

# Prediction-based Resource Allocation

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# Agenda

- Introduction
- Motivation
- Next activity and time prediction
- Resource allocation
- Experiments
- Results
- Future Work & Limitations



# Introduction

- Predictive Business Process Monitoring and Management
  - Efficient scheduling of activities
  - Efficient allocation of resources
- Use Machine Learning to improve Business Processes
- Assessment of the paper Prediction-based resource allocation [1]

# Motivation

- Resource allocation
  - Improved productivity
  - Reduced execution costs
  - Balanced resource usage
- Non-clairvoyant online-over time problem [2]



# Example

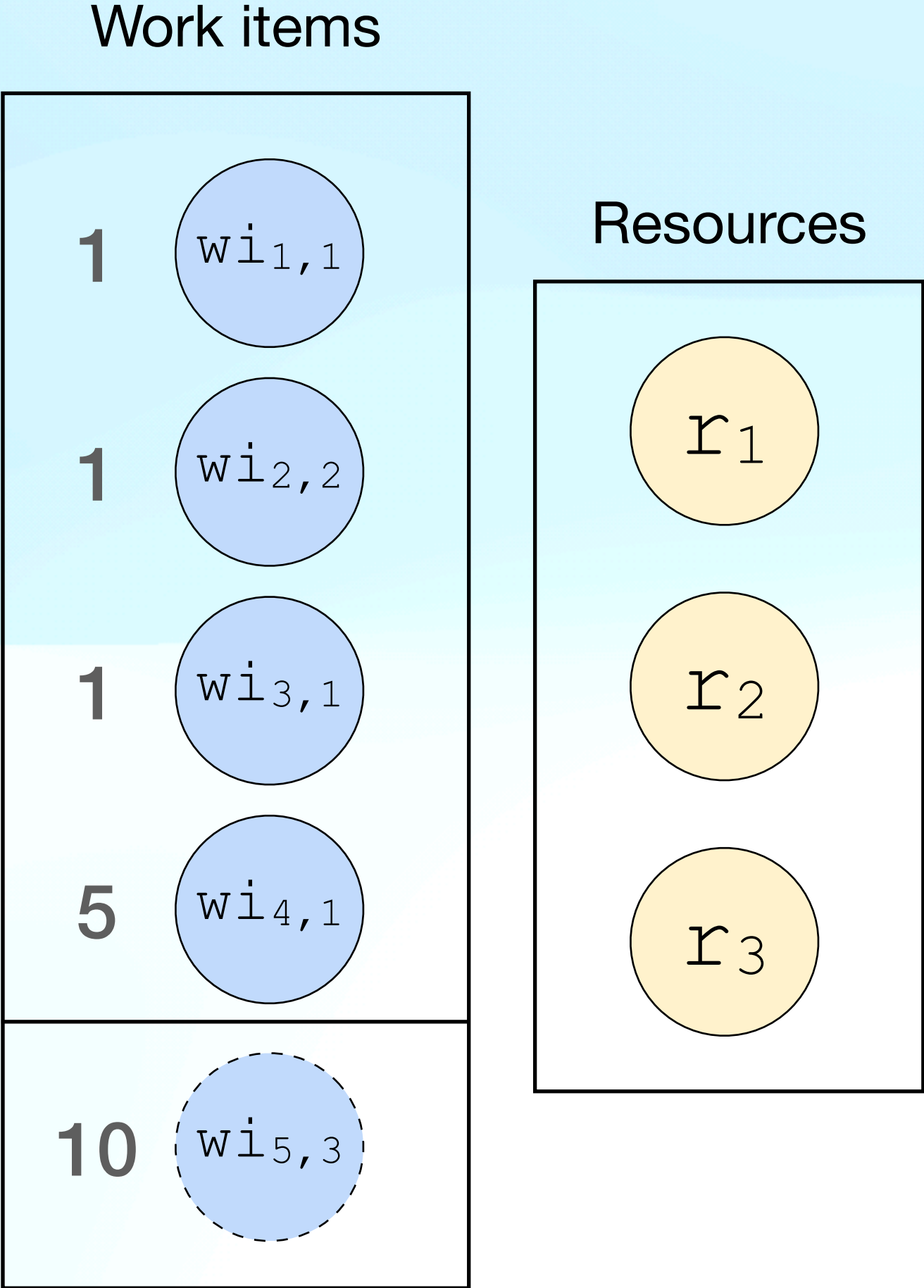
# Example

Work items

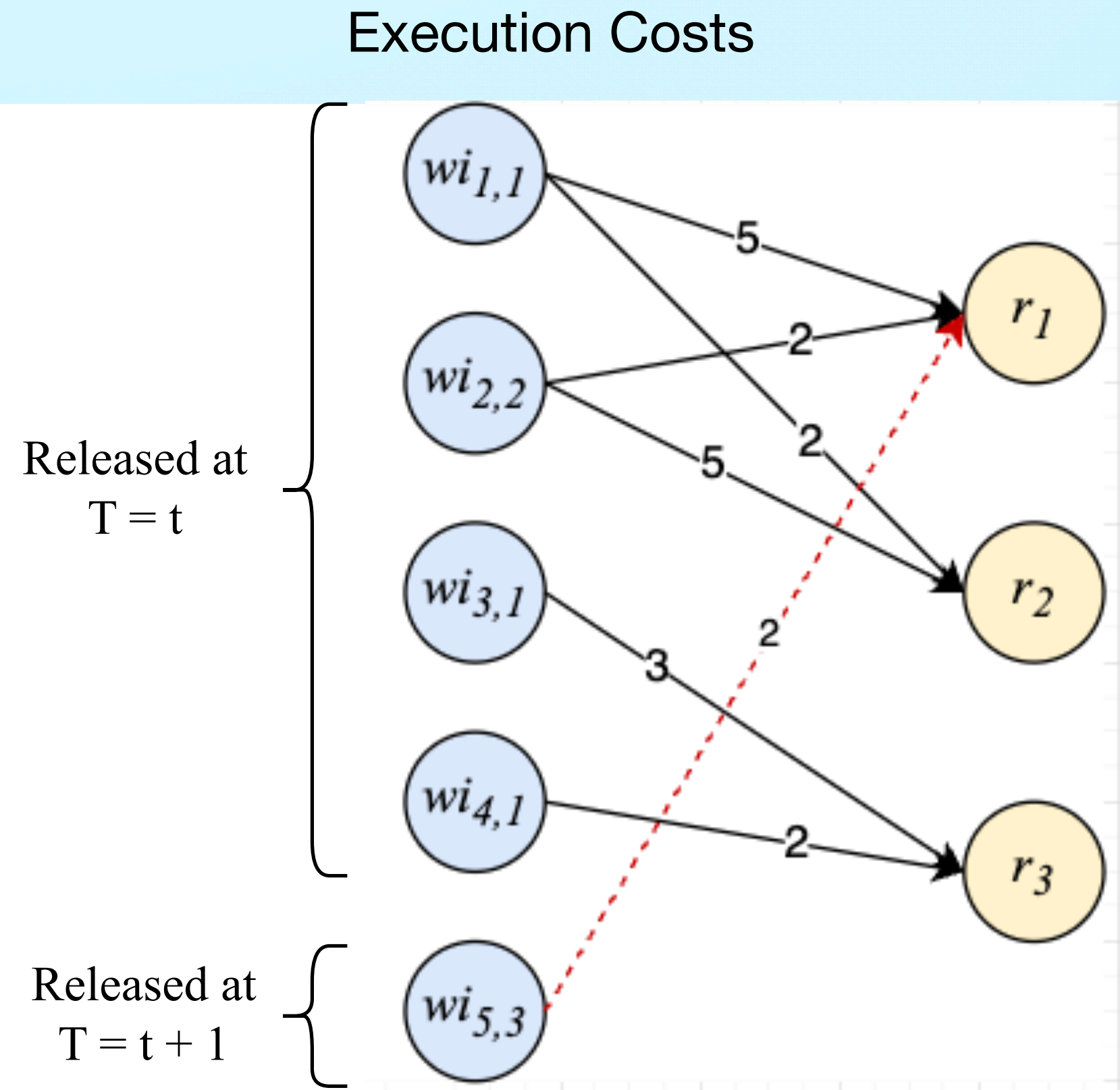
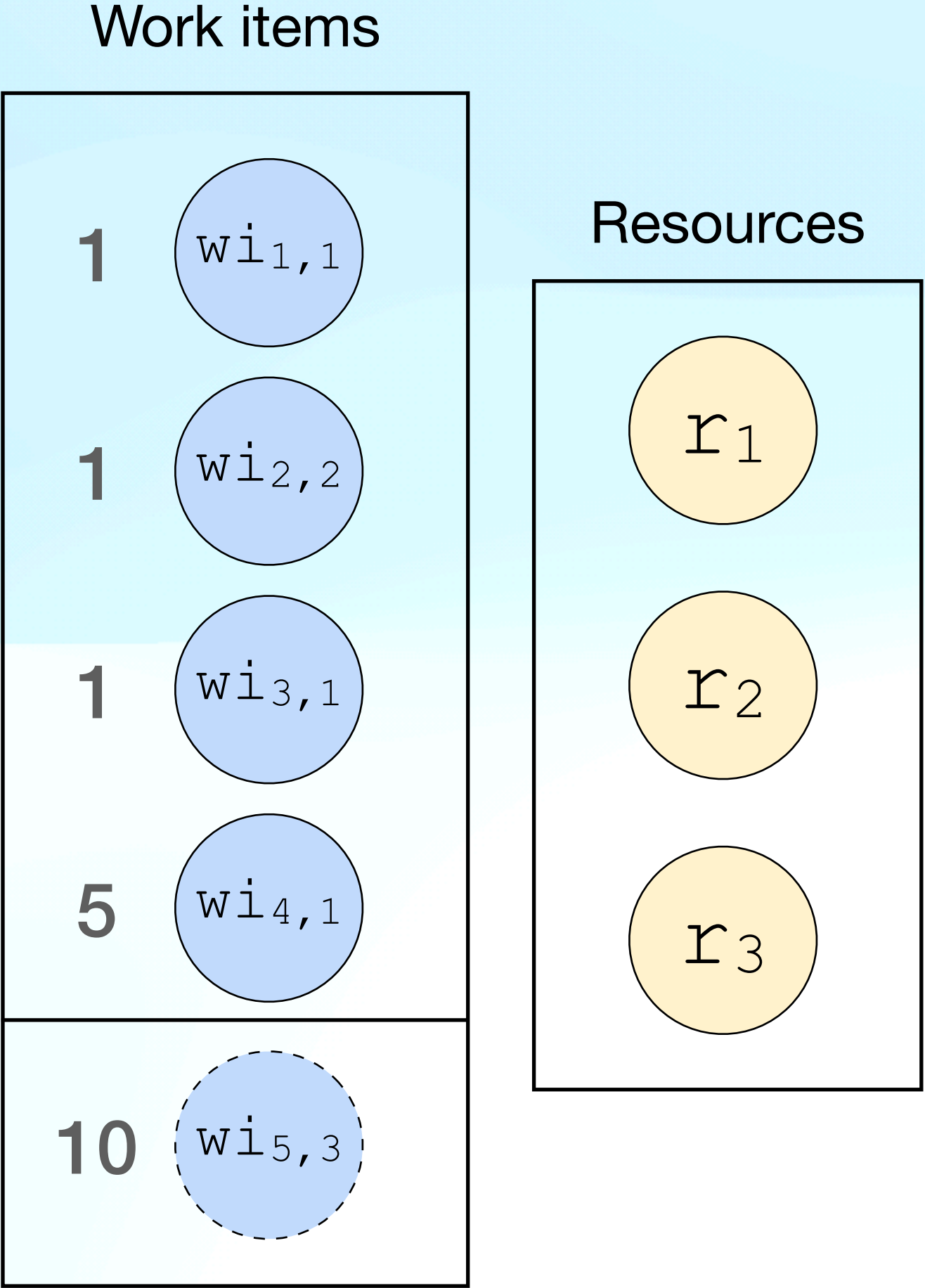
1	$w_{1,1}$
1	$w_{2,2}$
1	$w_{3,1}$
5	$w_{4,1}$
10	$w_{5,3}$



