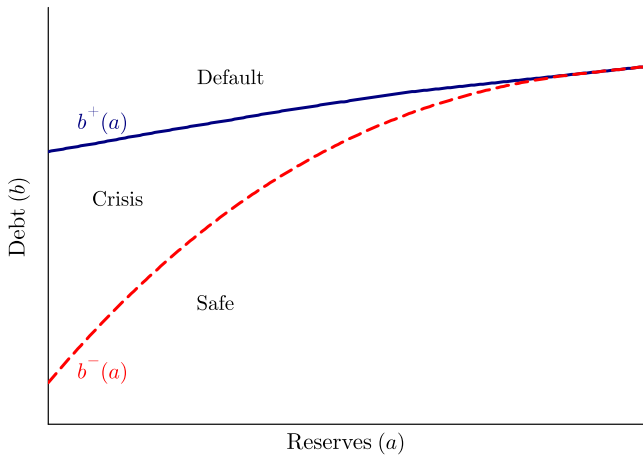
Default thresholds

For a given level of reserves, two thresholds



Sunspot: assume government faces a run w/ prob π when initial portfolio (a, b) is in the crisis zone

The Three Zones



Given debt: higher reserves lower vulnerability

Escaping the Crisis Zone

How to Exit the Crisis Zone?

Remaining in the crisis zone is risky:

- in case of a run, the gov't defaults

But exiting is also costly:

- requires cutting consumption and improving NFA

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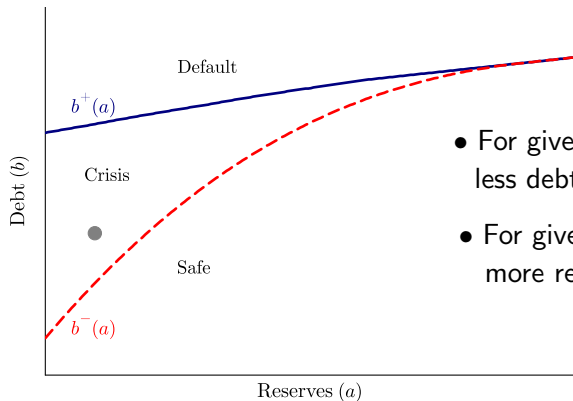
But exiting is also costly:

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What's the best exit strategy for a country that is in the crisis zone (but didn't face a run today) ?

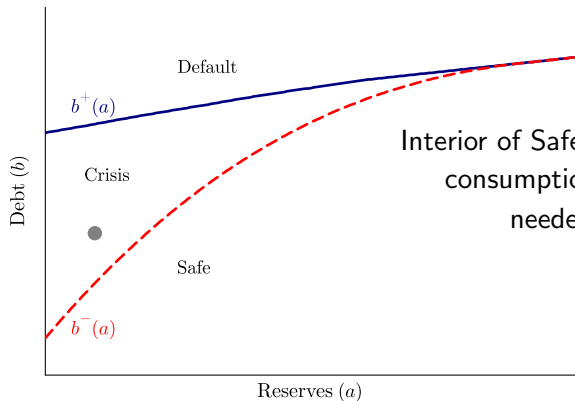
- Accumulate reserves ($a \uparrow$) or reduce debt ($b \downarrow$)?

Possible Exit Paths



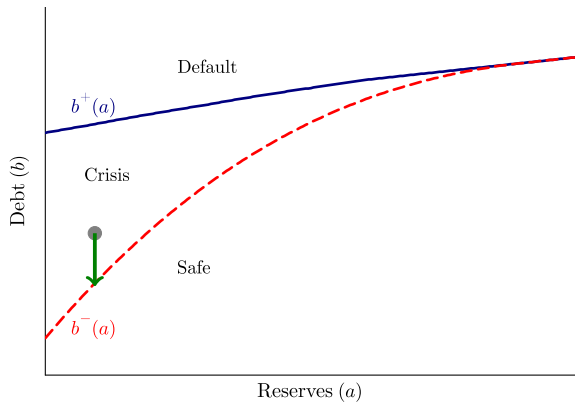
- For given reserves level:
less debt lowers vulnerability
- For given debt level:
more reserves lower vulnerability

Possible Exit Paths

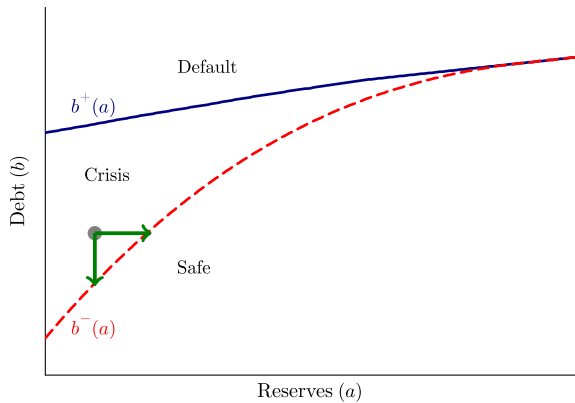


Interior of Safe zone isn't optimal:
consumption cut larger than
needed to be safe

