

CSC148H Week 4

January 28, 2015

Announcements

- ▶ Assignment 1 - due next week, February 4 at 22:00
 - ▶ What is an anagram?
 - ▶ Can you redo before an undo?
 - ▶ Note: All assignments will be checked for plagiarism.
- ▶ Quiz 1 - this Friday during lecture. Please bring a pen!
 - ▶ 15 minutes
 - ▶ Content covered: week 1 up to and including week 3
 - ▶ Short answer questions (correction, no multiple choice)

Summing a Nested List

Let's write a recursive function to sum all items in a list with n nested lists. We're going to solve this without using `flatten`.

- ▶ What is the base case?
- ▶ What is the recursive structure?

```
def sumlist(lst):  
    '''(list of int) -> int  
    lst is arbitrarily nested.  
    Return the sum of lst.  
  
    >>> sumlist([1, 2, [3, [4]], 5])  
    15  
    '''
```

Summing a Nested List, Base Case

```
def sumlist(lst):  
    '''(list of int) -> int  
    lst is arbitrarily nested.  
    Return the sum of lst.  
  
    >>> sumlist([1,2,[3,[4]],5])  
    15  
    '''  
  
    total = 0  
  
    for i in lst:  
        total += i  
    return total
```

Summing a Nested List...

```
def sumlist(lst):  
    '''(list of int) -> int  
    lst is arbitrarily nested.  
    Return the sum of lst.  
  
    >>> sumlist([1,2,[3,[4]],5])  
    15  
    ''',  
  
    total = 0  
  
    for i in lst:  
        if isinstance(i, list):  
            total += sumlist(i)  
        else:  
            total += i  
  
    return total
```

Summing a Nested List...

Evaluate when `lst = [1, 2, [3, [4]], 5]`

`sumlist([1, 2, [3, [4]], 5])`

```
def sumlist(lst):  
    '''(list of int) -> int  
  
    lst is arbitrarily nested.  
    Return the sum of lst.  
  
>>> sumlist([1, 2, [3, [4]], 5])  
  
15  
'''  
  
total = 0  
  
for i in lst:  
    if isinstance(i, list):  
        total += sumlist(i)  
    else:  
        total += i  
  
return total
```

`[1, 2, [3, [4]], 5]`
↓

```
def sumlist(lst):  
    '''(list of int) -> int  
  
    lst is arbitrarily nested.  
    Return the sum of lst.  
  
>>> sumlist([1, 2, [3, [4]], 5])  
  
15  
'''  
  
total = 0  
  
1 → for i in lst:  
    if isinstance(i, list):  
        total += sumlist(i)  
    else:  
        total += i  
  
return total
```

`total = 1` → `total += i`

Summing a Nested List...

Evaluate when lst = [1, 2, [3, [4]], 5]

sumlist([1, 2, [3, [4]], 5])

[1, 2, [3, [4]], 5]

def sumlist(lst):

'''(list of int) -> int

lst is arbitrarily nested.

Return the sum of lst.

>>> sumlist([1, 2, [3, [4]], 5])

15

'''

total = 0

2 → [1, 2, [3, [4]], 5]

for i in lst:

if isinstance(i, list):

total += sumlist(i)

else:

total = 3 → total += i

return total

Evaluate when lst = [1, 2, [3, [4]], 5]

sumlist([1, 2, [3, [4]], 5])

[1, 2, [3, [4]], 5]

def sumlist(lst):

'''(list of int) -> int

lst is arbitrarily nested.

Return the sum of lst.

>>> sumlist([1, 2, [3, [4]], 5])

15

'''

total = 0

[3, [4]] → [1, 2, [3, [4]], 5]

for i in lst:

if isinstance(i, list):

sumlist([3, [4]])

total += sumlist(i)

else:

total += i

return total

Summing a Nested List...

Evaluate when lst = [1, 2, [3, [4]], 5]

sumlist([1, 2, [3, [4]], 5])

[3, [4]]
↓
def sumlist(lst):
 """(list of int) -> int

 lst is arbitrarily nested.
 Return the sum of lst.

