

Assignment VIII

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Submission Date: 15/03/2013 Time:23:59 hrs.

Aim of the Problem:

The problem involves the generation of random variables following conditional distributions. The focus on generating numbers using Cholesky method.

Part I:

This question wants us to generate 1000 random numbers following bivariate normal distribution. For this we take two normal variates of mean 5 and 8 and use the Cholesky Decomposition technique.

Implementation using R:

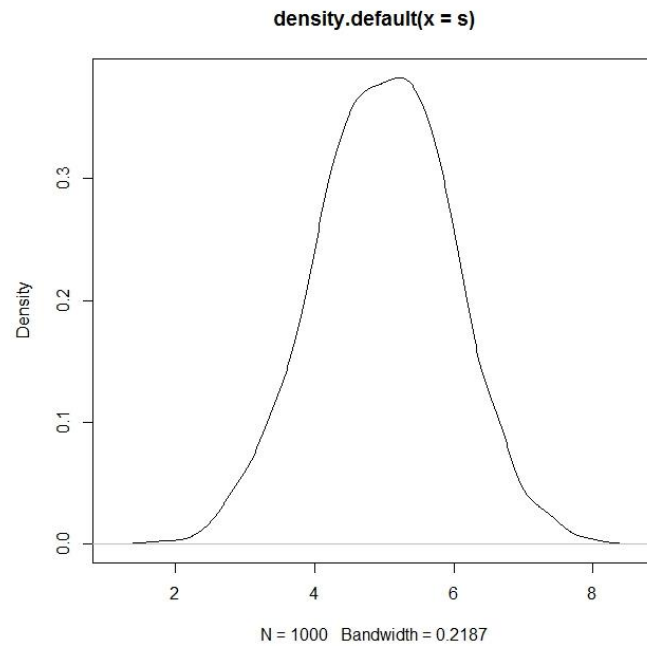
```
newnormal<-function(n,a){  
  RN<-NULL;  
  for(i in 1:n){  
    z1<-rnorm(n=1,m=0,sd=1);  
    z2<-rnorm(n=1,m=0,sd=1);  
    x1<-5+1*(z1);  
    v1<-1;  
    v2<-2;  
    cv<-2*a/(1*2);  
    #nmn<-5+cv*(v1/v2)*(x2-8);  
    nvr<-2*sqrt(1-(cv*cv));  
    x2<-8+(cv*v2*z1)+nvr*z2;  
    RN<-cbind(RN,c(x1,x2));  
  }  
  return (RN);  
}  
  
s<-newnormal(1000,0.25);  
s1<-newnormal(1000,0);  
s2<-newnormal(1000,-0.25);
```

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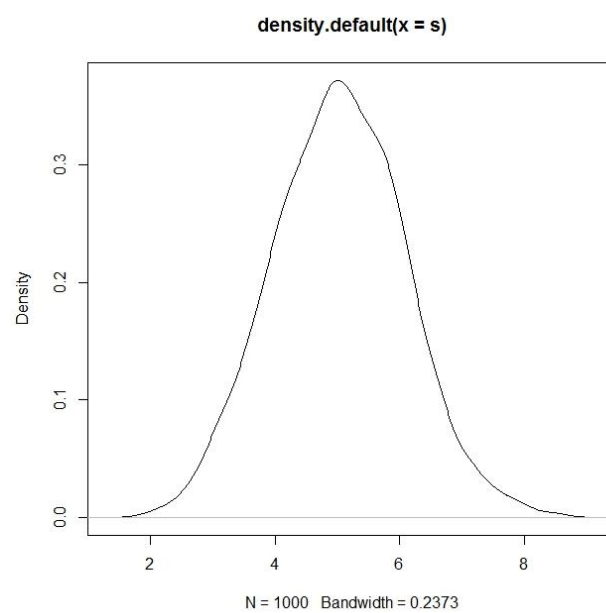
	A=-0.25	A=0.00	A=0.25
Variance	1.0121	1.069964	1.019461
Mean	4.991	4.998	5.024
Covariance	-0.301	-0.0103	0.26

Using the output the following density function was generated:

For $a=-0.25$

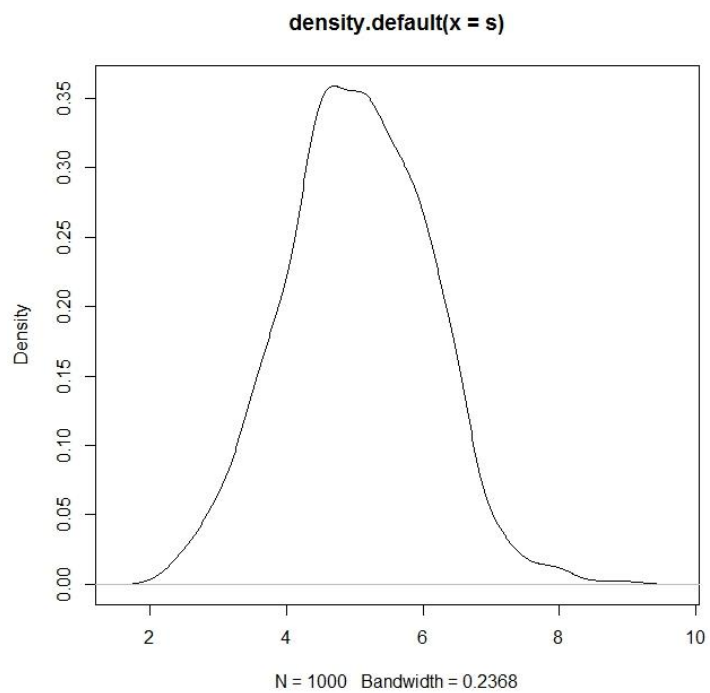


For $a=0$:



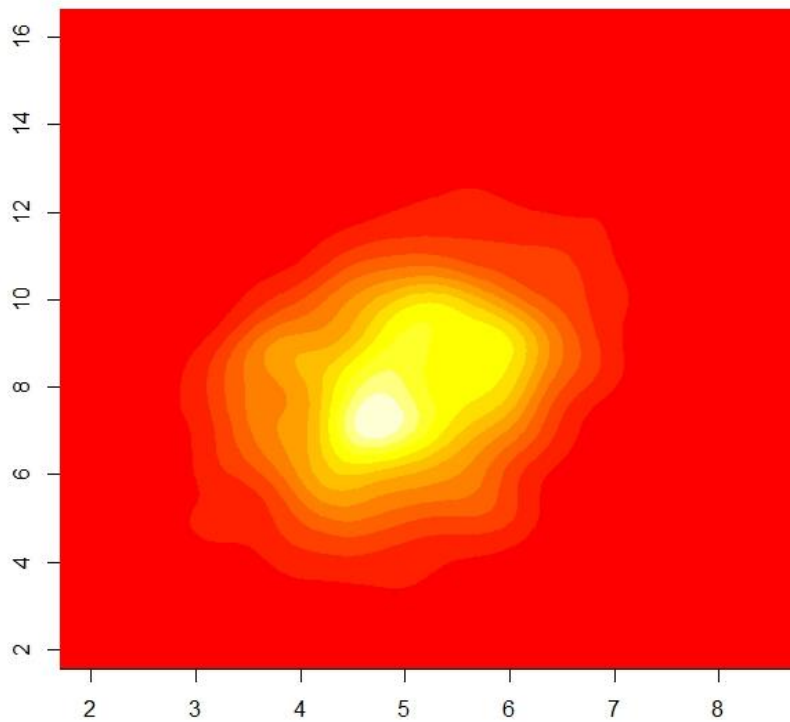
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For $a=0.25$