# Example

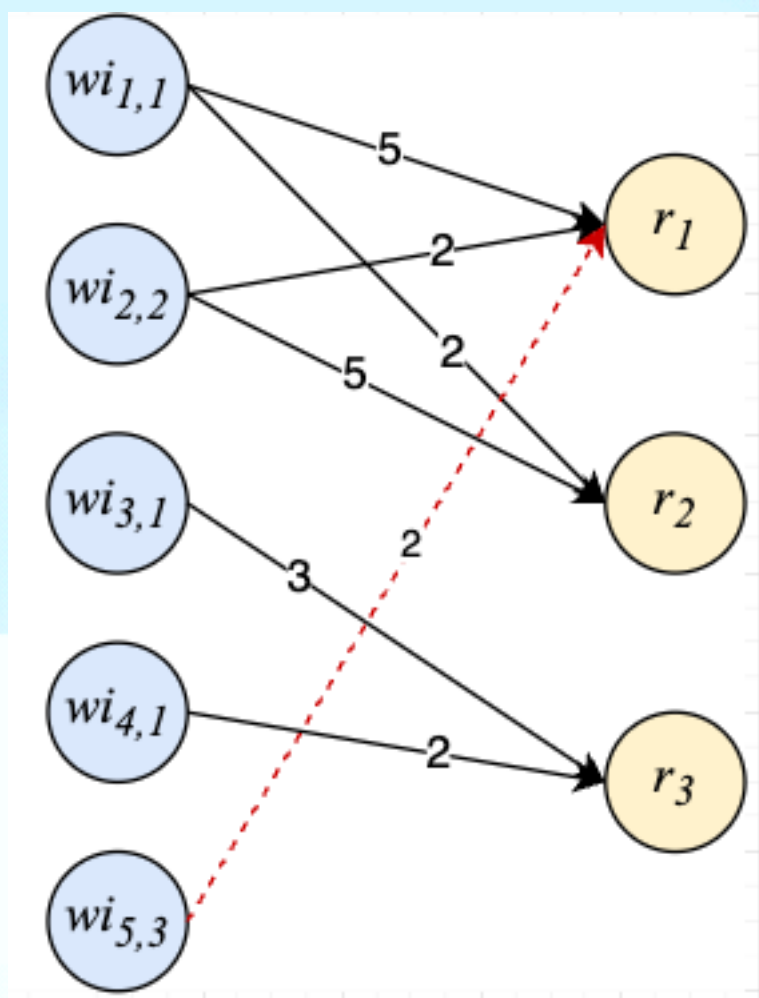


# Example





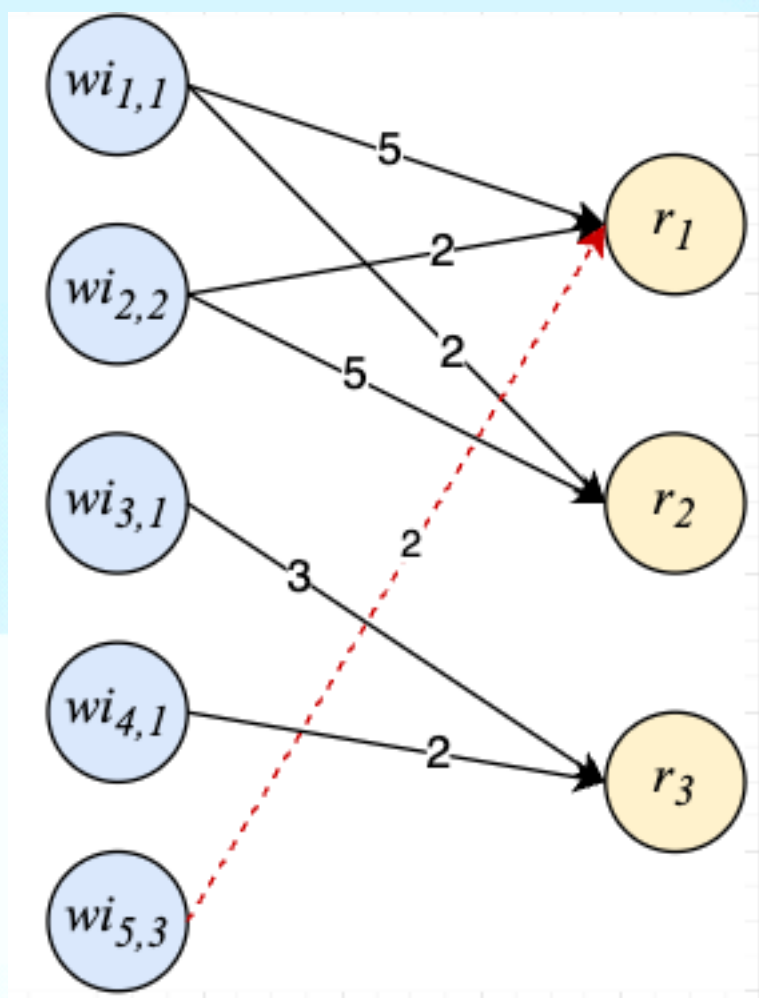
# Baseline



resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
r <sub>1</sub>								
r <sub>2</sub>								
r <sub>3</sub>								