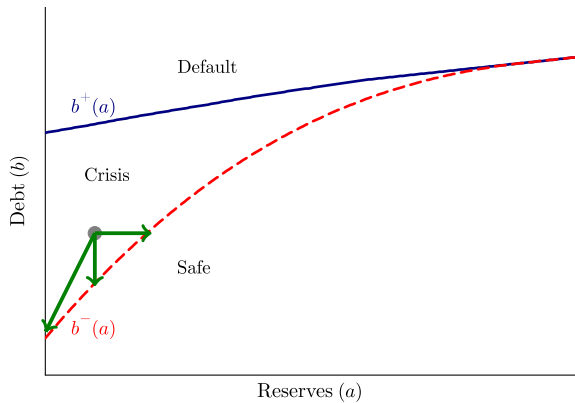
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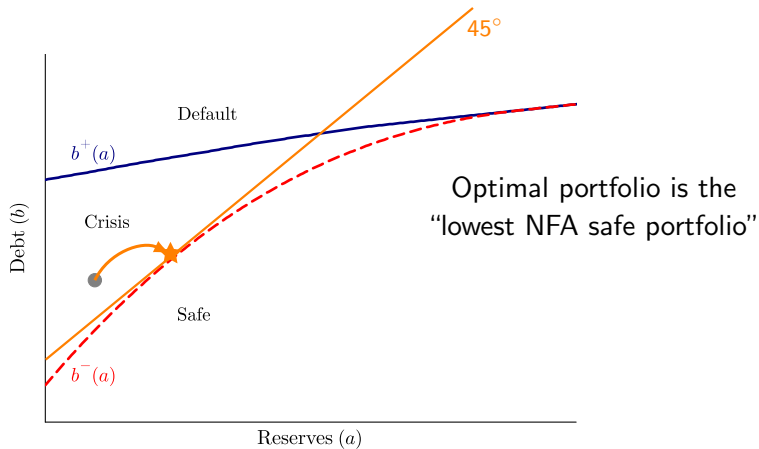
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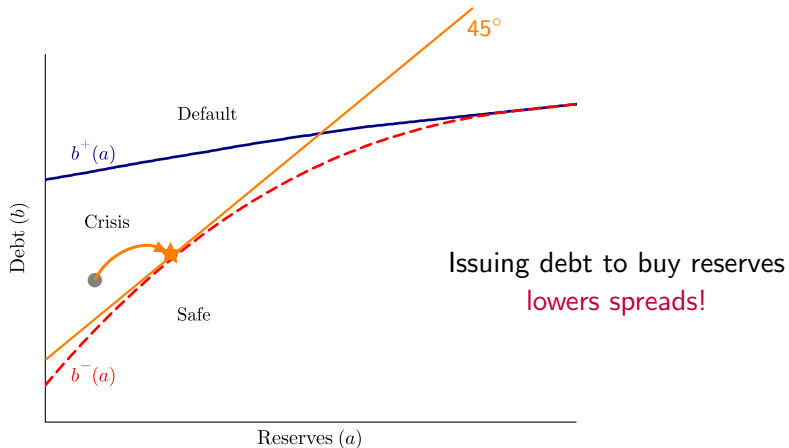
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Why do reserves help exit the crisis zone?

Getting to the safe zone requires $V_R^-(a, b) \geq V_D(a)$

- More reserves help sustain higher gross debt & net debt
... even though reserves increase default value $V_D(a)$.

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Intuition:

- Only a fraction κ of debt is due every period
- Reserves are liquid and can be used in a run:

$$c = y + \underbrace{a - \kappa b}_{\text{more resources}} - \frac{a'}{1+r}$$

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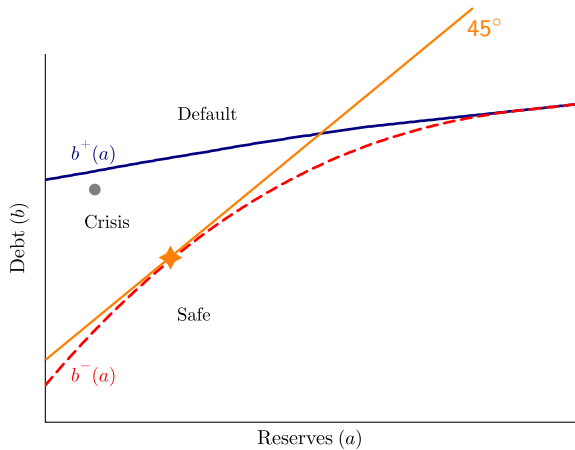
- Reserves also make default more attractive, but have lower marginal value:

$$c_D = y + a - \frac{a'}{1+r}$$

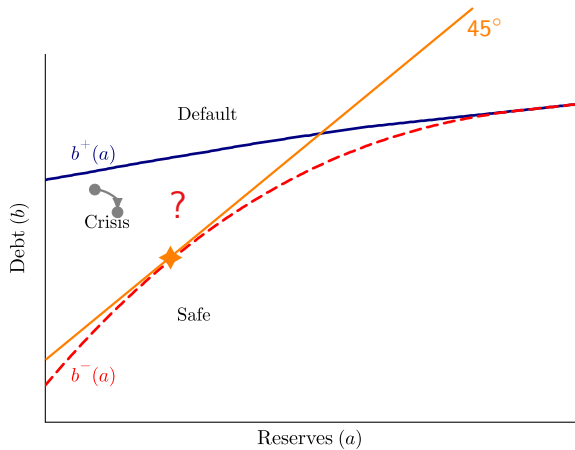
Deep in the Crisis Zone

Country has **higher** initial debt level: what to do?

