

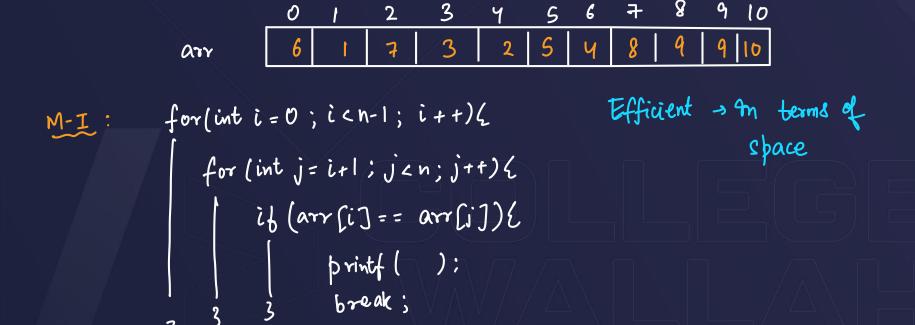
## Sorting Algorithms



## Today's Checklist

- Time Complexity
- 2 Pointer approach
- Bubble sort
- Selection sort
- Insertion sort

Ques: Given an array of integers with 1 to n elements and the size of the array if n+1. One element is occurring more than once i.e duplicate number is present. Find the duplicate element.





M-2 brr

visited array

Efficient = In terms of time ..

Not Efficient - In terms of space - O(n) Extra space

We are using extra space

M-3

										9 10
aty	6	1	7	3	2	5	4	8	9	9 10

Sum of numbers from 1 to 10 
$$\Rightarrow$$
  $\frac{|0 \times 1|}{2} = 55$ 

$$S_n = n(n+1) \qquad 64-SS = \boxed{9}$$

Efficient in terms of time & space both

3<sup>rd</sup> gen i3



3 gen i3



Time Complexity

Space Comparity

TLE > stime limit exceeded

for (int i=0; i<n; i++){ print f (" Hello"); n operations  $\rightarrow O(n)$ for (int i = -2; i < n; i++){ print f (" Kello");  $n+3 \rightarrow O(n+3) \sim O(n)$ 

$$O(n+a) \simeq O(n)$$
constant

Big O Notation?

for (int 
$$i=1$$
;  $i \leq 3^{4}n$ ;  $i+1$ )  $i \neq 1$ ;  $i \neq 1$ ;  $i \neq 1$ ;  $i \neq 1$ )  $i \neq 1$ ;  $i \neq 1$ ;

for (int 
$$i = 1$$
;  $i \le n$ ;  $i + t \ne 1$ )  
for (int  $j = 10$ ;  $j \le n$ ;  $j + t \ne 1$ )  
 $j \le n$ ;  $j \ne t \ne 1$ )  
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Q,

Q, for (int 
$$i = 1$$
;  $i \le n$ ;  $i+t$ )  $\begin{cases} 0(n(\frac{n+1}{2})) = 0(\frac{n^2}{2} + \frac{n}{2}) \\ for (int  $j = 1$ ;  $j \le i$ ;  $j+t$ )  $\end{cases} = 0(\frac{1}{2}n^2 + \frac{1}{2}n)$ 

| print  $f((n^2))$ ;

|  $\frac{3}{2}$  print  $f((n^2))$ ;

|  $\frac{3}{2}$  print  $\frac{n(n+1)}{2}$  operations
|  $\frac{n(n+1)}{2}$  operations$ 

i=1 → j=1 ton

$$O(3n^3 + 2n^2 + 8n) \approx O(n^3 + n^2 + n) \approx O(n^3)$$

$$0 (n^{3/2} + n + 1) \approx 0(n^{3/2})$$

Extra Space: 'n' size array, n' size array, 
$$\frac{n}{2}$$
 size  $\rightarrow$  5 size array  $\rightarrow$   $\times$ 

What is Sorting:

9 1 2 8 6 4

1 2 4 6 8 9

Sort + put in ascending order

Sort in + put in decreasing descending order

\*2-pointers - algorithme

Ques: Given an array of integers numbers that is already sorted in non-decreasing order, find two numbers such that they add up to a specific target number.

comparisms

int target = 8 int arrs ] = int i= 0; int j = n-1;

```
2 3 4
                              - max - 2h
       3 4 5
if (arr[i] + arr[i] = = target) {
2 11 found
 if (arr(i) + arr(i) > target) 4
     1--; // to decrease
  if (arr [i] + arr [i] x target) 4
  3 i++; // to increase
```

```
int i = 0; O(n)

int j = n-1;

while (i < j)?

if (arr[i] + arr[j] = target)?
```

```
printf ( )
break;
else if (arr[i] + arr[i] > target) j--;
Else i++;
```

Bubble Sort :

