Script7

Yosune Miquelajauregui

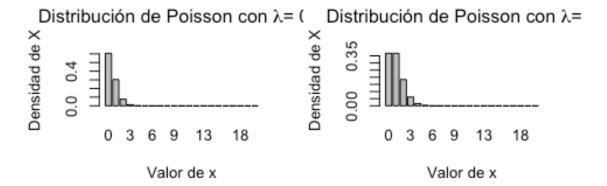
31/12/2017

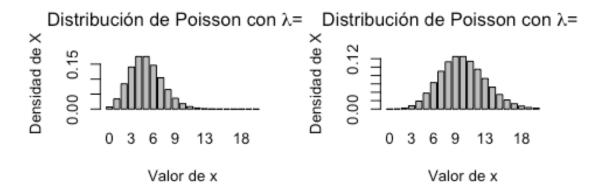
Modelos lineales generalizados

Regresión Poisson

Función de densidad para valores que siguen una distribución Poisson con media dada por lamba

```
x1<-dpois(0:20, lambda=0.5)
x2<-dpois(0:20, lambda=1)
x3<-dpois(0:20, lambda=5)
x4<-dpois(0:20, lambda=10)
par(mfrow=c(2,2))
barplot(x1, main=expression(paste("Distribución de Poisson con ", lambda,
"= 0.5")), names.arg=0:20, ylab="Densidad de X", xlab="Valor de x")
barplot(x2, main=expression(paste("Distribución de Poisson con ", lambda,
"= 1")), names.arg=0:20, ylab="Densidad de X", xlab="Valor de x")
barplot(x3, main=expression(paste("Distribución de Poisson con ", lambda,
"= 5")), names.arg=0:20, ylab="Densidad de X", xlab="Valor de x")
barplot(x4, main=expression(paste("Distribución de Poisson con ", lambda,
"= 10")), names.arg=0:20, ylab="Densidad de X", xlab="Valor de x")</pre>
```

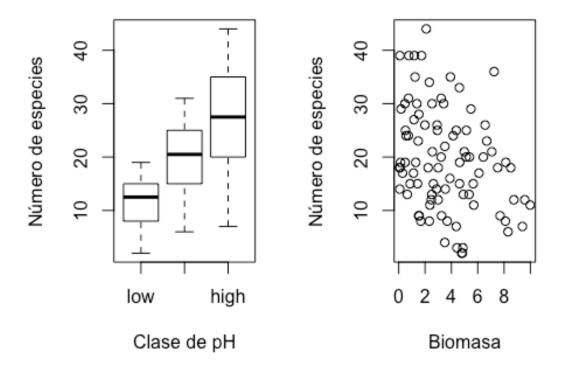




Regresión Poisson. Datos del libro Crawley

```
especies<-read.table("Species.txt", header=TRUE)</pre>
str(especies)
                     90 obs. of 3 variables:
## 'data.frame':
             : Factor w/ 3 levels "high", "low", "mid": 1 1 1 1 1 1 1 1 1 1 1 1
    $ Biomasa: num 0.469 1.731 2.09 3.926 4.367 ...
##
    $ Especie: int 30 39 44 35 25 29 23 18 19 12 ...
especies$pH <- factor(especies$pH , levels = c("low", "mid", "high"))</pre>
spp<-split(especies$Especie, especies$pH)</pre>
bio<-split(especies$Biomasa, especies$pH)</pre>
par(mfrow=c(1,2))
plot(especies$Especie~especies$pH, ylab="Número de especies", xlab="Clase
de pH", main="Número de especies vs pH")
plot(especies$Especie~especies$Biomasa, ylab="Número de especies",
xlab="Biomasa", main="Número de especies vs Biomasa")
```

Número de especies vs lúmero de especies vs Bio



Ajustar un modelo de regresión Poisson

```
mod1<-glm(Especie~Biomasa+pH+Biomasa:pH, family=poisson(link = log),</pre>
data=especies)
names(mod1)
##
    [1] "coefficients"
                              "residuals"
                                                   "fitted.values"
                              "R"
        "effects"
                                                   "rank"
##
    [4]
        "ar"
                              "family"
                                                   "linear.predictors"
##
    [7]
## [10]
        "deviance"
                              "aic"
                                                   "null.deviance"
       "iter"
                                                   "prior.weights"
   [13]
                              "weights"
                                                   "y"
## [16] "df.residual"
                              "df.null"
## [19]
        "converged"
                              "boundary"
                                                   "model"
                                                   "terms"
## [22]
        "call"
                              "formula"
        "data"
                              "offset"
                                                   "control"
## [25]
## [28] "method"
                              "contrasts"
                                                   "xlevels"
summary(mod1)
##
## Call:
## glm(formula = Especie ~ Biomasa + pH + Biomasa:pH, family =
poisson(link = log),
       data = especies)
```

```
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                   3Q
                                           Max
## -2.4978
           -0.7485 -0.0402
                               0.5575
                                        3.2297
##
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
                              0.08240 35.833 < 2e-16 ***
## (Intercept)
                   2.95255
## Biomasa
                  -0.26216
                              0.03803 -6.893 5.47e-12 ***
                                       4.515 6.34e-06 ***
## pHmid
                   0.48411
                              0.10723
## pHhigh
                   0.81557
                              0.10284
                                        7.931 2.18e-15 ***
## Biomasa:pHmid
                   0.12314
                              0.04270
                                        2.884 0.003927 **
## Biomasa:pHhigh 0.15503
                              0.04003
                                        3.873 0.000108 ***
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 452.346
                               on 89
                                      degrees of freedom
## Residual deviance: 83.201
                               on 84 degrees of freedom
## AIC: 514.39
##
## Number of Fisher Scoring iterations: 4
```