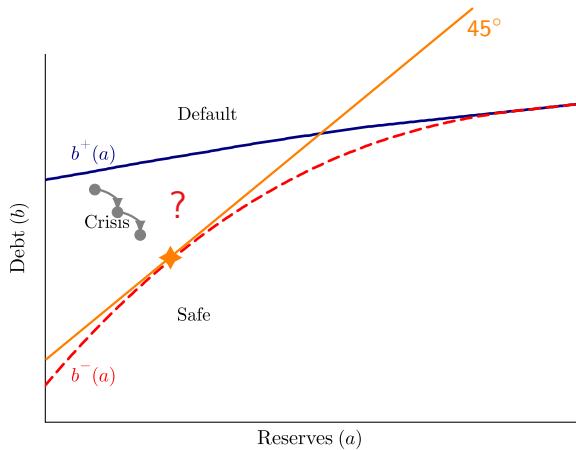
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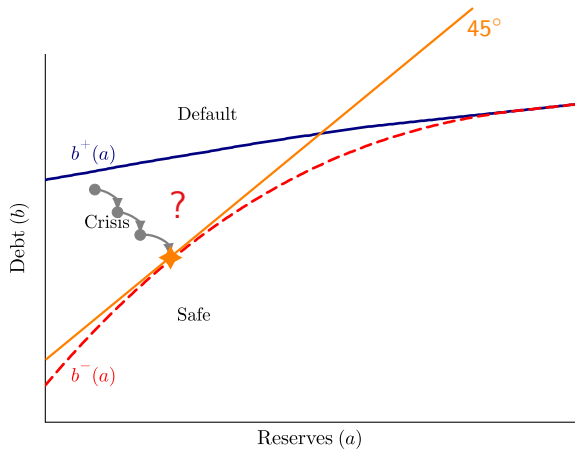
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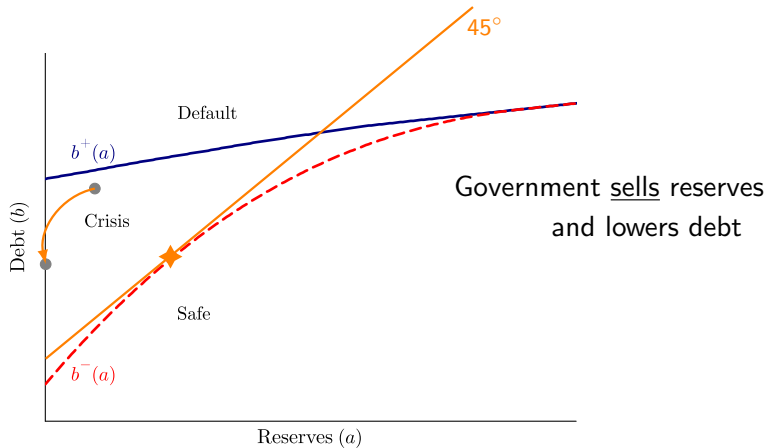
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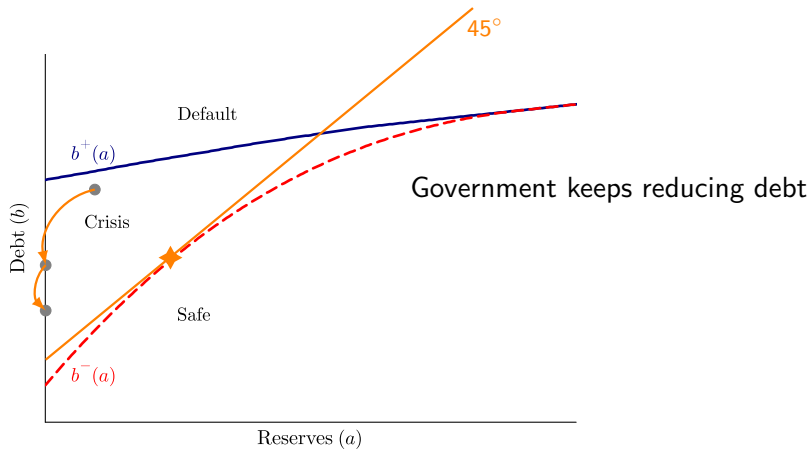
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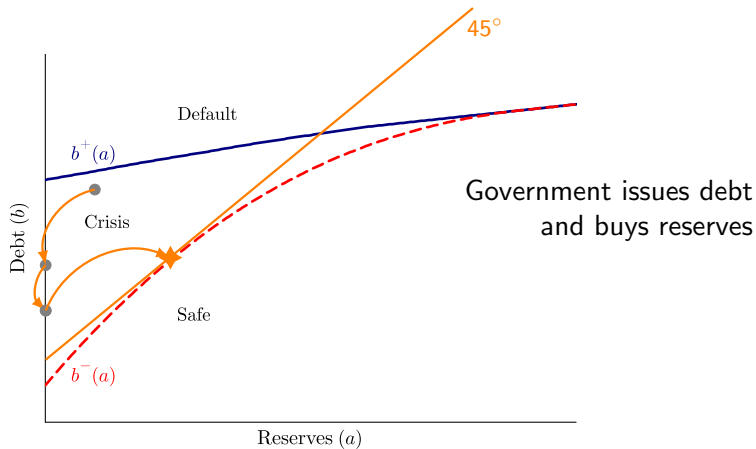
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Deep in the Crisis Zone