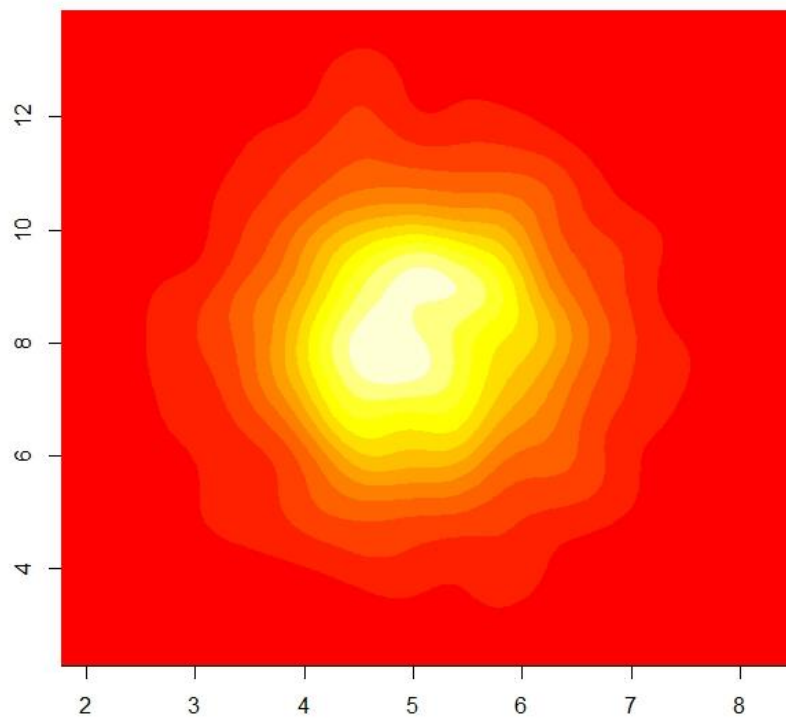
The corresponding contour plots:

$A=0.25$

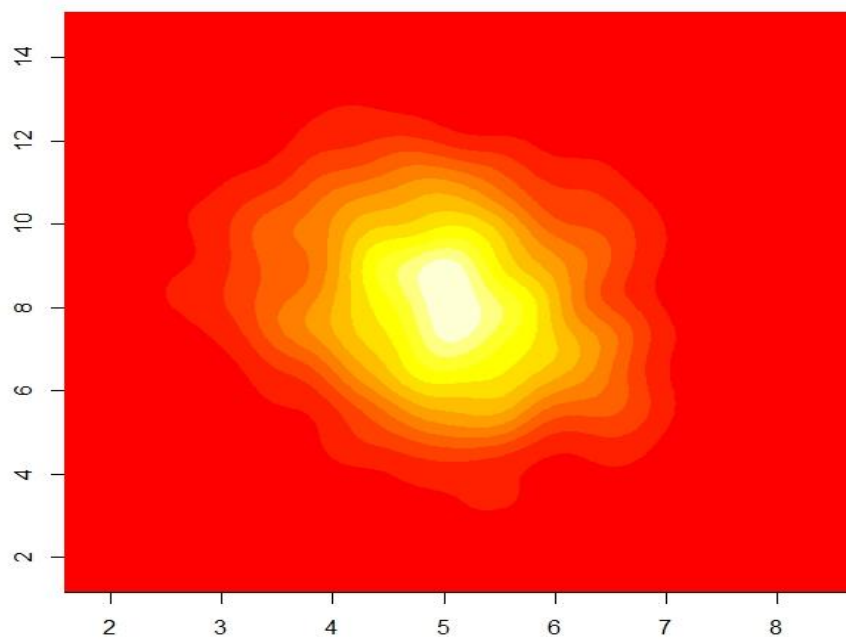


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$A=0.0$



$A=-0.25$

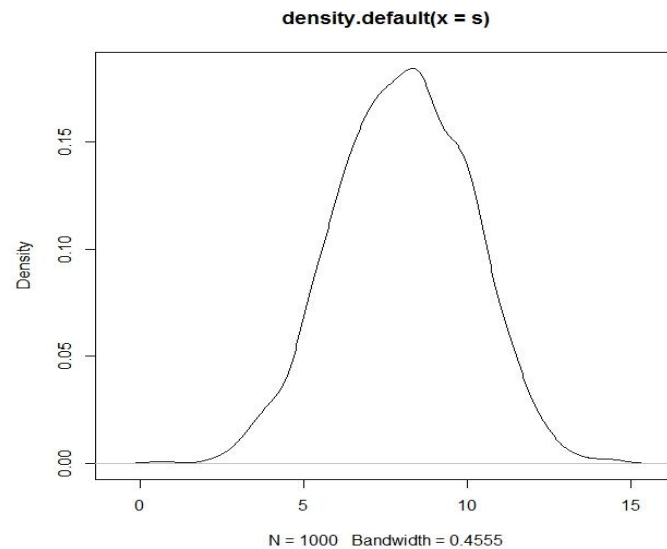


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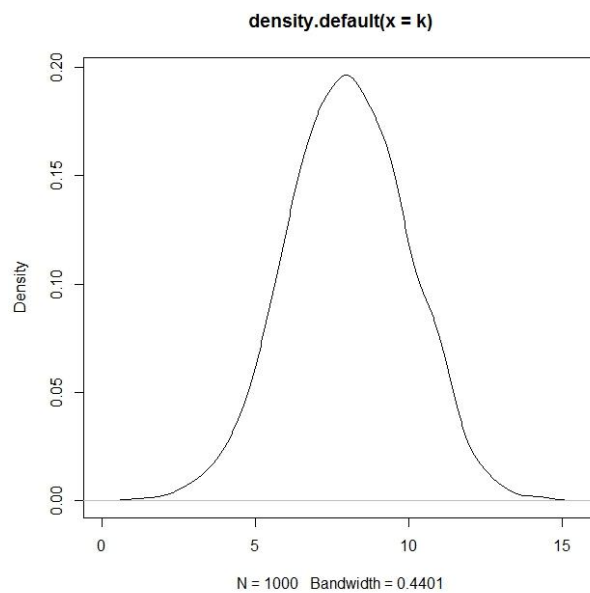
Part II:

Here we need to plot the marginal densities of X_1 and X_2 .

Density of X_1 :

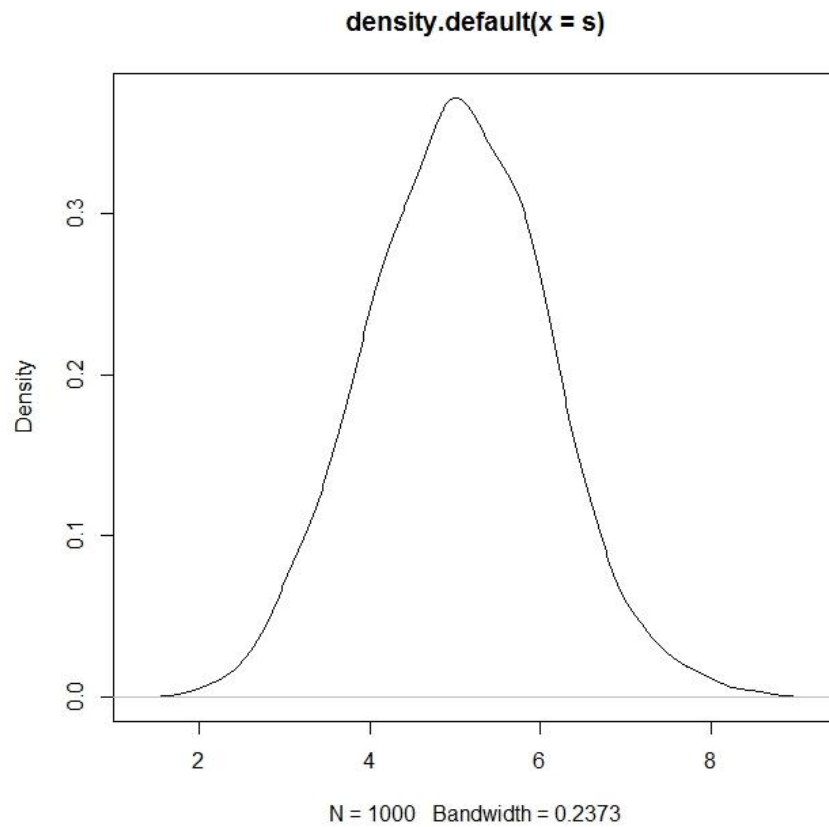


The empirical density of X_1 :

