

A comparison of five epidemiological models for transmission of SARS-CoV-2 in India

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19 *ABSTRACT*

20 *Background*

21 Many popular disease transmission models have helped nations respond to the COVID-19 pandemic by
22 informing decisions about pandemic planning, resource allocation, implementation of social distancing
23 measures, lockdowns, and other non-pharmaceutical interventions. We study how five epidemiological
24 models forecast and assess the course of the pandemic in India: a baseline curve-fitting model, an
25 extended SIR (eSIR) model, two extended SEIR (SAPHIRE and SEIR-fansy) models, and a semi-
26 mechanistic Bayesian hierarchical model (ICM).

27 *Methods*

28 Using COVID-19 case-recovery-death count data reported in India from March 15 to October 15 to train
29 the models, we generate predictions from each of the five models from October 16 to December 31. To
30 compare prediction accuracy with respect to reported cumulative and active case counts and reported
31 cumulative death counts, we compute the symmetric mean absolute prediction error (SMAPE) for each
32 of the five models. For reported cumulative cases and deaths, we compute Pearson's and Lin's correlation
33 coefficients to investigate how well the projected and observed reported counts agree. We also present
34 underreporting factors when available, and comment on uncertainty of projections from each model.

35 *Results*

36 For active case counts, SMAPE values are 35.14% (SEIR-fansy) and 37.96% (eSIR). For cumulative
37 case counts, SMAPE values are 6.89% (baseline), 6.59% (eSIR), 2.25% (SAPHIRE) and 2.29% (SEIR-
38 fansy). For cumulative death counts, the SMAPE values are 4.74% (SEIR-fansy), 8.94% (eSIR) and
39 0.77% (ICM). Three models (SAPHIRE, SEIR-fansy and ICM) return total (sum of reported and

unreported) cumulative case counts as well. We compute underreporting factors as of October 31 and note that for cumulative cases, the SEIR-fansy model yields an underreporting factor of 7.25 and ICM model yields 4.54 for the same quantity. For total (sum of reported and unreported) cumulative deaths the SEIR-fansy model reports an underreporting factor of 2.97. On October 31, we observe 8.18 million cumulative reported cases, while the projections (in millions) from the baseline model are 8.71 (95% credible interval: 8.63 – 8.80), while eSIR yields 8.35 (7.19 – 9.60), SAPHIRE returns 8.17 (7.90 – 8.52) and SEIR-fansy projects 8.51 (8.18 – 8.85) million cases. Cumulative case projections from the eSIR model have the highest uncertainty in terms of width of 95% credible intervals, followed by those from SAPHIRE, the baseline model and finally SEIR-fansy.

Conclusions

In this comparative paper, we describe five different models used to study the transmission dynamics of the SARS-Cov-2 virus in India. While simulation studies are the only gold standard way to compare the accuracy of the models, here we were uniquely poised to compare the projected case-counts against observed data on a test period. The largest variability across models is observed in predicting the “total” number of infections including reported and unreported cases (on which we have no validation data). The degree of under-reporting has been a major concern in India and is characterized in this report. Overall, the SEIR-fansy model appeared to be a good choice with publicly available R-package and desired flexibility plus accuracy.

KEYWORDS

Compartmental Models; Low and Middle Income Countries; Prediction Uncertainty, Statistical Models;

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63 ***DECLARATIONS***

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73 (Tables and Figures). Rupam Bhattacharyya and Maxwell Salvatore (eSIR), Xuelin Gu (SAPHIRE),
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84

85 ***1. BACKGROUND***

86 Coronavirus disease 2019 (COVID-19) is an infectious disease caused by severe acute respiratory
87 syndrome coronavirus 2 (SARS-CoV-2) (1). At the time of revising this paper (March 24, 2020), roughly
88 124 million cases have been reported worldwide. The disease was first identified in Wuhan, Hubei
89 Province, China in December 2019 (2). Since then, more than 2.74 million lives have been lost as a direct
90 consequence of the disease. Notable outbreaks were recorded in the United States of America, Brazil and
91 India -- which remains a crucial battleground against the outbreak. The Indian government imposed very
92 strict lockdown measures early in the course of the pandemic in order to reduce the spread of the virus.
93 Said measures have not been as effective as was intended (3), with India now reporting the largest number
94 of confirmed cases in Asia, and the third highest number of confirmed cases in the world after the United
95 States and Brazil (4), with the number of confirmed cases crossing the 10 million mark on December 18,
96 2020. On March 24, 2020, the Government of India ordered a 21-day nationwide lockdown, later
97 extending it until May 3. This was followed by two-week extensions starting May 3 and 17 with
98 substantial relaxations. From June 1, the government started ‘unlocking’ most regions of the country in
99 five unlock phases. In order to formulate and implement policy geared toward containment and
100 mitigation, it is important to recognize the presence of highly variable contagion patterns across different
101 Indian states (5). India saw a decay in the virus curve in September, 2020 with daily number of cases
102 going below 10000. At the time of revising the paper, the daily incidence curve is sharply rising again,

103 as India faces its second wave. There is a rising interest in studying potential trajectories that the infection
104 can take in India to improve policy decisions.

105 A spectrum of models for projecting infectious disease spread have become widely popular in wake of
106 the pandemic. Some popular models include the ones developed at the Institute of Health Metrics (IHME)
107 (6) (University of Washington, Seattle) and at the Imperial College London (7). The IHME COVID-19
108 project initially relied on an extendable nonlinear mixed effects model for fitting parametrized curves to
109 COVID-19 data, before moving to a compartmental model to analyze the pandemic and generate
110 projections. The Imperial College model (henceforth referred to as ICM) works backwards from
111 observed death counts to estimate transmission that occurred several weeks ago, allowing for the time
112 lag between infection and death. A Bayesian mechanistic model is introduced - linking the infection
113 cycle to observed deaths, inferring the total population infected (attack rates) as well as the time-varying
114 reproduction number $R(t)$. With the onset of the pandemic, there has been renewed interest in multi-
115 compartment models, which have played a central role in modeling infectious disease dynamics since
116 the 20th century (8). The simplest of compartmental models include the standard SIR (9) model, which
117 has been extended (10) to incorporate various types of time-varying quarantine protocols, including
118 government-level macro isolation policies and community-level micro inspection measures. Further
119 extensions include one which adds a spatial component to this temporal model by making use of a cellular
120 automata structure (11). Larger compartmental models include those which incorporate different states
121 of transition between susceptible, exposed, infected and removed (SEIR) compartments, which have been
122 used in the early days of the pandemic in the Wuhan province of China (12). The SEIR compartmental
123 model has been further extended to the SAPHIRE model (13), which accounts for the infectiousness of
124 asymptomatic (14) and pre-symptomatic (15) individuals in the population (both of which are crucial

125 transmission features of COVID-19), time varying ascertainment rates, transmission rates and population
126 movement.

127 Researchers and policymakers are relying on these models to plan and implement public health policies
128 at the national and local levels. New models are emerging rapidly. Models often have conflicting
129 messages, and it is hard to distinguish a good model from an unreliable one. Different models operate
130 under different assumptions and provide different deliverables. In light of this, it is important to
131 investigate and compare the findings of various models on a given test dataset. While some work has
132 been done in terms of trying to reconcile results from different models of disease transmission that can
133 be fit to emerging data (16), more comparisons need to be done to investigate how differences between
134 competing models might lead to differing projections on the same dataset. In the context of India, such
135 head-to-head comparison across models are largely unavailable.

136 We consider five different models of different genre, starting from the simplest baseline model. The
137 baseline model we investigate relies on curve-fitting methods, with cumulative number of infected cases
138 modeled as an exponential process (17). Next, we consider the extended SIR (eSIR) model (10), which
139 uses a Bayesian hierarchical model to generate projections of proportions of infected and removed people
140 at future time points. The SAPHIRE (13) model has been demonstrated to reconstruct the full-spectrum
141 dynamics of COVID-19 in Wuhan between January and March 2020 across five periods defined by
142 events and interventions. Using this, we study the evolution of the pandemic in India over nine well-
143 defined lockdown and unlock periods, each with distinct transmission and ascertainment features.
144 Another model, SEIR-fansy (18) modifies the SEIR model to account for high false negative rate and
145 symptom-based administration of COVID-19 tests. Finally, we study the ICM model, which utilizes a
146 semi-mechanistic Bayesian hierarchical model based on renewal equations that model infections as a

147 latent process and links deaths to infections with the help of survival analysis. Each of the models
148 mentioned above have had appreciable success in being able to satisfactorily analyze and project the
149 trajectory of the pandemic in different countries (19)(20)(21).

150 In order to fairly compare and contrast the models mentioned above, we study their respective treatment
151 of the different lockdown and unlock periods declared by the Government of India. Additionally, we
152 compare their projections based on reported data, with special emphasis on how the models deal with (if
153 they do, at all) under-reporting and under-detection of COVID-cases, which has been a major point of
154 discussion in the scientific community, particularly for India (22). We also compare the uncertainty
155 associated with the projections across the models which is often overlooked in the literature.

156 The rest of the paper is organized as follows. In *Section 2* we provide an overview of the various models
157 considered in our analysis. The supplement has detailed discussion on the formulation, assumptions and
158 estimation methods utilized by each of the models. We present the numerical findings of our comparative
159 investigation of the models in *Section 3* by comparing projected COVID-counts (i.e., case and death
160 counts associated with COVID-19) and (wherever possible) parameter estimates which help understand
161 transmission dynamics of the pandemic. Next, in *Section 4* we discuss sensitivity analyses and note
162 applications of the models studied in the context of data from countries other than India. Finally, we
163 discuss the implications of our findings in *Section 5*.

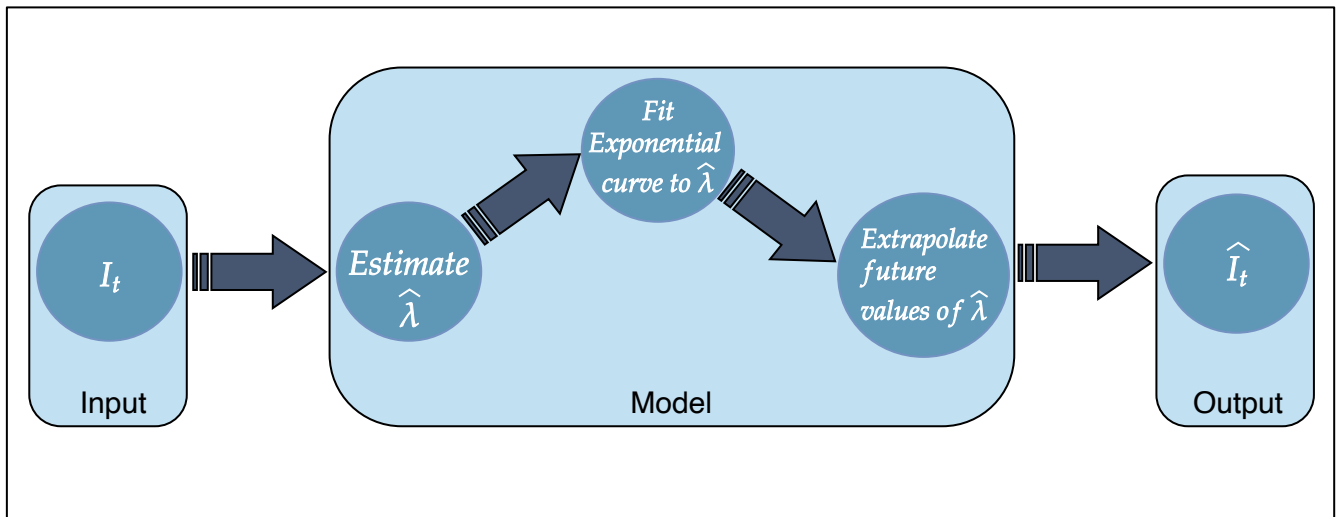
164 **2. METHODS**

165 **2.1. Overview of models**

166 In this section, we discuss the assumptions and formulation of each of the five classes of models described
167 above.

168 **2.1.a. Baseline model**

169 *Overview:* The baseline model we investigate aims to predict the evolution of the COVID-19 pandemic
170 by means of a regression-based predictive model (17). More specifically, the model relies on a
171 regression analysis of the daily cumulative count of infected cases based on the least-squares fitting.
172 In particular, the growth rate of the infection is modeled as an exponentially decaying process. *Figure*
173 *1* provides a schematic overview of this model.



174 *Figure 1: Schematic overview of the baseline model.*

175 *Formulation:* The baseline model assumes that the following simple differential equation governs
176 the evolution of a disease in a fixed population:

$$\frac{dI(t)}{dt} = \lambda I(t), \quad (1)$$

where $I(t)$ is defined as the number of infected people at time t and λ is the growth rate of infection. Unlike the other models described in subsequent sections, the baseline model analyses and projects only the cumulative number of infections, and not counts/proportions associated with other compartments like deaths and recoveries. The model uses reported field data of the infections in India over a specific time period. The growth rate can be numerically approximated from Equation (1) above as

$$\hat{\lambda}_t = \frac{I_t - I_{t-2}}{2 \cdot I_t} \quad (2)$$

Having estimated the growth rate, the model uses a least-squares method to fit an exponential time-varying curve to $\hat{\lambda}_t$, obtained from Equation (2) above. Since all the other methods involve Bayesian estimation methods and use posterior distributions to obtain estimates and associated credible intervals, we place a non-informative prior on the random error in the above curve fitting method (23) to ensure comparable results. Specifically, we consider a uniform prior for the log of error variance. Using projected values of $\hat{\lambda}_t$, we extrapolate the number of infections which will occur in future. The baseline model described above has been implemented in R (24) using standard packages for exponential curve fitting.

2.1.b. *Extended SIR (eSIR) model*

Overview: We use an extension of the standard susceptible-infected-removed (SIR) compartmental model known as the extended SIR (eSIR) model (10). To implement the eSIR model, a Bayesian hierarchical framework is used to model time series data on the proportion of individuals in the infected and removed compartments. Markov chain Monte Carlo (MCMC) methods are used to implement this

197 model, which provides not only posterior estimation of parameters and prevalence values associated with
 198 all three compartments of the SIR model, but also predicted proportions of the infected and the removed
 199 people at future time points. *Figure 2* is a diagrammatic representation of the eSIR model.

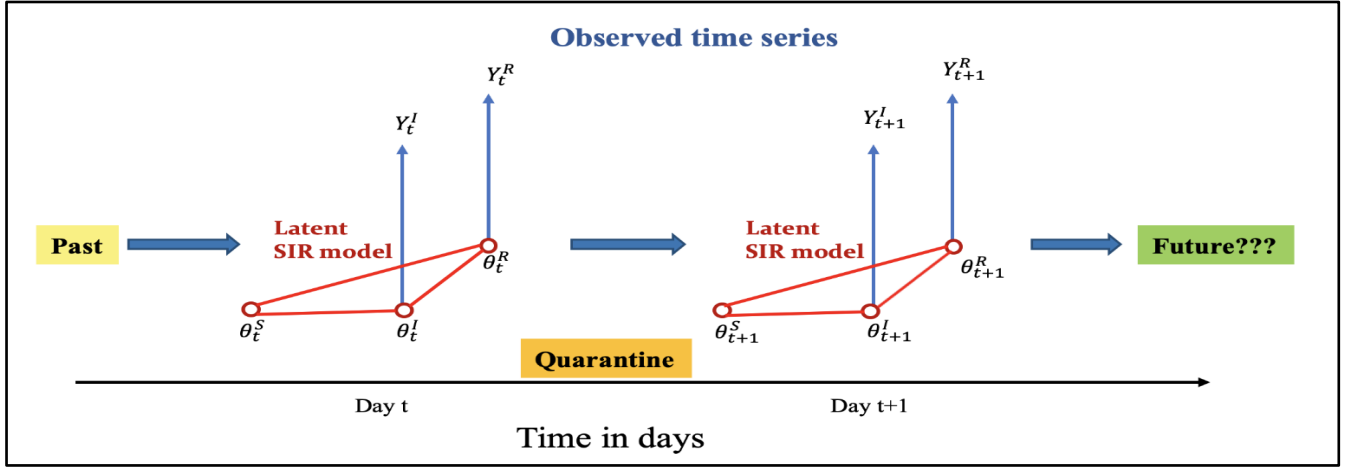


Figure 2: The eSIR model with a latent SIR model on the unobserved proportions. Reproduced from Wang et al., 2020 (10).

201 *Formulation:* The eSIR model assumes the true underlying probabilities of the three compartments
 202 follow a latent Markov transition process and require observed daily proportions of infected and removed
 203 cases as input.

