## CS – 204: Assignment 1

15 . 02 . 2021

Group 13

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- 1.  $L^*$  ab aa baa ab aa aa baa aa baa aa baa aa
  - $L^4$  aa aa baa aa baa aa baa aa baa
- 2. Given,

$$\Sigma = \{a, b\}$$

$$L = \{aa, bb\}$$

So,

$$\begin{split} \overline{L} &= \Sigma^* - L \\ &= \{ w \mid w \in \Sigma^n, n > 2 \} + \{ \lambda, a, b, ab, ba \} \end{split}$$

- 3. Note: Regex is Regular Expression
  - a) Regex b\*ab\*  $P: S \rightarrow bS \mid Sb \mid a$  $G = (\{S\}, \{a, b\}, S, P)$
  - b) Regex (a \* b\*) \* a(a \* b\*)\*  $P: S \to aS \mid Sa \mid bS \mid Sb \mid a$  $G = (\{S\}, \{a, b\}, S, P)$
  - c) Regex b \* ab \* ab \* ab \*

$$P$$
:

$$S \to aS_1 \mid bS \mid \lambda$$

$$S_1 \to aS_2 \mid bS_1 \mid \lambda$$

$$S_2 \to aS_3 \mid bS_2 \mid \lambda$$

$$S_3 \to bS_3 \mid \lambda$$

$$G = (\{S, S_1, S_2, S_3\}, \{a, b, \lambda\}, S, P)$$

d) Regex - (a \* b\*) \* a(a \* b\*) \* a(a \* b\*) \* a(a \* b\*) \* P:

$$S \to aS_1 \mid aS \mid Sa \mid bS \mid Sb$$
  
$$S_1 \to aS_2 \mid aS_1 \mid S_1a \mid bS_1 \mid S_1b$$

$$S_2 \rightarrow aS_3 \mid aS_2 \mid S_2a \mid bS_2 \mid S_2b$$

$$S_3 \to \lambda \mid aS_3 \mid S_3a \mid bS_3 \mid S_3b$$

$$G = (\{S, S_1, S_2, S_3\}, \{a, b, \lambda\}, S, P)$$

- 4. a) Regex  $a^n b^m$ ,  $m > n \ge 0$   $P: S \to aSb \mid Sb \mid b$   $G = (\{S\}, \{a, b\}, S, P)$ 
  - b) Regex  $a^n(bb)^n$ ,  $n \ge 0$   $P: S \to aSbb \mid \lambda$  $G = (\{S\}, \{a, b\}, S, P)$
  - c) Regex  $aaa(a^nb^n)b$ ,  $n \ge 0$   $P: S \to aSb \mid aaab$  $G = (\{S\}, \{a, b\}, S, P)$
  - d) Regex  $(aaa)a^nb^n, n \ge 0$   $P: S \to aSb \mid aaa$  $G = (\{S\}, \{a, b\}, S, P)$
  - e) Regex  $a^n b^m \cdot a^n (bb)^n$ ,  $m > n \ge 0$  P: $S \to S_1 S_2$

$$S \to S_1 S_2$$

$$S_1 \to a S_1 b \mid S_1 b \mid b$$

$$S_2 \to a S_2 b b \mid \lambda$$

$$G = (\{S, S_1, S_2\}, \{a, b, \lambda\}, S, P)$$

f) Regex -  $a^n b^m$ ,  $m \ge n \ge 0$ It can be observed that  $L_1 \cup L_2 = L_1 \cup \{\lambda\}$ .  $P: S \to aSb \mid Sb \mid b \mid \lambda$ 

$$G = (\{S\}, \{a, b, \lambda\}, S, P)$$

- g) Regex  $a^n b^m \cdot a^n b^m \cdot a^n b^m$ ,  $m > n \ge 0$  P:  $S \to S_1 S_2 S_3$   $S_1 \to a S_1 b \mid S_1 b \mid b$   $S_2 \to a S_2 b \mid S_2 b \mid b$  $S_3 \to a S_3 b \mid S_3 b \mid b$
- h) Regex  $(a^nb^m)*, m > n \ge 0$  P:  $S \to SS$  $S \to aSb \mid Sb \mid b$

 $G = (\{S, A, B\}, \{a, b, \lambda\}, S, P)$ 

 $G = (\{S\}, \{a, b\}, S, P)$ 

5. We will prove that the 2 grammars,  $G_1$  and  $G_2$  are not equivalent by providing a counterexample.

Deriving from the  $G_1$ ,

$$S \Rightarrow aSb \Rightarrow aSSb \Rightarrow aaSb \Rightarrow aaab$$

Similarly, for  $G_2$ 

$$S \Rightarrow aSb \Rightarrow aab$$
  
 $\Rightarrow aaSbb \Rightarrow aaabb$ 

Thus,  $aaab \in G_1$  but  $aaab \notin G_2$ . As a result, they are not equivalent.

