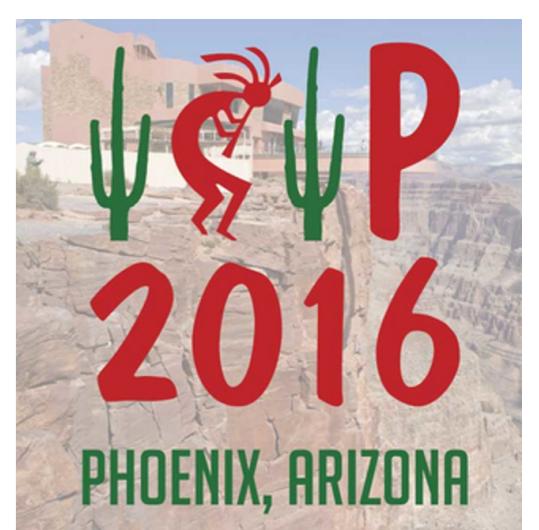


Splicing Localization in Motion Blurred 3D Scenes

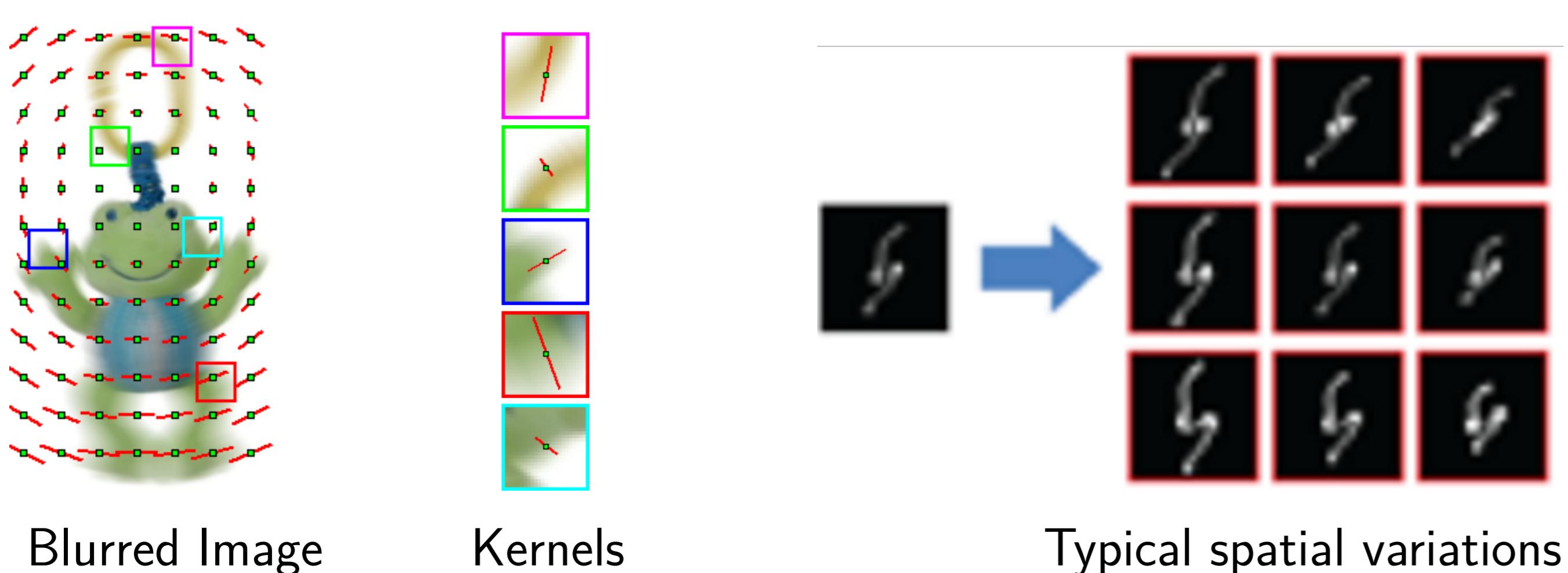
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Introduction and motivation

- Given a single image of a static 3D scene, this work solves two tasks: a **Exposing Image Forgery** and a **Depth-based Scene Segmentation** by recovering camera motion that occurred during exposure.
- Necessary, since it is not possible to detect using naked eye. Previous techniques could not handle 3D scenes containing motion blur.
- High level idea:** Scene Depth, camera trajectory and motion-blur kernels are inter-related.
- Challenge:** Knowledge of one is required to estimate the other.
- Solution:** Discovered a consistency between horizontal and vertical projections of spatially-varying blur kernels within an image.