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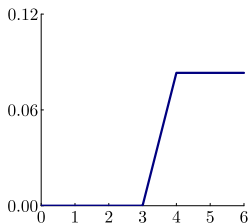
Why selling reserves (initially)?

- When the government is 'deep' in the Crisis Zone, on the margin reserves do not change the probability of a run
- Using the reserves to lower debt allows the govt to save on interest payments and helps deleveraging

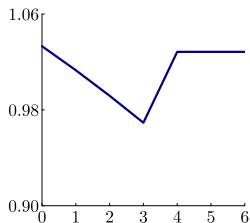
Deleveraging Dynamics

[▶ More](#)

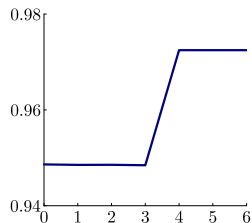
Reserves, a



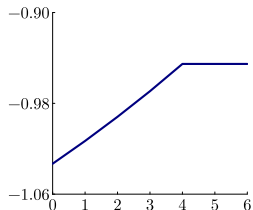
Debt, b



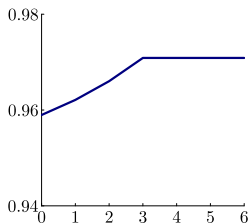
Consumption



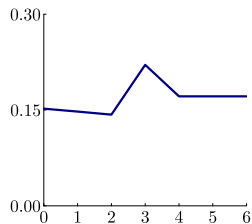
Net Foreign Assets



Debt Price, $q(a', b', s)$



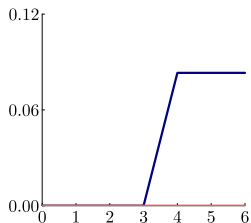
Issuance, $b' - (1 - \delta)b$



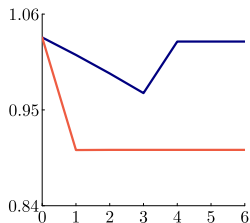
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► More

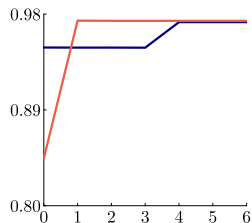
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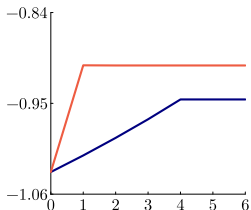
Debt, b



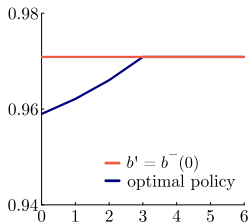
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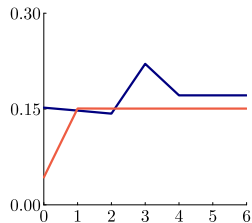
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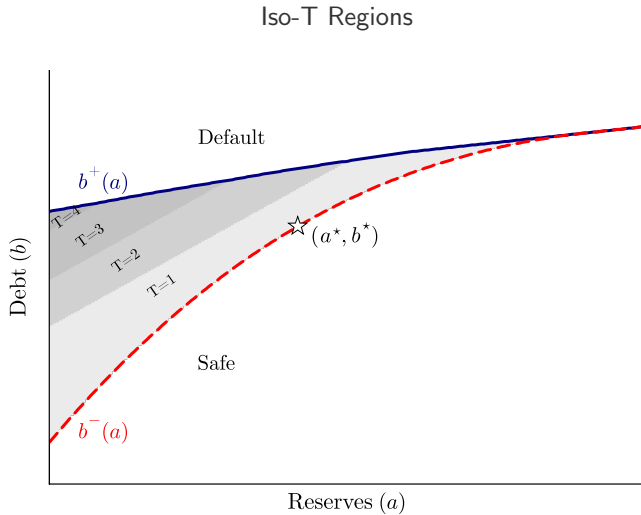
Debt Price, $q(a', b', s)$



Issuance, $b' - (1 - \delta)b$



How many periods until exit?