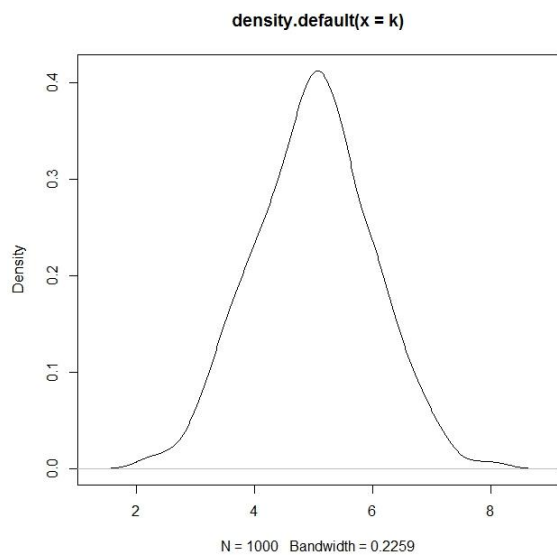


Density of X_2 :

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Empirical density of X_2 :

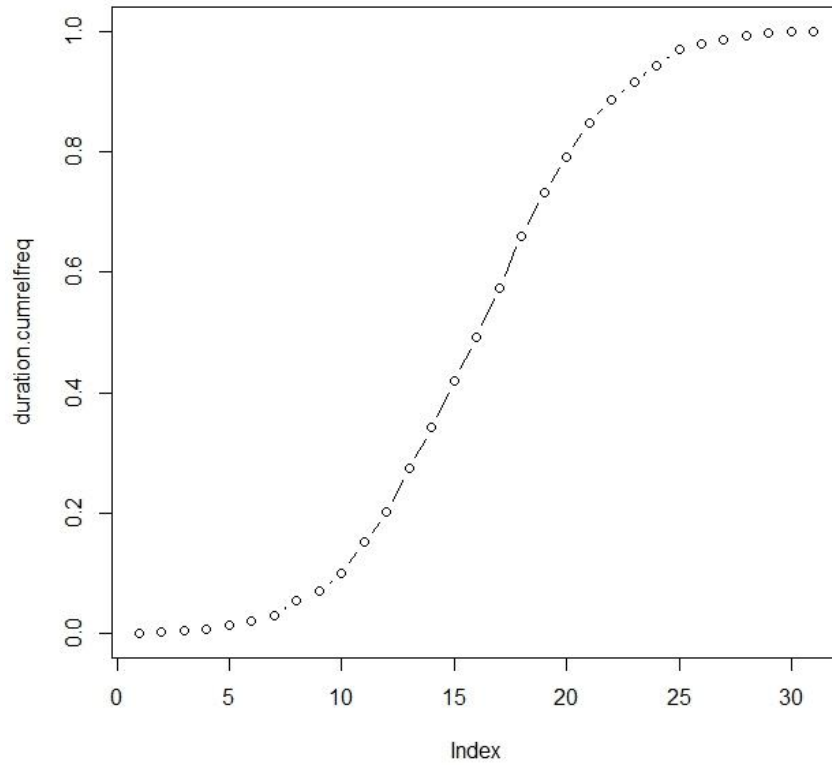


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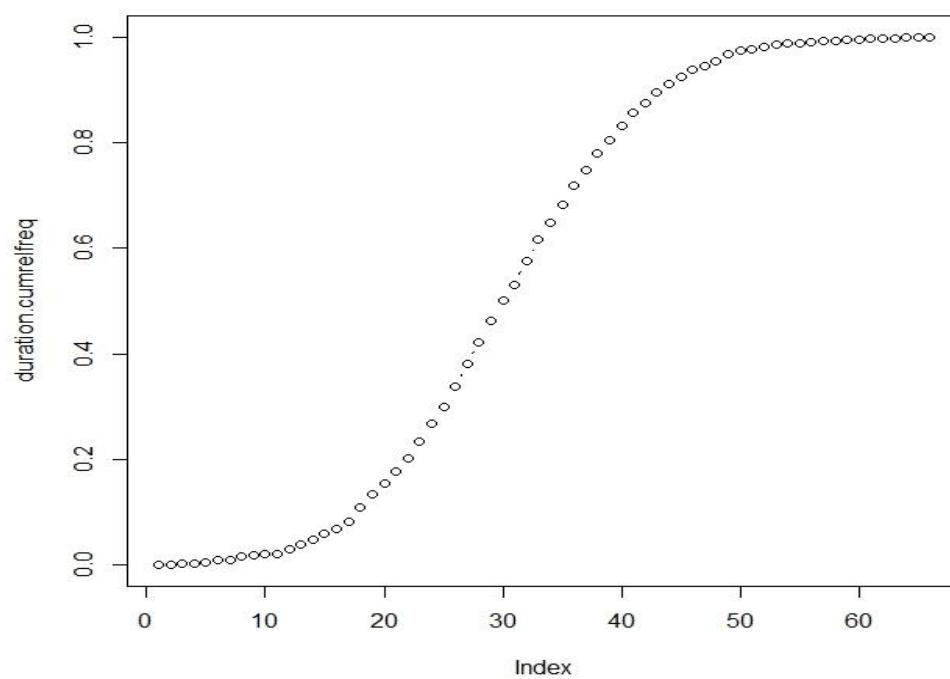
The cumulative density functions:

A=0.25

X1:



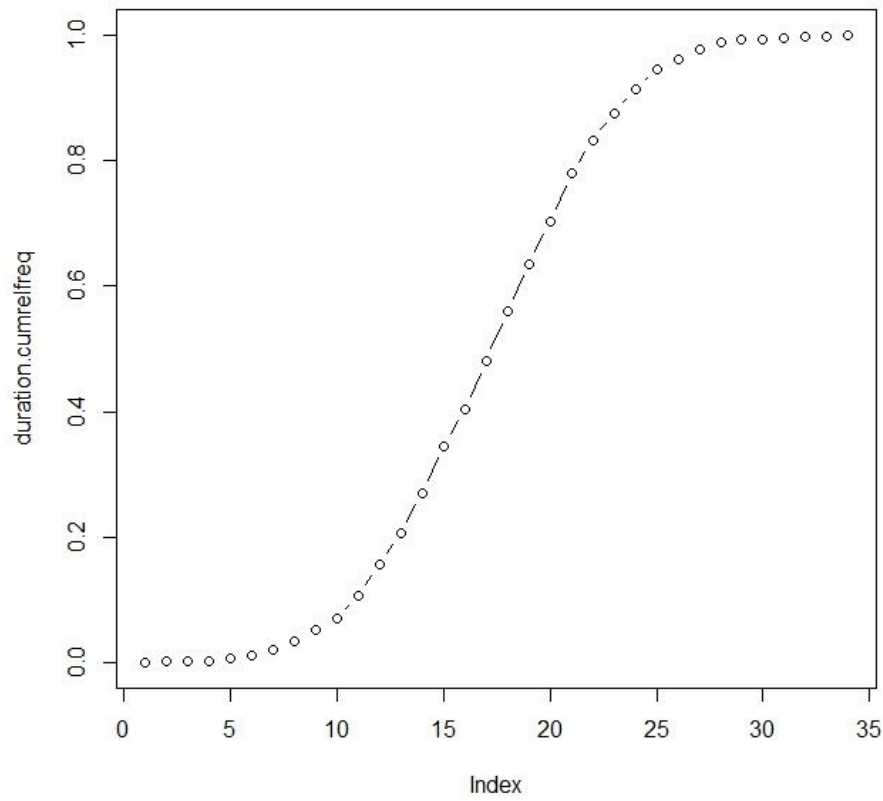
X2:



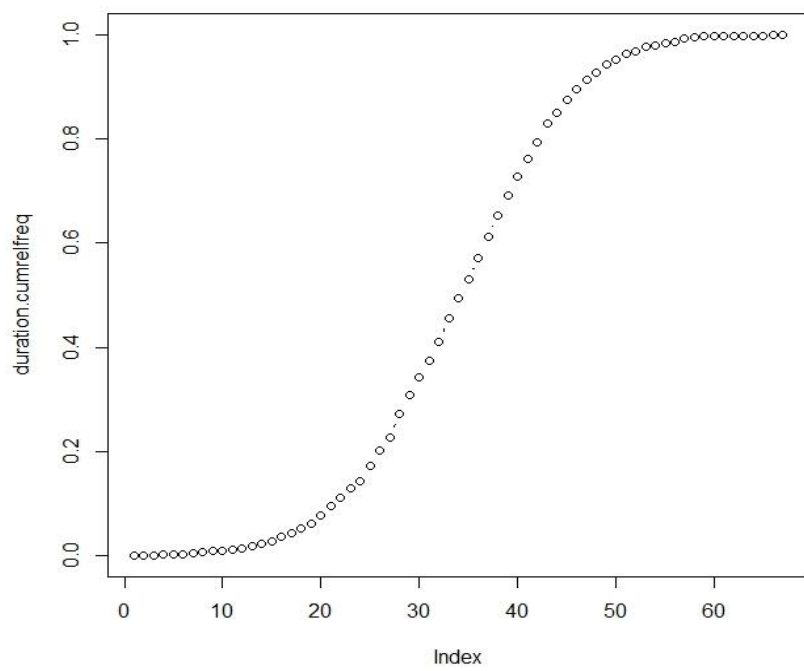
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A=0.0