Table. Baseline Resource allocation

# Baseline

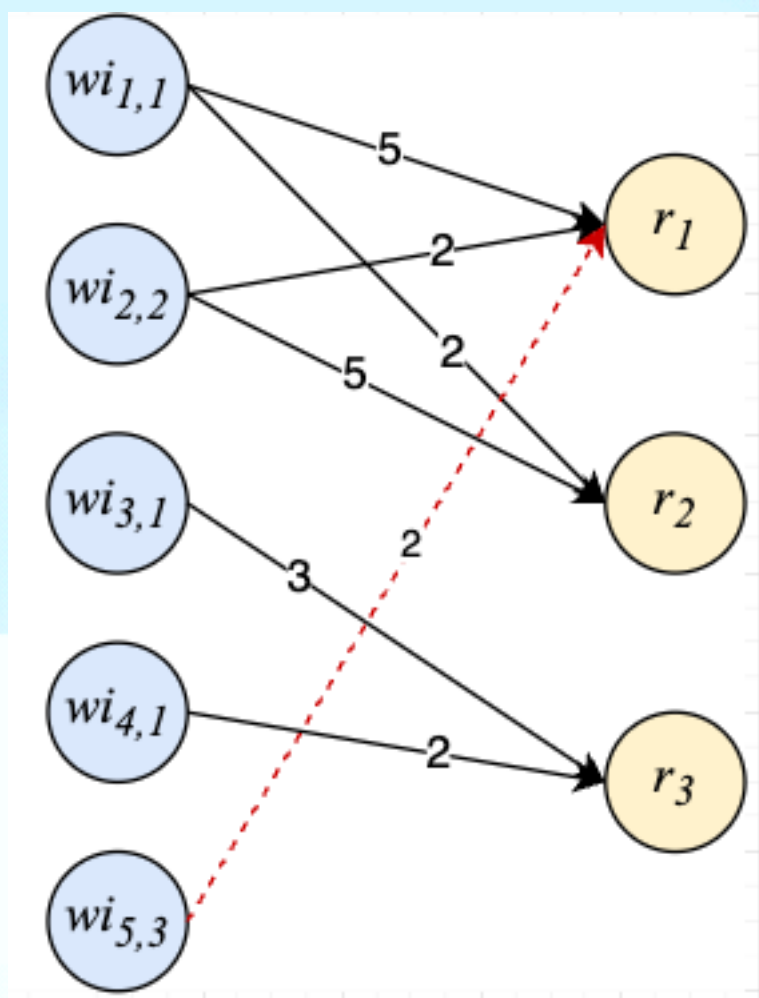


resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
r <sub>1</sub>	w <sub>i<sub>1</sub>,1</sub>							
r <sub>2</sub>	w <sub>i<sub>2</sub>,2</sub>							
r <sub>3</sub>	w <sub>i<sub>4</sub>,1</sub>							

Table. Baseline Resource allocation



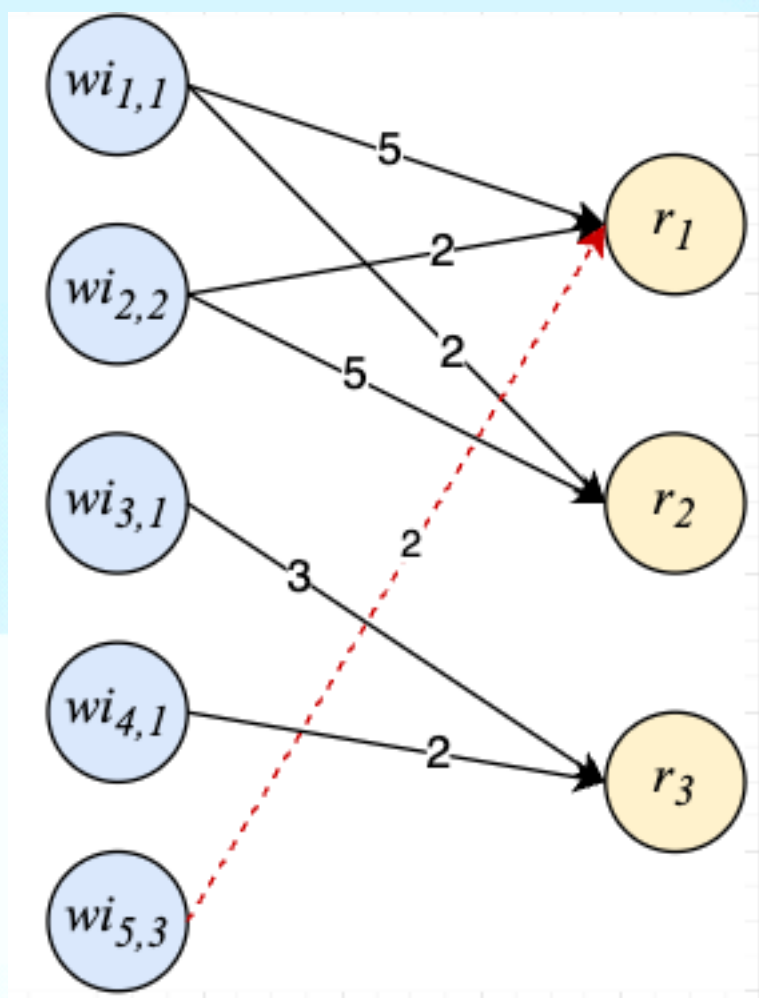
# Baseline



resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
<b>r<sub>1</sub></b>	$w_{i_1,1}$							
<b>r<sub>2</sub></b>	$w_{i_2,2}$							
<b>r<sub>3</sub></b>	$w_{i_4,1}$		$w_{i_3,1}$					

Table. Baseline Resource allocation

# Baseline

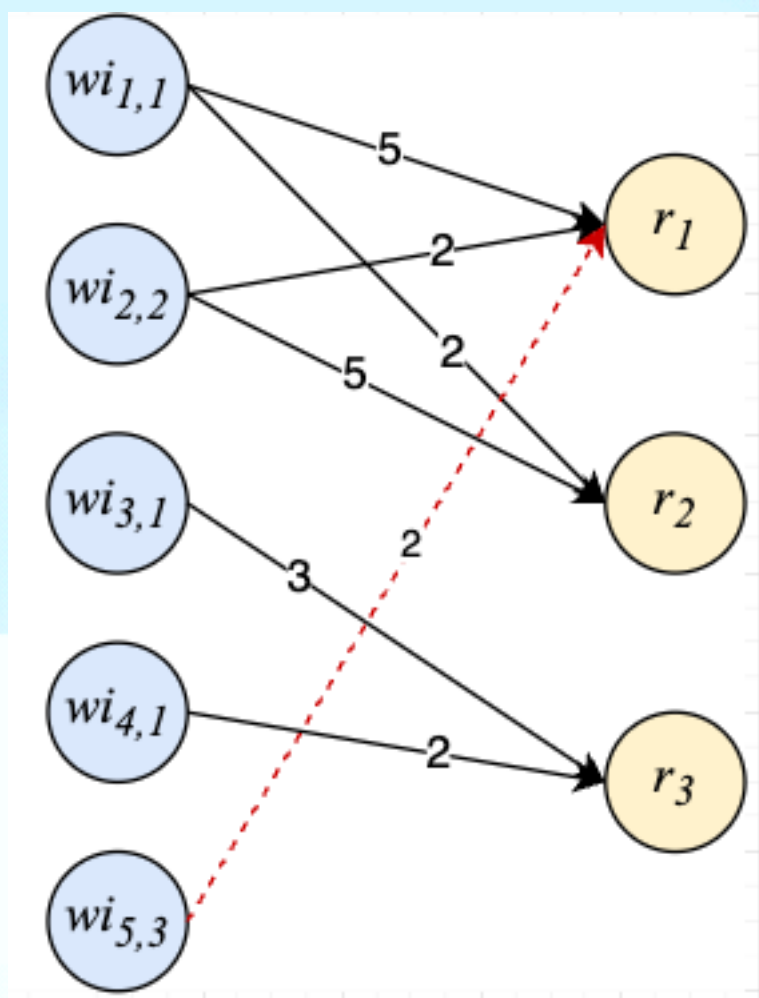


resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
<b>r<sub>1</sub></b>	$w_{i,1}$					$w_{i,5}$		
<b>r<sub>2</sub></b>	$w_{i,2}$							
<b>r<sub>3</sub></b>	$w_{i,4}$		$w_{i,3}$					

Table. Baseline Resource allocation



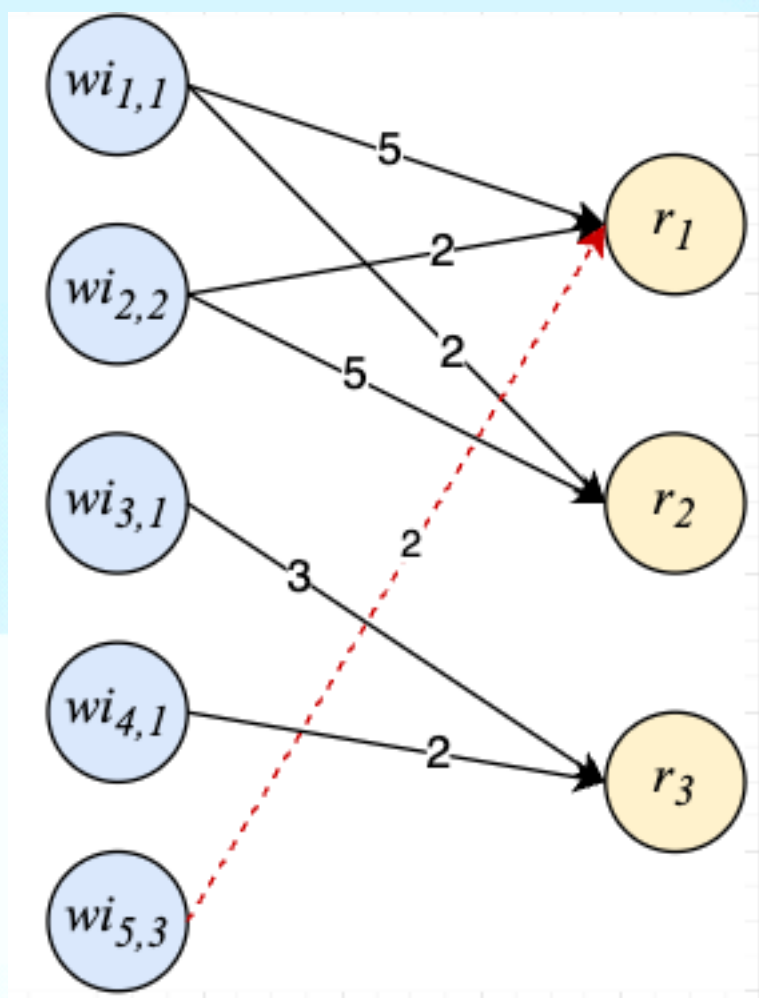
# Baseline



resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
r1	wi_{1,1}					wi_{5,1}		65
r2	wi_{2,2}							
r3	wi_{4,1}		wi_{3,1}					