Formalizing the Results

Formalizing the Results: (a^*, b^*) portfolio

(a^*, b^*) is a focal point – we call it **Lowest-NFA safe portfolio**

When do we have $a^* > 0$?

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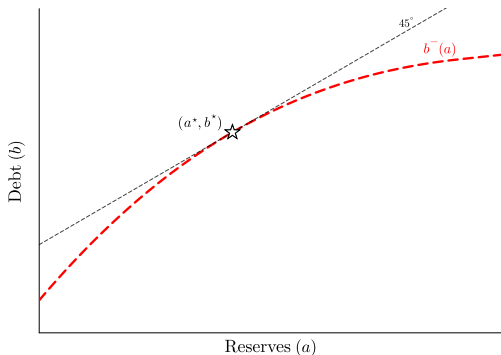
Answer: when $\left. \frac{\partial b^-(a)}{\partial a} \right|_{a=0} > 1$

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Proposition 3 (Positive reserves)

Suppose that the boundary of the crisis region at zero reserves $b^-(0)$ satisfies

$$\beta(1-\delta) [u'(y - \kappa b^-(0)) - u'(y - (1-\beta)(1-\delta)b^-(0))] > u'(y)$$

Then, the lowest-NFA safe portfolio has strictly positive reserves, $a^* > 0$

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1. low curvature in $u(c)$,

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1. low curvature in $u(c)$,
2. one-period debt ($\delta = 1$) [**Prop. 4**]

► figure

► sensitivity

Formalizing the Results: Optimal portfolio

To exit crisis zone, first deleverage, then raise debt and reserves

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Proposition 5 (Optimal portfolio)

Consider an initial portfolio $(a, b) \in \mathbf{C}$. The optimal portfolio satisfies:

- If (a, b) is such that $a - b < a^* - b^*$ and $(a', b') \in \mathbf{S}$. Then we have $T = 1$ and $a' = a^*, b' = b^*$
- If (a, b) is such that $a - b \geq a^* - b^*$. Then, we have $T = 1$ and any portfolio $(a', b') \in \mathbf{S}$ and $a - b = a' - b'$ is optimal.
If $a = 0, b = b^* - a^*$, then $a' = a^*, b = b^*$.
- If (a, b) is such that $(a', b') \in \mathbf{C}$. Then, the optimal solution features $a' = 0$.

Connecting with the data

Theory predicts that borrowing to accum. reserves lowers spreads

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$$\Delta \log(\text{Spread})_{it} = \Delta \text{Reserves}_{it} + \Delta \text{Debt}_{it} + \text{Controls}_{it} + \varepsilon_{it}$$

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	Full Sample
Δ Reserves	-2.14*** (0.74)
Δ Debt	0.46* (0.24)
Num.Obs.	4,468
R2 Adj.	0.352

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Theory also predicts **stronger** effect for low Debt or high NFA

Connecting with the data

Stronger effect in **low debt** periods ...

	Full Sample	Low Debt	High Debt
Δ Reserves	-2.14*** (0.74)	-3.72* (1.73)	-1.23*** (0.46)
Δ Debt	0.46* (0.24)	1.24*** (0.32)	0.19 (0.28)
Num.Obs.	4,468	2,559	1,909
R2 Adj.	0.352	0.424	0.263

All specs. include year dummies and additional macro controls (as in Sosa-Padilla and Sturzenegger, 2023).

Robust standard errors in parentheses. * $p < 0.1$; ** $p < 0.05$; *** $p < 0.01$.

... also stronger effect in **high NFA** periods

	Full Sample	Low NFA	High NFA
Δ Reserves	-2.14*** (0.74)	-1.32*** (0.51)	-3.27** (1.56)
Δ Debt	0.46* (0.24)	0.34 (0.25)	1.19** (0.49)
Num.Obs.	4,468	2, 226	2,242
R2 Adj.	0.352	0. 282	0.416

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Conclusions

- Simple theory of optimal res. management w/ rollover crises
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- Optimal to accumulate reserves to reduce vulnerability
 - However, only after debt has been reduced towards safety
- Reserves as 'buffer': after buildup, no use of reserves in eqm.
 - Not using them doesn't mean they're unnecessary

Conclusions

- Simple theory of optimal res. management w/ rollover crises
- Optimal to accumulate reserves to reduce vulnerability
 - However, only after debt has been reduced towards safety
- Reserves as 'buffer': after buildup, no use of reserves in eqm.
 - Not using them doesn't mean they're unnecessary
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Conclusions