Podemos resumir la información con una tabla análoga de ANOVA que lidie con variables dicretas (número de especies)

```
anova(mod1, test="Chisq")
## Analysis of Deviance Table
##
## Model: poisson, link: log
##
## Response: Especie
##
## Terms added sequentially (first to last)
##
##
##
              Df Deviance Resid. Df Resid. Dev Pr(>Chi)
## NULL
                                  89
                                         452.35
               1
                   44.673
                                  88
                                         407.67 2.328e-11 ***
## Biomasa
                                          99.24 < 2.2e-16 ***
## pH
               2
                 308.431
                                  86
## Biomasa:pH 2
                   16.040
                                  84
                                         83.20 0.0003288 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Análisis de devianza

```
mod2<-glm(Especie~Biomasa+pH, family=poisson, data=especies)
mod3<-glm(Especie~Biomasa, family=poisson, data=especies)
anova(mod2, mod1, test="Chi")</pre>
```

```
## Analysis of Deviance Table
##
## Model 1: Especie ~ Biomasa + pH
## Model 2: Especie ~ Biomasa + pH + Biomasa:pH
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
            86
                   99.242
## 2
            84
                   83.201 2
                                 16.04 0.0003288 ***
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
LR < -2*(logLik(mod2)[1] - logLik(mod1)[1])
df<-df.residual(mod2)-df.residual(mod1)</pre>
pchisq(LR,df,lower.tail=F)
## [1] 0.0003287607
```

Devianza residual

```
dev.residual1<-2*sum(especies$Especie*log(especies$Especie/mod1$fitted)-
  (especies$Especie-mod1$fitted))
  mod1$deviance

## [1] 83.20114

mod2$deviance

## [1] 99.2415

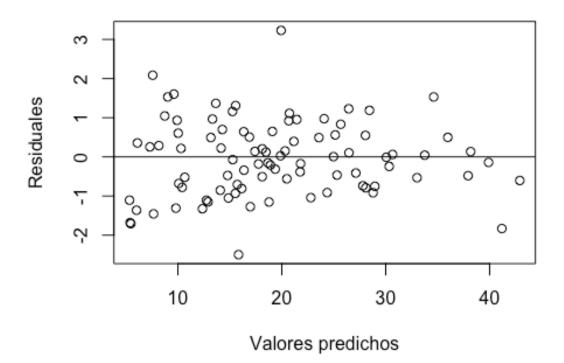
residual.dev2<-2*sum(especies$Especie*log(especies$Especie/mod3$fitted)-
  (especies$Especie-mod3$fitted))</pre>
```

Verificar supuestos