204 The observed proportions of infected and removed cases on day t are denoted by Y_t^I and Y_t^R , respectively.
 205 Further, we denote the true underlying probabilities of the S, I, and R compartments on day t by θ_t^S , θ_t^I ,
 206 and θ_t^R , respectively, and assume that for any t , $\theta_t^S + \theta_t^I + \theta_t^R = 1$. Assuming a usual SIR model on the
 207 true proportions we have the following set of differential equations

$$208 \quad \frac{d\theta_t^S}{dt} = -\beta\theta_t^S\theta_t^I, \quad (3a)$$

$$\frac{d\theta_t^I}{dt} = \beta\theta_t^S\theta_t^I - \gamma\theta_t^I, \quad (3b)$$

$$\frac{d\theta_t^R}{dt} = \gamma\theta_t^I, \quad (3c)$$

where $\beta > 0$ denotes the disease transmission rate, and $\gamma > 0$ denotes the removal rate. The basic reproduction number $R_0 := \beta/\gamma$ indicates the expected number of cases generated by one infected case in the absence of any intervention and assuming that the whole population is susceptible. We assume a Beta-Dirichlet state space model for the observed infected and removed proportions, which are conditionally independently distributed as

$$Y_t^I | \boldsymbol{\theta}_t, \boldsymbol{\tau} \sim \text{Beta}(\lambda^I \theta_t^I, \lambda^I (1 - \theta_t^I)) \quad (4a)$$

$$Y_t^R | \boldsymbol{\theta}_t, \boldsymbol{\tau} \sim \text{Beta}(\lambda^R \theta_t^R, \lambda^R (1 - \theta_t^R)). \quad (4b)$$

Further, the Markov process associated with the latent proportions is built as:

$$\boldsymbol{\theta}_t | \boldsymbol{\theta}_{t-1}, \boldsymbol{\tau} \sim \text{Dirichlet}(\kappa f(\boldsymbol{\theta}_{t-1}, \beta, \gamma)) \quad (5)$$

where $\boldsymbol{\theta}_t$ denotes the vector of the underlying population probabilities of the three compartments, whose mean is modeled as an unknown function of the probability vector from the previous time point, along with the transition parameters. $\boldsymbol{\tau} = (\beta, \gamma, \boldsymbol{\theta}_0^T, \boldsymbol{\lambda}, \kappa)$ denotes the whole set of parameters where λ^I, λ^R and κ are parameters controlling variability of the observation and latent process, respectively. The function $f(\cdot)$ is then solved as the mean transition probability determined by the SIR dynamic system, using a fourth order Runge-Kutta approximation (25).

226 *Priors and MCMC algorithm:* The prior on the initial vector of latent probabilities is set as
 227 $\boldsymbol{\theta}_0 \sim \text{Dirichlet}(1 - Y_1^I - Y_1^R, Y_1^I, Y_1^R)$, $\theta_0^S = 1 - \theta_0^I - \theta_0^R$. The prior distribution of the basic reproduction
 228 number is lognormal such that $E(R_0) = 3.28$ (26) (this value was also confirmed by calculating the
 229 average time-varying $R(t)$ by from January 30 till March 24, 2020, using the package developed by (27)).
 230 The prior distribution of the removal rate is also lognormal such that $E(\gamma) = 0.5436$. We use the
 231 proportion of death within the removed compartment as 0.0184 so that the initial infection fatality ratio
 232 is 0.01 (28). For the variability parameters, the default choice is to set large variances in both observed
 233 and latent processes, which may be adjusted over the course of epidemic with more data becoming
 234 available: $\kappa, \lambda^I, \lambda^R \stackrel{iid}{\sim} \text{Gamma}(2, 10^{-4})$.

235 Denoting t_0 as the last date of data availability, and assuming that the forecast spans over the period
 236 $[t_0 + 1, T]$, the eSIR algorithm is as follows.

237 Step 0. Take M draws from the posterior $[\boldsymbol{\theta}_{1:t_0}, \boldsymbol{\tau} | \mathbf{Y}_{1:t_0}]$.

238 Step 1. For each solution path $m \in \{1, \dots, M\}$, iterate between the following two steps via MCMC.

239 i. Draw $\boldsymbol{\theta}_t^{(m)}$ from $[\boldsymbol{\theta}_t | \boldsymbol{\theta}_{t-1}^{(m-1)}, \boldsymbol{\tau}^{(m)}]$, $t \in \{t_0 + 1, \dots, T\}$.

240 ii. Draw $\mathbf{Y}_t^{(m)}$ from $[\mathbf{Y}_t | \boldsymbol{\theta}_t^{(m)}, \boldsymbol{\tau}^{(m)}]$, $t \in \{t_0 + 1, \dots, T\}$.

241 *Implementation:* We implement the proposed algorithm in R package *rjags* (29) and the differential
 242 equations were solved via the fourth-order Runge–Kutta approximation. To ensure the quality of the
 243 MCMC procedure, we fix the adaptation number (which denotes the number of MCMC samples
 244 discarded by JAGS in order to tune parameters which in turn improves speed or de-correlation of
 245 sampling) at 10^4 , thin the chain by keeping one draw from every 10 random draws to further reduce

246 autocorrelation, set a burn-in period of 10^5 draws under 2×10^5 iterations for four parallel chains. This
247 implementation provides not only posterior estimation of parameters and prevalence of all the three
248 compartments in the SIR model, but also predicts proportions of the infected and the removed people at
249 future time point(s). The R package for implementing this general model for understanding disease
250 dynamics is publicly available at <https://github.com/lilywang1988/eSIR>.

251 **2.1.c. SAPHIRE model**

252 *Overview:* This model (13) extends the classic SEIR model to estimate COVID-related transmission
253 parameters, in addition to projecting COVID-19 case counts, while accounting for pre-symptomatic
254 infectiousness, time-varying ascertainment rates (i.e. reporting rates), transmission rates and population
255 movements. *Figure 3* provides a schematic diagram of the compartments and transitions conceptualized
256 in this model. The model includes seven compartments: susceptible (S), exposed (E), pre-symptomatic
257 infectious (P), reported infectious (I), unreported infectious (A), isolation in hospital (H) and removed
258 (R). Compared with the classic SEIR model, SAPHIRE explicitly models population movement and
259 introduce two additional compartments (A and H) to account for the fact that only reported cases would
260 seek medical care and thus be quarantined by hospitalization. The model described and implemented
261 here relies on the same methodology and arguments as presented by (13). The only difference is that
262 while the original model analyzed data from China over a time period of December 2019 to March 2020
263 (which constituted the initial days of the pandemic in China), we analyze data from India. Additionally,
264 the original manuscript adjusted the model to account for population movement. Data on population
265 movement not being available consistently over time and regions in India, we make no such
266 modifications. We further note that the SAPHIRE model returns reported and unreported cumulative
267 COVID-case counts, in addition to cumulative counts of the removed compartment. As such, for the

268 purpose of comparisons, the SAPHIRE model is used only to study cumulative COVID-case counts
 269 (reported and unreported). The R package for implementing this general model for understanding disease
 270 dynamics is publicly available at <https://github.com/chaolongwang/SAPHIRE>.

271 *Formulation:* The dynamics of the 7 compartments described above at time t are described by the set of
 272 ordinary differential equations

$$273 \quad \frac{dS}{dt} = n - \frac{bS(\alpha P + \alpha A + I)}{N} - \frac{nS}{N}, \quad (6a)$$

$$274 \quad \frac{dE}{dt} = \frac{bS(\alpha P + \alpha A + I)}{N} - \frac{E}{D_e} - \frac{nE}{N}, \quad (6b)$$

$$275 \quad \frac{dP}{dt} = \frac{E}{D_e} - \frac{P}{D_p} - \frac{nP}{N}, \quad (6c)$$

$$276 \quad \frac{dA}{dt} = \frac{(1-r)P}{D_p} - \frac{A}{D_i} - \frac{nA}{N}, \quad (6d)$$

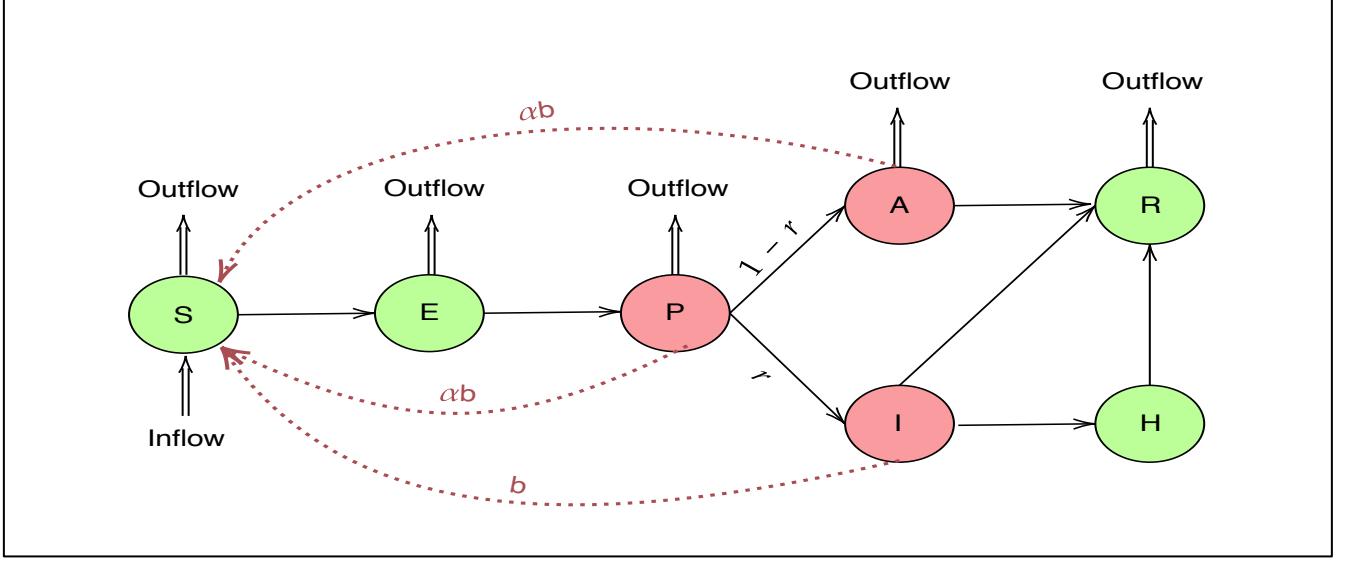
$$277 \quad \frac{dI}{dt} = \frac{rP}{D_p} - \frac{I}{D_i} - \frac{I}{D_q}, \quad (6e)$$

$$278 \quad \frac{dH}{dt} = \frac{I}{D_q} - \frac{H}{D_h}, \quad (6f)$$

$$279 \quad \frac{dR}{dt} = \frac{A + I}{D_i} + \frac{H}{D_h} - \frac{nR}{N}, \quad (6g)$$

280 in which b is the transmission rate for reported cases (defined as the number of individuals that an
 281 reported case can infect per day), α is the ratio of the transmission rate of unreported cases to that of
 282 reported cases, r is the ascertainment rate, D_e is the latent period, D_p is the pre-symptomatic infectious

283 period, D_i is the symptomatic infectiousness period, D_q is the duration from illness onset to isolation and
 284 D_h is the isolation period in the hospital. Further, we set $N = 1.34 \times 10^9$ as the population size for India
 285 and set $n = 0$ to indicate no incoming or outgoing travelers.



286

Figure 3: The SAPHIRE model includes seven compartments: susceptible (S), exposed (E), pre-symptomatic infectious (P), reported infectious (I), unreported infectious (A), isolation in hospital (H) and removed (R).

287 Under this setup, the reproductive number R (as presented in the original manuscript) may be expressed
 288 as

289
$$R = ab \left(D_p^{-1} + \frac{n}{N} \right)^{-1} + (1 - r)ab \left(D_i^{-1} + \frac{n}{N} \right)^{-1} + rb(D_i^{-1} + D_q^{-1})^{-1}, \quad (7)$$

290 in which the three terms represent infections contributed by pre-symptomatic individuals, unreported
 291 cases and reported cases, respectively. The model adjusts the infectious periods of each type of case by
 292 taking isolation of patients who test positive (by means of D_q^{-1}) into account.

293 *Initial states and parameter settings:* We set $\alpha = 0.55$, assuming lower transmissibility for unreported
 294 cases (30). Compartment P contains both reported and unreported cases in the pre-symptomatic phase.
 295 We set the transmissibility of P to be the same as unreported cases, because it has previously been
 296 reported that the majority of cases are unreported (30). We assume an incubation period of 5.2 days and
 297 a pre-symptomatic infectious period $D_p = 2.3$ days (31,32). The latent period was $D_e = 2.9$ days. Since
 298 pre-symptomatic infectiousness was estimated to account for 44% of the total infections from reported
 299 cases (31), we set the mean of total infectious period as $(D_p + D_i) = D_p/0.44 = 5.2$ days, assuming
 300 constant infectiousness across the pre-symptomatic and symptomatic phases of reported cases (33) – thus
 301 the mean symptomatic infectious period was $D_i = 2.9$ days. We set a long isolation period of $D_h = 17$
 302 days, based on a study investigating hospitalisation of COVID-19 patients in the state of Karnataka (34).
 303 The duration from the onset of symptoms to isolation was estimated to be $D_q = 7$ (35,36) as the median
 304 time length from onset to confirmed diagnosis. On the basis of the parameter settings above, the initial
 305 state of the model is specified on March 15. The initial number of reported symptomatic cases $I(0)$ is
 306 specified as the number of reported cases who experienced symptom onset during 12-14 March. The
 307 initial ascertainment rate is assumed to be $r_0 = 0.10$ (37), and thus the initial number of unreported
 308 cases is $A(0) = r_0^{-1}(1 - r_0)I(0)$. $P_1(0)$ and $E_1(0)$ denote the numbers of reported cases in which
 309 individuals experienced symptom onset during 15–16 March and 17–19 March, respectively. Then, the
 310 initial numbers of exposed and pre-symptomatic individuals are set as $E(0) = r_0^{-1}E_1(0)$ and $P(0) =$
 311 $r_0^{-1}P_1(0)$, respectively. The initial number of the hospitalized cases $H(0)$ is set as half of the cumulative
 312 reported cases on 8 March since $D_q = 7$ and there would be more severe cases among the reported cases
 313 in the early phase of the epidemic.

314 *Likelihood and MCMC algorithm:* Considering the time-varying strength of control measures
 315 implemented in India over the trajectory of the pandemic, we chose to break the training period into ten
 316 sequential blocks: pre-lockdown (March 15 – 24), lockdown phases 1, 2, 3, and 4 (March 25 – April 14,
 317 April 15 – May 3, May 4 – 17, and May 18 – 31 respectively) followed by unlock phases 1, 2, 3, 4 and
 318 5 (June 1 – 30, July 1 – 31, August 1 – 31, September 1 – 30 and October 1 – 15 respectively). In other
 319 words, the model assumes that the value of b (and r) corresponding to the i^{th} lockdown period to vary
 320 as b_i (and r_i) for $i = 1, 2, 3, \dots, 10$. The observed number of reported cases in which individuals
 321 experience symptom onset on day t – denoted by x_t – is assumed to follow a Poisson distribution with
 322 rate $\lambda_t = rP_{t-1}D_p^{-1}$, with P_t denoting the expected number of pre-symptomatic individuals on day t . The
 323 following likelihood equation is used to fit the model using observed data from March 15 (T_0) to October
 324 15 (T_1).

$$325 \quad L(b_1, b_2, \dots, b_{10}, r_1, r_2, \dots, r_{10}) = \prod_{t=T_0}^{T_1} \frac{e^{-\lambda_t} \lambda_t^{x_t}}{x_t!},$$

326 and the model is used to predict COVID-counts from October 16 to December 31. A non-informative
 327 prior of $U(0, 2)$ is used for b_1, b_2, \dots, b_{10} . For r_1 , an informative prior of Beta(10, 90) is used based on
 328 the findings of (37). We reparameterise r_2, \dots, r_{10} as

$$329 \quad \text{logit}(r_i) = \text{logit}(r_{i-1}) + \delta_i \text{ for } i = 2, 3, \dots, 10$$

330 where $\text{logit}(t) = \log(t/(1-t))$ is the standard logit function. In the MCMC, $\delta_i \sim N(0, 1)$ for $i =$
 331 2, 3, \dots , 10. A burn-in period of 100,000 iterations is fixed, with a total of 200,000 iterations being run.