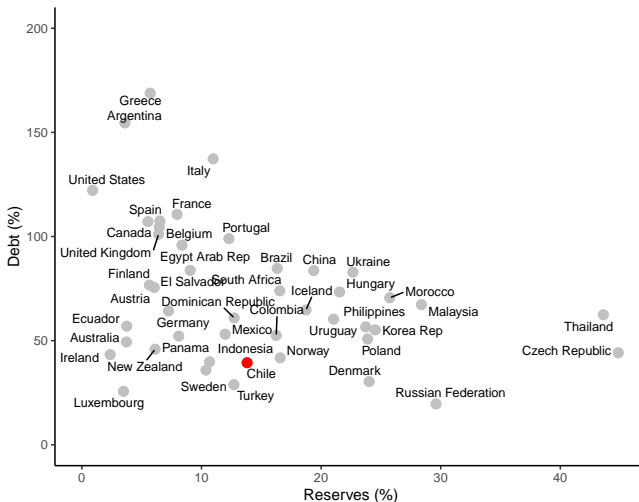
- Simple theory of optimal res. management w/ rollover crises
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- Issuing debt to accumulate reserves can reduce spreads
- Findings speak to policy discussions on appropriate level of FX reserves (e.g. IMF)
 - Following a debt crisis, IMF often prescribes increasing reserves
 - However, we find holding reserves not optimal at beginning of deleveraging process



Scan to find the paper!

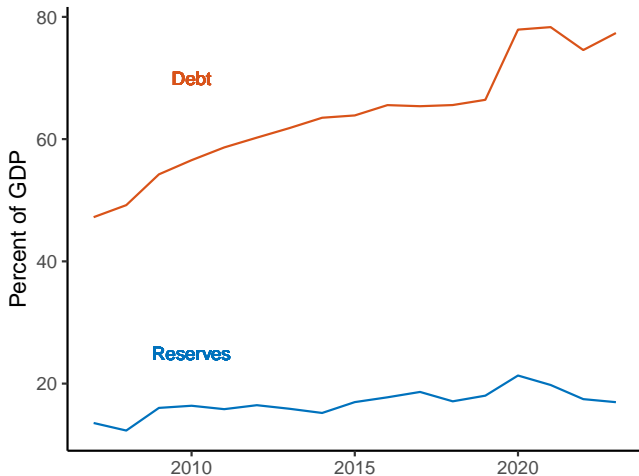
THANKS!

Data: Government Debt and International Reserves

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Government debt and reserves (as % of GDP), 2023

Evolution of Debt and Reserves

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Avg. Government debt and reserves (as % of GDP)

- If $(a, b) \in \mathbf{S}$: we assume gov. stays in safe zone

$$V^S(a - b) = \frac{u(y + (1 - \beta)(a - b))}{1 - \beta}$$

- **Note:** relevant state variable is the NFA, $a - b$

For a high enough δ : can establish that gov. finds it optimal to stay in \mathbf{S}

- If $(a, b) \in \mathbf{C}$, govt. seeks to exit in finite time (may default along the way if bad sunspot hits)
 - Staying in the crisis zone implies eventually costly default
 - Speed of exit depends on curvature of $u(\cdot)$ and probability of bad sunspot

Continuation value:

$$\mathbb{E}V(a', b', \zeta') = \begin{cases} V^S(a' - b') & \text{if } (a', b') \in \mathbf{S} \\ (1 - \lambda)V_R^+(a', b') + \lambda V_D(a') & \text{if } (a', b') \in \mathbf{C} \\ V_D(a') & \text{if } (a', b') \in \mathbf{D} \end{cases}$$

Characterization: Fundamental Bond Price

We have that for any $T > 0$ the bond price is given by

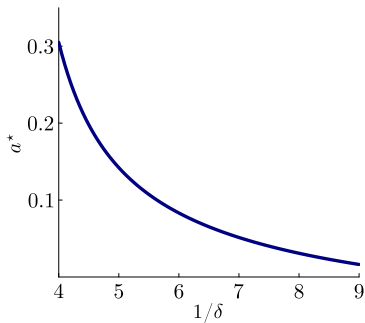
$$q(a', b') = \frac{\delta + r}{1 + r} \sum_{t=1}^{T-1} \left(\frac{1 - \lambda}{1 + r} \right)^t (1 - \delta)^{t-1} + \left[\frac{(1 - \lambda)(1 - \delta)}{1 + r} \right]^{T-1} \frac{1}{1 + r}$$

- First term: bond coupon payments investors expect to receive
- Second term: risk-free price of the bond once the government exits the crisis zone

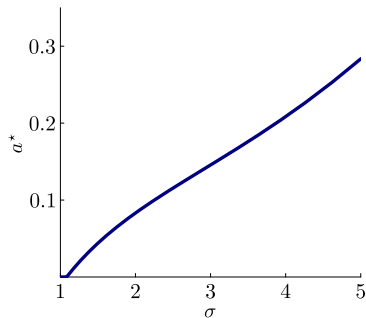
Sensitivity: effect of maturity and risk-aversion on a^*

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Maturity



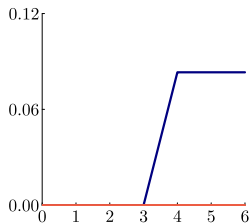
Risk aversion



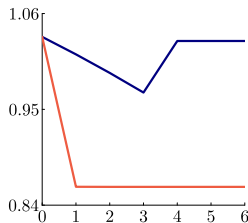
Deleveraging Dynamics: $b' = (1 - \delta)b_0$

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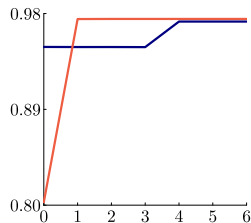
Reserves, a