```
residuals(mod1, type="response")
##
                             2
                                            3
                                                          4
                                                                        5
##
   -11.17568365
                   3.02962044
                                  9.38642086
                                                6.56687473
                                                             -2.12104570
##
##
     4.93301929
                   1.84249672
                                 -1.36373626
                                                0.88170028
                                                             -3.52828937
##
              11
                            12
                                          13
                                                         14
                                                                       15
    -3.89865196
                  -2.92486021
                                 -3.01184170
                                               -0.05507520
                                                              6.56243292
##
##
              16
                            17
                                          18
                                                         19
                                                                       20
    -4.36338032
                   4.55992223
                                16.06886644
                                                0.58849504
                                                             -8.83262593
##
##
              21
                            22
                                          23
                                                         24
                                                                       25
##
    -0.89221934
                   0.82852195
                                  0.24819521
                                                0.34312577
                                                             -3.79958067
##
              26
                            27
                                          28
                                                         29
                                                                       30
##
     0.02740658
                  -1.76150805
                                  0.68833709
                                               -4.96536739
                                                             -3.86156982
##
              31
                            32
                                          33
                                                         34
                                                                       35
##
    -1.33269497
                   4.33164743
                                 -0.80219122
                                               -2.48222560
                                                             -2.71589053
##
              36
                                          38
                                                         39
                                                                       40
                            37
##
    -1.78813331
                  -1.65674603
                                 -4.78015784
                                                2.43019563
                                                              5.26670199
##
              41
                            42
                                          43
                                                         44
                                                                       45
```

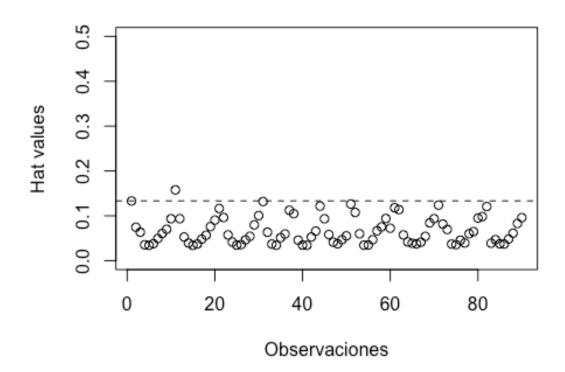
```
##
     0.12417538
                    5.44552367
                                  0.84631309
                                               -2.08031387
                                                               2.95403747
##
              46
                            47
                                           48
                                                         49
                                                                        50
                   -4.79058101
                                                               4.74763238
                                 -2.11103182
                                                 2.66229074
##
     2.86191891
##
              51
                                                         54
                                                                        55
##
    -3.80389778
                   -3.95034583
                                 -2.30885776
                                                 4.32979131
                                                               2.90700288
##
              56
                             57
                                           58
                                                         59
                                                                        60
##
    -1.35724563
                   -3.07864101
                                  3.67557501
                                                -4.08305508
                                                               0.53920339
                                                         64
##
              61
                             62
                                           63
                                                                        65
##
    -0.65500122
                    0.52869799
                                 -0.27435072
                                                5.35185887
                                                               1.97340098
##
                                                         69
                                                                        70
              66
                             67
                                           68
##
     0.70002350
                    5.38540597
                                  0.83432381
                                                -3.01663552
                                                              -3.46970582
##
              71
                             72
                                           73
                                                         74
                                                                        75
    -0.90447189
                    2.12264452
                                 -3.14241797
                                                -3.74078784
##
                                                              -4.35819106
##
                            77
                                           78
                                                         79
                                                                        80
              76
##
     4.97367900
                    3.08204281
                                 -3.65705655
                                                 0.69809237
                                                              -3.39744137
##
                                                                        85
              81
                             82
                                           83
                                                         84
##
    -0.75379420
                   -4.76923995
                                  1.83024026
                                                 2.72169583
                                                              -3.90003785
##
              86
                             87
                                           88
                                                         89
                                                                        90
##
    -2.41016343
                    3.26616805
                                  6.42400054
                                                 0.89960748
                                                              -2.34258662
plot(residuals(mod1)~fitted(mod1), ylab="Residuales", xlab="Valores
predichos", main="Residuales vs valores predichos")
abline(h=0)
```

Residuales vs valores predichos



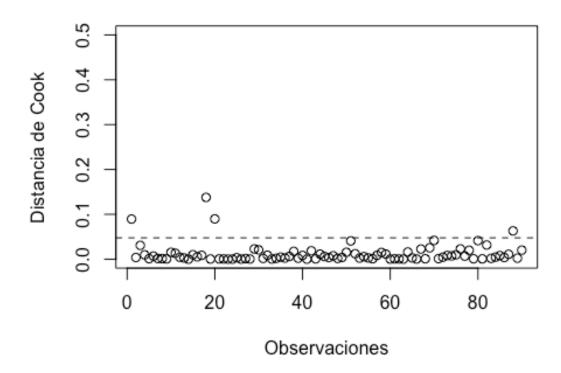
```
plot(hatvalues(mod1), ylim=c(0,0.5), ylab="Hat values",
xlab="Observaciones", main="Efecto levier")
abline(h=6*2/90, lty=2) # hat = k/n, donde k es el número de parámetros,
n es el tamaño muestral
```

Efecto levier



```
plot(cooks.distance(mod1), ylab="Distancia de Cook",
xlab="Observaciones", ylim=c(0,0.5), main="Influencia de las
observaciones")
abline(h=4/(90-6), lty=2)
```

Influencia de las observaciones



```
chisq<-sum(((especies$Especie-mod1$fitted)^2)/mod1$fitted)
c_hat<-chisq/mod1$df.residual</pre>
```

Interpretar output del mod1

```
##Correr an'álisis separado para cada nivel de pH
low<-especies[especies$pH=="low", ]</pre>
mid<-especies[especies$pH=="mid", ]</pre>
high<-especies[especies$pH=="high", ]</pre>
mod_low<-glm(Especie~Biomasa, family=poisson, data=low)</pre>
mod mid<-glm(Especie~Biomasa, family=poisson, data=mid)</pre>
mod_high<-glm(Especie~Biomasa, family=poisson, data=high)</pre>
##comparar output de los tres modelos
mod low
##
          glm(formula = Especie ~ Biomasa, family = poisson, data = low)
##
## Coefficients:
## (Intercept)
                     Biomasa
##
        2.9526
                     -0.2622
##
## Degrees of Freedom: 29 Total (i.e. Null); 28 Residual
```

