Convolutional & Denoising Autoencoders

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The insights, Convolutional Neural Networks, suggest we incorporate convolutional layers into the autoencoder to extract information characteristic of the grid-like structure of image data. Source: https: //blog.keras.io/building-autoencoders-in-keras.html

Imports & Settings

```
from os.path import join
import pandas as pd
import numpy as np
from numpy.random import choice
from numpy.linalg import norm
import seaborn as sns
import matplotlib.pyplot as plt
from matplotlib.colors import ListedColormap
from matplotlib.offsetbox import AnnotationBbox, OffsetImage
from mpl toolkits.axes grid1 import make axes locatable
from keras.layers import Input, Dense, Conv2D, MaxPooling2D, UpSampling2D
from keras import regularizers
from keras.models import Model, model from ison
from keras.callbacks import TensorBoard, EarlyStopping, ModelCheckpoint
from keras.datasets import fashion mnist
from keras import backend as K
from sklearn.preprocessing import minmax scale
from sklearn.manifold import TSNE
from sklearn.model selection import train test split
from scipy.spatial.distance import pdist, cdist Using TensorFlow backend. %matplotlib inline
plt.style.use('ggplot')
n classes = 10 \# all \ examples \ have \ 10 \ classes
cmap = sns.color palette('Paired', n classes)
pd.options.display.float format = '\{:,.2f\}'.format
Fashion MNIST Data
(X train, y train), (X test, y test) = fashion mnist.load data() X train.shape, X test.shape ((60000,
```

```
28, 28), (10000, 28, 28)) class dict = {0: 'T-shirt/top',
1: 'Trouser',
2: 'Pullover',
3: 'Dress',
4: 'Coat',
5: 'Sandal',
6: 'Shirt',
7: 'Sneaker',
8: 'Bag',
9: 'Ankle boot'}
classes = list(class dict.keys())
```

Reshape & normalize Fashion MNIST data

```
image_size = 28 def data_prep_conv(x, size=image_size):

return x.reshape(-1, size, size, 1).astype('float32')/255 X_train_scaled = data_prep_conv(X_train)

X_test_scaled = data_prep_conv(X_test) X_train_scaled.shape, X_test_scaled.shape ((60000, 28, 28, 1), (10000, 28, 28, 1))
```

Combine training steps into function

```
\label{eq:def-train} \begin{tabular}{ll} $\operatorname{def-train}_{\operatorname{autoencoder}}(\operatorname{path,\ model},\ x\_\operatorname{train}=X\_\operatorname{train}_{\operatorname{scaled}},\ x\_\operatorname{test}=X\_\operatorname{test}_{\operatorname{scaled}})$: $\operatorname{callbacks} = [\operatorname{EarlyStopping}(\operatorname{patience}=5,\ \operatorname{restore}_{\operatorname{best}}_{\operatorname{weights}}=\operatorname{True})$, $\operatorname{ModelCheckpoint}(\operatorname{filepath}=\operatorname{path},\ \operatorname{save}_{\operatorname{best}}_{\operatorname{only}}=\operatorname{True},\ \operatorname{save}_{\operatorname{weights}}_{\operatorname{only}}=\operatorname{True})]$ $\operatorname{model.fit}(x=x\_\operatorname{train},\ y=x\_\operatorname{train},\ \operatorname{epochs}=100,\ \operatorname{validation}_{\operatorname{split}}=.1,\ \operatorname{callbacks}=\operatorname{callbacks})$ $\operatorname{model.load}_{\operatorname{weights}}(\operatorname{path})$ $\operatorname{mse} = \operatorname{model.evaluate}(x=x\_\operatorname{test},\ y=x\_\operatorname{test})$ $\operatorname{return\ model},\ \operatorname{mse}$
```

Convolutional Autoencoder

We define a three-layer encoder that uses 2D convolutions with 32, 16, and 8 filters, respectively, ReLU activations, and 'same' padding to maintain the input size. The resulting encoding size at the third layer is 4x4x8, higher than for the preceding examples:

3-dim input

```
input = Input(shape=(28, 28, 1), name='Input 3D')
```

Encoding Layers

```
x = Conv2D(filters=32, kernel_size = (3, 3), activation =' relu', padding='same', name='Encoding_Conv_1')(input_)

x = MaxPooling2D(pool_size=(2, 2), padding='same', name='Encoding_Max_1')(x)

x = Conv2D(filters=16, kernel_size = (3, 3), activation =' relu', padding='same', name='Encoding_Conv_2')(x)

x = MaxPooling2D(pool_size=(2, 2), padding='same', name='Encoding_Max_2')(x)

x = Conv2D(filters=8, kernel_size = (3, 3), activation =' relu', padding='same', name='Encoding_Conv_3')(x)

encoded_conv = MaxPooling2D(pool_size=(2, 2), padding='same', name='Encoding_Max_3')(x)

WARNING:tensorflow:From /home/stefan/.pyenv/versions/miniconda3-latest/envs/ml4t/lib/python3.6/site-packages/tensorflow/python/framework/op_def_library.py:263: colocate_with (from tensorflow.python.framework.ops) is deprecated and will be removed in a future version.

Instructions for updating:
```