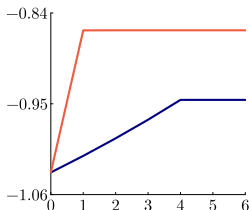
Debt, b



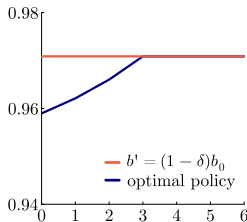
Consumption



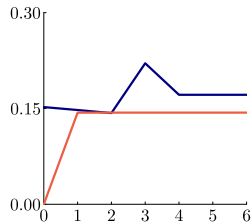
Net Foreign Assets



Debt Price, $q(a', b', s)$

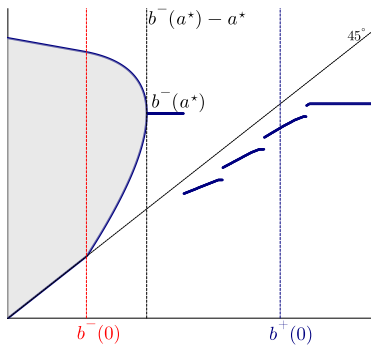


Issuance, $b' - (1 - \delta)b$

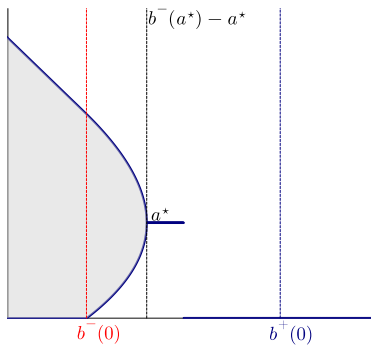


— $b' = (1 - \delta)b_0$
— optimal policy

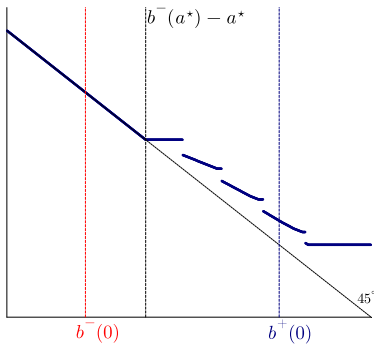
Debt, b'



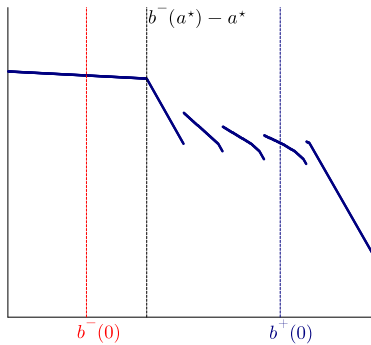
Reserves, a'



Net Foreign Assets, $a' - b'$

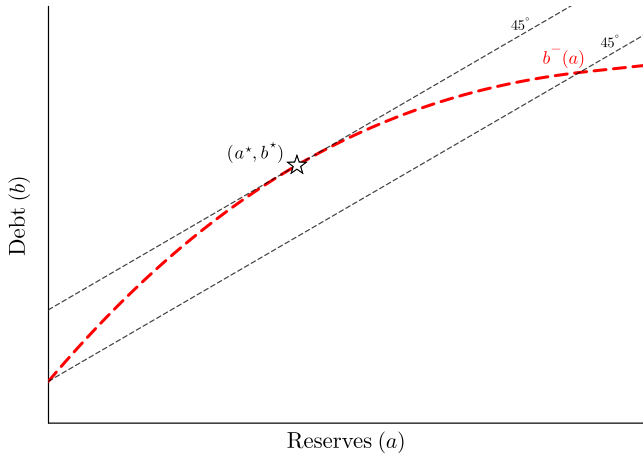


Consumption



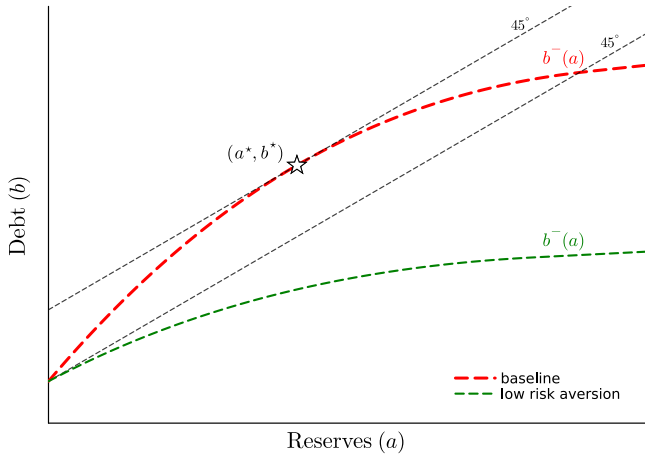
Lowest-NFA safe portfolio, (a^*, b^*)

► back



Lowest-NFA safe portfolio, (a^*, b^*)