Blurring Model

- Pixel correspondences \mathbf{x} and \mathbf{x}_λ at depth Z , after a transformation $[\phi^\lambda, T^\lambda]$

$$\mathbf{x}_\lambda = \mathbf{K} \mathbf{R}_\lambda \mathbf{K}^{-1} \mathbf{x} + \frac{\mathbf{K} \mathbf{T}_\lambda}{Z} \quad (1) \quad \mathbf{x}_\lambda = \mathbf{P}_{\phi^\lambda, T^\lambda}(\mathbf{x}) = \begin{pmatrix} 1 & -\phi_z^\lambda f \frac{t_x^\lambda}{Z} \\ \phi_z^\lambda & 1 & f \frac{t_y^\lambda}{Z} \\ 0 & 0 & 1 \end{pmatrix} \mathbf{x}$$

- If w_i denotes the fraction of time camera spent in position i , motion blurred image B can be derived from focussed image I as

$$B(\mathbf{x}) = \sum_{i=1}^N w_i I(\mathbf{P}_{\phi_i^\lambda, T_i}^{-1}(\mathbf{x})) \quad (2)$$

- Similarly, PSF at $\mathbf{x} = (x, y)$ can be derived from a single point:

$$p(x, y) = \sum_{i=1}^N w_i \delta(\mathbf{P}_{\phi_i^\lambda, T_i}^{-1}(x, y)) \quad (3)$$

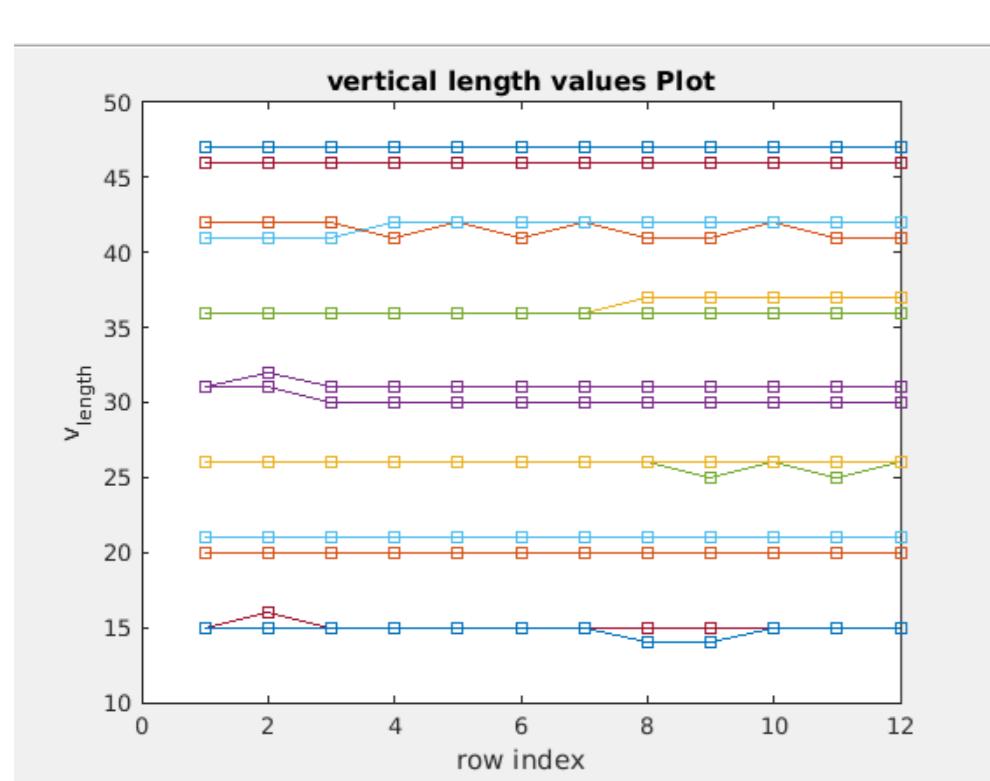
- In matrix form, it is equivalent to $\mathbf{p}^{(x,y)} = \mathbf{M}^{(x,y)} \mathbf{W}_D$