332

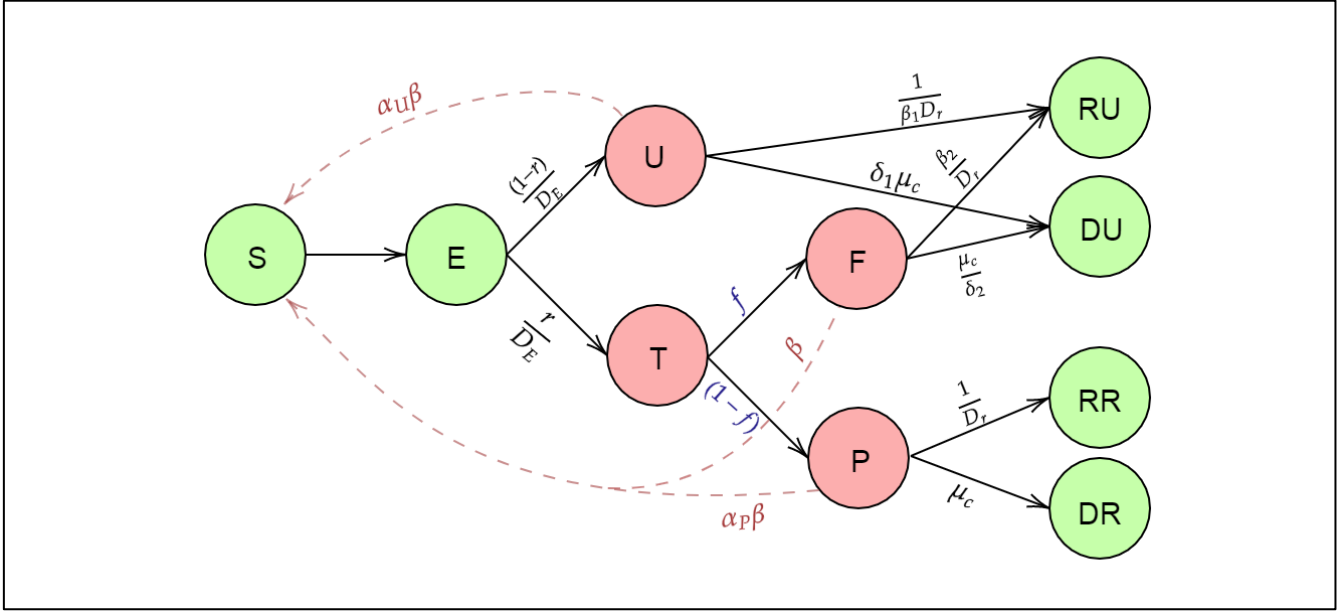
333 *2.1.d. SEIR-fansy model*

334 *Overview:* One of the problems with applying a standard SIR model in the context of the COVID-19
335 pandemic is the presence of a long incubation period. As a result, extensions of SIR model like the SEIR
336 model are more applicable. In the previous subsection, we have seen an extension which includes the
337 ‘pre-symptomatic infectious’ compartment (people who are infected at time t and contributing to the
338 spread of the virus, but do not show any symptom yet). In the SEIR-fansy model, we use an alternate
339 formulation by defining an ‘untested infectious’ compartment for infected people who are spreading
340 infection but are not tested after the incubation period. This compartment is necessary because there is a
341 large proportion of infected people who are not being tested (a part of them are asymptomatic or mildly
342 symptomatic but for a country like India there are other reasons like access to care and stigma that can
343 prevent someone from getting tested/diagnosed). We have assumed that after the ‘exposed’ compartment,
344 a person enters either the ‘untested infectious’ compartment or the ‘tested infectious’ compartment. To
345 incorporate the possible effect of misclassifications due to imperfect testing, we include a compartment
346 for false negatives (infected people who are tested but reported as negative). As a result, after being
347 tested, an infected person enters either into the ‘false negative’ compartment or the ‘tested positive’
348 compartment (infected people who are tested and reported to be positive). We keep separate
349 compartments for the recovered and deceased persons coming from the untested and false negatives
350 compartments which are ‘recovered unreported’ and ‘deceased unreported’ respectively. For the ‘tested
351 positive’ compartment, the recovered and the death compartments are denoted by ‘recovered reported’
352 and ‘deceased reported’ respectively. Thus, we divide the entire population into ten main compartments:
353 S (Susceptible), E (Exposed), T (Tested), U (Untested), P (Tested positive), F (Tested False Negative),

354 RR (Reported Recovered), RU (Unreported Recovered), DR (Reported Deaths) and DU (Unreported
355 Deaths). This model is implemented using the R package SEIRfansy (38).

356 *Formulation:* Like most compartmental models, this model assumes exponential times for the duration
357 of an individual staying in a compartment. For simplicity, we approximate this continuous-time process
358 by a discrete-time modeling process. The main parameters of this model are β (rate of transmission of
359 infection by false negative individuals), α_p (scaling factor that measures the rate of spread of infection
360 by patients who test positive for COVID-19 relative to infected patients who return false negative test
361 results), α_u (scaling factor for the rate of spread of infection by untested individuals), D_e (incubation
362 period in days), D_r (mean days till recovery for positive individuals), D_t (mean number of days for the
363 test result to come after a person is being tested), μ_c (death rate due to COVID-19 which is the inverse
364 of the average number of days for death due to COVID-19 starting from the onset of disease multiplied
365 by the probability death of an infected individual due to COVID), λ and μ (natural birth and death rates
366 respectively, assumed to be equal for the sake of simplicity), r (probability of being tested for infectious
367 individuals), f (false negative probability of RT-PCR test), β_1 and β_2^{-1} (scaling factors for rate of
368 recovery for undetected and false negative individuals respectively), δ_1 and δ_2^{-1} (scaling factors for
369 death rate for undetected and false negative individuals respectively). The number of individuals at the
370 time point t in each compartment is governed by the system of differential equations given by Equations
371 (8a) – (8i). To simplify this model, we assume that testing is instantaneous. In other words, we assume
372 there is no time difference from the onset of the disease after the incubation period to getting test results.
373 This is a reasonable assumption to make as the time for testing is about 1-2 days which is much less than
374 the mean duration of stay for the other compartments. Further, once a person shows symptoms for

375 COVID-19 like diseases, they are sent to get tested almost immediately. *Figure 4* provides a schematic
 376 overview of the model.



377

Figure 4: Schematic diagram for the SEIR-fansy model with imperfect testing and misclassification. The model has ten compartments: S (Susceptible), E (Exposed), T (Tested), U (Untested), P (Tested positive), F (Tested False Negative), RR (Reported Recovered), RU (Unreported Recovered), DR (Reported Deaths) and DU (Unreported Deaths). Reproduced from Bhaduri, Kundu et al., 2020 (18).

378 The following differential equations summarize the transmission dynamics being modeled.

379
$$\frac{\partial S}{\partial t} = -\beta \frac{S(t)}{N} (\alpha_P P(t) + \alpha_U U(t) + F(t)) + \lambda N - \mu S(t), \quad (8a)$$

380
$$\frac{\partial E}{\partial t} = \beta \frac{S(t)}{N} (\alpha_P P(t) + \alpha_U U(t) + F(t)) - \frac{E(t)}{D_e} - \mu E(t), \quad (8b)$$

381
$$\frac{\partial U}{\partial t} = (1-r) \frac{E(t)}{D_e} - \frac{U(t)}{\beta_1 D_r} - \delta_1 \mu_c U(t) - \mu U(t), \quad (8c)$$

$$\frac{\partial P}{\partial t} = (1-f)r \frac{E(t)}{D_e} - \frac{P(t)}{D_r} - \mu_c P(t) - \mu P(t), \quad (8d)$$

$$\frac{\partial F}{\partial t} = fr \frac{E(t)}{D_e} - \frac{\beta_2 F(t)}{D_r} - \frac{\mu_c F(t)}{\delta_2} - \mu F(t), \quad (8e)$$

$$\frac{\partial RU}{\partial t} = \frac{U(t)}{\beta_1 D_r} + \frac{\beta_2 F(t)}{D_r} - \mu RU(t), \quad (8f)$$

$$\frac{\partial RR}{\partial t} = \frac{P(t)}{D_r} - \mu RR(t), \quad (8g)$$

$$\frac{\partial DU}{\partial t} = \delta_1 \mu_c U(t) + \frac{\mu_c F(t)}{\delta_2}, \quad (8h)$$

$$\frac{\partial DR}{\partial t} = \mu_c P(t). \quad (8i)$$

Using the Next Generation Matrix Method (39), we calculate the basic reproduction number

$$R_0 = \frac{\beta S_0}{\mu D_e + 1} \left(\frac{\alpha_U (1-r)}{\frac{1}{\beta_1 D_r} + \delta_1 \mu_c + \mu} + \frac{\alpha_P r (1-f)}{\frac{1}{D_r} + \mu_c + \mu} + \frac{rf}{\frac{\beta_2}{D_r} + \frac{\mu_c}{\delta_2} + \mu} \right), \quad (9)$$

where $S_0 = \lambda/\mu = 1$ since we assume that natural birth and death rates are equal within this short period of time. *Supplementary Table S1* describes the parameters in greater detail.

Likelihood assumptions and estimation: Parameters are estimated using Bayesian estimation techniques and MCMC methods (namely, Metropolis-Hastings method (40) with Gaussian proposal distribution). First, we approximated the above set of differential equations by a discrete time approximation using daily differences. After we start with an initial value for each of the compartments on the day 1, using

the discrete time recurrence relations we obtain the counts for each of the compartments at the next days. To proceed with the MCMC-based estimation, we specify the likelihood explicitly. We assume (conditional on the parameters) the number of new confirmed cases on day t depend only on the number of exposed individuals on the previous day. Specifically, we use multinomial modeling to incorporate the data on recovered and deceased cases as well. The joint conditional distribution is

$$\begin{aligned}
P[P_{new}(t), RR_{new}(t), DR_{new}(t)|E(t-1), P(t-1)] \\
&= P[P_{new}(t)|E(t-1), P(t-1)] \cdot P[RR_{new}(t), DR_{new}(t)|E(t-1), P(t-1)] \\
&= P[P_{new}(t)|E(t-1)] \cdot P[RR_{new}(t), DR_{new}(t)|P(t-1)].
\end{aligned}$$

A multinomial distribution-like structure is then defined

$$P_{new}(t)|E(t-1) \sim \text{Bin}(E(t-1), r(1-f)/D_e) \quad (10a)$$

$$RR_{new}(t), DR_{new}(t)|P(t-1) \sim \text{Mult}(P(t-1), (D_r^{-1}, \mu_c, 1 - D_r^{-1} - \mu_c)) \quad (10b)$$

Note: the expected values of $E(t-1)$ and $P(t-1)$ are obtained by solving the discrete time differential equations specified by Equations (8a) – (8i).

Prior assumptions and MCMC: For the parameter r , we assume a $U(0,1)$ prior, while for β , we assume an improper non-informative flat prior with the set of positive real numbers as support. After specifying the likelihood and the prior distributions of the parameters, we draw samples from the posterior distribution of the parameters using the Metropolis-Hastings algorithm with a Gaussian proposal distribution. We run the algorithm for 200,000 iterations with a burn-in period of 100,000. Finally, the mean of the parameters in each of the iterations are obtained as the final estimates of β and r for the different time periods. As in the case of the SAPHIRE model, we again break the training period into ten

sequential blocks: pre-lockdown (March 15 – 24), lockdown phases 1, 2, 3, and 4 (March 25 – April 14, April 15 – May 3, May 4 – 17, and May 18 – 31 respectively) followed by unlock phases 1, 2, 3, 4 and 5 (June 1 – 30, July 1 – 31, August 1 – 31, September 1 – 30 and October 1 – 15 respectively).

2.1.e. *Imperial College London model (ICM)*

Overview: We examine a Bayesian semi-mechanistic model for estimating the transmission intensity of SARS-CoV-2 (7). The model defines a renewal equation using the time-varying reproduction number R_t to generate new infections. As a lot of cases in SARS-CoV-2 are asymptomatic and reported case data is unreliable especially in early part of the epidemic in India, the model relies on observed deaths data and calculates backwards to infer the true number of infections. The latent daily infections are modeled as the product of R_t with a discrete convolution of the previous infections, weighted using an infection-to-transmission distribution specific to SARS-CoV-2. We implement this Bayesian semi-mechanistic model in the context of COVID-19 data arising from India in order to estimate the reproduction number over time, along with plausible upper and lower bounds (95% Bayesian credible intervals (CrI)) of the daily infections and the daily number of infectious people. We parametrize R_t with a fixed effect and a random effect for each week over the course of the epidemic for each state. The fixed effect accounts for the variations in R_t across India as a whole whereas the random effect allows for variations among different states. The weekly effects are encoded as a random walk, where at each successive step the random effect has an equal chance of moving upwards or downwards from its current value. The model is implemented using *epidemia* (41), a general purpose R package for semi-mechanistic Bayesian modelling of epidemics. *Figure 5* represents a schematic overview of the model.

436 *Formulation:* The true number of infected individuals, i , is modelled using a discrete renewal process.
 437 We specify a generation distribution (42) g with density $g(\tau)$ as $g \sim \text{Gamma}(6.5, 0.62)$. Given the
 438 generation distribution, the number of infections $i_{t,m}$ on a given day t , and state m is given by the
 439 discrete convolution function:

$$440 \quad i_{t,m} = S_{t,m} R_{t,m} \sum_{\tau=0}^{t-1} i_{\tau,m} g_{t-\tau}, \quad (11a)$$

$$441 \quad S_{t,m} = 1 - \frac{\sum_{j=0}^{t-1} i_{j,m}}{N_m}, \quad (11b)$$

442 where the generation distribution is discretized by $g_s = \int_{s-0.5}^{s+0.5} g(\tau) d\tau$ for $s = 2, 3, \dots$, and $g_1 =$
 443 $\int_0^{1.5} g(\tau) d\tau$. The population of state m is denoted by N_m . We include the adjustment factor $S_{t,m}$ to
 444 account for the number of susceptible individuals left in the population.

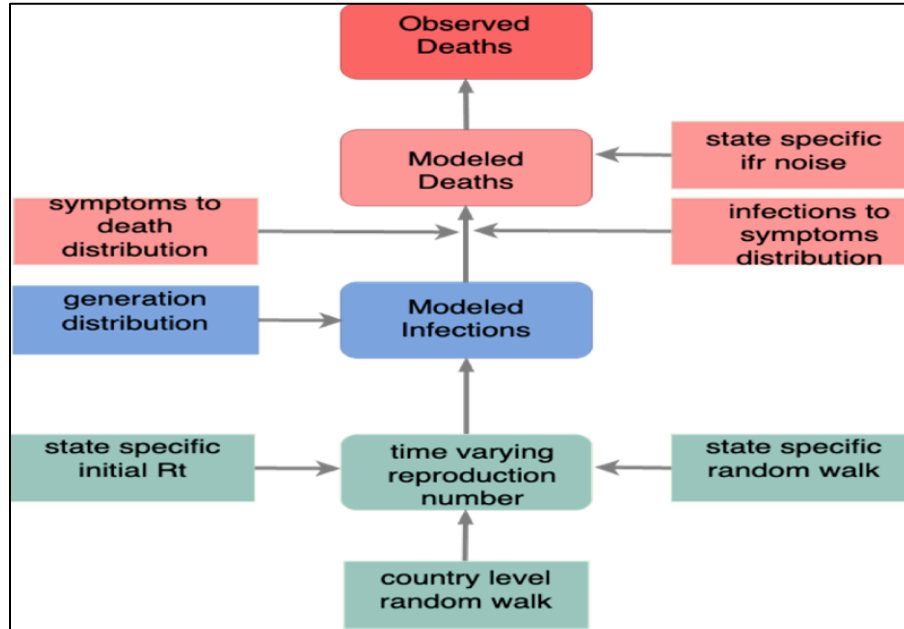


Figure 5: Schematic overview of ICM.

446 We define daily deaths, $D_{t,m}$, for days $t \in \{1, \dots, n\}$ and states $m \in \{1, \dots, M\}$. These daily deaths are
 447 modelled using a positive real-valued function $d_{t,m} = E[D_{t,m}]$ that represents the expected number of
 448 deaths attributed to COVID-19. The daily deaths $D_{t,m}$ are assumed to follow a negative binomial
 449 distribution with mean $d_{t,m}$ and variance $d_{t,m} + d_{t,m}^2/\psi_1$, where ψ_1 follows a positive half normal
 450 distribution, i.e.,

$$451 \quad D_{t,m} \sim NB(d_{t,m}, d_{t,m} + d_{t,m}^2/\psi_1), \quad t = 1, \dots, n, \quad (12a)$$

$$452 \quad \psi_1 \sim N^+(0,5). \quad (12b)$$

453 We link our observed deaths mechanistically to transmission (7). We use a previously estimated COVID-
 454 19 infection fatality ratio (IFR, probability of death given infection) of 0.1% (43,44) together with a
 455 distribution of times from infection to death π . To incorporate the uncertainty inherent in this estimate
 456 we modify the ifr for every state to have additional noise around the mean, denoted by ifr_m^* . Specifically,
 457 we assume

$$458 \quad \text{ifr}_m^* \sim \text{ifr} \cdot N(1, 0.1), \quad (13)$$

459 where ifr_m^* represents the noise-added analog of ifr. Using estimated epidemiological information from
 460 previous studies, we assume the distribution of times from infection to death π (infection-to-death) to
 461 be the convolution of an infection-to-onset distribution (π') (45) and an onset-to-death distribution (28)

$$462 \quad \pi \sim \text{Gamma}(5.1, 0.86) + \text{Gamma}(17.8, 0.45). \quad (14)$$

463 The expected number of deaths $d_{t,m}$, on a given day t , for state m is given by the following discrete sum

$$464 \quad d_{t,m} = \text{ifr}_m^* \sum_{\tau=0}^{t-1} i_{\tau,m} \pi_{t-\tau}, \quad (15)$$

26

465 where $i_{\tau,m}$ is the number of new infections on day τ in state m and where, similar to the generation
 466 distribution, π is discretized via $\pi_s = \int_{s-0.5}^{s+0.5} \pi(\tau) d\tau$ for $s = 2, 3, \dots$, and $\pi_1 = \int_0^{1.5} \pi(\tau) d\tau$, where $\pi(\tau)$
 467 is the density of π .

468 We parametrize $R_{t,m}$ with a random effect for each week of the epidemic as follows

$$469 \quad R_{t,m} = R_0 \cdot f(-\epsilon_{w(t,m)} - \epsilon_{m,w(t,m)}^{state}), \quad (16)$$

470 where $f(x) = 2 \exp(x) / (1 + \exp(x))$ is twice the inverse logit function, and $\epsilon_{w(t)}$ and
 471 $\epsilon_{m,w(t,m)}^{state}$ follow a weekly random walk process, that captures variation between $R_{t,m}$ in each subsequent
 472 week. $\epsilon_{w(t)}$ is a fixed effect estimated across all the states and $\epsilon_{m,w(t,m)}^{state}$ is the random effect specific to
 473 each state in India. The prior distribution for R_0 (26) was chosen to be

$$474 \quad R_0 \sim N(3.28, 0.5). \quad (17)$$

475 We assume that seeding of new infections begins 30 days before the day after a state has cumulatively
 476 observed 10 deaths. From this date, we seed our model with 6 sequential days of an equal number of
 477 infections: $i_1 = \dots = i_6 \sim \text{Exponential}(\tau^{-1})$, where $\tau \sim \text{Exponential}(0.03)$. These seed infections are
 478 inferred in our Bayesian posterior distribution. Fitting was done with the R package *epidemia* (41) which
 479 uses STAN (46), a probabilistic programming language, using an adaptive Hamiltonian Monte Carlo
 480 (HMC) sampler.

