Transparency conversion from sRGB to Linear color space
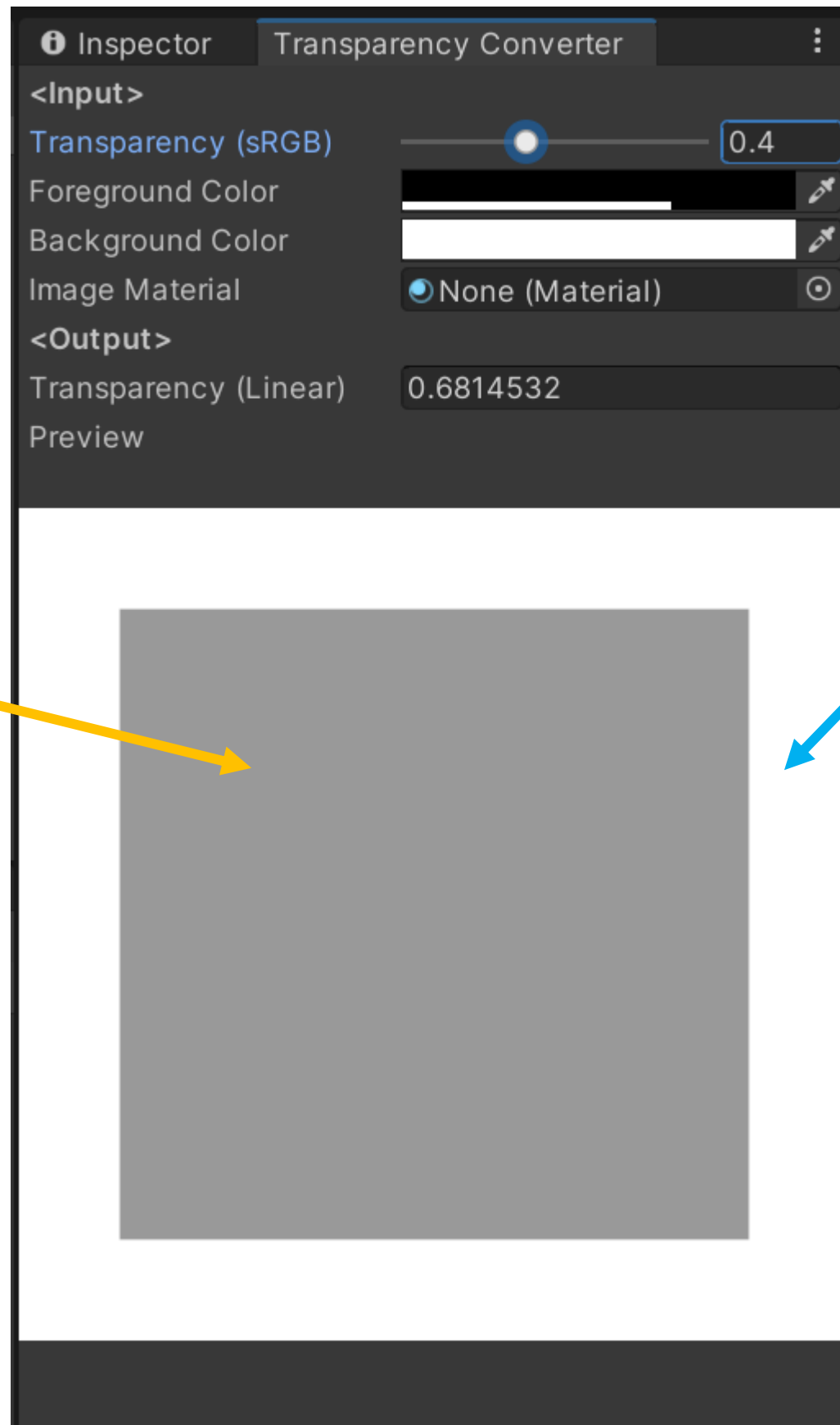
https://github.com/sotanmochi/TransparencyConverter

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Transparency conversion from sRGB color space to linear color space

Inspector	Transparency Converter	

\<Input\>

Transparency (sRGB)	●————	0.4
Foreground Color		
Background Color		
Image Material	● None (Material)	◎

\<Output\>

Transparency (Linear)   0.6814532

Preview

Foreground (Transparent)
+
Background (Opaque)

$$(R_F, G_F, B_F, \alpha)$$
$$+$$
$$(R_B, G_B, B_B, 1)$$

Background (Opaque)

$$(R_B, G_B, B_B, 1)$$

Transparency conversion from sRGB color space to linear color space

$$C_{output} = C_F\alpha + C_B(1 - \alpha)$$

where $0 \leq c_F \leq 1$, $0 \leq c_B \leq 1$ and $0 \leq \alpha \leq 1$.