Consistency of h_{length} and v_{length}

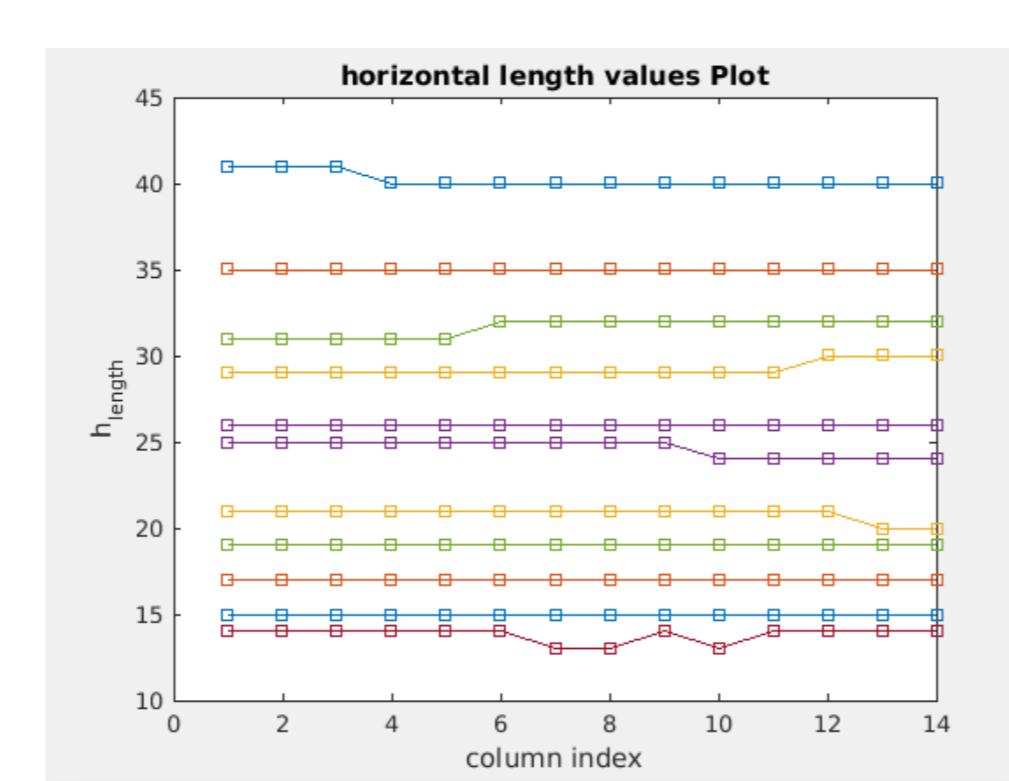
- Assumption** Small angle of rotation ϕ .
- If we pick any two points: \mathbf{x}_i and \mathbf{x}_j on a PSF, the difference in their spatial locations can be expressed in terms of the PSF's pixel coordinate x and y :

$$\Delta x_{ij}^l = (x^l \ y^l \ 1) \begin{pmatrix} 0 \\ -(\phi^j - \phi^i) \\ (t_x^j - t_x^i)f \\ Z^l \end{pmatrix} = -y^l (\Delta \phi^{ij}) + \frac{(\Delta t_x^{ij})f}{Z^l} \quad (4)$$

$$\Delta y_{ij}^l = (x^l \ y^l \ 1) \begin{pmatrix} (\phi^j - \phi^i) \\ 0 \\ (t_y^j - t_y^i)f \\ Z^l \end{pmatrix} = x^l (\Delta \phi^{ij}) + \frac{(\Delta t_y^{ij})f}{Z^l} \quad (5)$$



(a) Vertical-lengths vs rows



(b) Horizontal-lengths vs columns

Figure 1: We can see that values Δx_{ij}^l and Δy_{ij}^l turn out to be constant for all the PSFs lying on same column index y and same row index x , respectively.