X1:



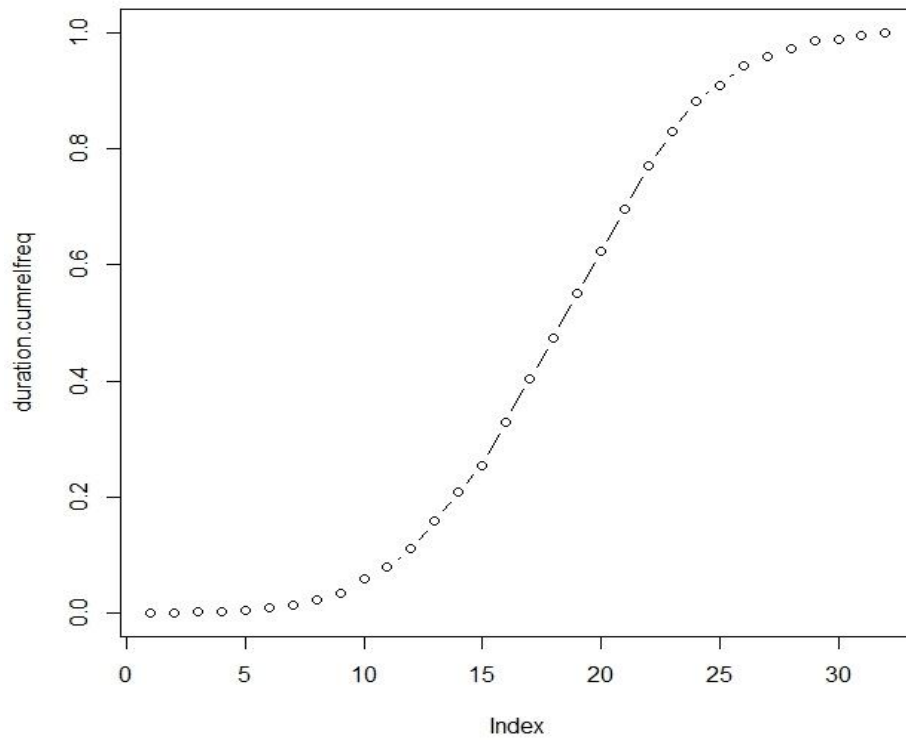
X2:



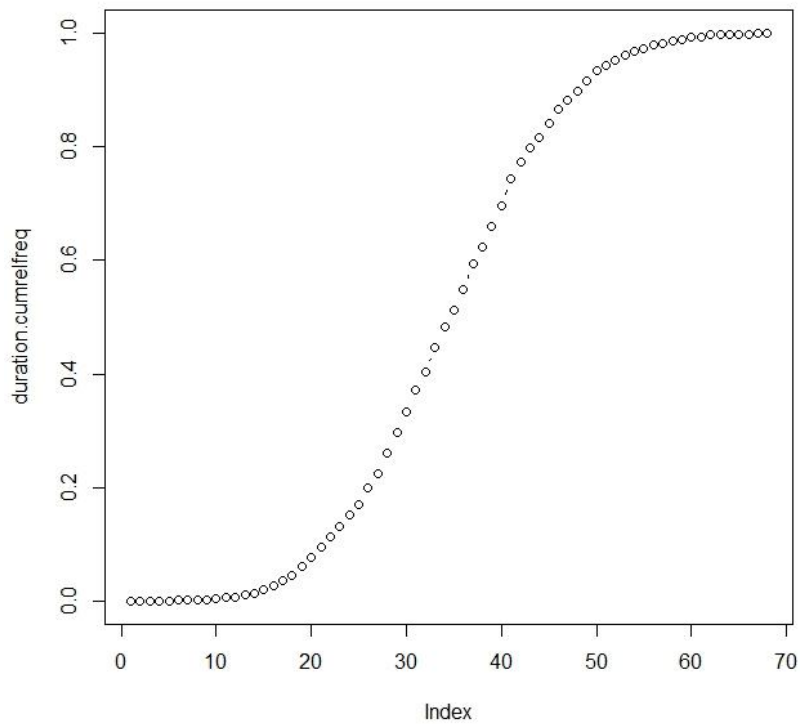
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A=-0.25