$$C_{linear} = C_F\alpha_{linear} + C_B(1 - \alpha_{linear})$$

$$C_{sRGB} = C_F\alpha_{sRGB} + C_B(1 - \alpha_{sRGB})$$

$$C_{linear} = g(C_{sRGB})$$

where $g(x)$ is conversion function from sRGB color space to linear color space.

$$C_F\alpha_{linear} + C_B(1 - \alpha_{linear}) = g(C_{sRGB})$$

$$\alpha_{linear} = f(C_F, C_B, \alpha_{sRGB}) = \frac{-C_B + g(C_{sRGB})}{C_F - C_B}$$

where $C_F \neq C_B$ and $C_{sRGB} = C_F\alpha_{sRGB} + C_B(1 - \alpha_{sRGB})$.

Transparency conversion from sRGB color space to linear color space

$$\alpha_{linear} = f(C_F, C_B, \alpha_{sRGB}) = \frac{-C_B + g(C_{sRGB})}{C_F - C_B}$$

where $C_F \neq C_B$ and $C_{sRGB} = C_F \alpha_{sRGB} + C_B(1 - \alpha_{sRGB})$.

Considering the following constraints.

$$0 \leq \alpha_{linear} \leq 1$$

$$\alpha_{linear} = \frac{f(C_F, C_B, \alpha_{sRGB}) - f_{MIN}}{f_{MAX} - f_{MIN}}$$

$$f(C_F, C_B, \alpha_{sRGB}) = \frac{-C_B + g(C_{sRGB})}{C_F - C_B}$$

$$f(C_F, C_B, \alpha_{sRGB}) = f_{MAX} \quad \rightarrow \quad \alpha_{linear} = 1$$

$$f(C_F, C_B, \alpha_{sRGB}) = f_{MIN} \quad \rightarrow \quad \alpha_{linear} = 0$$

$$f(C_F, C_B, \alpha_{sRGB}) = (f_{MAX} + f_{MIN})/2 \quad \rightarrow \quad \alpha_{linear} = 0.5$$

Transparency conversion from sRGB color space to linear color space

The conversion function $g(x)$ is monotonically increasing function.

When $C_F > C_B$, the funcfion $g(C_{sRGB}) = g(C_F \alpha_{sRGB} + C_B(1 - \alpha_{sRGB}))$ is monotonically increasing for α_{sRGB} .

When $C_F < C_B$, the funcfion $g(C_{sRGB}) = g(C_F \alpha_{sRGB} + C_B(1 - \alpha_{sRGB}))$ is monotonically decreasing for α_{sRGB} .

The funcfion $f(C_F, C_B, \alpha_{sRGB})$ is monotonically increasing for all α_{sRGB} .

$$f_{MAX} = f(C_F, C_B, 1) = \frac{-C_B + g(C_F)}{C_F - C_B}$$

$$f_{MIN} = f(C_F, C_B, 0) = \frac{-C_B + g(C_B)}{C_F - C_B}$$

Transparency conversion from sRGB color space to linear color space

$$\alpha_{linear} = \frac{f(C_F, C_B, \alpha_{SRGB}) - f_{MIN}}{f_{MAX} - f_{MIN}}$$

$$\alpha_{linear} = \frac{\dfrac{-C_B + g(C_F \alpha_{SRGB} + C_B(1 - \alpha_{SRGB}))}{C_F - C_B} - \dfrac{-C_B + g(C_B)}{C_F - C_B}}{\dfrac{-C_B + g(C_F)}{C_F - C_B} - \dfrac{-C_B + g(C_B)}{C_F - C_B}}$$

$$= \frac{\dfrac{g(C_F \alpha_{SRGB} + C_B(1 - \alpha_{SRGB})) - g(C_B)}{C_F - C_B}}{\dfrac{g(C_F) - g(C_B)}{C_F - C_B}}$$

$$= \frac{g(C_F \alpha_{SRGB} + C_B(1 - \alpha_{SRGB})) - g(C_B)}{g(C_F) - g(C_B)}$$

Transparency conversion from sRGB color space to linear color space

Therefore,

$$\alpha_{linear} = \frac{g\big(C_F \alpha_{sRGB} + C_B(1 - \alpha_{sRGB})\big) - g(C_B)}{g(C_F) - g(C_B)}$$

where $0 \leq c_F \leq 1, \ \ 0 \leq c_B \leq 1, \ \ 0 \leq \alpha_{sRGB} \leq 1$
and $g(x)$ is conversion function from sRGB color space to linear color space.