 >>> sumlist([1, 2, [3, [4]], 5])

 15
 """

 total = 0

 3 → for i in lst:
 ↓ [3, [4]]
 if isinstance(i, list):
 total += sumlist(i)
 else:
 total += i
 return total ← total = 3

Evaluate when lst = [1, 2, [3, [4]], 5]

sumlist([1, 2, [3, [4]], 5])

[3, [4]]
↓
def sumlist(lst):
 """(list of int) -> int

 lst is arbitrarily nested.
 Return the sum of lst.

 >>> sumlist([1, 2, [3, [4]], 5])

 15
 """

 total = 0

 [4] → for i in lst:
 ↓ [3, [4]]
 if isinstance(i, list):
 ↓ sumlist([4])
 total += sumlist(i)
 else:
 total += i
 return total

Summing a Nested List...

Evaluate when `lst = [1, 2, [3, [4]], 5]`

`sumlist([1, 2, [3, [4]], 5])`

`[4]`
↓
`def sumlist(lst):`
 `'''(list of int) -> int`
 `lst is arbitrarily nested.`
 `Return the sum of lst.`
`>>> sumlist([1, 2, [3, [4]], 5])`
`15`
`'''`
`total = 0`

`4` →
↓
`for i in lst:`
 `if isinstance(i, list):`
 `total += sumlist(i)`
 `else:`
`total = 4` → `total += i`
 `return total` ← `total = 4`

Evaluate when `lst = [1, 2, [3, [4]], 5]`

`sumlist([1, 2, [3, [4]], 5])`

`[3, [4]]`
↓
`def sumlist(lst):`
 `'''(list of int) -> int`
 `lst is arbitrarily nested.`
 `Return the sum of lst.`
`>>> sumlist([1, 2, [3, [4]], 5])`
`15`
`'''`
`total = 0`

`[4]` → `[3, [4]]` →
↓ ↓
`for i in lst:`
 `if isinstance(i, list):` → `sumlist([4]) = 4`
 `total += sumlist(i)`
 `else:`
 `total += i`
 `return total`

Summing a Nested List...

Evaluate when `lst = [1, 2, [3, [4]], 5]`

`sumlist([1, 2, [3, [4]], 5])`

`[1, 2, [3, [4]], 5]`

`def sumlist(lst):`

`'''(list of int) -> int`

`lst is arbitrarily nested.`

`Return the sum of lst.`

`>>> sumlist([1, 2, [3, [4]], 5])`

`15`

`'''`

`total = 0`

`[3, [4]]` → `[1, 2, [3, [4]], 5]`

`for i in lst:`

`if isinstance(i, list):`

`total += sumlist(i)` `sumlist([3, [4]]) = 7`

`else:`

`total += i`

`return total`

Evaluate when `lst = [1, 2, [3, [4]], 5]`

`sumlist([1, 2, [3, [4]], 5])`

`[1, 2, [3, [4]], 5]`

`def sumlist(lst):`

`'''(list of int) -> int`

`lst is arbitrarily nested.`

`Return the sum of lst.`

`>>> sumlist([1, 2, [3, [4]], 5])`

`15`

`'''`

`total = 0`

`5` → `[1, 2, [3, [4]], 5]`

`for i in lst:`

`if isinstance(i, list):`

`total += sumlist(i)`

`else:`

`total = 15` → `total += i`

`return total` ← `total = 15`

Summing a Nested List...Let's Use Exceptions

```
def sumlist(lst):  
    '''(list of int) -> int  
    lst is arbitrarily nested.  
    Return the sum of lst.  
  
    >>> sumlist([1,2,[3,[4]],5])  
    15  
    '''  
  
    total = 0  
  
    for i in lst:  
        try:  
            total += i  
        except TypeError:  
            total += sumlist(i)  
    return total
```

Removing 3s

Let's write a recursive function to return a new list with all elements of a list except the 3s.