Table. Baseline Resource allocation

# Baseline

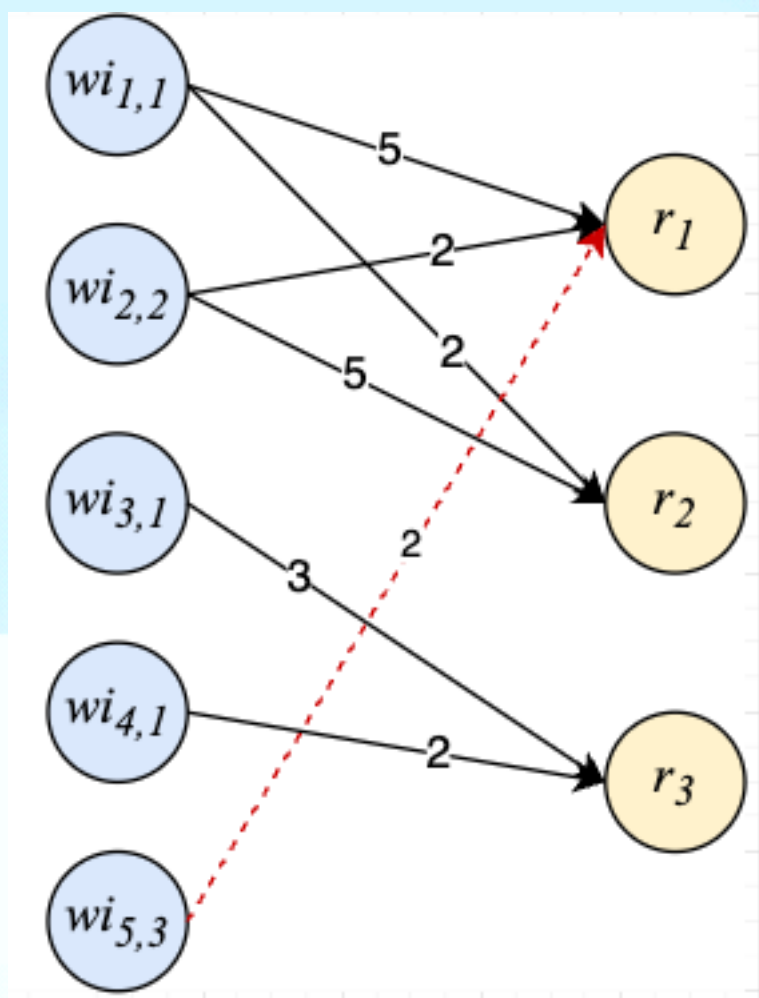


resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
r <sub>1</sub>	w <sub>i<sub>1</sub>,1</sub>					w <sub>i<sub>5</sub>,1</sub>		65
r <sub>2</sub>	w <sub>i<sub>2</sub>,2</sub>							5
r <sub>3</sub>	w <sub>i<sub>4</sub>,1</sub>		w <sub>i<sub>3</sub>,1</sub>					

Table. Baseline Resource allocation



# Baseline

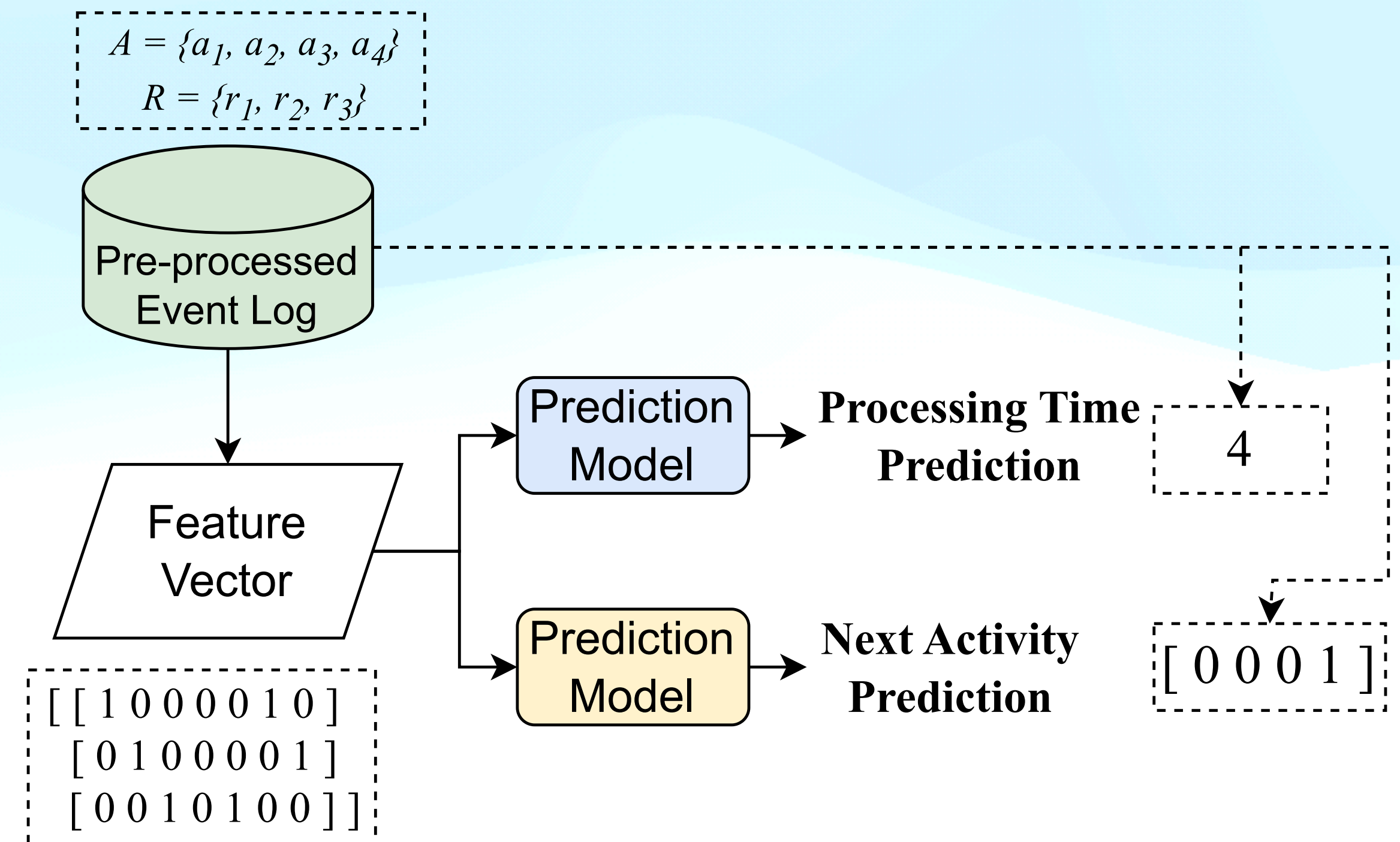


resource	t	t+1	t+2	t+3	t+4	t+5	t+6	$\sum c_i w_i$
r <sub>1</sub>	w <sub>i,1</sub>					w <sub>i,5</sub>		65
r <sub>2</sub>	w <sub>i,2</sub>							5
r <sub>3</sub>	w <sub>i,4</sub>		w <sub>i,3</sub>					15

Table. Baseline Resource allocation

# Next activity & Time prediction

- User one-hot encoded resource and activities as input
- Processing time prediction: numerical value
- Next activity prediction: one-hot-encoded activity values





# Resource allocation

---

**Algorithm 1** Resource Scheduling algorithm

---

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i_i}, r_{r_j}, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

---

# Resource allocation

## Algorithm 1 Resource Scheduling algorithm

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

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    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i,i}, r_{r_j}, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

1



# Resource allocation

---

**Algorithm 1** Resource Scheduling algorithm

---

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

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    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i_i}, rr_j, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

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2

# Resource allocation

## Algorithm 1 Resource Scheduling algorithm

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

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$c \leftarrow (p_{i,k,j} + \max(r_{i,i}, r_{r_j}, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