Colocations handled automatically by placer. We also define a matching decoder that reverses the number of filters and uses 2D upsampling instead of max pooling to reverse the reduction of the filter sizes. The three-layer autoencoder has 12,785 parameters, a little more than 5% of the capacity of the preceding deep autoencoder. $x = \text{Conv2D}(\text{filters=8, kernel}_size = (3,3), activation = 'relu', padding='same', name='Decoding Conv 1')(encoded)$

```
 \begin{split} \mathbf{x} &= \mathbf{UpSampling2D}(\mathbf{size=(2, 2)}, \, \mathbf{name='Decoding\_Upsample\_1'})(\mathbf{x}) \\ \mathbf{x} &= \mathbf{Conv2D}(\mathbf{filters=16}, \, \mathbf{kernel_size} = (3, 3), \, activation =' \, relu', \, padding='\mathbf{same'}, \, \mathbf{name='Decoding\_Conv\_2'})(\mathbf{x}) \\ \mathbf{x} &= \mathbf{UpSampling2D}(\mathbf{size=(2, 2)}, \, \mathbf{name='Decoding\_Upsample\_2'})(\mathbf{x}) \\ \mathbf{x} &= \mathbf{Conv2D}(\mathbf{filters=32}, \, \mathbf{kernel_size} = (3, 3), \, activation =' \, relu', \, name='\mathbf{Decoding\_Conv\_3'})(\mathbf{x}) \\ \end{split}
```

```
x = UpSampling2D(size=(2, 2), name='Decoding Upsample 3')(x)
      decoded conv = Conv2D(filters=1, kernel size=(3, 3), activation='sigmoid', padding='same', name='Decoding Conv
      autoencoder conv = Model(input , decoded conv)
autoencoder conv.compile(optimizer='adam', loss='mse')
      autoencoder conv.summary()
Layer (type)
                                                 Output Shape
                                                                                                  Param #
Input 3D (InputLayer)
                                                          (None, 28, 28, 1)
                                                                                                        0
Encoding Conv 1 (Conv2D)
                                                                  (None, 28, 28, 32)
                                                                                                                320
Encoding Max 1 (MaxPooling2D (None, 14, 14, 32)
                                                                                                                    0
Encoding Conv 2 (Conv2D)
                                                                 (None, 14, 14, 16)
                                                                                                                4624
Encoding Max 2 (MaxPooling2D (None, 7, 7, 16)
                                                                                                                   0
Encoding Conv 3 (Conv2D)
                                                                  (None, 7, 7, 8)
                                                                                                              1160
Encoding Max 3 (MaxPooling2D (None, 4, 4, 8)
                                                                                                                  0
Decoding Conv 1 (Conv2D)
                                                                                                              584
                                                                  (None, 4, 4, 8)
Decoding Upsample 1 (UpSampl (None, 8, 8, 8)
                                                                                                                 0
Decoding Conv 2 (Conv2D)
                                                                  (None, 8, 8, 16)
                                                                                                               1168
Decoding Upsample 2 (UpSampl (None, 16, 16, 16)
                                                                                                                    0
Decoding Conv 3 (Conv2D)
                                                                 (None, 14, 14, 32)
                                                                                                                4640
Decoding Upsample 3 (UpSampl (None, 28, 28, 32)
                                                                                                                    0
Decoding Conv 4 (Conv2D)
                                                                  (None, 28, 28, 1)
                                                                                                                289
Total params: 12,785
Trainable params: 12,785
Non-trainable params: 0
 path = 'models/fashion mnist.autencoder conv.32.weights.hdf5' autoencoder conv, mse = train autoencoder(path,
autoencoder conv,
x_train=X_train_scaled,
x test=X test scaled)
      WARNING: tensorflow: From / home/stefan/.pyenv/versions/miniconda3-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/site-latest/envs/ml4t/lib/python3.6/si
packages/tensorflow/python/ops/math ops.py:3066: to int32 (from tensorflow.python.ops.math ops) is
deprecated and will be removed in a future version.
Instructions for updating:
Use tf.cast instead.
Train on 54000 samples, validate on 6000 samples
Epoch 1/100
54000/54000 [=
                                                                                    0.0160
```