```
## Null Deviance: 83.77
## Residual Deviance: 32.72
                                AIC: 161.1
mod_mid
##
## Call: glm(formula = Especie ~ Biomasa, family = poisson, data = mid)
##
## Coefficients:
## (Intercept)
                    Biomasa
                     -0.139
##
         3.437
##
## Degrees of Freedom: 29 Total (i.e. Null); 28 Residual
## Null Deviance:
                        71.43
## Residual Deviance: 16.54
                                AIC: 163.8
mod_high
##
## Call: glm(formula = Especie ~ Biomasa, family = poisson, data = high)
##
## Coefficients:
                    Biomasa
## (Intercept)
##
                    -0.1071
        3.7681
##
## Degrees of Freedom: 29 Total (i.e. Null); 28 Residual
## Null Deviance:
                        109.9
## Residual Deviance: 33.94
                                AIC: 189.5
mod1
##
## Call: glm(formula = Especie ~ Biomasa + pH + Biomasa:pH, family =
poisson(link = log),
##
       data = especies)
##
## Coefficients:
##
      (Intercept)
                          Biomasa
                                            pHmid
                                                           pHhigh
                                           0.4841
##
           2.9526
                          -0.2622
                                                           0.8156
## Biomasa:pHmid Biomasa:pHhigh
##
           0.1231
                           0.1550
##
## Degrees of Freedom: 89 Total (i.e. Null); 84 Residual
## Null Deviance:
                        452.3
## Residual Deviance: 83.2 AIC: 514.4
```

Crear hoja dedatos con los valores predichos para cada nivel de pH

```
fit low<-data.frame(fit=fitted(mod low), low)</pre>
fit low<-fit low[order(fit low$fit), ]</pre>
fit_mid<-data.frame(fit=fitted(mod_mid), mid)</pre>
fit_mid<-fit_mid[order(fit_mid$fit), ]</pre>
```

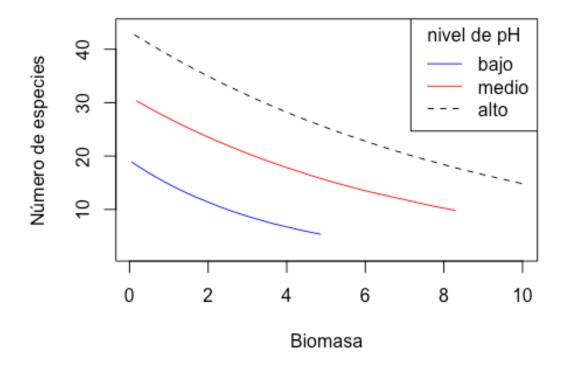
```
fit_high<-data.frame(fit=fitted(mod_high), high)
fit_high<-fit_high[order(fit_high$fit), ]</pre>
```

Graficar

```
plot(1~1, ylab="Número de especies", xlab="Biomasa", type="n",
ylim=range(especies$Especie), xlim=range(especies$Biomasa))

## Warning in plot.formula(1 ~ 1, ylab = "Número de especies", xlab =
## "Biomasa", : the formula '1 ~ 1' is treated as '1 ~ 1'

lines(fit_low$fit~fit_low$Biomasa, lty="solid", col="blue")
lines(fit_mid$fit~fit_mid$Biomasa, lty="solid", col="red")
lines(fit_high$fit~fit_high$Biomasa, lty="dashed", col="black")
legend(x="topright", lty=c("solid", "solid", "dashed"), col=c("blue",
"red", "black"), legend=c("bajo", "medio", "alto"), title="nivel de pH")
```



Precitor lineal y valores predichos