- ▶ What is the base case?
- ▶ What is the recursive structure?

```
def remove_three(lst):
```

```
    '''(list of int) -> list of int
```

```
    Return a new list with all elements of lst except the 3s.
    lst has no nesting.
```

```
>>> remove_three([1, 2, 3, 3, 4])
[1, 2, 4]
'''
```

Removing 3s, Base Case

```
def remove_three(lst):  
    '''(list of int) -> list of int
```

*Return a new list with all elements of lst except the 3s.
lst has no nesting.*

```
>>> remove_three([1, 2, 3, 3, 4])  
[1, 2, 4]  
'''
```

```
if len(lst) == 0:  
    return []
```

Removing 3s...

```
def remove_three(lst):  
    '''(list of int) -> list of int  
  
    Return a new list with all elements of lst except the 3s.  
    lst has no nesting.  
  
    >>> remove_three([1, 2, 3, 3, 4])  
    [1, 2, 4]  
    '''  
    if len(lst) == 0:  
        return []  
  
    if lst[0] == 3:  
        return remove_three(lst[1:])  
    else:  
        return [lst[0]] + remove_three(lst[1:])
```

Removing 3s In A Nested List

Let's revisit our previous example, except this time our list can contain nested lists. The goal is to write a recursive function to return a new list with all elements of a list except the 3s.

- ▶ What is the base case?
- ▶ What is the recursive structure?

```
def remove_three_nested(lst):  
    '''(list of int) -> list of int
```

*Return a new list with all elements of lst except the 3s.
lst may have nesting to arbitrary depth.*

```
>>> remove_three_nested([1, [2, 3], 3, 4])  
[1, [2], 4]  
,,,
```

Removing 3s In A Nested List, Base Case

```
def remove_three_nested(lst):  
    '''(list of int) -> list of int
```

*Return a new list with all elements of lst except the 3s.
lst may have nesting to arbitrary depth.*

```
>>> remove_three_nested([1, [2, 3], 3, 4])  
[1, [2], 4]  
,,,
```

```
no_three = []  
for element in lst:  
    if isinstance(element, int):  
        if element != 3:  
            no_three.append(element)  
return no_three
```


Removing 3s In A Nested List...

```
def remove_three_nested(lst):  
    '''(list of int) -> list of int
```

*Return a new list with all elements of lst except the 3s.
lst may have nesting to arbitrary depth.*

```
>>> remove_three_nested([1, [2, 3], 3, 4])  
[1, [2], 4]  
,,,
```

```
no_three = []  
for element in lst:  
    if isinstance(element, int):  
        if element != 3:  
            no_three.append(element)  
    else:  
        no_three.append(remove_three_nested(element))  
return no_three
```

Removing 3s In A Nested List...

Evaluate when lst is [1, [2, 3], 3, 4]

remove_three_nested([1, [2, 3], 3, 4])

```
def remove_three_nested(lst):
```

```
    """(list of int) -> list of int
```

```
    Return a new list with all elements of lst except the 3s.
```

```
    lst may have nesting to arbitrary depth.
```

```
>>> remove_three_nested([1, [2, 3], 3, 4])
```

```
[1, [2], 4]
```

```
"""
```

```
no_three = []
```

```
for element in lst:
```

```
    if isinstance(element, int):
```

```
        if element != 3:
```

```
            no_three.append(element)
```

```
    else:
```

```
        no_three.append(remove_three_nested(element))
```

```
return no_three
```

[1, [2, 3], 3, 4]



```
def remove_three_nested(lst):
```

```
    """(list of int) -> list of int
```

```
    Return a new list with all elements of lst except the 3s.
```

```
    lst may have nesting to arbitrary depth.
```

```
>>> remove_three_nested([1, [2, 3], 3, 4])
```

```
[1, [2], 4]
```

```
"""
```

```
no_three = []
```

1

```
for element in lst:
```

```
    if isinstance(element, int):
```

```
        if element != 3:
```

```
            no_three.append(element)
```

```
    else:
```

```
        no_three.append(remove_three_nested(element))
```

```
return no_three
```

Removing 3s In A Nested List...