481

482 **2.2 Comparing models and evaluating performance**

483 Having established differences in the formulation of the different models, we compare their respective
 484 projections and inferences. In order to do so, we use the same data sources(47)-(48) for all five models.

Well-defined time points are used to denote training (March 15 to October 15) and test (October 16 to December 31) periods.

Using the parameter values specified above along with data from the training period as inputs, we compare the projections of the five models with observed data from the test period. In order to do so, we use the symmetric mean absolute prediction error (SMAPE) and mean squared relative prediction error (MSRPE) metrics as measures of accuracy. Given observed time-varying data $\{O_t\}_{t=1}^T$ and an analogous time-series dataset of projections $\{P_t\}_{t=1}^T$, the SMAPE metric is defined as

$$SMAPE(T) = \frac{100}{T} \cdot \sum_{t=1}^{t=T} \frac{|P_t - O_t|}{(|P_t| + |O_t|)/2}, \quad (18)$$

where $|x|$ denotes the absolute value of x . The metric MSRPE is defined as

$$MSRPE(T) = \left[T^{-1} \sum_{t=1}^T \left(1 - \frac{P_t}{O_t} \right)^2 \right]^{1/2}. \quad (19)$$

It can be seen that $0 \leq SMAPE \leq 100$, with smaller values of both MSRPE and SMAPE indicating a more accurate fit. For active reported cases (cases that are active on a given day which is the difference of cumulative reported cases and cumulative reported counts of recoveries and deaths), we compute and compare the metrics defined above for projections from eSIR and SEIR-fansy models as no other model returns relevant projections. For cumulative reported cases we obtain projections from all models apart from ICM (which yields total, i.e., sum of reported and unreported, cumulative cases). For cumulative reported deaths we compare projections from eSIR, SEIR-fansy and ICM, since the baseline and SAPHIRE models do not yield relevant projections. *Supplementary Table S2* gives an overview of output from each of the models we consider and *Table 2* reports the values of accuracy metrics described above.

504 Further, we compare (when possible) the estimated time-varying reproduction number $R(t)$ over the
 505 different lockdown and unlock stages in India. Specifically, for each lockdown stage, we report the
 506 median $R(t)$ value along with the associated 95% credible interval (CrI). The values are presented in
 507 *Table 2*.

508 Since we are interested in comparing relative performances of the models (specifically, their projections),
 509 we define another metric – the relative mean squared prediction error (Rel-MSPE). Given time series
 510 data on observed cumulative cases (or deaths) $\{O_t\}_{t=1}^T$, projections from a model A $\{P_t^A\}_{t=1}^T$, and
 511 projections from some other model B, $\{P_t^B\}_{t=1}^T$, the Rel-MSPE of model B with respect to model A is
 512 defined as

$$513 \quad Rel - MSPE(B:A) = \left[\sum_{t=1}^T \left(\frac{O_t - P_t^A}{O_t - P_t^B} \right)^2 \right]^{1/2} \quad (20)$$

514 Higher values of Rel-MSPE(B:A) indicate better performance of model B over model A. Since the
 515 baseline model yields projections of cumulative reported cases, we compute Rel-MSPE for the other
 516 models with respect to the baseline model for reported cumulative cases. Projections from ICM represent
 517 total (i.e., sum of reported and unreported) cumulative cases and are left out of this comparison of
 518 reported counts. For cumulative reported deaths, we compute Rel-MSPE of the SEIR-fansy and ICM
 519 models relative to the eSIR model. In addition to comparing the accuracy of fits that arise from the
 520 different models, we also investigate if projections from the different models are correlated with observed
 521 data. We use the standard Pearson’s correlation coefficient and Lin’s concordance correlation coefficient
 522 (49) as summary measures to study said correlation. Higher values of these correlation metrics indicate
 523 better concordance of model projections and the observed data from the test period. Rel-MSPE and

correlation metrics are presented in *Table 3*. Since we have projections for total (sum of reported and unreported cases) for active cases from SEIR-fansy, for cumulative cases from SAPHIRE, SEIR-fansy and ICM, and for cumulative deaths from SEIR-fansy, we present the projected totals along with 95% credible intervals and associated underreporting factors on three specific dates – October 31, November 30 and December 31 in *Table 4*. The table also includes projected cumulative reported counts (which are available from all models under investigation apart from ICM) with 95% credible intervals for the three dates mentioned above.

2.3 Data source

The data on confirmed cases, recovered cases and deaths for India and the 20 states of interest are taken from COVID-19 India (47) and the JHU CSSE COVID-19 GitHub repository (48). In addition to this and other similar articles concerning the spread of this disease in India, we have created an interactive dashboard (50) summarizing COVID-19 data and forecasts for India and its states (generated with the eSIR model discussed in this paper). While the models are trained using data from March 15 to October 15, 2020, their performances are compared by examining their respective projections from October 16 to December 31, 2020.

3. RESULTS

3.1. Estimation of the reproduction number

From *Table 2*, we compare the mean of the time-varying effective reproduction number $R(t)$ over the four phases of lockdown and subsequent unlock phased in India. The eSIR model returns a mean value

544 of 2.08 (95% credible interval: 1.41– 2.12) over the entire training period. Factoring in different levels
 545 of government interventions which modified transmission dynamics during lockdown, we get period
 546 specific estimates ranging from 2.12 (1.44 – 2.16) in lockdown phase 1, which drops to 1.48 (1.00 – 1.51)
 547 in lockdown phase 2 and then reports a steady decline over the subsequent lockdown and unlock phases.
 548 The mean values returned by the SAPHIRE model varied from 2.54 (2.41 – 2.74) during phase 1 of the
 549 lockdown, 1.60 (1.36 – 2.17) for phase 2, 1.69 (1.46 – 1.97) for phase 3 and 1.54 (1.29 – 2.00) for the
 550 fourth and final lockdown phase. The estimated values for subsequent unlock phases are quite close to
 551 each other, starting from 1.27 (1.19 – 1.32) in unlock phase 1 and dropping to 1.09 (0.91– 1.69) in the
 552 fifth unlock phase. The SEIR-fansy notes that the mean $R(t)$ drops from 5.03 (5.01 – 5.04) during the
 553 first phase of lockdown, to 1.90 (1.89 – 1.91) during the second lockdown phase, before rising again to
 554 2.33 (2.30 – 2.36) during lockdown phase 4. The estimated mean drops steadily from 1.80 (1.79 – 1.81)
 555 during unlock phase 2 to 0.86 (0.85 – 0.87) during unlock phase 5. The ICM-based mean values fluctuate,
 556 from 1.77 (1.58 – 1.96) during the first lockdown phase, followed by 1.22 (1.18 – 1.27), then dropping
 557 to 1.33 (1.28 – 1.38) and finally rising to 1.41 again (1.35 – 1.47) for the fourth phase of lockdown.
 558 Estimates from ICM during unlock phases behave like those from the SEIR-fansy model – in unlock
 559 phase 2 the estimated mean is 1.11 (1.08 – 1.14) and in unlock phase 5, the mean is 0.83 (0.82 – 0.84).
 560 In terms of agreement of reported values, SAPHIRE, SEIR-fansy and ICM report the highest mean R for
 561 phase one of the lockdown. Values reported by SAPHIRE, SEIR-fansy and ICM report a drop in
 562 intermediate lockdown phases, followed by a rise. Values during unlock period increase from phase 1 to
 563 phase 2, followed by a steady decline. SAPHIRE, SEIR-fansy and ICM report the lowest value of R for
 564 unlock phase 5.

565 ***3.2 Estimation of reported case counts***

566 From *Figure 6* and *Figure 9*, we note that the eSIR model overestimates the count of active cases – a
567 behavior which gets worse with time. While the observed counts decrease steadily in the test period, the
568 eSIR model fails to capture this behaviour and returns projections which rise over time. In comparison,
569 the SEIR-fansy model is able to replicate the decreasing behaviour but yields projections which are
570 higher than observed counts. In terms of prediction accuracy, the SEIR-fansy model has an SMAPE
571 value of 35.14% and an MSRPE value of 1.11. For eSIR model, those values are at 37.96% (SMAPE)
572 and 2.28 (MSRPE).

573 From *Figure 7* and *Figure 10* we note that while the SAPHIRE model underestimates the count of
574 cumulative cases, the baseline, eSIR and SEIR-fansy models overestimate the count. *Table 2* reveals that
575 SAPHIRE performs the best in terms of SMAPE metric with a value of 2.25%, followed closely by
576 SEIR-fansy (2.29%). The eSIR and baseline models perform poorly in comparison, yielding 6.59% and
577 6.89% respectively. The SEIR-fansy model performs best in terms of MSRPE with a value of 0.05,
578 followed closely by SAPHIRE (0.06). *Table 3* further reveals a similar relative performance through Rel-
579 MSPE values (all Rel-MSPE figures reported here are relative to the baseline model). The SEIR-fansy
580 model performs the best with Rel-MSPE value of 3.27, followed by SAPHIRE (3.01), and finally, the
581 eSIR model (1.72). All four sets of projections are highly correlated with the observed time series – with
582 all model projections having a Pearson’s correlation coefficient of nearly 1 with the observed data. Lin’s
583 concordance coefficient yields an ordering (from worst to best) of the eSIR model (0.48), followed by
584 the baseline model (0.51), the SAPHIRE model (0.74) and finally, the SEIR-fansy model (0.89).

585 ***3.3. Estimation of reported death counts***

586 From *Figure 8* and *Figure 11*, we note that the eSIR and SEIR-fansy models almost always overestimate,
587 whereas the ICM model slightly underestimates the confirmed cumulative death counts. From *Table 2*

588 and Table 3, the SMAPE and MSRPE values, along with comparison of projections with observed data
589 reveal that the ICM model is most accurate (SMAPE: 0.77%, MSRPE: 0.020), followed by SEIR-fansy
590 (SMAPE: 4.74%, MSRPE: 0.12) followed by the eSIR model (SMAPE: 8.94%, MSRPE: 0.25). Relative
591 to the eSIR model, the Rel-MSPE values of the models reveal that the SEIR-fansy model performs better
592 (Rel-MSPE: 6.96), followed by ICM (Rel-MSPE: 3.64). Judging by values of Pearson's correlation
593 coefficient, all three sets of projections are highly correlated with the observed data. Lin's concordance
594 coefficient yields an ordering (from best to worst) of ICM (0.96), followed by SEIR-fansy (0.62) and
595 finally eSIR (0.34).

596 ***3.4. Estimation of unreported case and death counts***

597 From Table 4, we note that the SEIR-fansy model yields underreporting factors of about 10 for active
598 cases on October 31, November 30 and December 31. Further, we observe that the SAPHIRE model
599 projects the maximum count of total cumulative cases on the above three dates, followed by the SEIR-
600 fansy and then ICM. SAPHIRE returns under-reporting factors of the order of approximately 65, while
601 SEIR-fansy and ICM return under-reporting factors which are approximately 7 and 4 respectively. For
602 cumulative deaths, SEIR-fansy estimates underreporting factors approximately equal 3.

603 ***3.5 Uncertainty quantification of estimates and predictions***

604 From Figure 12 we observe that the width of 95% credible intervals associated with projections from
605 each of the models vary significantly. While the eSIR model consistently returns the widest intervals,
606 SEIR-fansy has the narrowest intervals. In case of cumulative counts, the ordering (best to worst) starts
607 with SEIR-fansy, followed by the baseline, followed by SAPHIRE and finally the eSIR model. For
608 cumulative deaths, the ordering (best to worst) starts with SEIR-fansy, followed by ICM and finally

eSIR. From *Table 4*, we compare projections of reported cumulative cases for each model (apart from ICM which returns projections of cumulative total cases and not cumulative reported cases) and their associated prediction intervals on October 31, November 30 and December 31, 2020. On October 31, we observe 8.18 million cumulative reported cases, while the projections (in millions) from the baseline model are 8.71 (95% credible interval: 8.63 – 8.80), while eSIR yields 8.35 (7.19 – 9.60), SAPHIRE returns 8.17 (7.90 – 8.52) and SEIR-fansy projects 8.51 (8.18 – 8.85) million cases. We do not present our projections for November 30 and December 31, 2020 here in the interest of conciseness.

616

617 **4. SENSITIVITY ANALYSES AND PERFORMANCE IN OTHER COUNTRIES**

Sensitivity analyses for some of the discussed models have been carried out in several other publications. In the interest of conciseness, we refer to said publications and comment on what parameters are central to estimation and generating projections for the models examined here. We also include information on how these models have performed in the context of data from other countries.

622 **4.1 eSIR**

Evaluation of the model results in terms of their sensitivity to initial parameter choices and under-reporting and clustering issues within the data have been discussed in the context of India in prior literature (51). The range of scenarios considered earlier include 10-fold underreporting of cases, clustering of cases in metropolitan areas, and prior mean of R_0 ranging from 2-4 (See Supplementary Table S3). Even though the posterior estimates and predictions changed in scale to some extent across these scenarios, they did not significantly change the broad conclusions. It is undeniable that the exact predicted case counts are sensitive to the choice of priors, but with new data coming in over a longer

630 time frame, as seen in the results from this work, the model is capable of washing out the prior effects in
631 the posterior outcomes.

632 The eSIR model has been successfully implemented and utilized in the context of COVID-19 across
633 different geographical locations, including China (52–54), Poland (55), Italy (52), Bangladesh and
634 Pakistan (56). These countries cover a broad range in terms of socio-economic status, health
635 infrastructure and pandemic management strategies. In each of these cases the eSIR model was seen to
636 be successfully capturing the patterns of growth of the pandemic via estimated parameters, as well as
637 efficiently forecasting future case counts via predictive modeling.

638 **4.2. SAPHIRE**

639 We conducted the sensitivity analysis (results not shown) by changing the initial parameters as 20%
640 lower or higher than the specified values in the SAPHIRE model. The estimated R and ascertainment
641 rates were robust to misspecification of the duration from the onset of symptoms to isolation and of the
642 relative transmissibility of unreported versus reported cases. R estimates were positively correlated with
643 the specified latent and infectious periods, and the estimated ascertainment rates were positively
644 correlated with the specified ascertainment rate in the initial state. This finding is consistent with
645 sensitivity analyses of the SAPHIRE model implemented in Wuhan (13). The estimated ascertainment
646 rates were positively correlated with the specified ascertainment rate in the initial state while the under-
647 reported factors were negatively associated with initial ascertainment. The estimated under-reported
648 factor on October 31 (see Table 4) decreases dramatically from 117 to 0.07 with the initial ascertainment
649 rate increasing from 0.07 to 0.14, with an initial ascertainment rate of 0.10 providing the best fit, which
650 is presented in this article.

651 The SAPHIRE model was originally developed in the context of data from China and was successfully
652 able to delineate the transmission dynamics of COVID-19 in Wuhan (13) and in South Africa (57).

653 **4.3 *SEIR-fansy***

654 In the paper, we fix most parameters in our model and examine transmission dynamics only through β
655 and r . It is necessary to design and implement a sensitivity analysis focusing on various combinations of
656 the parameters that were previously fixed. The details of the sensitivity analyses are described in detail
657 in (18). The basic findings from the sensitivity analyses are summarized as follows. We observe that the
658 predictions for the reported active cases (P) remains same for all parameter choices. The estimates for
659 R_0 mainly differ in the first period, although some variation is noted for the second period as well.
660 However, the estimated R are almost the same for the later stages of the pandemic in the different models.
661 For the untested cases, in some of the settings of our analysis, there are substantial deviations from the
662 true numbers. The total number of active cases (which include both the unreported and the reported cases)
663 also varies substantially with different parameter values. Consequently, we note how the estimation of
664 unreported cases is sensitive to different choices for the parameter values. In particular, we see different
665 values of E_0 have the most impact on our sensitivity analysis, while different choices of D_E have the least
666 impact.

667 The SEIR-fansy model has not been run for different countries, but it has been implemented for most
668 Indian states separately (18) which showed that the model was able to capture the transmission dynamics
669 of COVID-19 in most states of India quite efficiently. For instance, this model was able to match the
670 sero-survey results of Delhi quite well (43). For other states, the predicted reported cases came out to be

quite close to the observed reported cases (with observed cases lying within the credible interval of projections).

4.4. ICM

The parameters critical to the estimation and projection methods include the infection-to-death distribution (28), infection fatality ratio (43,44), generation distribution (42), prior for R_0 (7,26) and seeding (7). Researchers have performed sensitivity analysis for various choices of infection-to-death distribution and found the resultant projections to be robust under changes (7). We used a range of values for our prior of IFR, with mean 1%, 0.4% and 0.1%. We found that the model fits and estimated R_t are more or less the same for all three choices but certainly our estimates for total infections changes. This implies the ascertainment of cases (positive results) will be affected. Sensitivity analyses towards the choice of the generation distribution was performed by other researchers (7) who found the models to be robust against various choices. It has a very minimal effect on the estimation of time varying reproduction number and total infections by the model. We used the R_0 prior suggested in both (7,26). We did run sensitivity on a few other choices and found that our prior choice affected the inferred R_t values for only the first few days and subsequent dynamics are the same irrespective of the choice. Finally, as discussed in (7) we validated our seeding scheme through an importance sampling leave-one-out cross validation scheme (58,59).

