

4 3 2 1 5 = len=5

1 3 2 4 5

```
for i in range(len(arr) -1)  1           len = 3-1
    index=i # min value  1 3 2
    for j in range ( i+1, len(arr) )
        if arr[j] < arr[index]
            index = j  2
    if index != i:
        arr[index],arr[i]=arr[i],arr[index]
```

selection Sort: ->

1 5 3 6 4

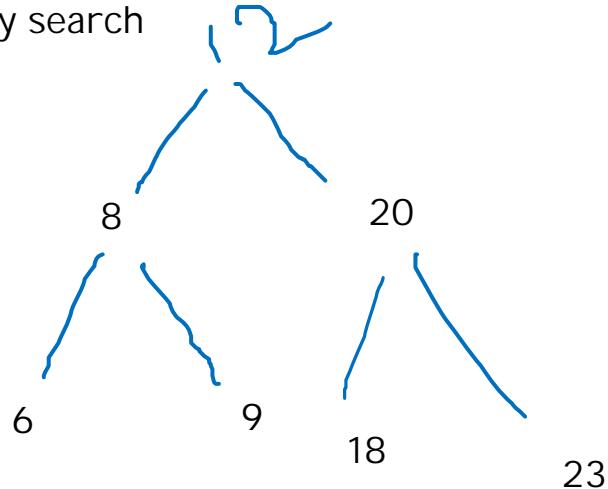
```
for i in range(len(arr)):
    j=i
    while j>=0 and arr[j-1]>arr[j]:
        arr[j-1],arr[j]=arr[j],arr[j-1]
        j=j-1
```

quick sort :

```
class QuickSort:  
    def __init__(self,data):  
        self.data=data  
  
    def sort(self):  
        self.quick_sort(0,len(self.data)-1)  
  
    def quick_sort(self,low,high):  
        if low>=high:  
            return  
  
        pivot_index=self.partition(low,high)  
        self.quick_sort(low,pivot_index-1)  
        self.quick_sort(pivot_index+1,high)  
  
    def partition(self,low,high):  
        pivot_index=(low+high)//2  
        self.data[pivot_index],self.data[high]=self.data[high],self.data[pivot_index]  
  
        for i in range(low,high):  
            if self.data[i]<=self.data[high]  
                self.data[i],self.data[low]=self.data[low],self.data[i]  
                low+=1  
        self.data[high],self.data[low]=self.data[low],self.data[high]  
        return low
```

```
if __name__=="__main__":  
    x=[2,13,5,1]  
    quickSort=QuickSort(x)  
    quickSort.sort()  
    print(x)
```

binary search



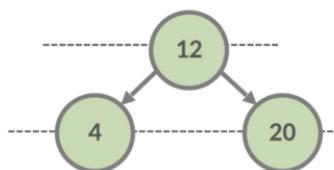
def linear search(arr,x):

for i in range(len(arr)):

if arr[i]==x:

print(f"index {i} : {x}")

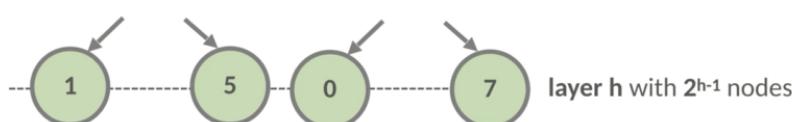
## Binary Search Trees



layer 1 with  $2^0$  nodes

layer 2 with  $2^1$  nodes

...



layer  $h$  with  $2^{h-1}$  nodes

how many  $N$  nodes are there in a complete binary search tree with  $h$  height?

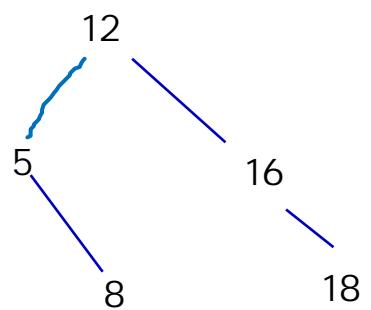
$$\begin{aligned}2^{h-1} &= N \\ \log_2 2^{h-1} &= \log_2 N \\ h &= \log_2 N + 1 \\ h &= O(\log N)\end{aligned}$$

```

def common(a,b,c):
    n1,n2,n3=len(a),len(b),len(c)
    i
    w
    it: 1
    .
    p
    1, 2, 3      ↘
    3, 4, 5
    3, 6, 9
    while i<n1 and j<n2 and k < n3:    i : 0 | j : 0 k: 0
        if a[i] == b[j] and b[j] == c[k]:
            arr.append(a[i])
            i+=1
            j+=1
            k+=1
        elif a[i] < b[j]:
            i+=1
            ↙
        elif b[j] < c[k]
            j+=1
        else:
            k+=1

```

12 5 8 16 18



Bubble sort :

time complexity :  $O(n^2)$  #two for loop is needed

space complexity :  $O(1)$

swap no additional space is required that's why it is  $O(1)$

```
for i in range(len(arr)):  
    for j in range(len(arr)-1-i):  
        if arr[i]>arr[j+1] :  
            arr[i],arr[j+1]=arr[j+1],arr[i]
```

8, 22, 7, 9, 31, 5, 13

8 7 22 9 31 5 13

8 7 9 22 31 5 13

8 7 9 22 5 31 13

8 7 9 22 5 13 31

4

























































































































































































































































































































































































































































































































































































































































































































































































































































































































































































































































































