Maximum size square sub-matrix with all 1s

Given a binary matrix, find out the maximum size square sub-matrix with all 1s.

For example, consider the below binary matrix.

0	1	1	0	1
1	1	0	1	0
0	1	1	1	0
1	1	1	1	0
1	1	1	1	1
0	0	0	0	0

We strongly recommend that you click here and practice it, before moving on to the solution.

Algorithm:

#define R 6 #define C 5

Let the given binary matrix be M[R][C]. The idea of the algorithm is to construct an auxiliary size matrix S[][] in which each entry S[i][j] represents size of the square sub-matrix with all 1s including M[i][j] where M[i][j] is the rightmost and bottommost entry in sub-matrix.

```
a) Copy first row and first columns as it is from M[][] to S[][]
b) For other entries, use following expressions to construct S[][]
    If M[i][j] is 1 then
        S[i][j] = min(S[i][j-1], S[i-1][j], S[i-1][j-1]) + 1
    Else /*If M[i][j] is 0*/
        S[i][j] = 0
2) Find the maximum entry in S[R][C]
3) Using the value and coordinates of maximum entry in S[i], print sub-matrix of M[][]
For the given M[R][C] in above example, constructed S[R][C] would be:
```

0 1 1 0 1

value and its coordinates, we can find out the required sub-matrix.

Construct a sum matrix S[R][C] for the given M[R][C].

```
1 1 0 1 0
0 1 1 1 0
1 1 2 2 0
1 2 2 3 1
0 0 0 0 0

The value of maximum entry in above matrix is 3 and coordinates of the entry are (4, 3). Using the maximum
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#include<stdio.h>
#define bool int

```
void printMaxSubSquare(bool M[R][C])
  int i,j;
  int S[R][C];
  int max_of_s, max_i, max_j;
  /* Set first column of S[][]*/
  for(i = 0; i < R; i++)
     S[i][0] = M[i][0];
  /* Set first row of S[][]*/
 for(j = 0; j < C; j++)

S[0][j] = M[0][j];
  /* Construct other entries of S[][]*/
  for(i = 1; i < R; i++)
    for(j = 1; j < C; j++)
      if(M[i][j] == 1)
        S[i][j] = min(S[i][j-1], S[i-1][j], S[i-1][j-1]) + 1;
      else
        S[i][j] = 0;
  }
  /* Find the maximum entry, and indexes of maximum entry
     in S[][] */
 \max_{s} of_s = S[0][0]; \max_{s} i = 0; \max_{s} j = 0;
  for(i = 0; i < R; i++)
    for(j = 0; j < C; j++)
      if(max_of_s < S[i][j])
         max_of_s = S[i][j];
         max_i = i;
         \max_{j} = j;
 printf("\n Maximum size sub-matrix is: \n");
  for(i = max_i; i > max_i - max_of_s; i--)
    for(j = max_j; j > max_j - max_of_s; j--)
      printf("%d ", M[i][j]);
    printf("\n");
}
/* UTILITY FUNCTIONS */
/* Function to get minimum of three values */
int min(int a, int b, int c)
{
  int m = a;
  if (m > b)
   m = b;
  if (m > c)
    m = c;
  return m;
/* Driver function to test above functions */
int main()
{
  bool M[R][C] = \{\{0, 1, 1, 0, 1\},
```

Run on IDE

Time Complexity: O(m*n) where m is number of rows and n is number of columns in the given matrix.

Auxiliary Space: O(m*n) where m is number of rows and n is number of columns in the given matrix.

Algorithmic Paradigm: Dynamic Programming

printMaxSubSquare(M);

getchar();

{1, 1, 0, 1, 0}, {0, 1, 1, 1, 0}, {1, 1, 1, 1, 0}, {1, 1, 1, 1, 1}, {1, 0, 0, 0, 0, 0}};