3



# Resource allocation

## Algorithm 1 Resource Scheduling algorithm

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i,i}, r_{r_j}, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

Cost

3

# Resource allocation

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**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_i, rr_j, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

## Cost

- $p_{i,k,j}$ : processing time for work item  $wi_{i,k}$  by resource  $r_j$

3



# Resource allocation

## Algorithm 1 Resource Scheduling algorithm

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

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**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_i, rr_j, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

3

## Cost

- $p_{i,k,j}$ : processing time for work item  $wi_{i,k}$  by resource  $r_j$
- $ri_i$ : remaining time for item  $i$

# Resource allocation

## Algorithm 1 Resource Scheduling algorithm

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i_i}, rr_j, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

3

## Cost

- $p_{i,k,j}$ : processing time for work item  $wi_{i,k}$  by resource  $r_j$
- $r_{i_i}$ : remaining time for item  $i$
- $rr_j$ : remaining time for resource  $r_j$  to be ready



# Resource allocation

## Algorithm 1 Resource Scheduling algorithm

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

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**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i_i}, rr_j, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

3

## Cost

- $p_{i,k,j}$ : processing time for work item  $wi_{i,k}$  by resource  $r_j$
- $r_{i_i}$ : remaining time for item  $i$
- $rr_j$ : remaining time for resource  $r_j$  to be ready
- $w_i$ : weight of item  $i$

# Resource allocation

---

**Algorithm 1** Resource Scheduling algorithm

---

**Input:**  $\hat{W}I, \hat{R}$

**Output:** Psuedo-Assignment  $\hat{M}$

Produce source node  $s$ , sink node  $t$

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

    add edge  $(s, wi_{i,k}, (0, 1))$

**end for**

**for** node  $r_j \in \hat{R}$  **do**

    add edge  $(r_j, t, (0, 1))$

**end for**

**for** node  $wi_{i,k} \in \hat{W}I$  **do**

**for** node  $r_j \in \hat{R}$  **do**

$c \leftarrow (p_{i,k,j} + \max(r_{i_i}, rr_j, 0))/w_i$

        add edge  $(wi_{i,k}, r_j, (c, 1))$

**end for**

**end for**

$M \leftarrow \text{MinCostMaxFlow}(s, t)$

**return**  $M$

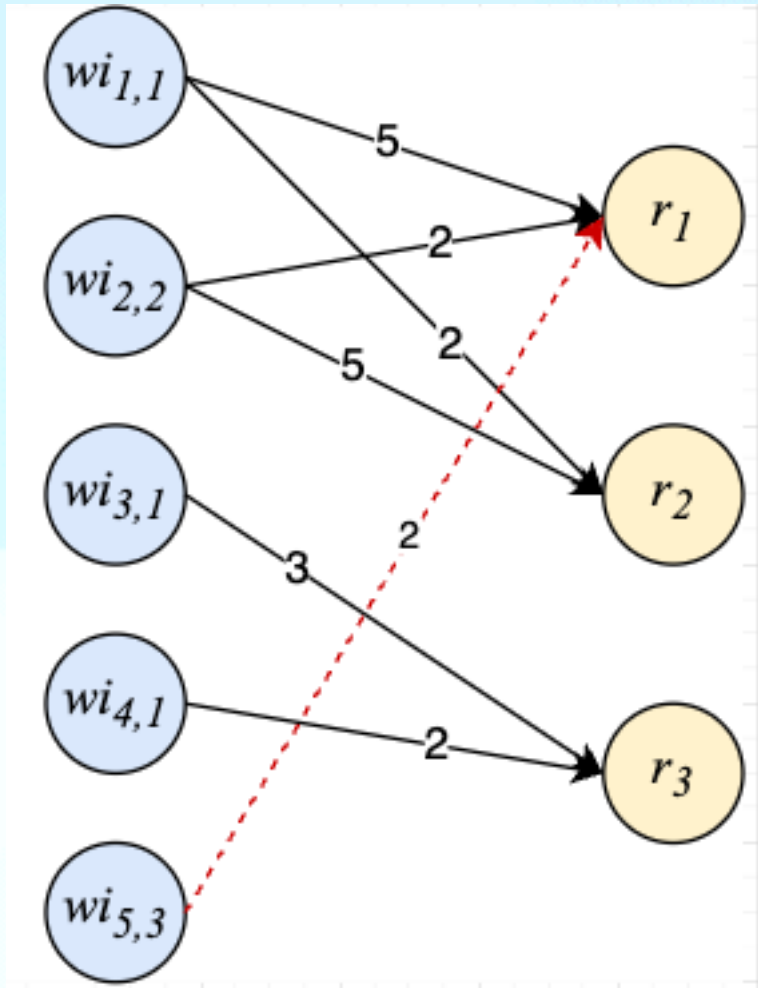
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## Cost

- $p_{i,k,j}$ : processing time for work item  $wi_{i,k}$  by resource  $r_j$
- $r_{i_i}$ : remaining time for item  $i$
- $rr_j$ : remaining time for resource  $r_j$  to be ready
- $w_i$ : weight of item  $i$

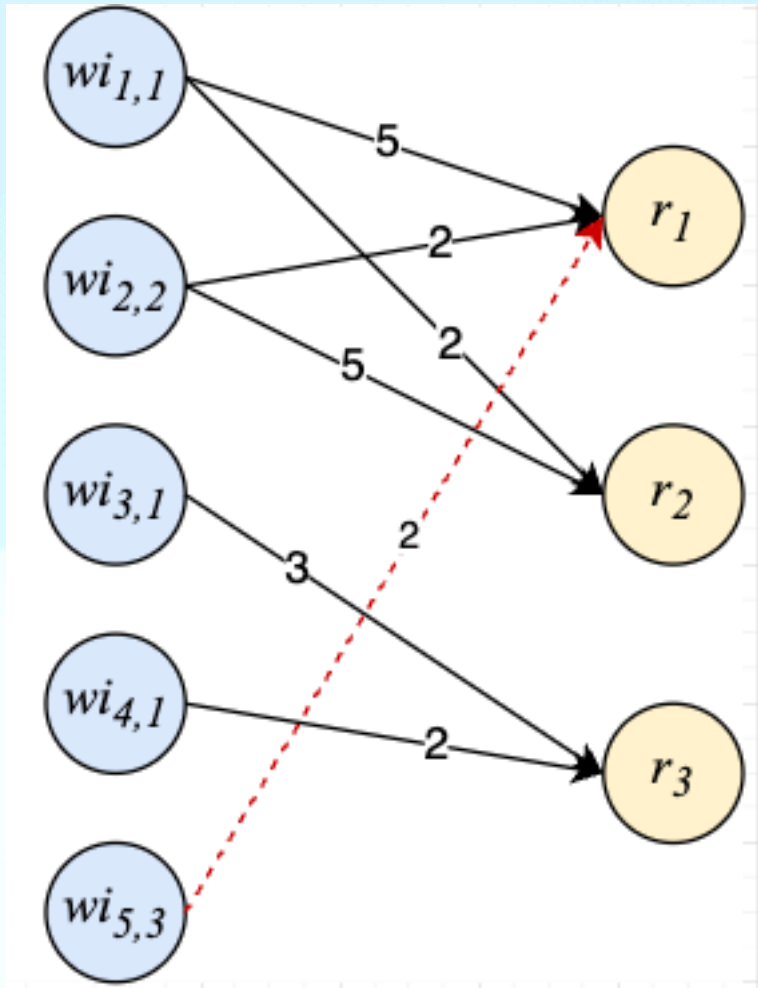


# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1						
r2						
r3						

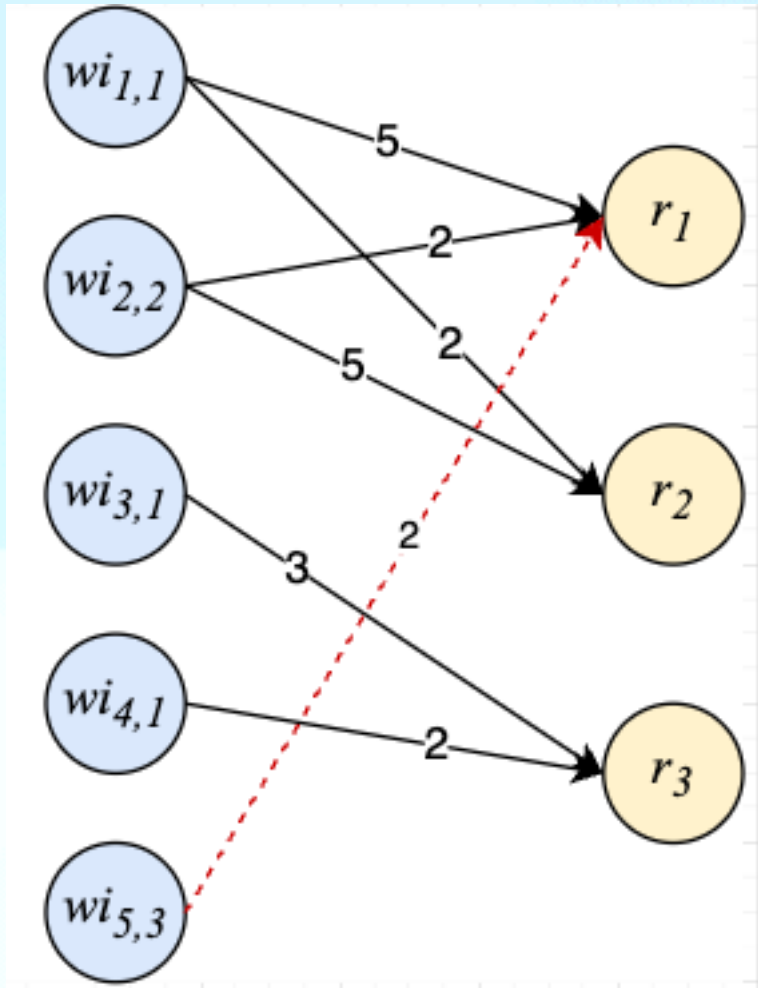
# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1						
r2	$w_{i1,1}$					
r3	$w_{i4,1}$					