```
especies [1,] #primera observación

## pH Biomasa Especie
## 1 high 0.4692972 30

mod1$linear.predictors[1:5]
```

```
2
##
           1
                              3
                                        4
                                                  5
## 3.717848 3.582696 3.544246 3.347555 3.300310
mod1$fitted.values[1:5]
                                                  5
##
           1
                     2
                               3
                                        4
## 41.17568 35.97038 34.61358 28.43313 27.12105
model.matrix(mod1) #extraer matriz
##
      (Intercept)
                       Biomasa pHmid pHhigh Biomasa:pHmid Biomasa:pHhigh
## 1
                 1 0.46929722
                                                  0.0000000
                                                                  0.46929722
                                    0
                                            1
## 2
                 1 1.73087043
                                    0
                                            1
                                                  0.0000000
                                                                  1.73087043
## 3
                 1 2.08977848
                                    0
                                            1
                                                                  2.08977848
                                                  0.0000000
                 1 3.92578714
## 4
                                    0
                                            1
                                                  0.0000000
                                                                  3.92578714
## 5
                 1 4.36679265
                                    0
                                            1
                                                  0.0000000
                                                                  4.36679265
## 6
                 1 5.48197468
                                    0
                                            1
                                                  0.0000000
                                                                  5.48197468
## 7
                 1 6.68468591
                                    0
                                            1
                                                  0.0000000
                                                                  6.68468591
## 8
                 1 7.51165063
                                    0
                                            1
                                                  0.0000000
                                                                  7.51165063
## 9
                 1 8.13220251
                                    0
                                            1
                                                  0.0000000
                                                                  8.13220251
                                            1
## 10
                 1 9.57212864
                                    0
                                                  0.0000000
                                                                  9.57212864
## 11
                 1 0.08665367
                                    0
                                            1
                                                  0.0000000
                                                                  0.08665367
## 12
                 1 1.23697390
                                    0
                                            1
                                                  0.0000000
                                                                  1.23697390
## 13
                 1 2.53204324
                                    0
                                            1
                                                  0.0000000
                                                                  2.53204324
## 14
                 1 3.40794153
                                    0
                                            1
                                                  0.0000000
                                                                  3.40794153
## 15
                 1 4.60504596
                                    0
                                            1
                                                  0.0000000
                                                                  4.60504596
## 16
                 1 5.36771709
                                    0
                                            1
                                                  0.0000000
                                                                  5.36771709
## 17
                                    0
                                            1
                 1 6.56084215
                                                  0.0000000
                                                                  6.56084215
## 18
                 1 7.24206214
                                    0
                                            1
                                                  0.0000000
                                                                  7.24206214
## 19
                 1 8.50363299
                                    0
                                            1
                                                                  8.50363299
                                                  0.0000000
## 20
                 1 9.39095342
                                    0
                                            1
                                                  0.0000000
                                                                  9.39095342
## 21
                 1 0.76488801
                                    0
                                            1
                                                  0.0000000
                                                                  0.76488801
## 22
                 1 1.17647020
                                    0
                                            1
                                                  0.0000000
                                                                  1.17647020
## 23
                 1 2.32512082
                                    0
                                            1
                                                  0.0000000
                                                                  2.32512082
## 24
                 1 3.22288207
                                    0
                                            1
                                                  0.0000000
                                                                  3.22288207
##
   25
                 1 4.13612930
                                    0
                                            1
                                                  0.0000000
                                                                  4.13612930
                 1 5.13717652
                                    0
## 26
                                            1
                                                  0.0000000
                                                                  5.13717652
                 1 6.42193811
## 27
                                    0
                                            1
                                                  0.0000000
                                                                  6.42193811
                 1 7.06552638
                                    0
                                            1
## 28
                                                  0.0000000
                                                                  7.06552638
## 29
                 1 8.74592918
                                    0
                                            1
                                                  0.0000000
                                                                  8.74592918
                 1 9.98177013
                                    0
                                            1
## 30
                                                  0.0000000
                                                                  9.98177013
## 31
                 1 0.17576270
                                    1
                                            0
                                                  0.1757627
                                                                  0.00000000
## 32
                 1 1.37677830
                                    1
                                            0
                                                  1.3767783
                                                                  0.00000000
## 33
                 1 2.55104256
                                    1
                                            0
                                                  2.5510426
                                                                  0.00000000
## 34
                 1 3.00027434
                                    1
                                            0
                                                  3.0002743
                                                                  0.00000000
                                                  4.9056239
## 35
                 1 4.90562386
                                    1
                                            0
                                                                  0.00000000
## 36
                 1 5.34330542
                                    1
                                            0
                                                  5.3433054
                                                                  0.00000000
## 37
                 1 7.70000000
                                    1
                                            0
                                                  7.7000000
                                                                  0.00000000
                 1 0.55368893
                                            0
## 38
                                    1
                                                  0.5536889
                                                                  0.00000000
## 39
                 1 1.99029644
                                    1
                                            0
                                                  1.9902964
                                                                  0.00000000
## 40
                 1 2.91263671
                                    1
                                                  2.9126367
                                                                  0.00000000
```

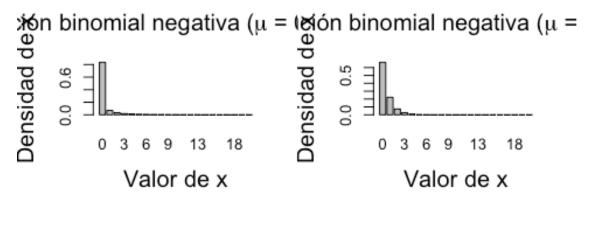
##	41	1 3.21645133	1	0	3.2164513	0.00000000
##	42	1 4.97988468	1	0	4.9798847	0.00000000
##	43	1 5.65872290	1	0	5.6587229	0.00000000
##	44	1 8.10000000	1	0	8.1000000	0.00000000
##	45	1 0.73956986	1	0	0.7395699	0.00000000
##	46	1 1.52693420	1	0	1.5269342	0.00000000
##	47	1 2.23212239	1	0	2.2321224	0.00000000
##	48	1 3.88528818	1	0	3.8852882	0.00000000
##	49	1 4.62650541	1	0	4.6265054	0.00000000
##	50	1 5.12096844	1	0	5.1209684	0.00000000
##	51	1 8.30000000	1	0	8.3000000	0.00000000
	52	1 0.51127858	1	0	0.5112786	0.00000000
##	53	1 1.47823269	1	0	1.4782327	0.00000000
##	54	1 2.93455800	1	0	2.9345580	0.00000000
##	55	1 3.50548891	1	0	3.5054889	0.00000000
##	56	1 4.61790914	1	0	4.6179091	0.00000000
##	57	1 5.69696382	1	0	5.6969638	0.00000000
##	58	1 6.09301688	1	0	6.0930169	0.00000000
##	59	1 0.73006280	1	0	0.7300628	0.00000000
##	60	1 1.15806838	1	0	1.1580684	0.00000000
	61	1 0.10084790	0	0	0.0000000	0.00000000
##	62	1 0.13859609	0	0	0.0000000	0.00000000
##	63	1 0.86351508	0	0	0.0000000	0.00000000
	64	1 1.29291903	0	0	0.0000000	0.00000000
	65	1 2.46916355	0	0	0.0000000	0.00000000
##	66	1 2.36655309	0	0	0.0000000	0.00000000
##	67	1 2.62921708	0	0	0.0000000	0.00000000
##	68	1 3.25228652	0	0	0.0000000	0.00000000
##	69	1 4.41727619	0	0	0.0000000	0.00000000
##	70	1 4.78081039	0	0	0.0000000	0.00000000
##	71	1 0.05017529	0	0	0.0000000	0.00000000
##	72	1 0.48283691	0	0	0.0000000	0.00000000
##	73	1 0.65266714	0	0	0.0000000	0.00000000
##	74	1 1.55533656	0	0	0.0000000	0.00000000
##	75	1 1.67163820	0	0	0.0000000	0.00000000
##	76	1 2.87005390	0	0	0.0000000	0.00000000
##	77	1 2.51072052	0	0	0.0000000	0.00000000
##	78	1 3.49760385	0	0	0.0000000	0.00000000
	79	1 3.67876186	0	0	0.0000000	0.00000000
	80	1 4.83154245	0	0	0.0000000	0.00000000
	81	1 0.28972266	0	0	0.0000000	0.00000000
	82	1 0.07756009	0	0	0.0000000	0.00000000
	83	1 1.42902041	0	0	0.0000000	0.00000000
	84	1 1.12074092	0	0	0.0000000	0.00000000
	85	1 1.50795384	0	0	0.0000000	0.00000000
	86	1 2.32596318	0	0	0.0000000	0.00000000
	87	1 2.99570582	0	0	0.0000000	0.00000000
	88	1 3.53819909	0	0	0.0000000	0.00000000
	89	1 4.36454121	0	0	0.0000000	0.00000000
	90	1 4.87050789	0	0	0.0000000	0.00000000

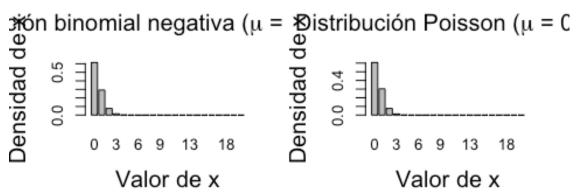
```
## attr(,"assign")
## [1] 0 1 2 2 3 3
## attr(,"contrasts")
## attr(,"contrasts")$pH
## [1] "contr.treatment"
coef(mod1)
##
      (Intercept)
                          Biomasa
                                            pHmid
                                                          pHhigh
Biomasa:pHmid
        2.9525524
                      -0.2621580
                                       0.4841087
                                                       0.8155712
0.1231362
## Biomasa:pHhigh
        0.1550282
##
especies [50,]
       pH Biomasa Especie
## 50 mid 5.120968
                         20
linpred<-model.matrix(mod1)[50,]%*%coef(mod1) #calcular valor predicho de</pre>
la observaci´ón 50
exp(linpred) #calcular valor predicho misma escala que la observación
original
##
            [,1]
## [1,] 15.25237
```

Regresión Binomial negativa

Función de densidad para valores que siguen una distribución binomial negativa con parámetro de dispersión size=k

