$\begin{array}{c} {\rm Math~1300~Fall~2013} \\ {\rm Wednesday~September~11~2013} \\ {\rm Exercises} \end{array}$

1. Find the inverse of the matrix:

 $\left[\begin{array}{cc} 0 & 1 \\ 1 & 0 \end{array}\right]$

$\begin{array}{c} {\rm Math~1300~Fall~2013} \\ {\rm Wednesday~September~11~2013} \\ {\rm Exercises} \end{array}$

2. Use a matrix equation to solve the system of linear equations:

$$\left\{\begin{array}{cccc} 5x & + & 3y & = & 1 \\ 7x & + & 4y & = & 2 \end{array}\right\}$$

$\begin{array}{c} {\rm Math~1300~Fall~2013} \\ {\rm Wednesday~September~11~2013} \\ {\rm Exercises} \end{array}$

3. A flu epidemic is spreading through a town of 48,000 people. It is found that if x and y denote the numbers of people sick and well in a given week, respectively, and if s and w denote the corresponding numbers for the following week, then:

$$\begin{array}{rcl} \frac{1}{3}x & + & \frac{1}{4}y & = & s \\ \frac{2}{3}x & + & \frac{3}{4}y & = & w \end{array}$$

- (a) Write this system of equations in matrix form.
- (b) Solve the resulting matrix equation for $X = \begin{bmatrix} x \\ y \end{bmatrix}$
- (c) Suppose that 13,000 people are sick in a given week. How many were sick the preceding week?
- (d) Same question as part (c), except assume that 14,000 people are sick.

$\begin{array}{c} \text{Math 1300 Fall 2013} \\ \text{Wednesday September 11 2013} \\ \text{Exercises} \end{array}$

- 4. A teacher estimates that of the students who pass a test, 80% will pass the next test, while of the students who fail a test, 50% will pass the next test. Let x and y denote the number of students who pass and fail a given test, and let u and v be the corresponding numbers for the following test.
 - (a) Write a matrix equation relating $\left[\begin{array}{c} x\\y\end{array}\right]$ to $\left[\begin{array}{c} u\\v\end{array}\right].$
 - (b) Suppose that 25 of the teacher's students pass the third test, and 8 fail the third test. How many students will pas the fourth test? Approximately how many passed the second test?