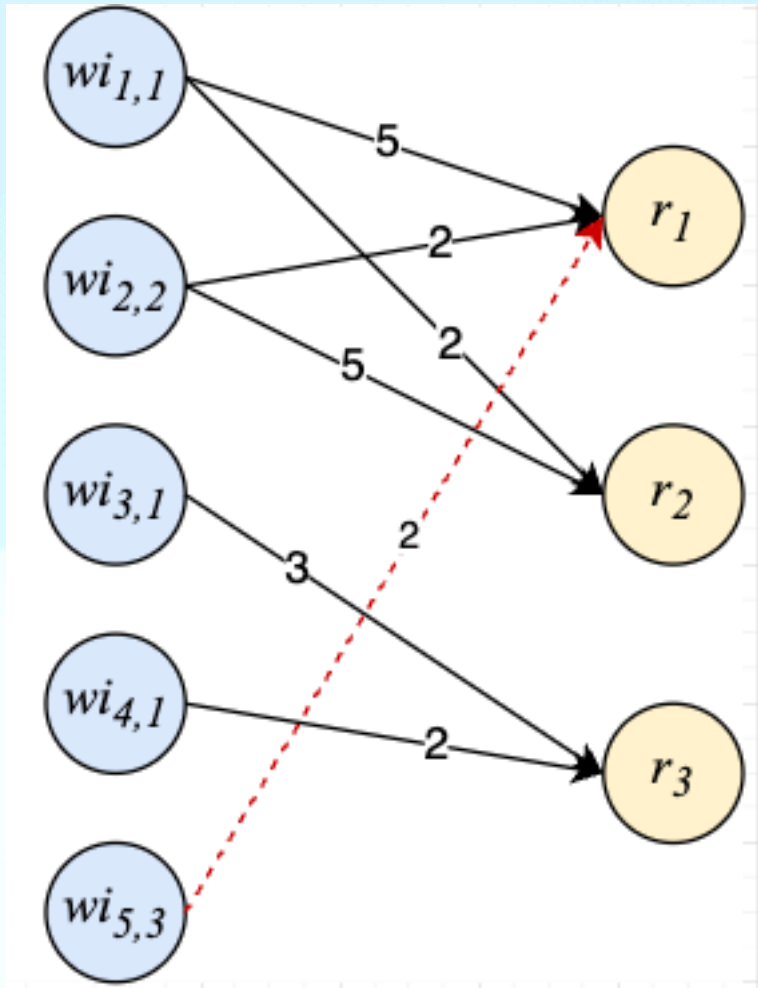


# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1		$w_{i5,1}$				
r2	$w_{i1,1}$					
r3	$w_{i4,1}$					

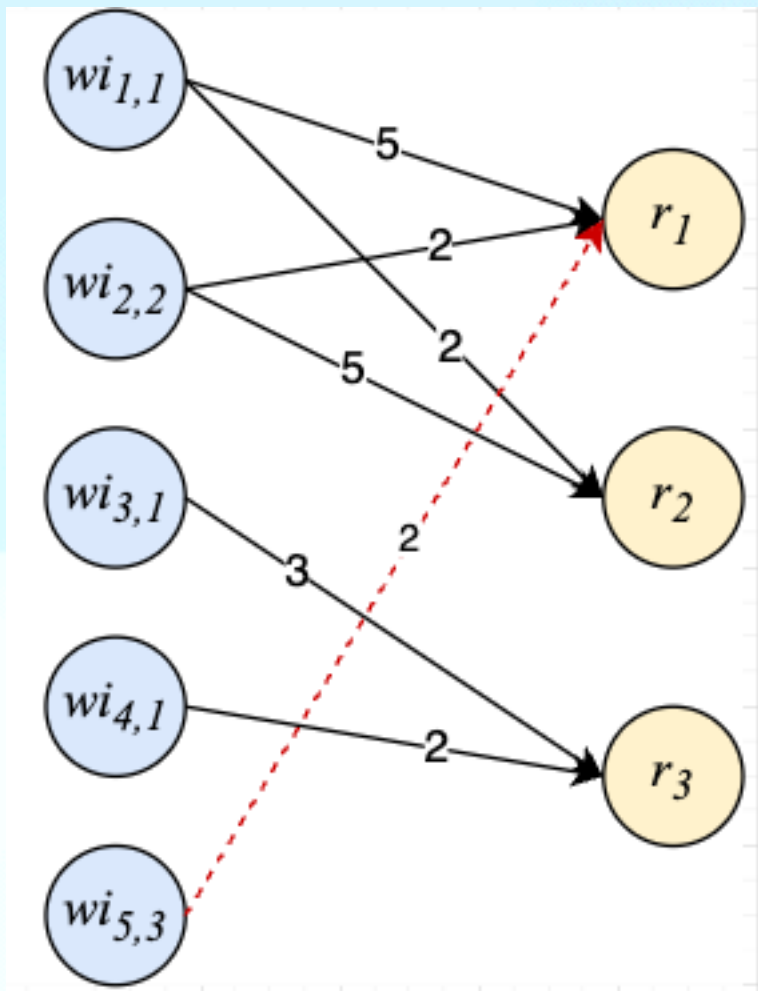
# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1		$w_{i5,1}$				
r2	$w_{i1,1}$					
r3	$w_{i4,1}$		$w_{i3,1}$			

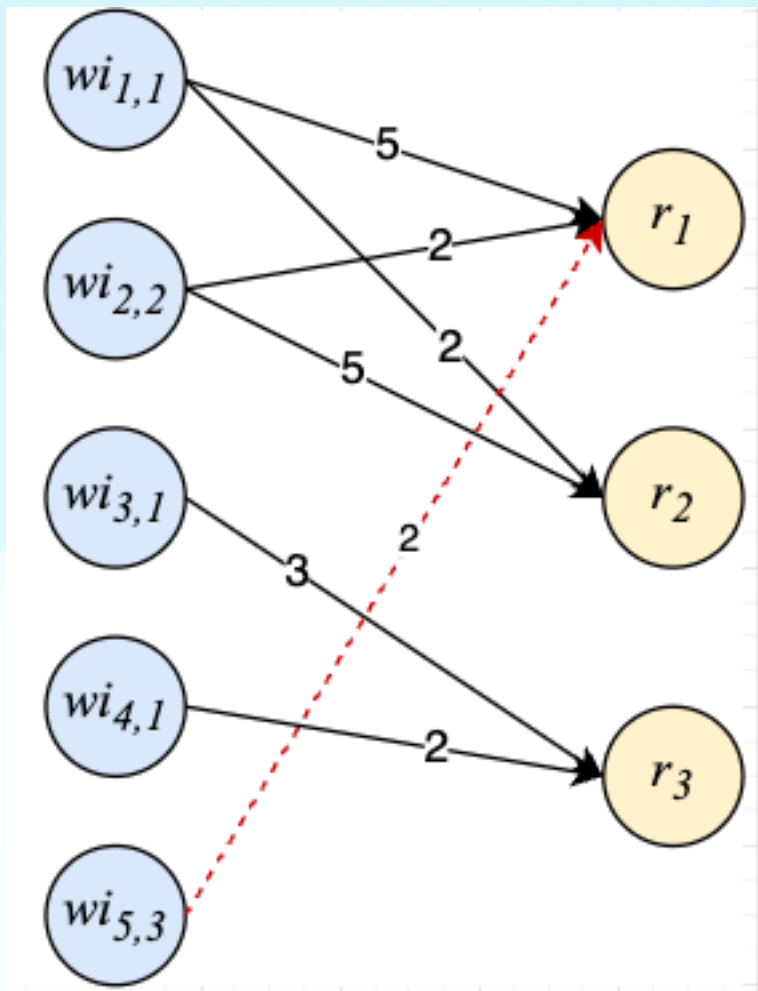


# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1		$w_{i5,1}$		$w_{i2,2}$		
r2	$w_{i1,1}$					
r3	$w_{i4,1}$		$w_{i3,1}$			