[1, [2, 3], 3, 4]
↓
`def remove_three_nested(lst):`
'''(list of int) -> list of int
Return a new list with all elements of lst except the 3s.
lst may have nesting to arbitrary depth.
>>> remove_three_nested([1, [2, 3], 3, 4])
[1, [2], 4]
'''
no_three = []

[2, 3] ————— **[1, [2, 3], 3, 4]**
↓ ↓
`for element in lst:`
 `if isinstance(element, int):`
 `if element != 3:`
 `no_three.append(element)`
`else:` ↓ **remove_three_nested([2, 3])**
 `no_three.append(remove_three_nested(element))`
`return no_three`

[2, 3]
↓
`def remove_three_nested(lst):`
'''(list of int) -> list of int
Return a new list with all elements of lst except the 3s.
lst may have nesting to arbitrary depth.
>>> remove_three_nested([1, [2, 3], 3, 4])
[1, [2], 4]
'''
no_three = []

2 ————— **[2, 3]**
↓ ↓
`for element in lst:`
 `if isinstance(element, int):`
 `if element != 3:`
 ↓ **[2]**
 `no_three.append(element)`
`else:`
 `no_three.append(remove_three_nested(element))`
`return no_three`

Removing 3s In A Nested List...

[2, 3]
↓

```
def remove_three_nested(lst):  
    '''(list of int) -> list of int  
    Return a new list with all elements of lst except the 3s.  
    lst may have nesting to arbitrary depth.  
    >>> remove_three_nested([1, [2, 3], 3, 4])  
    [1, [2], 4]  
    '''  
    no_three = []
```

3 ——— **[2, 3]**
↓ ↓
for element in lst:
 if isinstance(element, int):
 if element != 3:
 no_three.append(element)
 else:
 no_three.append(remove_three_nested(element))
return no_three

[1, [2, 3], 3, 4]
↓

```
def remove_three_nested(lst):  
    '''(list of int) -> list of int  
    Return a new list with all elements of lst except the 3s.  
    lst may have nesting to arbitrary depth.  
    >>> remove_three_nested([1, [2, 3], 3, 4])  
    [1, [2], 4]  
    '''  
    no_three = []
```

[2, 3] ——— **[1, [2, 3], 3, 4]**
↓ ↓
for element in lst:
 if isinstance(element, int):
 if element != 3:
 no_three.append(element)
 else:
 no_three.append(remove_three_nested(remove_three_nested([2, 3]) = [2])
return no_three

Removing 3s In A Nested List...

`remove_three_nested([1, [2, 3], 3, 4]) = [1, [2], 4]`

`[1, [2, 3], 3, 4]`



```
def remove_three_nested(lst):
```

```
    """(list of int) -> list of int
```

```
    Return a new list with all elements of lst except the 3s.
```

```
    lst may have nesting to arbitrary depth.
```

```
>>> remove_three_nested([1, [2, 3], 3, 4])
```

```
[1, [2], 4]
```

```
"""
```

```
no_three = []
```

3

```
for element in lst:
```

```
    if isinstance(element, int):
```

```
        if element != 3:
```

```
            no_three.append(element)
```

```
    else:
```

```
        no_three.append(remove_three_nested(element))
```

```
return no_three
```

`[1, [2, 3], 3, 4]`



```
def remove_three_nested(lst):
```

```
    """(list of int) -> list of int
```

```
    Return a new list with all elements of lst except the 3s.
```

```
    lst may have nesting to arbitrary depth.
```

```
>>> remove_three_nested([1, [2, 3], 3, 4])
```

```
[1, [2], 4]
```

```
"""
```

```
no_three = []
```

4

```
for element in lst:
```

```
    if isinstance(element, int):
```

```
        if element != 3:
```

```
            no_three.append([1, [2], 4])
```

```
    else:
```

```
        no_three.append(remove_three_nested(element))
```

```
return no_three ← [1, [2], 4]
```