Camera Trajectory Estimation

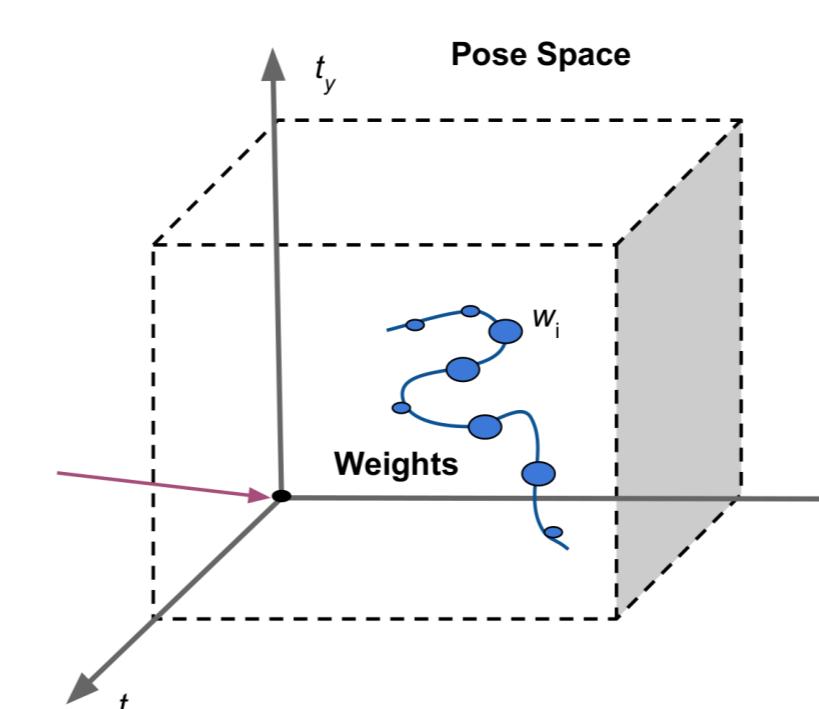


Figure 2: Camera Trajectory.

- Camera Trajectory estimation from local PSFs. Algorithm: [3].

$$\mathbf{p}^{\text{set}} = \mathbf{M}^{\text{set}} \mathbf{W}_D \quad (6)$$

- Minimize with sparsity constraint.

$$\| \mathbf{p}^{\text{set}} - \mathbf{M}^{\text{set}} \mathbf{W}_D \|^2 + c \| \mathbf{W}_D \|^1 \quad (7)$$

Matching PSFs at various depths

Using depth and camera trajectory, we generate all possible PSFs at location \mathbf{x} . If the pixel \mathbf{x} was actually situated at a different scene depth D_i , the PSF would be modified as follows

$$\mathbf{p}^{D_i}(\mathbf{x}, \mathbf{a}) = \sum_{\lambda=1}^N w_\lambda \delta(\mathbf{a} - (\mathbf{P}_{\phi_\lambda^\lambda, T_\lambda}(\mathbf{x}) - \mathbf{x})) d\tau \quad (8)$$