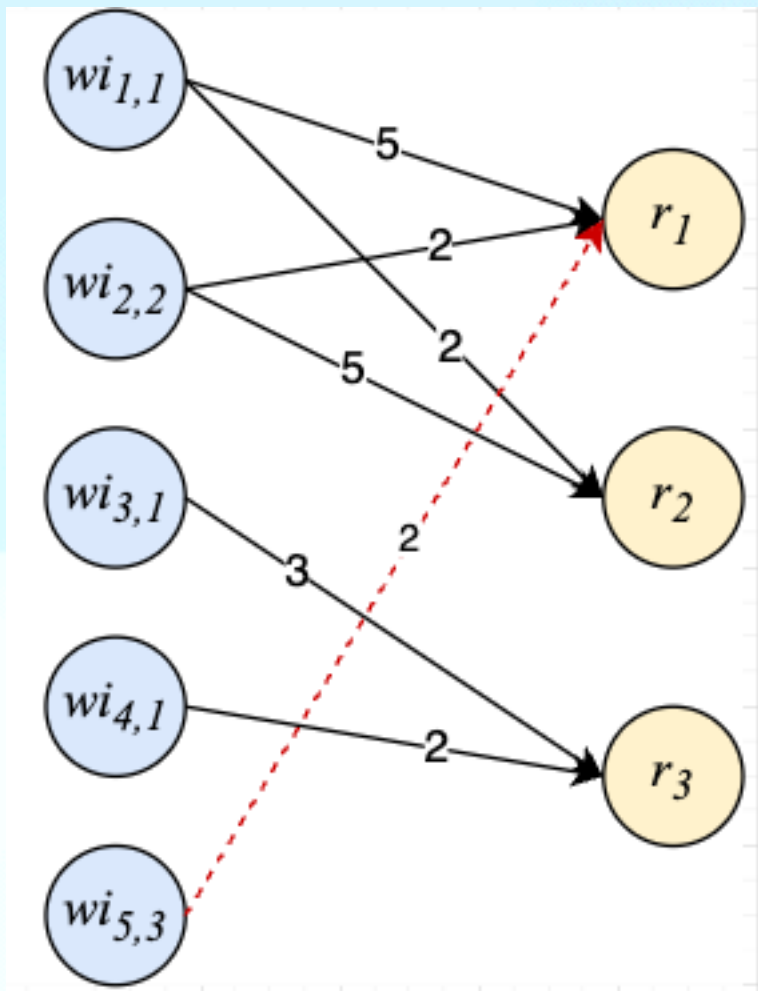
# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1		$w_{i5,1}$		$w_{i2,2}$		25
r2	$w_{i1,1}$					
r3	$w_{i4,1}$		$w_{i3,1}$			

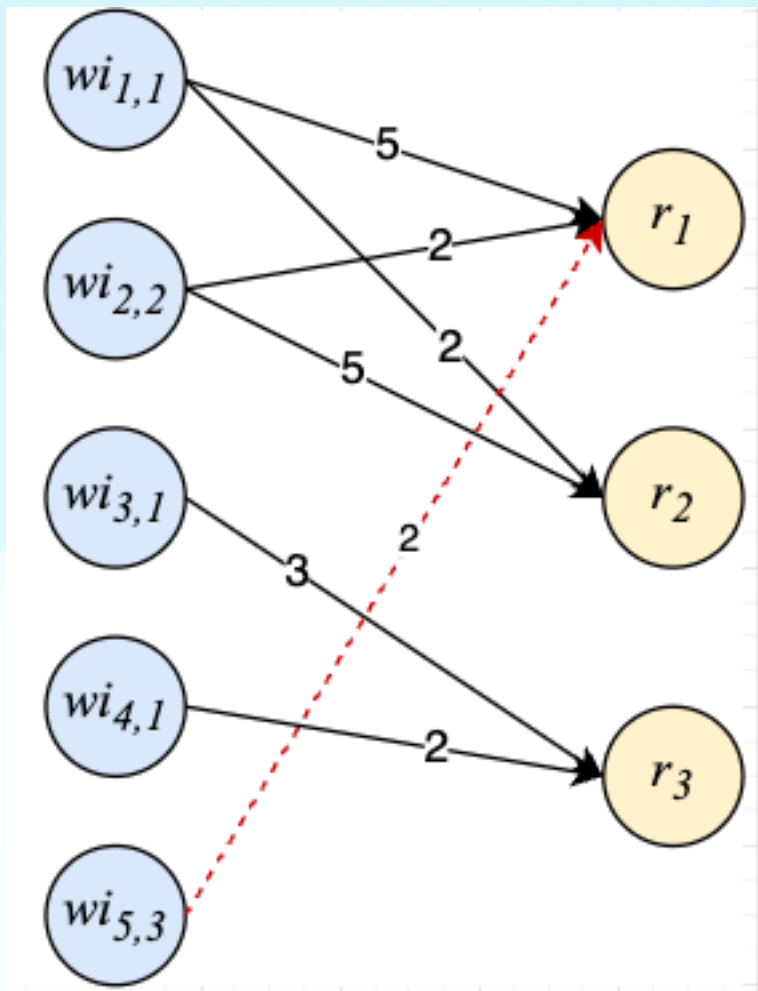


# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1		$w_{i_5,1}$		$w_{i_2,2}$		25
r2	$w_{i_1,1}$					5
r3	$w_{i_4,1}$		$w_{i_3,1}$			

# Resource allocation



resource	t	t+1	t+2	t+3	t+4	$\sum c_i w_i$
r1		$w_{i5,1}$		$w_{i2,2}$		25
r2	$w_{i1,1}$					5
r3	$w_{i4,1}$		$w_{i3,1}$			15



# Data

# Data

- BPIC'2012 Shared Task: Consumer Loan approvals process



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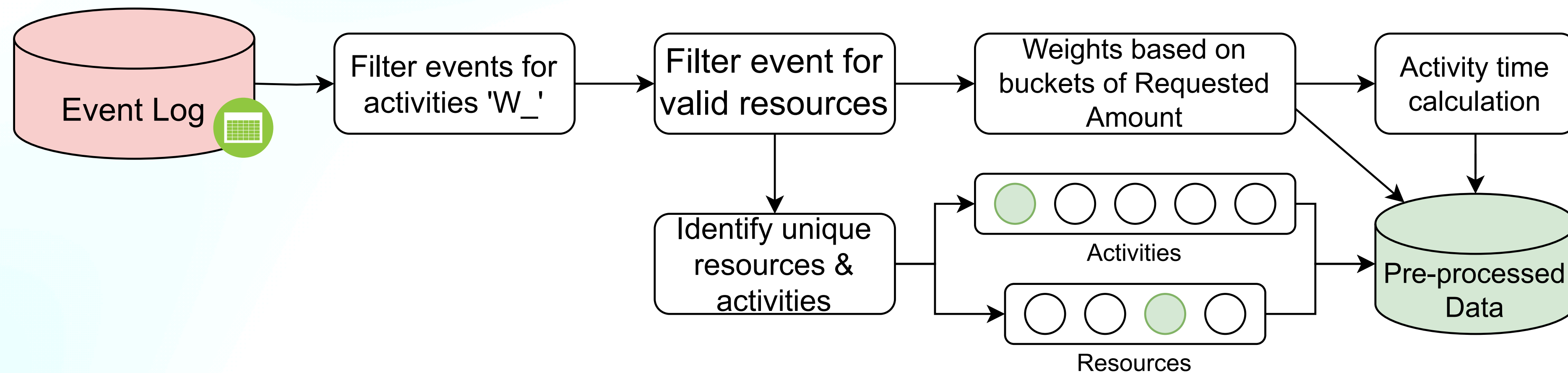


Figure. Data Filtering and preprocessing

# Data

- BPIC'2012 Shared Task: Consumer Loan approvals process
- Filtering: events with valid resource and are carried out manually

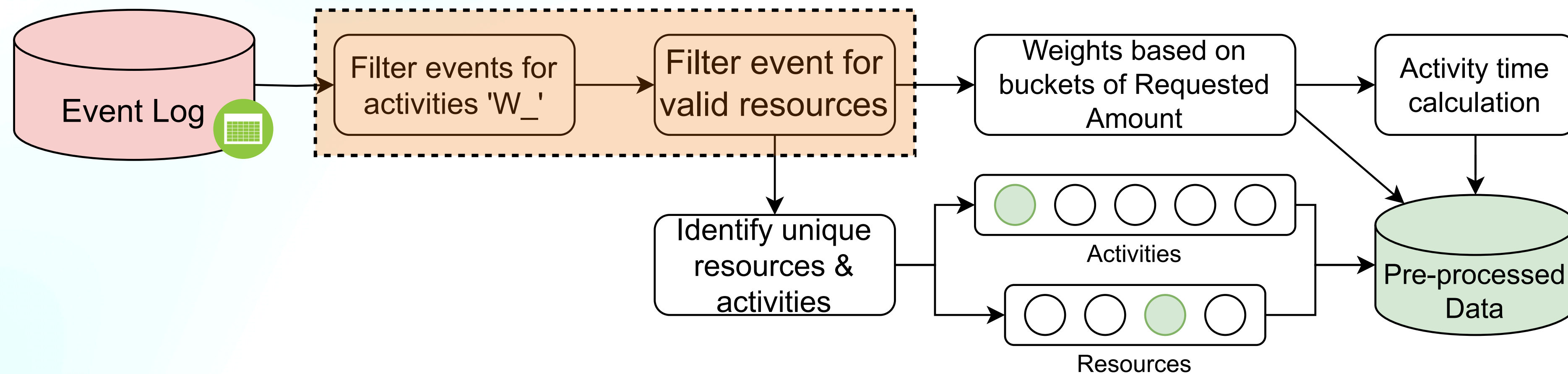


Figure. Data Filtering and preprocessing



# Data

- BPIC'2012 Shared Task: Consumer Loan approvals process
- Filtering: events with valid resource and are carried out manually
- Preprocessing: One-hot encoding of Activities and Resources