► back



$$u(c) = \frac{(c - \underline{c})^{1-\sigma}}{1-\sigma}$$

Parameter	Value	Description	Source
y	1	Endowment	Normalization
σ	2	Risk-aversion	Standard
r	3%	Risk-free rate	Standard
$1/\delta$	6	Maturity of debt	Italian Debt
\underline{c}	0.68	Consumption floor	Bocola-Dovis (2019)
β	0.97	Discount factor	$\beta(1+r) = 1$
λ	0.5%	Sunspot probability	Baseline
ϕ	0.33	Default Cost	Debt-to-income =100%
κ	$\frac{\delta+r}{1+r}$	Coupon	Normalization

Experiment – How reserves help exit crisis zone

- Assume gov. starts w/ portfolio (a, b) , **but** from $t+1$ onward,
 $a' = 0$

Experiment – How reserves help exit crisis zone

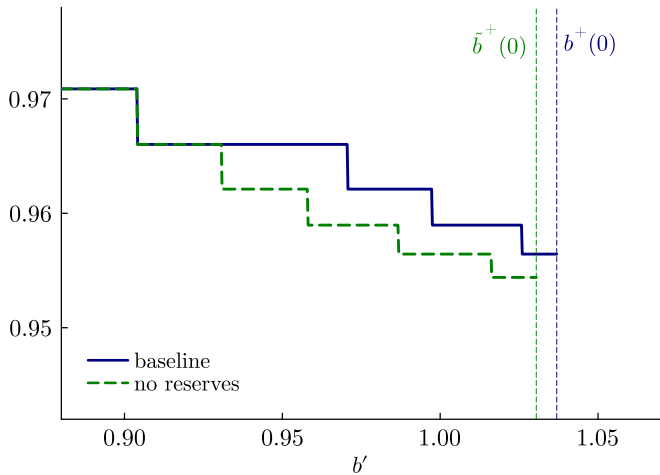
- Assume gov. starts w/ portfolio (a, b) , **but** from $t+1$ onward, $a' = 0$
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- Exiting takes longer to exit and cuts more consumption

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Without reserves: $\downarrow b^+$. More costly to deleverage \Rightarrow lower debt-carrying capacity

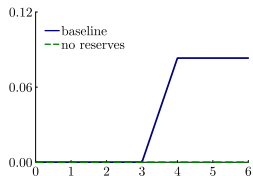
Price Schedule, $q(0, b')$

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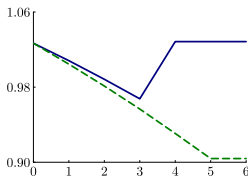
Lower consumption without reserves

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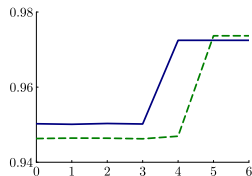
Reserves, a



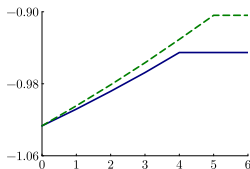
Debt, b



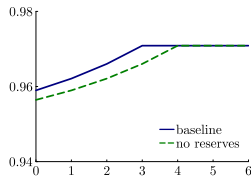
Consumption



Net Foreign Assets

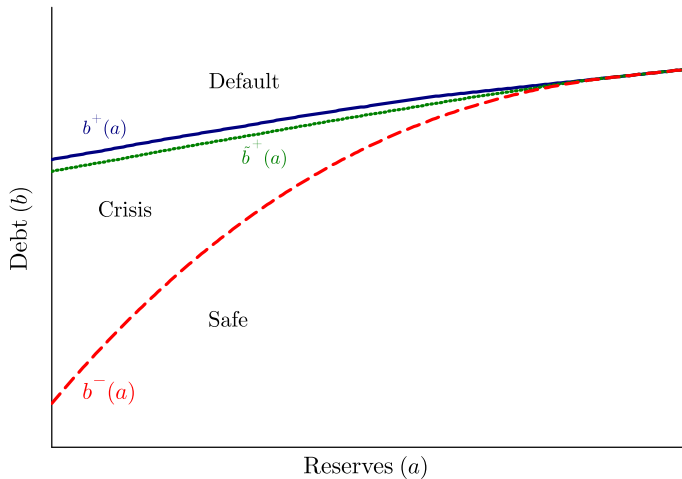


Debt Price, $q(a', b', s)$



Default zone expands

► back



Increasing reserves and debt lowers spreads (levels)

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Dep. Variable:	log(Spread)		
	(0)	(1)	(2)
Reserves	−2.39*** (0.11)		
Sov.Debt	1.25*** (0.10)	−1.13*** (0.14)	1.58*** (0.20)
NFA_public		−2.39*** (0.11)	−2.69 *** (0.11)
(Sov.Debt) ²			−5.48*** (0.31)
Num.Obs.	4497	4497	4497
R2	0.791	0.791	0.997

+ p < 0.1, * p < 0.05, ** p < 0.01, *** p < 0.001

All specs. include country FEs, year dummies and additional macro controls (as in Sosa-Padilla and Sturzenegger, 2023).