Epoch 2/100

Denoising Autoencoder

The application of an autoencoder to a denoising task only affects the training stage. In this example, we add noise to the Fashion MNIST data from a standard normal distribution while maintaining the pixel values in the range of [0, 1], as follows: def add_noise(x, noise_factor=.3):

 $\begin{array}{l} \textbf{return} \ np. clip(x \ + noise_factor * np. random. normal(size=x.shape), 0, 1) \ X_train_noisy = add_noise(X_train_scaled) \\ X_test_noisy = add_noise(X_test_scaled) \end{array}$

```
fig, axes = plt.subplots(nrows=2, ncols=5, figsize=(20, 4))
```

axes = axes.flatten()

for i, ax in enumerate(axes):

ax.imshow(X_test_noisy[i].reshape(28, 28), cmap='gray')
ax.axis('off')











```
x = \text{Conv2D}(\text{filters}=32, \text{kernel}_size = (3, 3), activation = 'relu', padding='same', name='Encoding Conv 1')(input)
     x = MaxPooling2D(pool size=(2, 2), padding='same', name='Encoding Max 1')(x)
x = \text{Conv2D}(\text{filters} = 16, \text{kernel}_{s}ize = (3, 3), activation = 'relu', padding = 'same', name = 'Encoding Conv 2')(x)
     encoded conv = MaxPooling2D(pool size=(2, 2), padding='same', name='Encoding Max 2')(x)
     x = \text{Conv2D}(\text{filters}=16, \text{kernel}_size = (3, 3), activation = 'relu', paddinq='same', name='Decoding Conv 1')(encoded converged to the 
     x = UpSampling2D(size=(2, 2), name='Decoding Upsample 1')(x)
     x = \text{Conv2D}(\text{filters}=32, \text{kernel}_size = (3, 3), activation = 'relu', padding='same', name='Decoding Conv 2')(x)
     x = UpSampling2D(size=(2, 2), name='Decoding Upsample 2')(x)
decoded conv = Conv2D(filters=1, kernel size=(3, 3), activation='sigmoid', padding='same', name='Decoding Conv 3')(
     autoencoder denoise = Model(input , decoded conv)
autoencoder denoise.compile(optimizer='adam', loss='mse')
     path = 'models/fashion mnist.autencoder denoise.32.weights.hdf5'
     callbacks = [EarlyStopping(patience=5, restore best weights=True),
ModelCheckpoint(filepath=path, save best only=True, save weights only=True)]
     We then proceed to train the convolutional autoencoder on noisy input with the objective to learn how
to generate the uncorrupted originals: autoencoder denoise.fit(x=X train noisy,
y=X train scaled,
epochs=100,
batch size=128,
shuffle=True,
validation split=.1,
callbacks=callbacks)
     Train on 54000 samples, validate on 6000 samples
Epoch 1/100
0.0158
[... training log continues ...]
Epoch 70/100
0.0085 < keras.callbacks.History at 0x7f2a0d71a400> autoencoder denoise.load weights(path) mse = au-
toencoder denoise.evaluate(x=X test noisy, y=X test scaled)
- 1s 106us/step 'MSE: 0.0086 | RMSE 0.0925'
Visualize Reconstructed Images
```

The following figure shows, from top to bottom, the original images as well as the noisy and denoised versions. It illustrates that the autoencoder is successful in producing compressed encodings from the noisy images that are quite similar to those produced from the original images: reconstructed_images = autoencoder_denoise.predict(X_test_noisy)

reconstructed_images_shape__(10000_28_28_1)__fig__axes = plt_subplots(ncols=n_classes_prows=3_fig-

```
coder_denoise.predict(X_test_noisy)
reconstructed_images.shape (10000, 28, 28, 1) fig, axes = plt.subplots(ncols=n_classes, nrows=3, fig-
size=(20, 6))
for i in range(n_classes):
axes[0, i].imshow(X_test[i].reshape(image_size, image_size), cmap='gray')
axes[0, i].axis('off')

axes[1, i].imshow(X_test_noisy[i].reshape(image_size, image_size), cmap='gray')
axes[1, i].axis('off')
```

 $axes[2,\,i].imshow(reconstructed_images[i].reshape(image_size,\,image_size)\;,\;cmap='gray')\;axes[2,\,i].axis('off')$

fig.suptitle('Originals, Corrupted and Reconstructed Images', fontsize=20)

fig.tight_layout()

fig.subplots_adjust(top=.9)

fig.savefig('figures/autoencoder_denoising', dpi=300)

Originals, Corrupted and Reconstructed Images