```
y1<-dnbinom(x=0:20, mu=0.5, size=0.1)
y2<-dnbinom(x=0:20, mu=0.5, size=1)
y3<-dnbinom(x=0:20, mu=0.5, size=10)
y4<-dpois(x=0:20, lambda=0.5)
layout(mat=matrix(1:4, nrow=2, ncol=2, byrow=TRUE))
barplot(y1, main=expression(paste("Distribución binomial negativa (", mu,
" = 0.5, ", italic(k), " = 0.1)")), names.arg=0:20, ylab="Densidad de x",
xlab="Valor de x", cex.lab=1.5, cex.main=1.5)
barplot(y2, main=expression(paste("Distribución binomial negativa (", mu,
" = 0.5, ", italic(k), " = 1)")), names.arg=0:20, ylab="Densidad de x",
xlab="Valor de x", cex.lab=1.5, cex.main=1.5)
barplot(y3, main=expression(paste("Distribución binomial negativa (", mu,
" = 0.5, ", italic(k), " = 10)")), names.arg=0:20, ylab="Densidad de x",
xlab="Valor de x", cex.lab=1.5, cex.main=1.5)
barplot(y4, main=expression(paste("Distribución Poisson (", mu, " =
0.5)")), names.arg=0:20, ylab="Densidad de x", xlab="Valor de x",
cex.lab=1.5, cex.main=1.5)
```



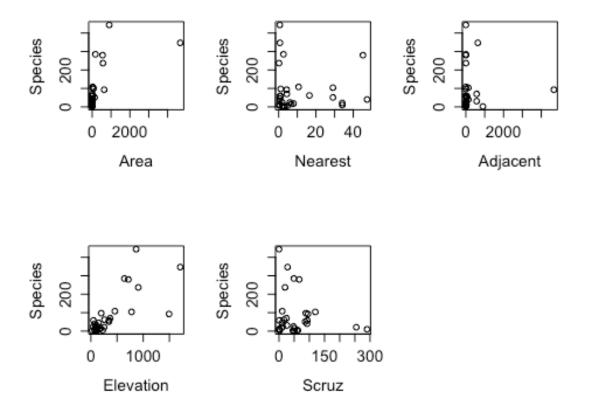


Cargar paquete faraway que contiene los datos gala