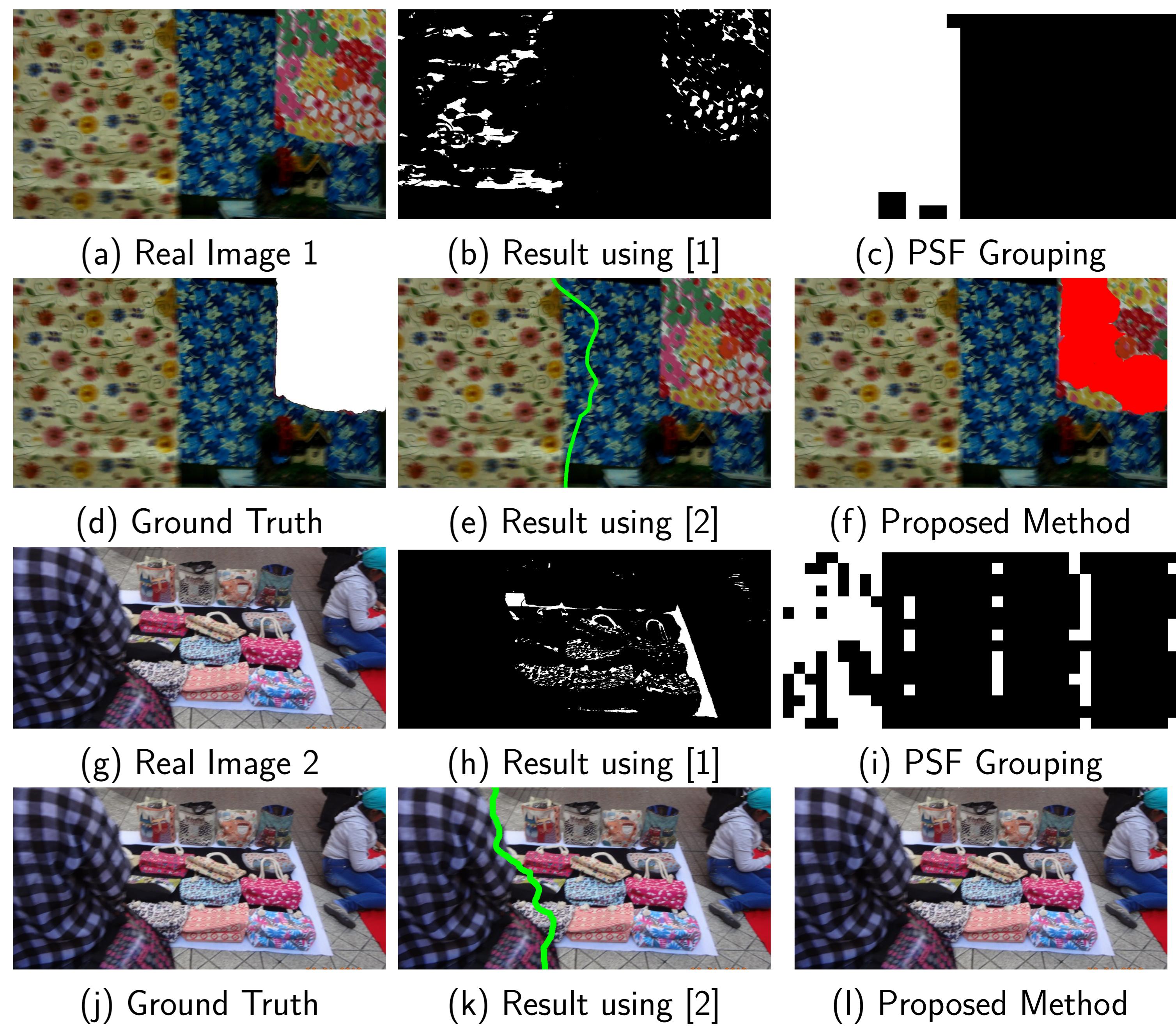
Low cross-correlation between actual PSF and estimated PSFs \rightarrow Region Spliced!

Results

- Finally, we utilize natural image texture segmentation [Mobahi, IJCV 2011] of the input image to obtain meaningful region boundaries.



Table 1: Intermediate results after each step (a) Input spliced image (b) PSF grouping (all white pixels belong to single depth layer) (c) Patch-wise inconsistency between blur kernels (d) Texture based segmentation of the input image (e) Final result showing localized spliced region in red



References

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- [2] M. P. Rao, A. N. Rajagopalan, and G. Seetharaman, "Harnessing motion blur to unveil splicing," vol. 9, no. 4. IEEE, 2014, pp. 583–595.
- [3] C. Paramanand and A. Rajagopalan, "Shape from sharp and motion-blurred image pair," *International journal of computer vision*, vol. 107, no. 3, pp. 272–292, 2014.