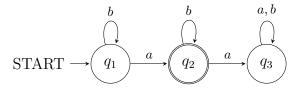


Figure 1: All strings with exactly one a

6. a)

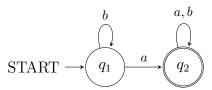


Figure 2: All strings with at least one a

b)

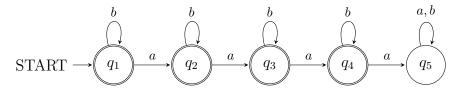


Figure 3: All strings with no more than 3 a's

c)

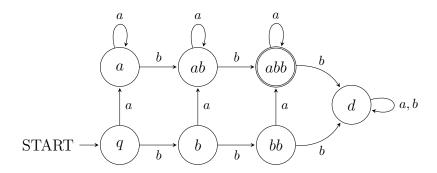


Figure 4: All strings with at least one a and exactly two b's

d)

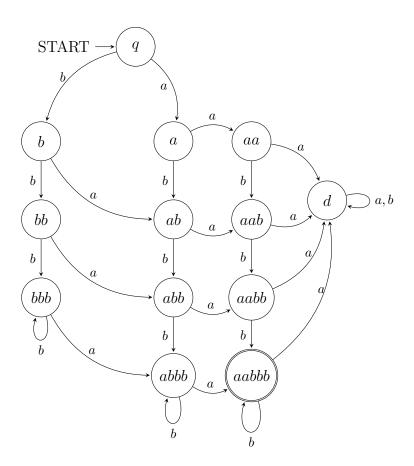


Figure 5: All strings with exactly two a's and more than two b's

e)

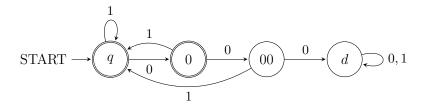


Figure 6: All strings where every 00 is followed by 1

7. a)

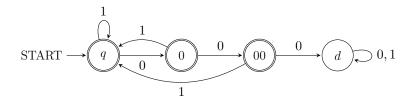


Figure 7: All strings containing 00 but not 000

b)

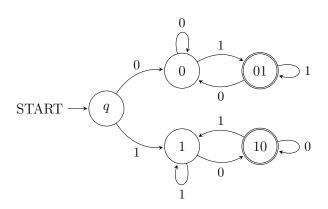
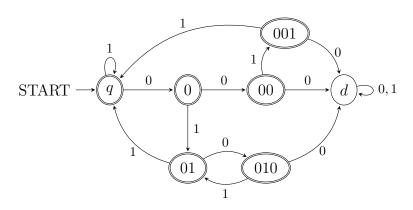


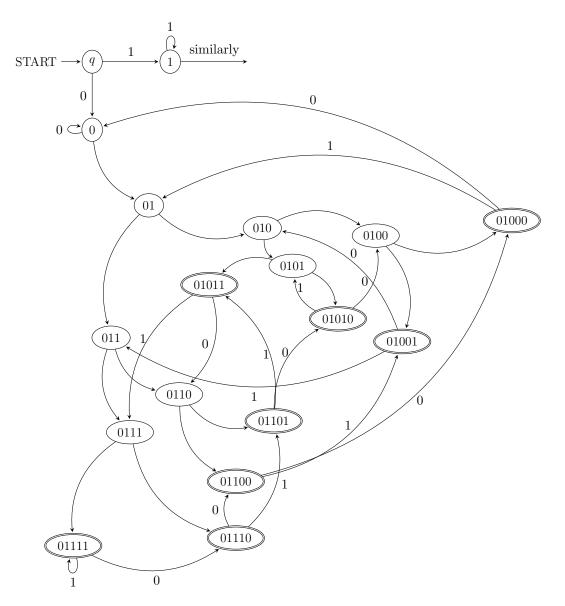
Figure 8: All strings where leftmost symbol differs from rightmost

c)



 $\textbf{Figure 9:} \ \textit{All strings where every substring of 4 symbols has at most 2 0's}$ 

d)



**Figure 10:** All strings of length 5 or more where 4th symbol from the right is different from leftmost

e)
Note that only 0's branch of the dfa is drawn. The 1's branch can generated in a similar way. Also, the transitions that are clearly marked by the states itself are ommitted to avoid cluttering.

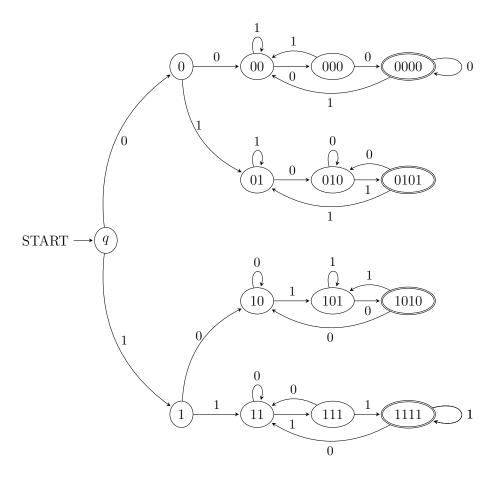


Figure 11: All strings where leftmost two and rightmost two symbols are identical

f)

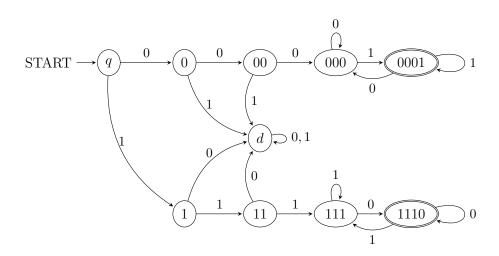


Figure 12: All strings where leftmost 3 symbols are identical, but different from rightmost symbol

g)