Different versions of ICM model has been applied to 11 European countries in (7). On a subregional basis the model is used in the USA (60), Brazil (20,61) and Italy (21). At a local level work the model is used for producing daily estimates for all local and regions in the UK (62,63). It is also used by Scotland government (64) and New York State government (65).

692

693 **4. DISCUSSION**

694 In this comparative paper we have described five different models of various stochastic structures that
695 have been used for modeling SARS-Cov-2 disease transmission in various countries across the world.
696 We applied them to a case-study in modeling the full disease transmission of the coronavirus in India.
697 While simulation studies are the only gold standard way to compare the accuracy of the models, here we
698 were uniquely poised to compare the projected case-counts and death-counts against observed data on a
699 test period. We learned several things from these models. While the estimation of the reproduction
700 number is relatively robust across the models, the prediction of active and cumulative number of cases
701 and cumulative deaths show variation across models. Our findings in terms of estimates of $R(t)$ are
702 reflective of the national and state-level implementations of four lockdown phases (66) which are
703 summarized in Supplementary Table S4. The largest variability across models is observed in predicting
704 the “total” number of infections including reported and unreported cases. The degree of underreporting
705 has been a major concern in India and other countries (67). We note from *Table 4* that the underreporting
706 factor from SAPHIRE is much higher than those reported by SEIR-fansy and ICM. This may be
707 attributed to the fact that SEIR-fansy and ICM both fit daily reported deaths with a pre-specified death
708 rate (which is higher than that for unreported cases), SAPHIRE does not include daily reported death
709 counts in the likelihood function. Additionally, SEIR-fansy also considered the false positive/negative
710 rates of tests and the selection bias in testing, which also contribute to more accurate unreported case
711 projections along with untested infectious case counts. With a comprehensive exposition and a single
712 beta-testing case-study we hope this paper will be useful to understand the mathematical nuance and the
713 differences in terms of deliverables for the models.

714 There are several limitations to this work. First and foremost, all model estimates are based on a scenario
715 where we assumed no change in either interventions or behavior of people in the forecast period. This is
716 not true as there is tremendous variation in policies across Indian states in the post lockdown phase. We
717 did observe regional lockdowns that were enacted in the forecast period. None of our models tried to
718 capture this variability. Second, the five models we compare are a subset of a vast amount of work that
719 has been done in this area, including models that incorporate age-specific contact network and
720 spatiotemporal variation (11,68). Third, we have not tested the models for predicting the oscillatory
721 growth and decay behavior of the virus incidence curve, in particular, predicting the second wave.
722 Finally, an extensive simulation study would be the best way to assess the models under different
723 scenarios, but we have restricted our attention to India.

724

725 ***LIST OF ABBREVIATIONS***

726 ICM: Imperial College Model

727 MCMC: Markov Chain-Monte Carlo

728 MSRPE: Mean squared relative prediction error

729 Rel-MSPE: Relative mean squared prediction error

730 SEIR: Susceptible-Exposed-Infected-Removed

731 SIR: Susceptible-Infected-Removed

732 SMAPE: Symmetric mean absolute prediction error

Table 1: Overview of models studied.

Name of model	Comments	Input(s) and output(s)	Parameter(s) and estimation
Baseline (Bhardwaj, R. 2020)	Curve-fitting model. Cumulative number of infected cases modeled as exponential process, with growth rate λ .	Daily time series of number of infected individuals from T_0 till T_1 ¹ (as input) and from T_1 to T_2 ² (as output).	Time varying growth rate of infection is estimated from input and modeled using least-squares regression. Estimation involves implementing MCMC ³ methods for a Bayesian framework.
eSIR (Wang, L. et al., 2020)	Extension of the standard SIR ² compartmental model.	Daily time series data on proportion of infected and recovered individuals from T_0 till T_1 ¹ (as input) and from T_1 to T_2 ² along with posterior distribution of parameters and prevalence values of the three compartments in the model (as output).	β and γ control transmission and removal rates respectively. λ and κ control variability of observed and latent processes respectively. Estimation involves implementing MCMC ³ methods for a hierarchical Bayesian framework.
SAPHIRE (Hao, X. et al., 2020)	Extension of the standard SEIR ² compartmental model.	Daily time series data from T_0 till T_1 ¹ on count of infected individuals (as input) and count of infected and removed individuals from T_1 to T_2 ² along with posterior distributions of parameters (as output). Unreported cases are also presented.	See Section 2.1.c for details on parameters. Estimation involves implementing MCMC ³ methods for a Bayesian framework.
SEIR-fansy (Bhaduri, R., Kundu, R. et al., 2020)	Another extension of standard SEIR ² , accounting for the possible effect of misclassifications due to imperfect testing.	Daily time series data from T_0 till T_1 ¹ on proportion of dead, infected and recovered individuals (as input) and from T_1 to T_2 ² along with posterior distributions of parameters and prevalence values of compartments in the model (as output). Unreported cases and deaths are also projected.	See Supplementary Table S1 for details on parameters. Estimation involves implementing MCMC ³ methods for a hierarchical Bayesian framework.
ICM (Flaxman et.al., 2020)	Renewal equation used to model infections as a latent process. Deaths are linked to infections via a survival distribution. Accounts for changes in behavior and various governmental policies enacted.	Daily time series data from T_0 till T_1 ¹ on count of dead individuals (as input) and from T_1 to T_2 ² (as output). Posterior over infections, deaths and various parameters. Infections include both symptomatic and asymptomatic ones.	See Section 2.1.c for details on parameters. Estimation is done via HMC ⁴ using STAN.

(1) T_0 : time of crossing 50 confirmed cases – March 12, 2020. T_1 : October 15, 2020. T_2 : December 31 2020.

(2) $S(E)IR$: susceptible-(exposed)-infected-removed.

(3) MCMC: Markov chain-Monte Carlo.

(4) Hamiltonian Monte Carlo.

Table 2: Comparison of estimated time-varying R_t and prediction accuracy of the models under consideration.

		Model				
		Baseline ^a	eSIR	SAPHIRE ^b	SEIR-fansy	ICM ^c
Estimated mean reproduction number R [95% CrI]	Lockdown 1.0 (March 25 – April 14)	-	2.12 [1.44, 2.16]	2.54 [2.41, 2.74]	5.03 [5.01, 5.04]	1.77 [1.58, 1.96]
	Lockdown 2.0 (April 15 – May 3)		1.48 [1.00, 1.51]	1.60 [1.36, 2.17]	1.90 [1.89, 1.91]	1.22 [1.18, 1.27]
	Lockdown 3.0 (May 4 – May 17)		0.87 [0.59, 0.89]	1.69 [1.46, 1.97]	2.71 [2.67, 2.73]	1.33 [1.28, 1.38]
	Lockdown 4.0 (May 18 – May 31)		0.89 [0.61, 0.91]	1.54 [1.29, 2.00]	2.33 [2.30, 2.36]	1.41 [1.35, 1.47]
	Unlock 1.0 (June 1 – June 30)		0.85 [0.58, 0.87]	1.27 [1.19, 1.32]	1.74 [1.73, 1.75]	1.05 [0.99, 1.10]
	Unlock 2.0 (July 1 – July 31)		0.77 [0.52, 0.78]	1.31 [1.22, 1.36]	1.80 [1.79, 1.81]	1.11 [1.08, 1.14]
	Unlock 3.0 (August 1 – August 31)		0.79 [0.54, 0.81]	1.16 [1.06, 1.31]	1.25 [1.24, 1.26]	1.05 [1.04, 1.07]
	Unlock 4.0 (September 1 – September 30)		0.69 [0.47, 0.7]	1.12 [0.98, 1.49]	1.06 [1.05, 1.07]	0.89 [0.86, 0.91]
	Unlock 5.0 (October 1 – October 15)		0.67 [0.45, 0.68]	1.09 [0.91, 1.69]	0.86 [0.85, 0.87]	0.83 [0.82, 0.84]
Prediction accuracy using %SMAPE (MSRPE) ^d	Active reported cases	-	37.955 (2.283)	-	35.141 (1.114)	-
	Cumulative reported cases	6.889 (0.173)	6.593 (0.198)	2.250 (0.056)	2.285 (0.048)	
	Cumulative reported deaths	-	8.943 (0.253)	-	4.737 (0.115)	0.771 (0.020)

^aThe baseline model does not return estimates of time-varying $R(t)$ or projections of active reported cases or cumulative reported deaths.

^bThe SAPHIRE model does not return projections of active reported cases or cumulative reported deaths.

^cThe ICM model does not return projections of active or cumulative reported cases.

^dWe compare model projections with observed reported data from October 16 till December 31, 2020.

Table 3: Comparison of relative performance and correlation with observed data of projections of the models under consideration from October 16 till December 31, 2020.

Observed data (confirmed)	Metric	Model				
		Baseline	eSIR	SAPHIRE	SEIR-fansy	ICM ^e
Cumulative cases	Rel-MSPE ^a	1	1.724	3.013	3.270	-
	Pearson's correlation coefficient ^b	0.996	0.969	0.984	0.999	
	Lin's concordance coefficient ^b	0.507	0.476	0.738	0.891	
Cumulative deaths	Rel-MSPE ^c	-	1	-	6.962	3.64
	Pearson's correlation coefficient ^d		1		1	0.996
	Lin's concordance coefficient ^d		0.339		0.616	0.956

^aFor cumulative reported cases, Rel-MSPE is defined relative to projections from the baseline model.

^bFor cumulative reported cases, the correlation coefficients of the projections are compared with respect to observed data.

^cFor cumulative reported deaths, Rel-MSPE is defined relative to projections from the eSIR model.

^dFor cumulative reported deaths, the correlation coefficients of the projections are compared with respect to observed data.

^eThe ICM model returns total (reported + unreported) cumulative case counts, so we leave it out of our comparisons.

Table 4: Projected counts of reported cumulative cases and total (sum of reported and unreported) counts of cases and deaths (cumulative) from the models under comparison

Projected cumulative reported counts (95% CrI) for specific dates in test period^c				
Counts	Model	October 31, 2020	November 30, 2020	December 31, 2020
Cumulative cases (in millions)	Observed	8.18	9.46	10.29
	Baseline	8.71 (8.63-8.80)	11.12 (10.83-11.43)	13.34 (12.81-13.93)
	eSIR	8.35 (7.19-9.60)	10.91 (8.38-13.93)	14.85 (9.88-21.81)
	SAPHIRE	8.17 (7.90-8.52)	8.93 (8.17-9.67)	9.26 (8.19-10.35)
	SEIR-fansy	8.51 (8.18-8.85)	9.91 (9.54-10.30)	10.97 (10.57-11.4)
Projected total counts^a (95% CrI) [under-reporting factor^b] for specific dates in test period^c				
Counts	Model	October 31, 2020	November 30, 2020	December 31, 2020
Active cases (in millions)	Observed	0.57	0.44	0.26
	SEIR-fansy	5.32 (5.12-5.52) [9.3]	3.99 (3.85-4.14) [9.13]	2.96 (2.85-3.06) [11.53]
Cumulative cases (in millions)	Observed	8.18	9.46	10.29
	SAPHIRE ^d	578.21 (46.41-1134.20) [70.7]	612.79 (52.253-1161.26) [64.8]	622.32 (55.79-1163.17) [60.5]
	SEIR-fansy	59.32 (56.8-61.72) [7.25]	68.71 (65.95-71.47) [7.26]	75.89 (72.89-78.86) [7.38]
	ICM ^d	37.17 (24.78-58.68) [4.54]	39.54 (25.63-63.12) [4.18]	41.38 (26.02-67.88) [4.02]
Cumulative deaths (thousand)	Observed	121.56	137.07	148.43
	SEIR-fansy	361.52 (347.23-375.85) [2.97]	442.25 (425.05-459.64) [3.23]	504.76 (485.50-524.07) [3.4]

^aProjected total count includes both reported as well as unreported values.

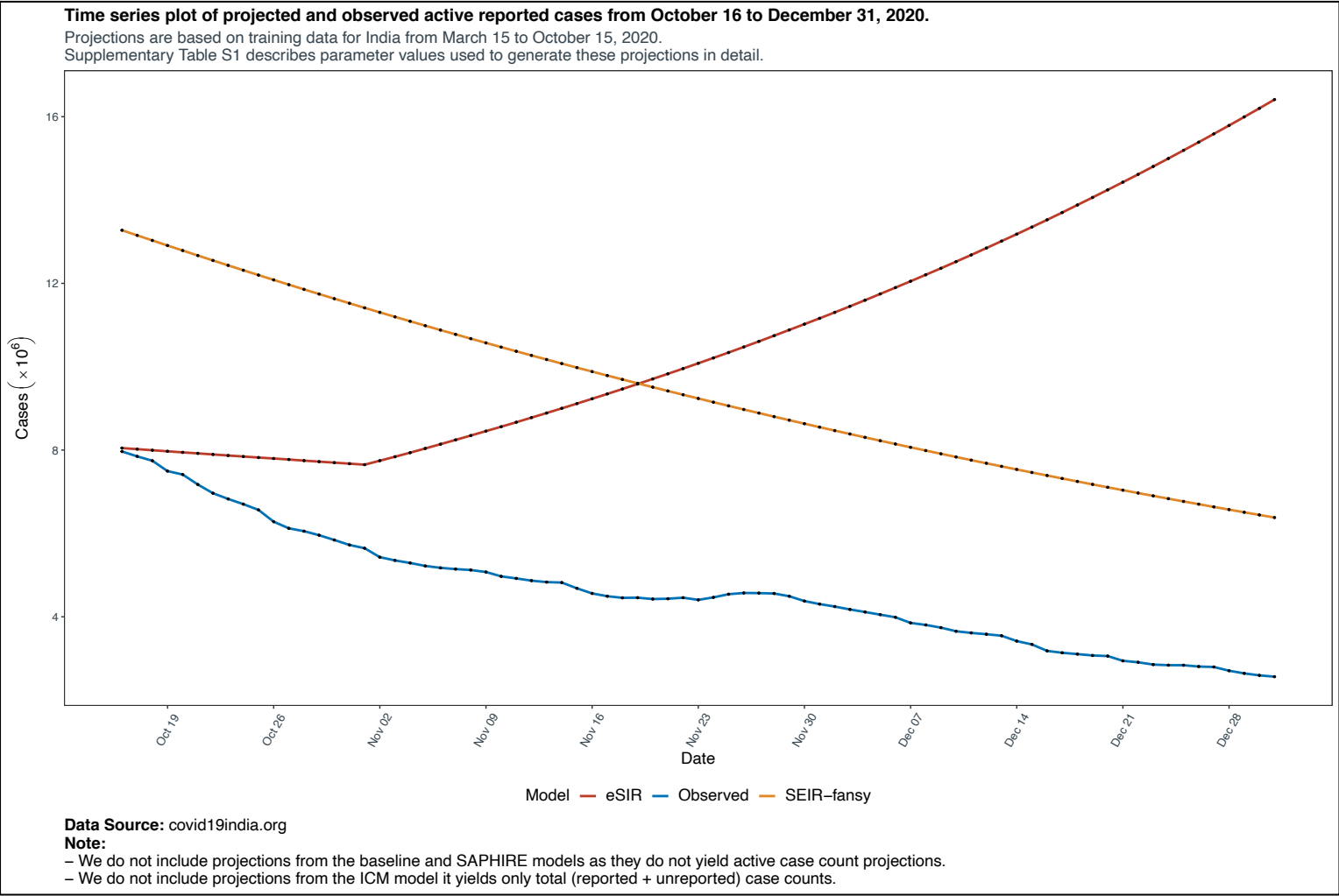
^bDefined as projected total/observed reported counts, where total is the sum of reported and unreported cases.

^cThe test period extends from October 16 till December 31, 2020. We examine projections of cumulative cases and counts on three specific dates within that period, namely, October 31, November 30 and December 31, 2020.

^dThe SAPHIRE model does not yield projections of active cases or cumulative deaths while the ICM model does not yield projections of cumulative reported cases, total active cases or total cumulative deaths.