```
library(faraway)
data(gala)
attach(gala)
```

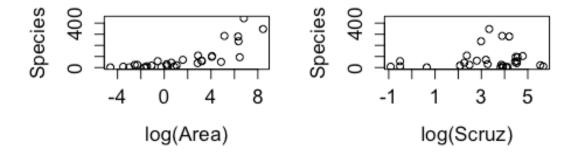
Checar relaciones entre variables

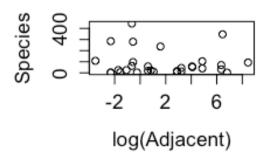
```
layout(mat=matrix(1:6, nrow=2, ncol=3))
plot(Species~Area, cex.lab=1.3, cex.axis=1.3)
plot(Species~Elevation, cex.lab=1.3, cex.axis=1.3)
plot(Species~Nearest, cex.lab=1.3, cex.axis=1.3)
plot(Species~Scruz, cex.lab=1.3, cex.axis=1.3)
plot(Species~Adjacent, cex.lab=1.3, cex.axis=1.3)
```



Transformar a logaritmo para mejorar distribuci'ón de observaciones

```
layout(mat=matrix(1:4, nrow=2, ncol=2))
plot(Species~log(Area), cex.lab=1.3, cex.axis=1.3)
plot(Species~log(Adjacent), cex.lab=1.3, cex.axis=1.3)
plot(Species~log(Scruz), cex.lab=1.3, cex.axis=1.3)
```





Linealizar relaciones

```
gala$log_Area<-log(gala$Area)
gala$log_Adjacent<-log(gala$Adjacent)
gala$log_Scruz<-log(gala$Scruz+1)</pre>
```

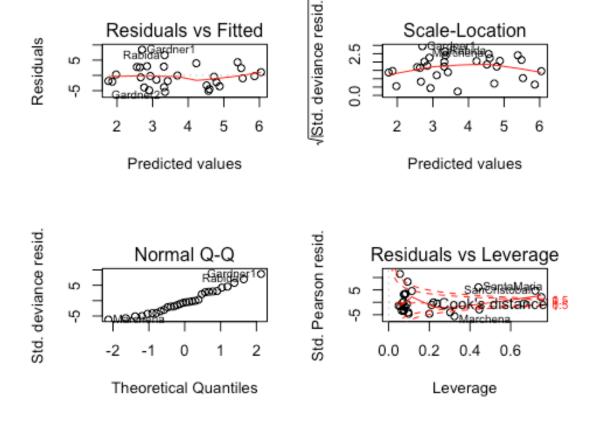
Correr modelo

```
gala1<-glm(Species~log_Area+Elevation+Nearest+log_Adjacent+log_Scruz,</pre>
data=gala, family=poisson)
summary(gala1)
##
## Call:
## glm(formula = Species ~ log_Area + Elevation + Nearest + log_Adjacent
##
       log_Scruz, family = poisson, data = gala)
##
## Deviance Residuals:
##
       Min
                 1Q
                       Median
                                    3Q
                                             Max
## -5.4341
           -3.0204
                     -0.5416
                                2.5770
                                         8.4359
##
## Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
##
```

```
## (Intercept)
                 3.505e+00 6.368e-02
                                       55.048 < 2e-16 ***
## log_Area
                 3.575e-01
                            1.615e-02
                                       22.135
                                               < 2e-16 ***
## Elevation
                 5.663e-05
                            1.044e-04
                                        0.543
                                               0.58732
## Nearest
                -3.431e-03
                            1.674e-03
                                       -2.050
                                               0.04038 *
## log Adjacent -9.130e-02
                            8.760e-03 -10.423
                                               < 2e-16 ***
## log_Scruz
                -5.003e-02 1.535e-02
                                       -3.259
                                               0.00112 **
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## (Dispersion parameter for poisson family taken to be 1)
##
                                      degrees of freedom
##
       Null deviance: 3510.73
                               on 29
                                      degrees of freedom
## Residual deviance: 361.17
                               on 24
## AIC: 534
##
## Number of Fisher Scoring iterations: 5
```

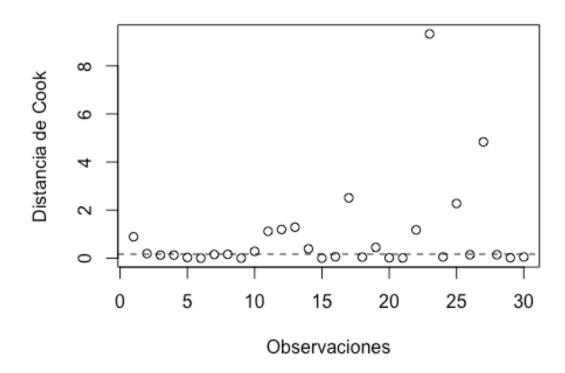
Verificar supuestos