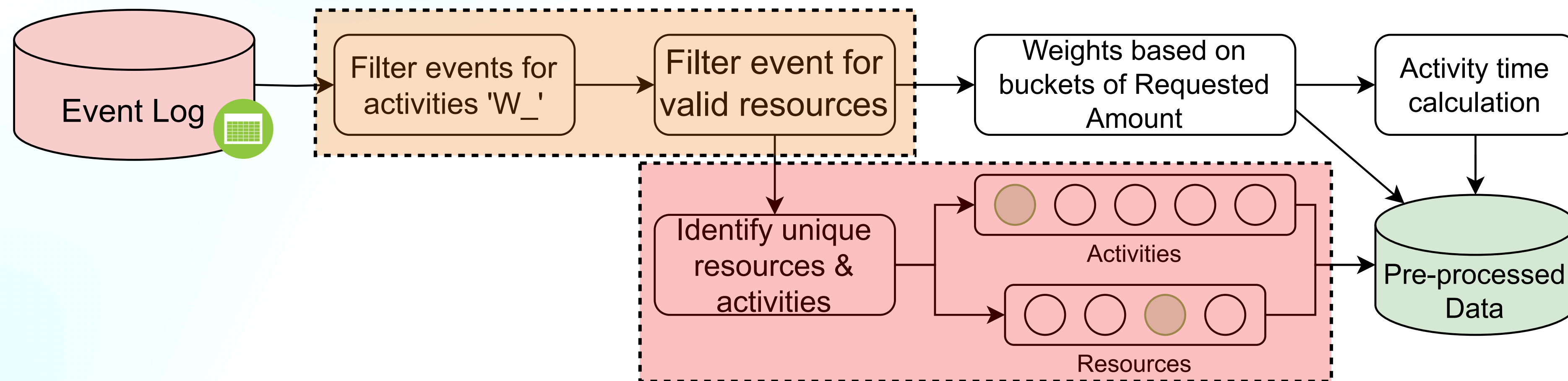


Figure. Data Filtering and preprocessing

# Data

- BPIC'2012 Shared Task: Consumer Loan approvals process
- Filtering: events with valid resource and are carried out manually
- Preprocessing: One-hot encoding of Activities and Resources
- Weights and activity time calculation

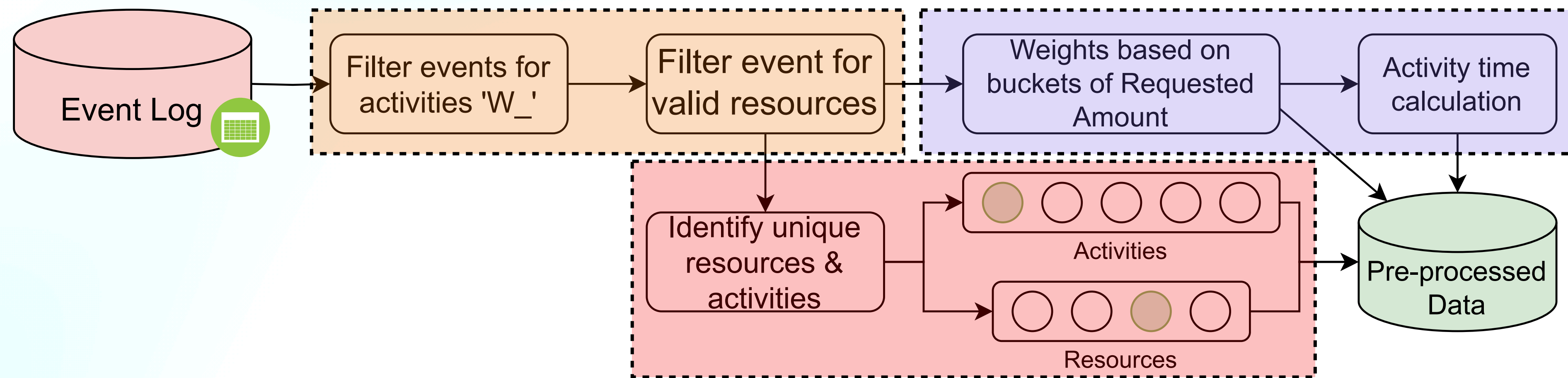


Figure. Data Filtering and preprocessing



# Experiments

- Replicate original implementation
  1. LSTM + Minimum cost maximum flow (MCMF)
- Major concern: performance of prediction model
- Train 3 additional models:
  1. BiLSTM + MCMF
  2. GRU + MCMF
  3. CNN + MCMF

# Experiments

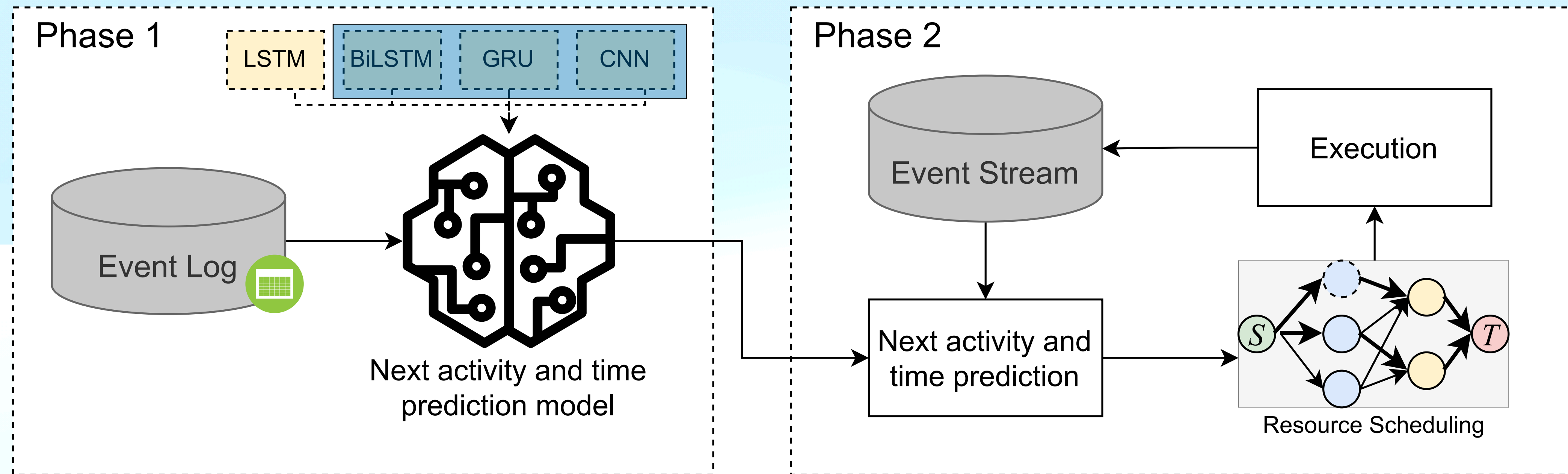


Figure. Experimental Setup



# Results

	Method	Weighted Completion	Computation Time	Prediction Time
Suggested in Original paper	Baseline	2695	60	56
	LSTM + MCMF	1823	3151	3145
Additional Prediction Models	BiLSTM + MCMF	1928	3194	3189
	GRU + MCMF	1658	3266	3261
	CNN + MCMF	807	3645	3639

Table. Results of our experiments

# Results

	Method	Weighted Completion	Computation Time	Prediction Time
Suggested in Original paper	Baseline	2695	60	56
	LSTM + MCMF	1823	3151	3145
Additional Prediction Models	BiLSTM + MCMF	1928	3194	3189
	GRU + MCMF	1658	3266	3261
	CNN + MCMF	807	3645	3639

Table. Results of our experiments



# Results

- CNN capturing spatial patterns from matrix-like data
- challenge conventional assumptions [3]
- suitable approaches for different tasks
- Complex architectures outperformed by simpler architectures like GRU and CNN
- Keeping prediction models simple

	Method	Weighted Completion	% change from baseline
Suggested in Original paper	Baseline	2695	0
	LSTM + MCMF	1823	47% ↑
Additional Prediction Models	BiLSTM + MCMF	1928	39% ↓
	GRU + MCMF	1658	62% ↑
	CNN + MCMF	807	233% ↑

Table. Results of our experiments

# Future Work & Limitations

- Different resource allocation method:
  - Eg. Ant Colony Optimisation
- Using different real-life datasets
- Limitations:
  - CNN performs best, contrary to studies
  - Prediction time



# References

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**Open to questions!**



**Thank you!**