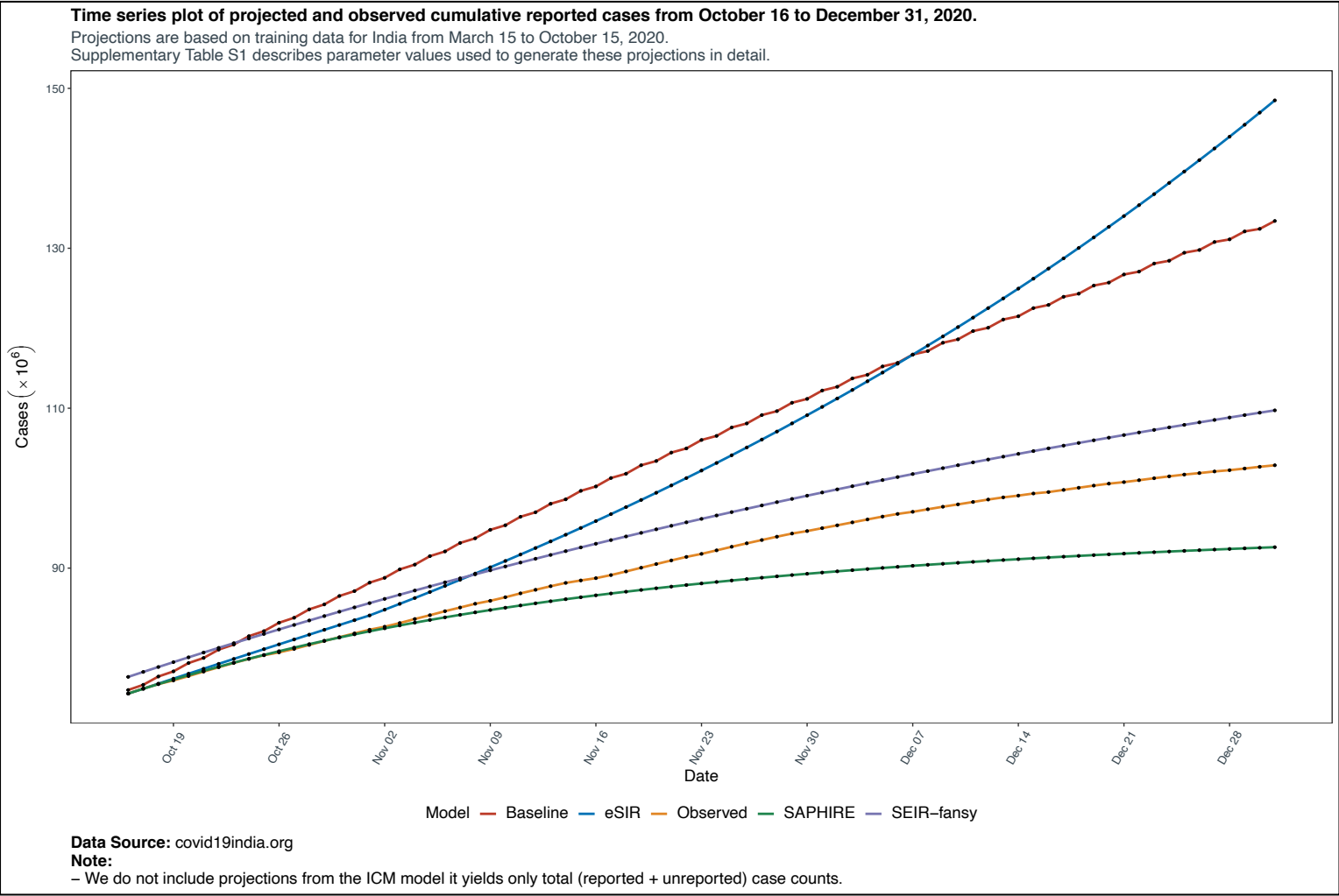
762 **FIGURES**

763 *Figure 6: Comparison of projected and observed reported active cases from October 16 to December 31 for India, using training data*
764 *from March 15 to October 15, 2020.*



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Figure 7: Comparison of projected and observed reported cumulative cases from October 16 to December 31 for India, using training data from March 15 to October 15, 2020.

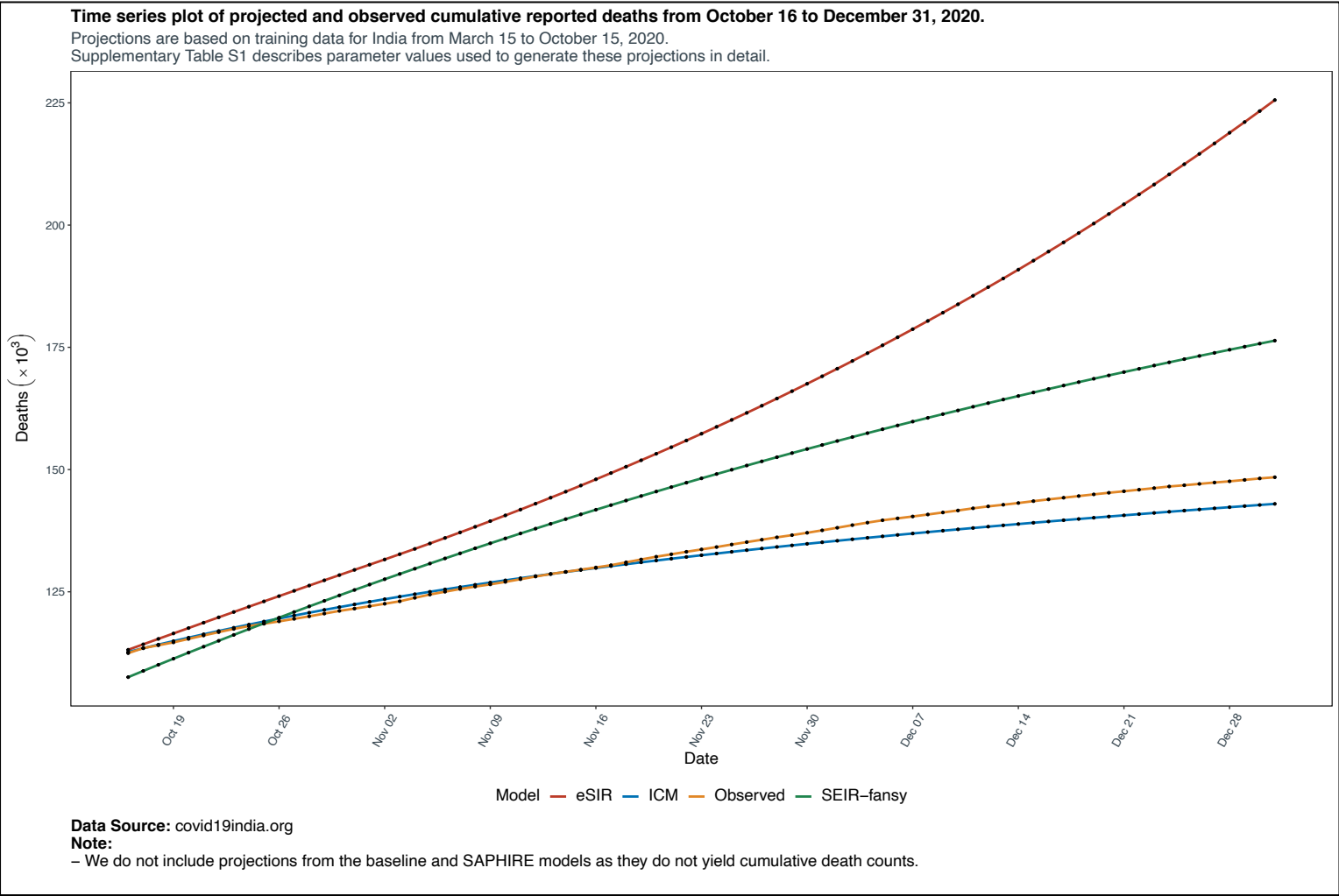


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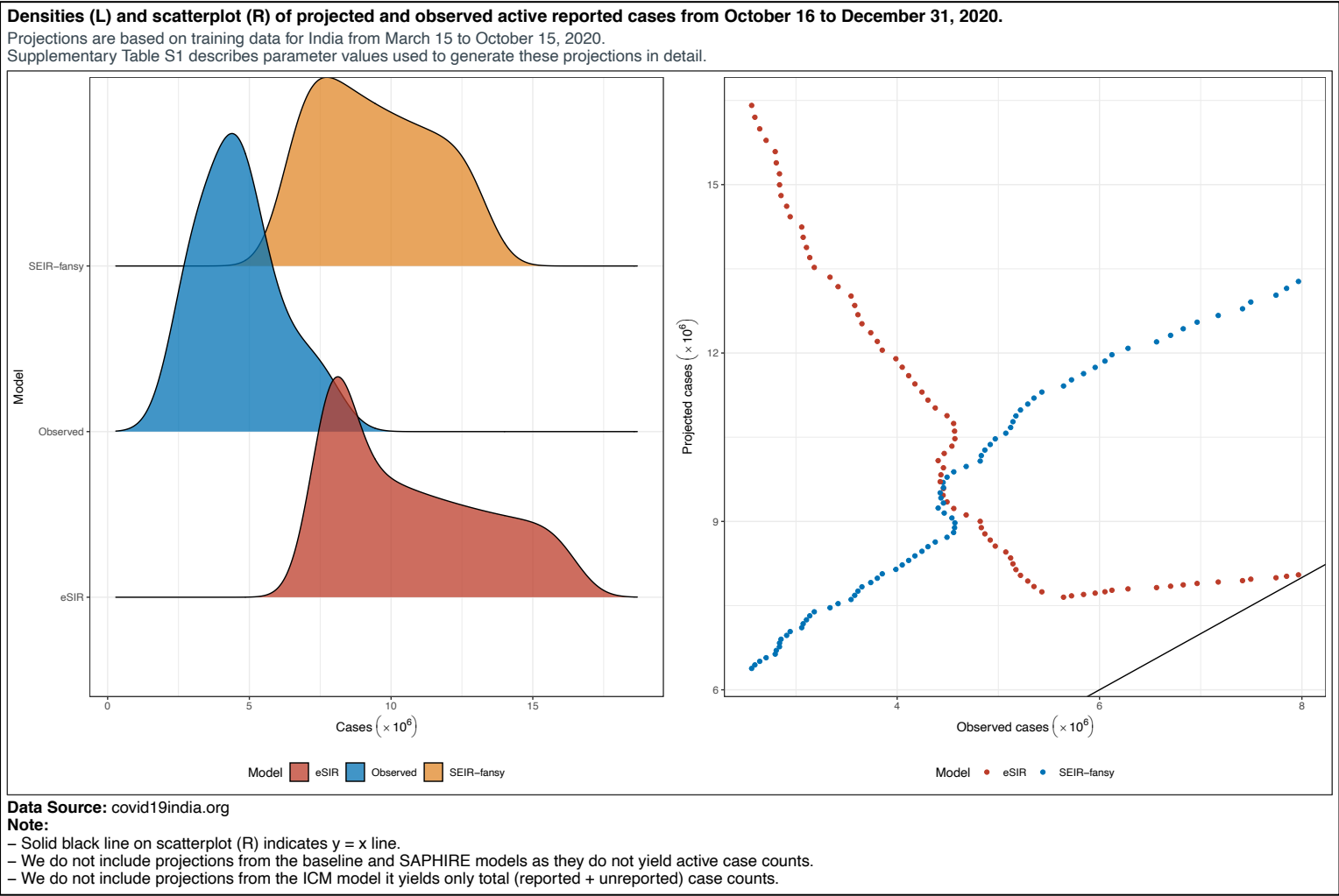
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Figure 8: Comparison of projected and observed reported cumulative deaths from October 16 to December 31 for India, using training data from March 15 to October 15, 2020.

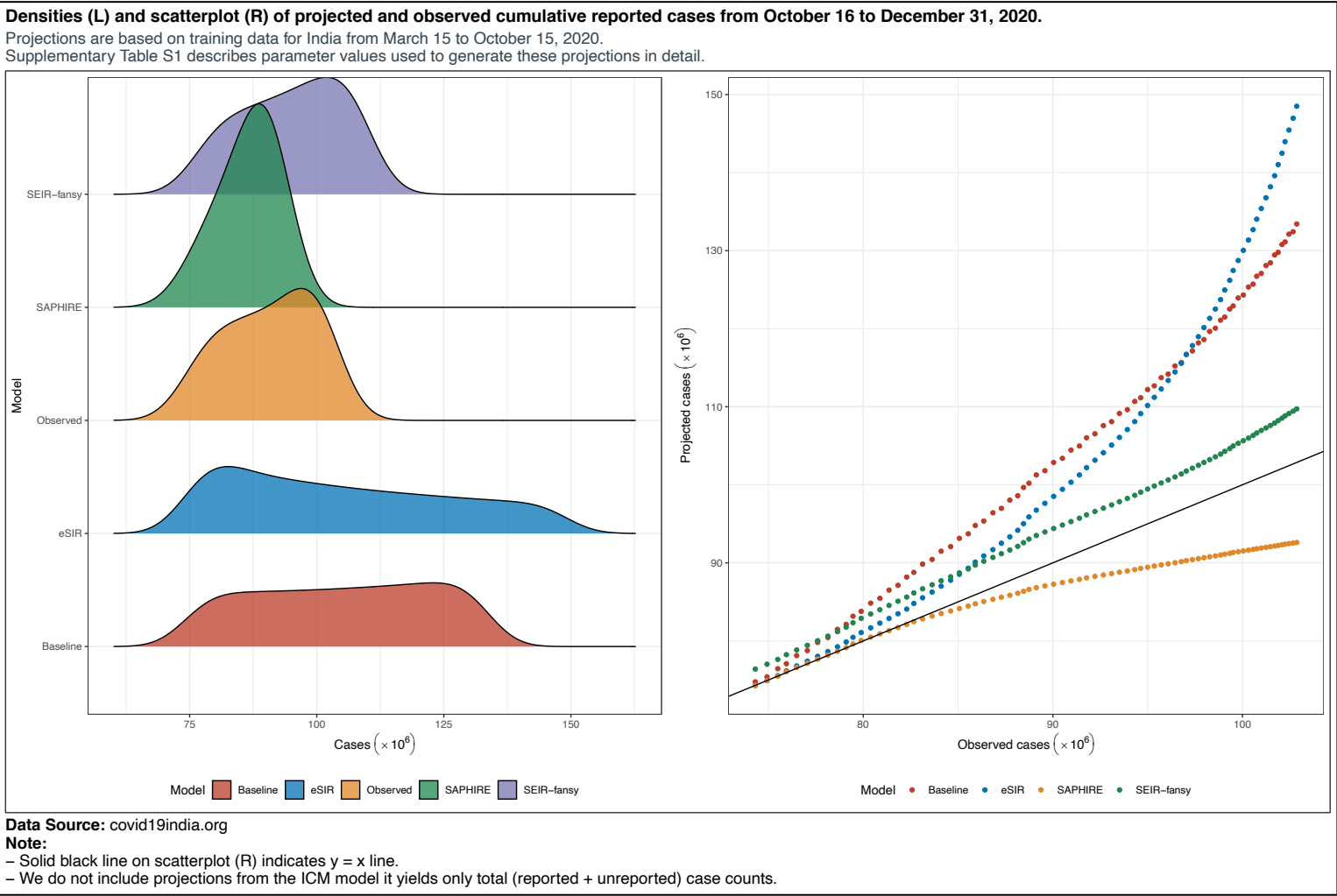


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802 *Figure 9: Scatter plot and marginal densities of projected and observed reported active cases from October 16 to December 31 for*
803 *India, using training data from March 15 to October 15, 2020.*

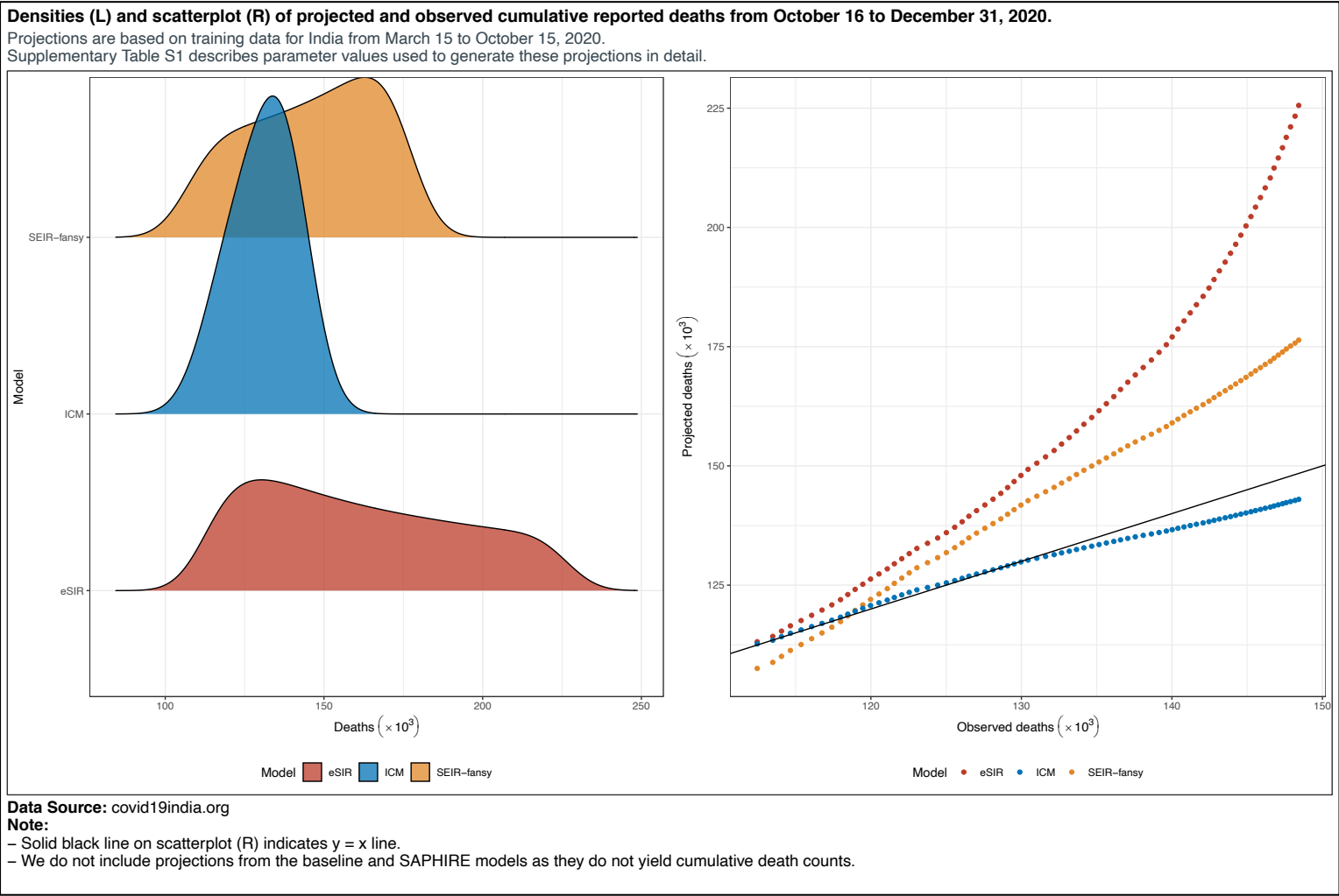


805 *Figure 10: Scatter plot and marginal densities of projected and observed cumulative cases from October 16 to December 31 for India,*
806 *using training data from March 15 to October 15, 2020.*