Transparency conversion from sRGB color space to linear color space

$$\alpha_{linear} = \frac{g\big(C_F\alpha_{sRGB} + C_B(1 - \alpha_{sRGB})\big) - g(C_B)}{g(C_F) - g(C_B)}$$

where $0 \leq c_F \leq 1, \;\; 0 \leq c_B \leq 1, \;\; 0 \leq \alpha_{sRGB} \leq 1$
and $g(x)$ is conversion function from sRGB color space to linear color space.

When $g(x) = x^{2.2}$,

$$\alpha_{linear} = \frac{\big(C_F\alpha_{sRGB} + C_B(1 - \alpha_{sRGB})\big)^{2.2} - C_B^{2.2}}{C_F^{2.2} - C_B^{2.2}}$$

where $0 \leq c_F \leq 1, 0 \leq c_B \leq 1$ and $0 \leq \alpha \leq 1$.

Particular cases

If $C_F = 0$ (black) and $C_B = 1$ (white),

$$\alpha_{linear} = 1 - (1 - \alpha_{sRGB})^{2.2}$$

If $C_F = 1$ (white) and $C_B = 0$ (black),

$$\alpha_{linear} = \alpha_{sRGB}^{2.2}$$

Transparency conversion from sRGB color space to linear color space

$$\alpha_{linear} = \frac{g\big(C_F \alpha_{sRGB} + C_B(1 - \alpha_{sRGB})\big) - g(C_B)}{g(C_F) - g(C_B)}$$

where $0 \le c_F \le 1, \ \ 0 \le c_B \le 1, \ \ 0 \le \alpha_{sRGB} \le 1$
and $g(x)$ is conversion function from sRGB color space to linear color space.

For the following $g(x)$ (Refer to https://en.wikipedia.org/wiki/SRGB#Transformation)

$$g(x) = \begin{cases} \dfrac{x}{12.92}, & x \le 0.04050 \\[2em] \left(\dfrac{x + 0.055}{1.055}\right)^{2.4}, & x > 0.04050 \end{cases}$$

$$\alpha_{linear} = \frac{\left(\dfrac{C_F \alpha_{sRGB} + C_B(1 - \alpha_{sRGB}) + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{C_B + 0.055}{1.055}\right)^{2.4}}{\left(\dfrac{C_F + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{C_B + 0.055}{1.055}\right)^{2.4}}$$

Transparency conversion from sRGB color space to linear color space

$$\alpha_{linear} = \frac{\left(\dfrac{C_F \alpha_{sRGB} + C_B (1 - \alpha_{sRGB}) + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{C_B + 0.055}{1.055}\right)^{2.4}}{\left(\dfrac{C_F + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{C_B + 0.055}{1.055}\right)^{2.4}}$$

where $0 \leq c_F \leq 1$, $0 \leq c_B \leq 1$ and $0 \leq \alpha \leq 1$.

Particular cases

If $C_F = 0$ (black) and $C_B = 1$ (white),

$$\alpha_{linear} = \frac{1}{1 - \left(\dfrac{0.055}{1.055}\right)^{2.4}}\left[1 - \left(\dfrac{1 - \alpha_{sRGB} + 0.055}{1.055}\right)^{2.4}\right]$$

If $C_F = 1$ (white) and $C_B = 0$ (black),

$$\alpha_{linear} = \frac{1}{1 - \left(\dfrac{0.055}{1.055}\right)^{2.4}}\left[\left(\dfrac{\alpha_{sRGB} + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{0.055}{1.055}\right)^{2.4}\right]$$

Transparency conversion from sRGB color space to linear color space

$$\alpha_{linear} = \frac{\left(\dfrac{C_F\alpha_{sRGB} + C_B(1 - \alpha_{sRGB}) + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{C_B + 0.055}{1.055}\right)^{2.4}}{\left(\dfrac{C_F + 0.055}{1.055}\right)^{2.4} - \left(\dfrac{C_B + 0.055}{1.055}\right)^{2.4}}$$

where $0 \leq c_F \leq 1$, $0 \leq c_B \leq 1$ and $0 \leq \alpha \leq 1$.

Particular cases

If $C_F = 0$ (black) and $C_B = 1$ (white),

$$\alpha_{linear} = \frac{1}{0.9991662}\left[1 - \left(\frac{1 - \alpha_{sRGB} + 0.055}{1.055}\right)^{2.4}\right]$$

If $C_F = 1$ (white) and $C_B = 0$ (black),

$$\alpha_{linear} = \frac{1}{0.9991662}\left[\left(\frac{\alpha_{sRGB} + 0.055}{1.055}\right)^{2.4} - 0.0008338\right]$$