X1:



X2:



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Part III:

This questions generates a random variable conditionally on another.

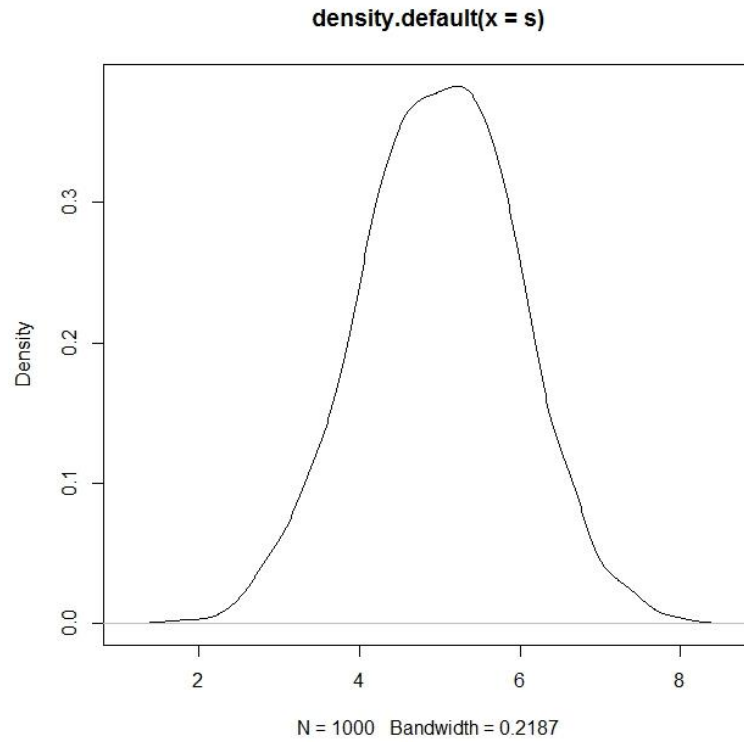
Algorithm:

1. Generate two independent $Z1, Z2 \sim N(0, 1)$.
2. First generate $X2$, i.e. set $X2 = \mu + \sigma_2 Z1$
3. Then generate $X1$ conditional on the $X2 = x$ generated on the previous step i.e. set $X1 = \mu^* + \sigma^* Z2$ where $\mu^* = \mu_1 + \rho(\sigma_1/\sigma_2)(x - \mu_2)$ and $\sigma^* = \sigma_1\sqrt{1 - \rho^2}$

Implementation using R:

```
newnormal<-function(n,a){
  RN<-NULL;
  for(i in 1:n){
    z1<-rnorm(n=1,m=0,sd=1);
    z2<-rnorm(n=1,m=0,sd=1);
    x2<-8+2*(z1);
    v1<-1;
    v2<-2;
    cv<-2*a/(1*2);
    nm<-5+cv*(v1/v2)*(x2-8);
    nvr<-1*sqrt(1-(cv*cv));
    x1<-nm+nvr*z2;
    RN<-c(RN,x1);
  }
  return (RN);}
s<-newnormal(1000,0.25);
s1<-newnormal(1000,0);
s2<-newnormal(1000,-0.25);
```

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	A=-0.25	A=0.00	A=0.25	X1	X2
Variance	1.0121	1.069964	1.019461	1	1
mean	4.991	4.998	5.024	5	8