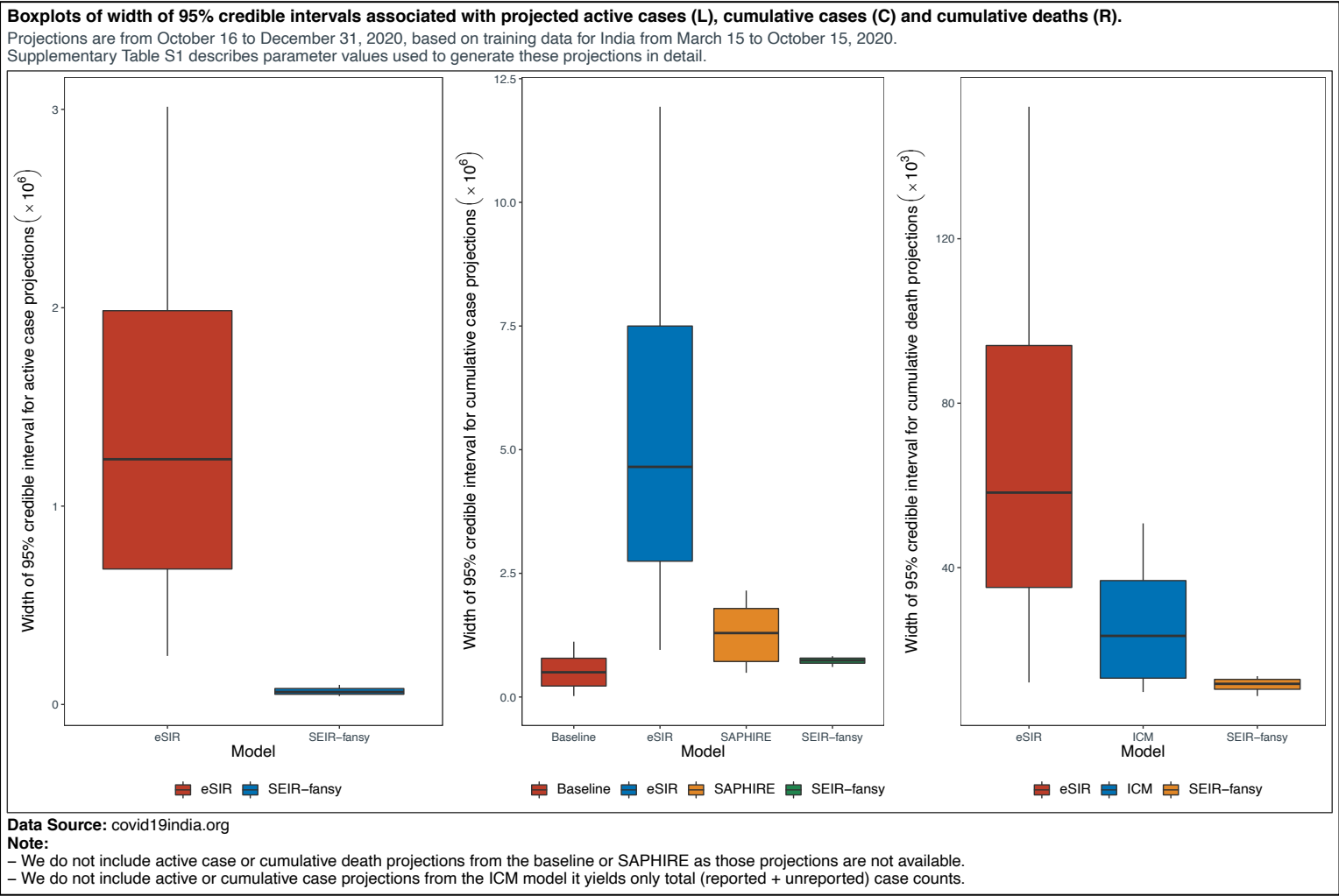
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808 *Figure 11: Scatter plot and marginal densities of projected and observed cumulative death from October 16 to December 31 for India,*
809 *using training data from March 15 to October 15, 2020.*



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811 *Figure 12: Boxplots showing width of 95% credible interval associated with projected active cases, cumulative cases and cumulative*
 812 *deaths from October 16 to December 31 for India, using training data from March 15 to October 15, 2020.*



814 *REFERENCES*

815

816 1. Mayo Clinic. Coronavirus disease 2019 (COVID-19)—Symptoms and causes [Internet]. 2020
817 [cited 2020 May 21]. Available from: [https://www.mayoclinic.org/diseases-](https://www.mayoclinic.org/diseases-conditions/coronavirus/symptoms-causes/syc-20479963)
818 [conditions/coronavirus/symptoms-causes/syc-20479963](https://www.mayoclinic.org/diseases-conditions/coronavirus/symptoms-causes/syc-20479963)

819 2. Wikipedia. Coronavirus disease 2019 [Internet]. [cited 2020 Aug 3]. Available from:
820 https://en.wikipedia.org/wiki/Coronavirus_disease_2019

821 3. Aiyar S. Covid-19 has exposed India’s failure to deliver even the most basic obligations to its
822 people [Internet]. CNN. 2020 [cited 2020 Aug 3]. Available from:
823 <https://www.cnn.com/2020/07/18/opinions/india-coronavirus-failures-opinion-intl-hnk/index.html>

824 4. Kulkarni S. India becomes third worst affected country by coronavirus, overtakes Russia Read
825 more at: [https://www.deccanherald.com/national/india-becomes-third-worst-affected-country-by-](https://www.deccanherald.com/national/india-becomes-third-worst-affected-country-by-coronavirus-overtakes-russia-857442.html)
826 [coronavirus-overtakes-russia-857442.html](https://www.deccanherald.com/national/india-becomes-third-worst-affected-country-by-coronavirus-overtakes-russia-857442.html) [Internet]. Deccan Herald. [cited 2020 Aug 3].
827 Available from: [https://www.deccanherald.com/national/india-becomes-third-worst-affected-](https://www.deccanherald.com/national/india-becomes-third-worst-affected-country-by-coronavirus-overtakes-russia-857442.html)
828 [country-by-coronavirus-overtakes-russia-857442.html](https://www.deccanherald.com/national/india-becomes-third-worst-affected-country-by-coronavirus-overtakes-russia-857442.html)

829 5. Basu D, Salvatore M, Ray D, Kleinsasser M, Purkayastha S, Bhattacharyya R, et al. A
830 Comprehensive Public Health Evaluation of Lockdown as a Non-pharmaceutical Intervention on
831 COVID-19 Spread in India: National Trends Masking State Level Variations [Internet].
832 Epidemiology; 2020 May [cited 2020 Aug 3]. Available from:
833 <http://medrxiv.org/lookup/doi/10.1101/2020.05.25.20113043>

834 6. IHME COVID-19 health service utilization forecasting team, Murray CJ. Forecasting COVID-19
835 impact on hospital bed-days, ICU-days, ventilator-days and deaths by US state in the next 4
836 months [Internet]. Infectious Diseases (except HIV/AIDS); 2020 Mar [cited 2020 Aug 18].
837 Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.03.27.20043752>

838 7. Imperial College COVID-19 Response Team, Flaxman S, Mishra S, Gandy A, Unwin HJT, Mellan
839 TA, et al. Estimating the effects of non-pharmaceutical interventions on COVID-19 in Europe.
840 Nature [Internet]. 2020 Jun 8 [cited 2020 Aug 7]; Available from:
841 <http://www.nature.com/articles/s41586-020-2405-7>

842 8. Tang L, Zhou Y, Wang L, Purkayastha S, Zhang L, He J, et al. A Review of Multi-Compartment
843 Infectious Disease Models. Int Stat Rev. 2020 Aug 3;insr.12402.

844 9. Kermack WO, McKendrick AG. Contributions to the mathematical theory of epidemics—I. Bull
845 Math Biol. 1991 Mar;53(1–2):33–55.

846 10. Song PX, Wang L, Zhou Y, He J, Zhu B, Wang F, et al. An epidemiological forecast model and
847 software assessing interventions on COVID-19 epidemic in China. medRxiv [Internet]. 2020;
848 Available from: <https://www.medrxiv.org/content/10.1101/2020.02.29.20029421v1>

- 849 11. Zhou Y, Wang L, Zhang L, Shi L, Yang K, He J, et al. A Spatiotemporal Epidemiological Prediction
850 Model to Inform County-Level COVID-19 Risk in the United States. *Harv Data Sci Rev*
851 [Internet]. 2020 Jun 17 [cited 2020 Aug 3]; Available from:
852 <https://hdsr.mitpress.mit.edu/pub/qqg19a0r>
- 853 12. Wu JT, Leung K, Leung GM. Nowcasting and forecasting the potential domestic and international
854 spread of the 2019-nCoV outbreak originating in Wuhan, China: a modelling study. *The Lancet*.
855 2020 Feb;395(10225):689–97.
- 856 13. Hao X, Cheng S, Wu D, Wu T, Lin X, Wang C. Reconstruction of the full transmission dynamics of
857 COVID-19 in Wuhan. *Nature* [Internet]. 2020 Jul 16 [cited 2020 Aug 18]; Available from:
858 <http://www.nature.com/articles/s41586-020-2554-8>
- 859 14. Bai Y, Yao L, Wei T, Tian F, Jin D-Y, Chen L, et al. Presumed Asymptomatic Carrier Transmission
860 of COVID-19. *JAMA*. 2020 Apr 14;323(14):1406.
- 861 15. Tong Z-D, Tang A, Li K-F, Li P, Wang H-L, Yi J-P, et al. Potential Presymptomatic Transmission of
862 SARS-CoV-2, Zhejiang Province, China, 2020. *Emerg Infect Dis*. 2020 May;26(5):1052–4.
- 863 16. Bertozzi AL, Franco E, Mohler G, Short MB, Sledge D. The challenges of modeling and
864 forecasting the spread of COVID-19. *Proc Natl Acad Sci*. 2020 Jul 2;202006520.
- 865 17. Bhardwaj R. A Predictive Model for the Evolution of COVID-19. *Trans Indian Natl Acad Eng*.
866 2020 Jun;5(2):133–40.
- 867 18. Bhaduri R, Kundu R, Purkayastha S, Kleinsasser M, Beesley LJ, Mukherjee B. Extending the
868 susceptible-exposed-infected-removed (SEIR) model to handle the high false negative rate and
869 symptom-based administration of COVID-19 diagnostic tests: SEIR-fansy [Internet].
870 *Epidemiology*; 2020 Sep [cited 2021 Feb 20]. Available from:
871 <http://medrxiv.org/lookup/doi/10.1101/2020.09.24.20200238>
- 872 19. Unwin HJT, Mishra S, Bradley VC, Gandy A, Mellan TA, Coupland H, et al. State-level tracking of
873 COVID-19 in the United States [Internet]. *Public and Global Health*; 2020 Jul [cited 2020 Sep
874 16]. Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.07.13.20152355>
- 875 20. Mellan TA, Hoeltgebaum HH, Mishra S, Whittaker C, Schnekenberg RP, Gandy A, et al.
876 Subnational analysis of the COVID-19 epidemic in Brazil [Internet]. *Epidemiology*; 2020 May
877 [cited 2020 Sep 16]. Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.05.09.20096701>
- 878 21. Vollmer MAC, Mishra S, Unwin HJT, Gandy A, Mellan TA, Bradley V, et al. A sub-national
879 analysis of the rate of transmission of COVID-19 in Italy [Internet]. *Public and Global Health*;
880 2020 May [cited 2020 Sep 16]. Available from:
881 <http://medrxiv.org/lookup/doi/10.1101/2020.05.05.20089359>

- 882 22. Lau H, Khosrawipour T, Kocbach P, Ichii H, Bania J, Khosrawipour V. Evaluating the massive
883 underreporting and undertesting of COVID-19 cases in multiple global epicenters. *Pulmonology*.
884 2020 Jun;S253104372030129X.
- 885 23. Gelman A. *Bayesian data analysis*. Third edition. Boca Raton: CRC Press; 2014. 661 p. (Chapman
886 & Hall/CRC texts in statistical science).
- 887 24. R Core Team. *R: A Language and Environment for Statistical Computing* [Internet]. Vienna,
888 Austria: R Foundation for Statistical Computing; 2017. Available from: [https://www.R-](https://www.R-project.org/)
889 [project.org/](https://www.R-project.org/)
- 890 25. Butcher JC. *Numerical methods for ordinary differential equations*. 2nd ed. Chichester, England ;
891 Hoboken, NJ: Wiley; 2008. 463 p.
- 892 26. Liu Y, Gayle AA, Wilder-Smith A, Rocklöv J. The reproductive number of COVID-19 is higher
893 compared to SARS coronavirus. *J Travel Med*. 2020 Mar 13;27(2):taaa021.
- 894 27. Cori A, Ferguson NM, Fraser C, Cauchemez S. A New Framework and Software to Estimate Time-
895 Varying Reproduction Numbers During Epidemics. *Am J Epidemiol*. 2013 Nov 1;178(9):1505–
896 12.
- 897 28. Verity R, Okell LC, Dorigatti I, Winskill P, Whittaker C, Imai N, et al. Estimates of the severity of
898 coronavirus disease 2019: a model-based analysis. *Lancet Infect Dis*. 2020 Jun;20(6):669–77.
- 899 29. Plummer M. *rjags: Bayesian graphical models using MCMC*. R Package Version. 2016;4(6).
- 900 30. Li R, Pei S, Chen B, Song Y, Zhang T, Yang W, et al. Substantial undocumented infection facilitates
901 the rapid dissemination of novel coronavirus (SARS-CoV-2). *Science*. 2020 May
902 1;368(6490):489–93.
- 903 31. He X, Lau EHY, Wu P, Deng X, Wang J, Hao X, et al. Temporal dynamics in viral shedding and
904 transmissibility of COVID-19. *Nat Med*. 2020 May;26(5):672–5.
- 905 32. Li Q, Guan X, Wu P, Wang X, Zhou L, Tong Y, et al. Early Transmission Dynamics in Wuhan,
906 China, of Novel Coronavirus–Infected Pneumonia. *N Engl J Med*. 2020 Mar 26;382(13):1199–
907 207.
- 908 33. Ferretti L, Wymant C, Kendall M, Zhao L, Nurtay A, Abeler-Dörner L, et al. Quantifying SARS-
909 CoV-2 transmission suggests epidemic control with digital contact tracing. *Science*. 2020 May
910 8;368(6491):eabb6936.
- 911 34. Mishra V, Burma A, Das S, Parivallal M, Amudhan S, Rao G. COVID-19-Hospitalized Patients in
912 Karnataka: Survival and Stay Characteristics. *Indian J Public Health*. 2020;64(6):221.
- 913 35. Garg S, Kim L, Whitaker M, O’Halloran A, Cummings C, Holstein R, et al. Hospitalization Rates
914 and Characteristics of Patients Hospitalized with Laboratory-Confirmed Coronavirus Disease