9 1 3 4 10 5 6 Original

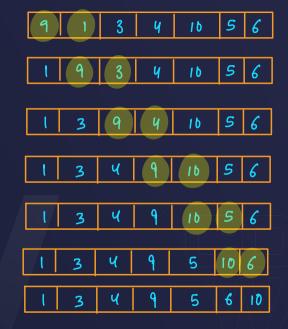
1 3 4 5 6 4 10 Sorted

1) Technique

4) Complexities

- 2) Enplanation
- 3) Optimization

arr



Swap (arr[i], arr[i+1])

original

Pau-2

Sorbed abready 1 3 4 5 6 9 10



5 4 3 2 1

4 5 3 2 1

4 3 5 2 1

4 3 2 5 1

4 3 2 1 5

4 3 2 1 5

3 4 2 1 5

3 2 4 1 5

3 2 1 4 5

yth Pas

3 2 1 4 5 2 3 1 4 5 2 1 3 4 5

1 2 3 4 5

- . 'n' elemente in the away -> 'n-1' passes
- · After every poss, we need to apply bulble sort on the unsorted elements only be we do not need to check the 'Dangest'

### Coding implementation of bubble sort

```
Nested Loops

( ) Outer loop will storned for no. of posses

I snow loop will do the swapping
```

```
// bubble sort
for(int i=0;i<n-1;i++){
    for(int j=0;j<n-1;j++){
        if(arr[j]>arr[j+1]){
            int temp = arr[j];
            arr[j] = arr[j+1];
            arr[j+1] = temp;
        }
}
```

```
j = 0 to n-1-i
```

## Time complexity

```
// bubble sort
for(int i=0;i<n-1;i++){
    for(int j=0;j<n-1-i;j++){
        if(arr[j]>arr[j+1]){
            int temp = arr[j];
            arr[j] = arr[j+1];
            arr[j+1] = temp;
```

```
Outer Loop - 0 = i sn-2 - n-1
                            boar dhologa
 Inner Loop
i=0 -> n-1 bour
i=1 -> n-2 baar
i=2 \rightarrow n-3 boar
i= 4 - n-4 boar
```

$$n \circ Ops = n-1 + n-2 + n-3 + n-4 + \cdots + 2 + 1$$

$$= (n-1)^{*}n \rightarrow O(\frac{n^{2}}{2} - \frac{n}{2}) \approx O(\frac{n^{2}}{2}) \approx O(n^{2})$$

## Maximum no of swaps in worst case in Bubble Sort

descending



## How to optimize the bubble sort in the case of nearly sorted arrays?

```
Check if array after every pass is already sorted or not.

I with the help of a checkmark.
```

🕼 skills

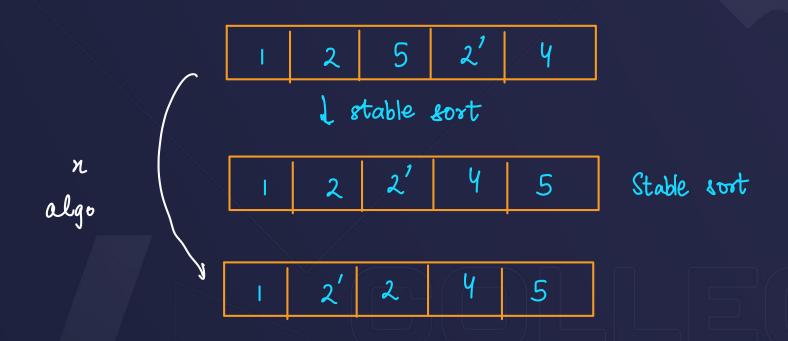
## Time Complexity of Bubble Sost in best case: flag = true; n -> n-1 $O(n-1) \approx O(n)$

log = true,

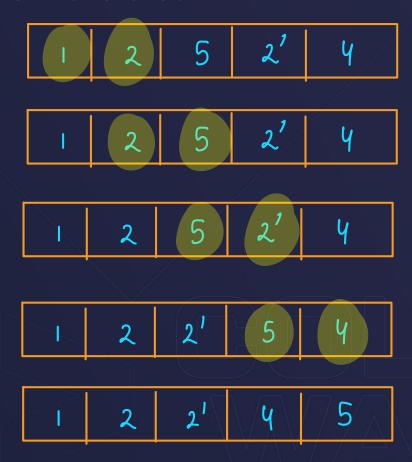
	Time Compleni	Space Complexity
Best Case	0(n)	0(1)
Avg. Case	0 (n²)	0(1)
Worst Care	0(n²)	0(1)



#### Is Bubble Sort Stable? Yes



#### Is Bubble Sort Stable?





## Ques: What is the best case time and space complexity of bubble sort:

- a) O(1) & O(1)
- b) O(n) & O(1)
- c) O(n) & O(n)
- d) O(logn) & O(1)



# Ques: Given an array of 6 elements, what is the max number of swaps we need to sort the array:

```
a) 21b) 15c) 10d) 28
```

```
654321
1
1-1+1-2+1-3+2+1=15
```

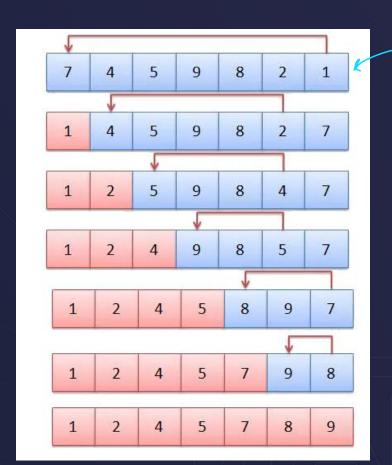
Bubble Sort - Unsorted array - ascending order

32514 - 54321

Q, Sort in descending order.