```
layout(mat=matrix(1:4, nrow=2, ncol=2))
plot(gala1)
```



```
plot(cooks.distance(gala1), ylab="Distancia de Cook",
xlab="Observaciones", main="Influencia de las observaciones")
abline(h=4/(30-6), lty=2)
```

Influencia de las observaciones



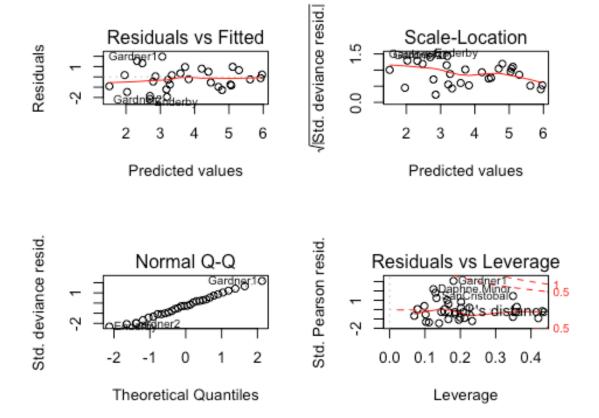
Chi-square/c_hat. Verificar sobredispersi'ón

```
chisq<-sum(((gala$Species-gala1$fitted)^2)/gala1$fitted)
c.hat<-chisq/gala1$df.residual</pre>
```

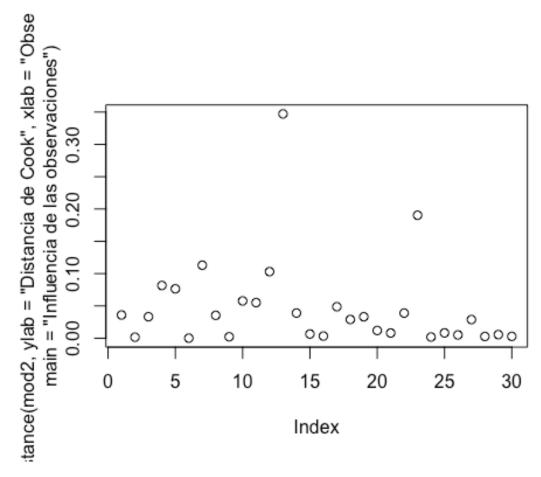
Intentar ajustear un modelo de regresión binomial

```
library(MASS)
mod2<-glm.nb(Species~log_Area+Elevation+Nearest+log_Adjacent+log_Scruz,</pre>
data=gala)
summary(mod2)
##
## Call:
## glm.nb(formula = Species ~ log_Area + Elevation + Nearest +
log_Adjacent +
       log Scruz, data = gala, init.theta = 2.938490105, link = log)
##
##
## Deviance Residuals:
       Min
                 1Q
                      Median
                                    3Q
                                            Max
```

```
## -2.1466 -0.8867 -0.2338 0.4581
                                      1.9671
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.5621341 0.2971453 11.988 < 2e-16 ***
## log_Area
               0.4215363 0.0660078 6.386 1.7e-10 ***
                                              0.304
## Elevation
              -0.0005481 0.0005335 -1.027
## Nearest
              -0.0137115 0.0102400 -1.339
                                              0.181
## log_Adjacent -0.0250659 0.0376654 -0.665
                                              0.506
## log_Scruz -0.0277083 0.0878747 -0.315
                                              0.753
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(2.9385) family taken to be
1)
##
##
      Null deviance: 149.161 on 29 degrees of freedom
## Residual deviance: 32.782 on 24 degrees of freedom
## AIC: 287.9
##
## Number of Fisher Scoring iterations: 1
##
##
##
                Theta: 2.938
##
            Std. Err.: 0.866
##
##
  2 x log-likelihood: -273.896
layout(mat=matrix(1:4, nrow=2))
plot(mod2)
```



plot(cooks.distance(mod2, ylab="Distancia de Cook", xlab="Observaciones",
main="Influencia de las observaciones"))



Correr modelo con glm y parámetro de dispersión obtenido en mod2

```
mod2b<-glm(Species~log_Area+Elevation+Nearest+log_Adjacent+log_Scruz,
data=gala,family=negative.binomial(theta=2.938))

logLik(mod2)

## 'log Lik.' -136.9479 (df=7)

#theta es un parámetro adicional
logLik(mod2b)

## 'log Lik.' -136.9479 (df=6)</pre>
```