- 915 2019 — COVID-NET, 14 States, March 1–30, 2020. *MMWR Morb Mortal Wkly Rep*. 2020 Apr
916 17;69(15):458–64.
- 917 36. Wang D, Hu B, Hu C, Zhu F, Liu X, Zhang J, et al. Clinical Characteristics of 138 Hospitalized
918 Patients With 2019 Novel Coronavirus–Infected Pneumonia in Wuhan, China. *JAMA*. 2020 Mar
919 17;323(11):1061.
- 920 37. Rahmandad H, Lim TY, Sterman J. Estimating the Global Spread of COVID-19. *SSRN Electron J*
921 [Internet]. 2020 [cited 2021 Mar 18]; Available from: <https://www.ssrn.com/abstract=3635047>
- 922 38. Bhaduri R, Kundu R, Purkayastha S, Beesley LJ, Kleinsasser M, Mukherjee B. SEIRfansy:
923 Extended Susceptible-Exposed-Infected-Recovery Model [Internet]. 2020. Available from:
924 <https://CRAN.R-project.org/package=SEIRfansy>
- 925 39. Diekmann O, Heesterbeek JAP, Roberts MG. The construction of next-generation matrices for
926 compartmental epidemic models. *J R Soc Interface*. 2010 Jun 6;7(47):873–85.
- 927 40. Robert CP, Casella G. Monte Carlo Statistical Methods [Internet]. New York, NY: Springer New
928 York; 2004 [cited 2020 Aug 14]. (Springer Texts in Statistics). Available from:
929 <http://link.springer.com/10.1007/978-1-4757-4145-2>
- 930 41. Scott J, Gandy A, Mishra S, Unwin J, Flaxman S, Bhatt S. *epidemia: Modeling of Epidemics using*
931 *Hierarchical Bayesian Models* [Internet]. 2020. Available from:
932 <https://imperialcollegelondon.github.io/epidemia/>
- 933 42. Bi Q, Wu Y, Mei S, Ye C, Zou X, Zhang Z, et al. Epidemiology and transmission of COVID-19 in
934 391 cases and 1286 of their close contacts in Shenzhen, China: a retrospective cohort study.
935 *Lancet Infect Dis*. 2020 Aug;20(8):911–9.
- 936 43. Bhattacharyya R, Bhaduri R, Kundu R, Salvatore M, Mukherjee B. Reconciling epidemiological
937 models with misclassified case-counts for SARS-CoV-2 with seroprevalence surveys: A case
938 study in Delhi, India [Internet]. *Infectious Diseases (except HIV/AIDS)*; 2020 Aug [cited 2021
939 Mar 19]. Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.07.31.20166249>
- 940 44. Murhekar MV, Bhatnagar T, Selvaraju S, Saravanakumar V, Thangaraj JWV, Shah N, et al. SARS-
941 CoV-2 antibody seroprevalence in India, August–September, 2020: findings from the second
942 nationwide household serosurvey. *Lancet Glob Health*. 2021 Mar;9(3):e257–66.
- 943 45. Walker PGT, Whittaker C, Watson OJ, Baguelin M, Winskill P, Hamlet A, et al. The impact of
944 COVID-19 and strategies for mitigation and suppression in low- and middle-income countries.
945 *Science*. 2020 Jun 12;eabc0035.
- 946 46. Carpenter B, Gelman A, Hoffman MD, Lee D, Goodrich B, Betancourt M, et al. *Stan : A*
947 *Probabilistic Programming Language*. *J Stat Softw* [Internet]. 2017 [cited 2020 Aug 29];76(1).
948 Available from: <http://www.jstatsoft.org/v76/i01/>

- 949 47. India C-19. Coronavirus Outbreak in India [Internet]. 2020 [cited 2020 May 21]. Available from:
950 <https://www.covid19india.org>
- 951 48. Johns Hopkins University. COVID-19 Dashboard by the Center for Systems Science and
952 Engineering (CSSE) at Johns Hopkins University (JHU) [Internet]. 2020 [cited 2020 May 21].
953 Available from: <https://coronavirus.jhu.edu/map.html>
- 954 49. Lin LI-K. A Concordance Correlation Coefficient to Evaluate Reproducibility. *Biometrics*. 1989
955 Mar;45(1):255.
- 956 50. Group C-I-19 S. COVID-19 Outbreak in India [Internet]. 2020 [cited 2020 May 21]. Available
957 from: <https://umich-biostatistics.shinyapps.io/covid19/>
- 958 51. Ray D, Salvatore M, Bhattacharyya R, Wang L, Du J, Mohammed S, et al. Predictions, Role of
959 Interventions and Effects of a Historic National Lockdown in India's Response to the the COVID-
960 19 Pandemic: Data Science Call to Arms. *Harv Data Sci Rev* [Internet]. 2020 05-14; Available
961 from: <https://hdr.mitpress.mit.edu/pub/r1qq01kw>
- 962 52. Wangping J, Ke H, Yang S, Wenzhe C, Shengshu W, Shanshan Y, et al. Extended SIR Prediction of
963 the Epidemics Trend of COVID-19 in Italy and Compared With Hunan, China. *Front Med*. 2020
964 May 6;7:169.
- 965 53. Wang L, Zhou Y, He J, Zhu B, Wang F, Tang L, et al. An epidemiological forecast model and
966 software assessing interventions on COVID-19 epidemic in China [Internet]. *Infectious Diseases*
967 (except HIV/AIDS); 2020 Mar [cited 2021 Mar 19]. Available from:
968 <http://medrxiv.org/lookup/doi/10.1101/2020.02.29.20029421>
- 969 54. Enrique Amaro J, Dudouet J, Nicolás Orce J. Global analysis of the COVID-19 pandemic using
970 simple epidemiological models. *Appl Math Model*. 2021 Feb;90:995–1008.
- 971 55. Orzechowska M, Bednarek AK. Forecasting COVID-19 pandemic in Poland according to
972 government regulations and people behavior [Internet]. *Infectious Diseases (except HIV/AIDS)*;
973 2020 May [cited 2021 Mar 19]. Available from:
974 <http://medrxiv.org/lookup/doi/10.1101/2020.05.26.20112458>
- 975 56. Singh BC, Alom Z, Rahman MM, Baowaly MK, Azim MA. COVID-19 Pandemic Outbreak in the
976 Subcontinent: A data-driven analysis. *ArXiv200809803 Cs* [Internet]. 2020 Aug 22 [cited 2021
977 Mar 19]; Available from: <http://arxiv.org/abs/2008.09803>
- 978 57. Gu X, Mukherjee B, Das S, Datta J. COVID-19 PREDICTION IN SOUTH AFRICA:
979 ESTIMATING THE UNASCERTAINED CASES- THE HIDDEN PART OF THE
980 EPIDEMIOLOGICAL ICEBERG [Internet]. *Epidemiology*; 2020 Dec [cited 2021 Mar 21].
981 Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.12.10.20247361>
- 982 58. Vehtari A, Gelman A, Gabry J. Practical Bayesian model evaluation using leave-one-out cross-
983 validation and WAIC. *Stat Comput*. 2017 Sep;27(5):1413–32.

984 59. Bürkner P-C, Gabry J, Vehtari A. Approximate leave-future-out cross-validation for Bayesian time
985 series models. *J Stat Comput Simul*. 2020 Sep 21;90(14):2499–523.

986 60. Unwin HJT, Mishra S, Bradley VC, Gandy A, Mellan TA, Coupland H, et al. State-level tracking of
987 COVID-19 in the United States. *Nat Commun*. 2020 Dec;11(1):6189.

988 61. Candido DS, Claro IM, de Jesus JG, Souza WM, Moreira FRR, Dellicour S, et al. Evolution and
989 epidemic spread of SARS-CoV-2 in Brazil. *Science*. 2020 Sep 4;369(6508):1255–60.

990 62. Mishra S, Scott J, Zhu H, Ferguson NM, Bhatt S, Flaxman S, et al. A COVID-19 Model for Local
991 Authorities of the United Kingdom [Internet]. *Infectious Diseases (except HIV/AIDS)*; 2020 Nov
992 [cited 2021 Mar 20]. Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.11.24.20236661>

993 63. Gandy A, Swapnil Mishra. ImperialCollegeLondon/covid19local: Website Release for Wednesday
994 11th Mar 2021, new doi for the week [Internet]. *Zenodo*; 2021 [cited 2021 Mar 20]. Available
995 from: <https://zenodo.org/record/4609660>

996 64. Scottish Government. Coronavirus (COVID-19): modelling the epidemic [Internet]. Available
997 from: <https://www.gov.scot/collections/coronavirus-covid-19-modelling-the-epidemic/>

998 65. Cuomo AM. American crisis. 2020.

999 66. Salvatore M, Basu D, Ray D, Kleinsasser M, Purkayastha S, Bhattacharyya R, et al.
1000 Comprehensive public health evaluation of lockdown as a non-pharmaceutical intervention on
1001 COVID-19 spread in India: national trends masking state-level variations. *BMJ Open*. 2020
1002 Dec;10(12):e041778.

1003 67. Rahmandad H, Lim TY, Sterman J. Estimating COVID-19 under-reporting across 86 nations:
1004 implications for projections and control [Internet]. *Epidemiology*; 2020 Jun [cited 2020 Sep 16].
1005 Available from: <http://medrxiv.org/lookup/doi/10.1101/2020.06.24.20139451>

1006 68. Balabdaoui F, Mohr D. Age-stratified discrete compartment model of the COVID-19 epidemic with
1007 application to Switzerland. *Sci Rep*. 2020 Dec;10(1):21306.

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Supplementary Table S1: Summary of initial values and parameter settings for application of the SEIR-fansy model in the context of COVID-19 data from India. Unless mentioned otherwise, we use these parameter settings for all other models when applicable.

Parameters	Settings	Description
β	Time-varying	Rate of infectious transmission by infected individuals with false negative test results.
α_p	0.5	Ratio of rate of spread of infection by patients who test positive, to rate of spread of infection by patients who get false negative results ^a .
α_U	0.7	Scaling factor for the rate of spread of infection by untested individuals ^a .
D_e	5.2	Incubation period (in days).
D_r	17	Recovery time (in days) for infected individuals.
D_t	0	Waiting time (in days) for test result for tested individuals.
μ_c	0.0562	Death rate attributable to COVID-19 ^b .
λ, μ	3.95×10^{-5}	Natural birth and death rates, respectively ^b .
r	Time-varying	Probability of being tested for infectious individuals.
f	0.30	Probability of a false negative RT-PCR diagnostic test result.
β_1, β_2	0.6 (β_1) and 0.7 (β_2)	Scaling factors for rate of recovery for undetected and false negative individuals respectively ^c .
δ_1, δ_2	0.3 (δ_1) and 0.7 (δ_2)	Scaling factors for death rate for undetected and false negative individuals respectively ^f .

- $\alpha_p < 1$ represents the scenario where individuals who test positive are infecting susceptible individuals at a lower rate than infected individuals with false negative test results. $\alpha_U < 1$ is assumed as U mostly consists of asymptomatic or mildly symptomatic cases who are known to spread the disease at a much lower rate than those with higher levels of symptoms.
- Equal to the inverse of the average number of days for death starting from the onset of disease, times the probability of death of an infected individual. Natural birth and death rates are assumed to be equal for simplicity.
- $\beta_1 < 1$, $\beta_2 < 1$ are assumed, since the recovery rate is slower for individuals with false negative test results as compared to those who have been hospitalized. The condition of untested individuals is not as severe as they consist of mostly asymptomatic people. Consequently, they are assumed to recover faster than those with positive test results.
- $\delta_1 < 1$, $\delta_2 < 1$ are assumed. The death rate for those with false negative test results is assumed to be higher than those with positive test results, since the former are not receiving proper treatment. For untested individuals, the death rate is taken to be lesser because they are mostly asymptomatic. As a result, their survival probability is much higher.

Supplementary Table S2: Overview of projected COVID-counts for each model considered.

Type of count projected	COVID-counts		
	Cumulative COVID-cases	Active COVID-cases	Cumulative COVID-deaths
Reported	Baseline, eSIR, SAPHIRE, SEIR-fansy	eSIR, SEIR-fansy	eSIR, SEIR-fansy, ICM
Unreported	SAPHIRE, SEIR-fansy	SEIR-fansy	SEIR-fansy
Total (reported + unreported)	SAPHIRE, SEIR-fansy, ICM	SEIR-fansy	SEIR-fansy

Supplementary Table S3: Comparison of estimated projections and posterior estimates of model parameters across different sensitivity analysis scenarios under 21-day lockdown with moderate return, using observed data till April 14. Prior SD for R_0 is 1.0. Reproduced from Ray et al., 2020 (51).

Sensitivity Analysis		Predictions		Posterior Estimates	
Scenario	May 1	May 15	R_0	β	γ
Under-reporting*	25,248	62,797	2.28	0.20	0.09
	[104,411]	[343,465]	[1.05, 4.20]	[0.05, 0.39]	[0.03, 0.19]
Case-clustering**	24,818	57,499	2.81	0.16	0.06
	[59,525]	[189,010]	[1.47, 4.70]	[0.07, 0.26]	[0.03, 0.10]
Prior mean for $R_0 = 2$	20,251	42,252	1.80	0.27	0.16
	[135,034]	[315,348]	[0.87, 3.26]	[0.06, 0.59]	[0.04, 0.35]
Prior mean for $R_0 = 3$	25,757	86,750	2.43	0.30	0.13
	[165,287]	[638,770]	[1.41, 4.07]	[0.09, 0.60]	[0.04, 0.30]
Prior mean for $R_0 = 4$	34,587	253,935	3.38	0.32	0.10
	[213,556]	[1,854,319]	[2.09, 5.27]	[0.10, 0.63]	[0.03, 0.23]

* Observed case-counts are multiplied by 10, Prior mean for $R_0 = 2$

** Assume that the cases happen in metro hotspots, use population size $N=32$ million instead of national population 1.34 billion, Prior mean for $R_0 = 2$

Supplementary Table S4: National and state-levels lockdown measures implemented over the course of COVID-19 pandemic in India. Reproduced from Salvatore et al., 2021 (66).

Lockdown phase	Nation-wide measures implemented	State-level variation in measures implemented
Phase one (25 March – 14 April)	All transport services – road, air and rail – were suspended, with exceptions for transportation of essential goods, fire, police and emergency services. Educational institutions, industrial establishments and hospitality services were also suspended. ^a Services such as food shops, banks and ATMs, petrol pumps, other essentials and their manufacturing were exempted. ^b	Gujarat, Himachal Pradesh, Karnataka, Maharashtra, Tamil Nadu, Sikkim and Telengana sealed state borders. Additionally, Maharashtra, Telengana and Tamil Nadu imposed Section 144, outlawing large gatherings of people. ^c
Phase two (15 April – 3 May)	Conditional relaxation promised after 20 April, subject to containment of spread. Lockdown areas classified into red, orange and green zones based on extent of spread of disease. Certain relaxations from 20 April: agricultural businesses, including dairy, aquaculture and plantations allowed to open. Cargo transportation vehicles allowed to operate. Banks and government centers distributing benefits allowed to open as well. ^d	In interest of economic recovery, certain states like Maharashtra chose to allow specific business activities to resume, in addition to national easing of restrictions. Karnataka chose to ease the lockdown in certain areas, while Delhi, Punjab and Telengana chose to enforce strict lockdown measures. ^e
Phase three (4 May – 17 May)	Zonal classification of regions into red, orange and green zones continued, with normal movement allowed in green zones. Movement of private and hired vehicles allowed in orange zones and red zones remained in lockdown. Zonal classifications revised on a weekly basis. ^f	Delhi allowed public- and private-sector offices to reopen, with social distancing measures in place. Maharashtra eased most industrial and commercial activities. Gujarat, and. Jharkhand allowed no relaxation, while Bihar, Uttar Pradesh, Rajasthan and Madhya Pradesh chose to mostly adhere to guidelines issued by the Union Home Ministry. ^g
Phase four (18 May – 31 May)	Unlike the previous phases, states were given a larger say in the demarcation of green, orange and red zones and the implementation roadmap. Red zones were further divided into containment and buffer zones. Local administrative bodies were given the authority to demarcate containment and buffer zones. ^h	Restricted individual movement allowed in Delhi, while Maharashtra, Tamil Nadu and Telengana extended the lockdown further. Karnataka allowed public transport with social distancing measures, while West Bengal began easing workplace restrictions. Standalone shops were allowed to open for short durations. ⁱ

- Guidelines on measures to be undertaken by ministries/departments of Government of India, State/Union Territory Governments and State/Union Territory Authorities for containment of COVID-19 epidemic in the Country (<https://www.mha.gov.in/sites/default/files/Guidelines.pdf>)
- The Economic Times: India's 21-day lockdown to counter coronavirus: What's exempt, what's not, 25 March 2020 (<https://economictimes.indiatimes.com/news/politics-and-nation/india-21-day-lockdown-what-is-exempted-what-is-not/articleshow/74798725.cms>)
- Wikipedia https://en.wikipedia.org/wiki/Indian_state_government_responses_to_the_COVID-19_pandemic
- BBC: Coronavirus lockdown guidelines: What has India changed under new rules? April 15, 2020 (<https://www.bbc.com/news/world-asia-india-52290761>)
- Hindustan Times: Complete list of states with no relaxation in lockdown 2.0 restrictions 20 April 2020 (<https://www.hindustantimes.com/india-news/complete-list-of-states-with-no-covid-19-lockdown-2-0-relaxation/story-pfE5K3Pn5LSZrgFEvC84hO.html>)

- f. India Today: Full list of Red, Yellow, Green Zone districts for Lockdown 3.0, *1 May 2020* (<https://www.indiatoday.in/india/story/red-orange-green-zones-full-current-update-list-districts-states-india-coronavirus-1673358-2020-05-01>)
- g. Hindustan Times: Covid-19 lockdown 3.0: A look at relaxations, restrictions across major states in India, *4 May 2020* (<https://www.hindustantimes.com/india-news/coronavirus-update-covid-19-lockdown-3-0-a-look-at-relaxations-restrictions-across-major-states-in-india/story-J5Z2IypwiagUTFflwYW0jN.html>)
- h. The Economic Times: Lockdown 4.0 guidelines: Nationwide lockdown extended till May 31, with considerable relaxations, *21 May 2020* (<https://economictimes.indiatimes.com/news/politics-and-nation/centre-extends-nationwide-lockdown-till-may-31-with-considerable-relaxations/articleshow/75790821.cms>)
- i. BBC: India lockdown 4.0: What is allowed in your city? *19 May 2020* (<https://www.bbc.com/news/world-asia-india-52707371>)