#### **Selection sort**

red - sorted part
blue - unsorted
pant



nuin clement

### Coding implementation of selection sort

bas-1 3 4 5 paus - 2 5 bass - 3 5 pass - 4 3 2

#### Observations:

- · For 'n' elements we need 'n-1' passes.
- In each pass we find out the unsorted part.
- After every pass the unsorted array reduces by 1 length.

5

```
i = 0 to 3
// selection sort
for(int i=0;i<n-1;i++){ // n-1 passes</pre>
   int min = INT MAX;
   int minidx = -1;
   for(int j=i;j<=n-1;j++){
       if(min>arr[j]){
                             i=01
           min = arr[j];
           minidx = j;
   int temp = arr[minidx];
   arr[minidx] = arr[i];
   arr[i] = temp;
   min = Int-Max 8 132/ Int Max 2
```

```
3
```

R SKILLS

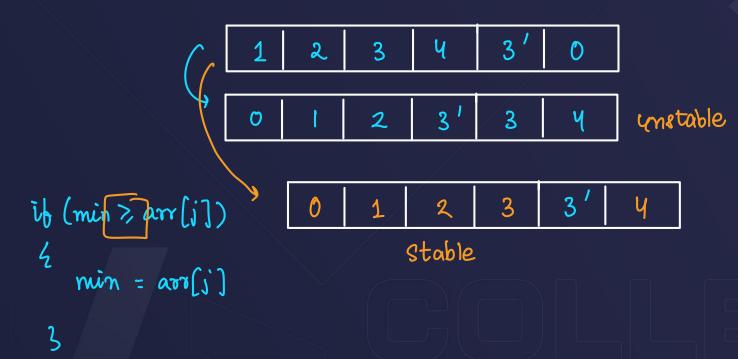
minidx = + \$1 x B A -13

### Time complexity

no of ope > 
$$n + n-1 + n-2 + ... + 2 + 1 = n(n+1) = n(n+$$



#### Is selection sort stable? No





## Ques: What will the array look like after the first iteration of selection sort [2,3,1,6,4]?

- a) [1,2,3,6,4]
- b) [1,3,2,4,6]
- **(c)** [1,3,2,6,4]
- d) [2,3,1,4,6]



## Ques: Which of the following is an advantage of selection sort over bubble sort:

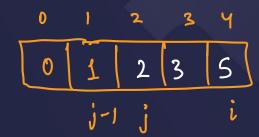
- a) It has a worst case complexity which is better than that of bubble sort.
- b) It takes O(N) swaps while the other techniques take O(N^2) swaps.
- c) The cost of swapping is an issue.
- d) All of these.

#### Insertion Sort: st Swapping from End ties the element finds its position. ~ml 3 Swap happens only when the uth element is smaller than its left clement 3

#### Best Case for Amertin Sort:

#### Coding implementation of insertion sort

· No of passes > n-1 basses for (int i=1; i <= n-1; i++){ int j = i; while ( j > 1 ll arr[j] < arr[j-1]) { Swap (arr [j], arr [j-1]);



### Time complexity

Worst Case - 
$$O(n^2)$$
  
Avg. Case -  $O(n^2)$   
Best Case -  $O(n)$ 



### Is Insertion Sort Stable? - Yes!!





# Ques: Which of the following examples represent the worst case input for an insertion sort?

- a) array in sorted order
- b) large array
- c) normal unsorted array
- d) array sorted in reverse order



Ques: How many passes would be required during insertion sort to sort an array of 5 elements?

- **a)** 1
- b) Depends on order of elements
- **9** 4
- d) 5

"Ques: Given an integer array arr, move all 0's to the end of it while maintaining the relative order of the non-zero elements.

T. 
$$C = O(n)$$
  
 $S \cdot C \cdot = O(n)$ 

Ques: Given an integer array arr, move all 0's to the end of it while maintaining the relative order of the non-zero elements.

Note that you must do this in-place without making a copy of the array.

Hint: Bubble Sort, Sort mat socho

arr 5 2 4 1 3 0 0 0 0

```
for (int i=0; i(n-1; i++){
   for (int j = 0; j < n-1-i; j++)&
if (arr[j] == 0) {

| Swap(arr[j], arr[j+1]);

3
```

5

Homework

🛞 skills

Ques: Given an integer array and an integer k where k <= size of array, We need to return the kth smallest element of the array.

5 2 1 3 4 n=5 K=3

0(K)

Ques: Given an array of digits (values are from 0 to 9), the task is to find the minimum possible sum of two numbers formed from digits of the array.

Please note that all digits of the given array must be used to form the two numbers.

5 3 1 2 45 12345 min no. 12535 12354 Sec. min no.

Homework: If last two index clements are same then?