

CS & IT ENGINEERING

Operating Systems

Memory Management



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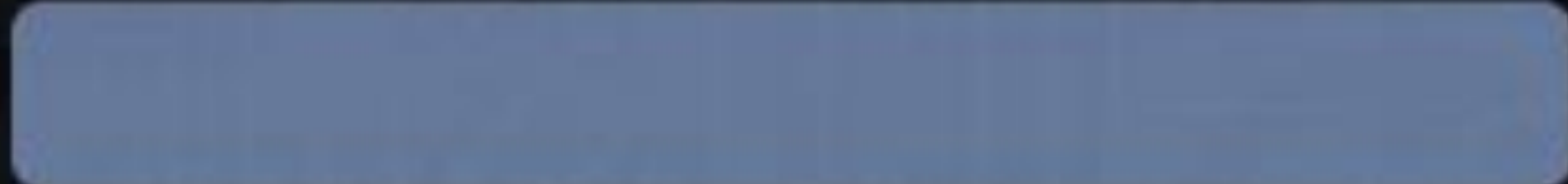
Lecture No. 11



TOPICS TO BE
COVERED

Page Replacement
Techniques

Problem Solving



$l=20$; $n=6$

Page Replacement Techniques

Ref. String: $\langle 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1 \rangle$

① FIFO:

Criteria: T.O.L

3 Frames = 15 (75%)
4 Frames = 10 (50%) ↓

As per graph
if No. of
frames
Alloc = 6

Ref. String: $\langle \underline{7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1} \rangle$

A) 9 B) 8
C) 6 D) 10

2) Optimal Replacement: \langle replace that page which will not be used for the longest duration of time in future references \rangle

3 Frames: 9

4 Frames: 8

→ Least P.F rate

7	2	2	2	2	2	7				
0	0	0	4	0	0	0				
1	1	3	3	3	1	1				

Practically opt. replacement is NOT implementable

Benchmark

Ref. String: $\langle 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1 \rangle$

3) Least Recently used (LRU) \langle replace that page which has not been used for the longest duration of time in the PAST \rangle

Criteria: T.O.R
reference

3 Frames: 12
4 Frames: 8 \downarrow

1
0
7

3 Frames

4) Most Recently used (MRU):

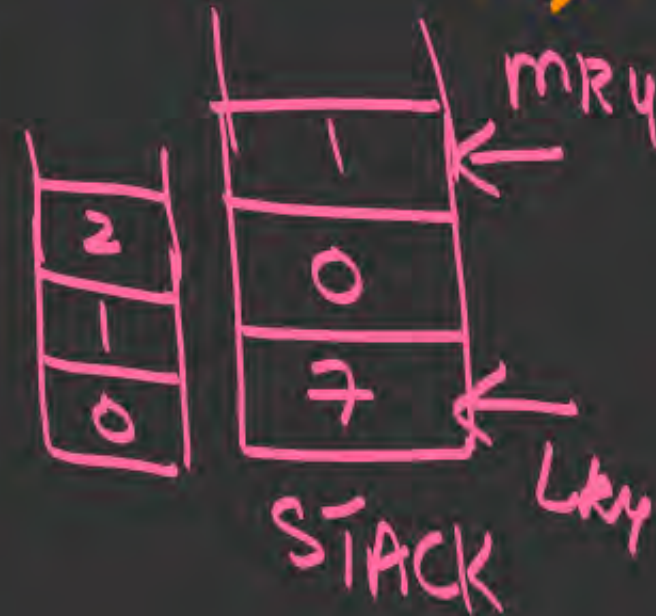
3F: 16
4F: 12(?)

7
4
2

Stack method (TOR)

Frames

7 2
0
1



< 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1 >

5) Counting Algo's

a) L.F.U [Least frequently used]
= 13

b) M.F.U [Most frequently used]
= 15

Sel. Criteria: C.O.R

< Count of Reference >

2	1
0	2
1	1

3- Frames

Among all the Algo.
optimal is having
Least P.F rate

LRU ~ optimal

(Many OS Impl. either LRU
or LRU Approximations)

Ref. String II: $\langle \underline{1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5} \rangle$ $l = 12$
 $n = \underline{\underline{5}}$

MRU:

H/W: LRU: 3/4
10/8

① FIFO: Pure D.P
 3 Frames: 9 ✓
 4 Frames: 10 ✓ ↑

1	4	4	4	5	5	5		
2	2	1	1	1	3	3		
3	3	3	2	2	2	4		

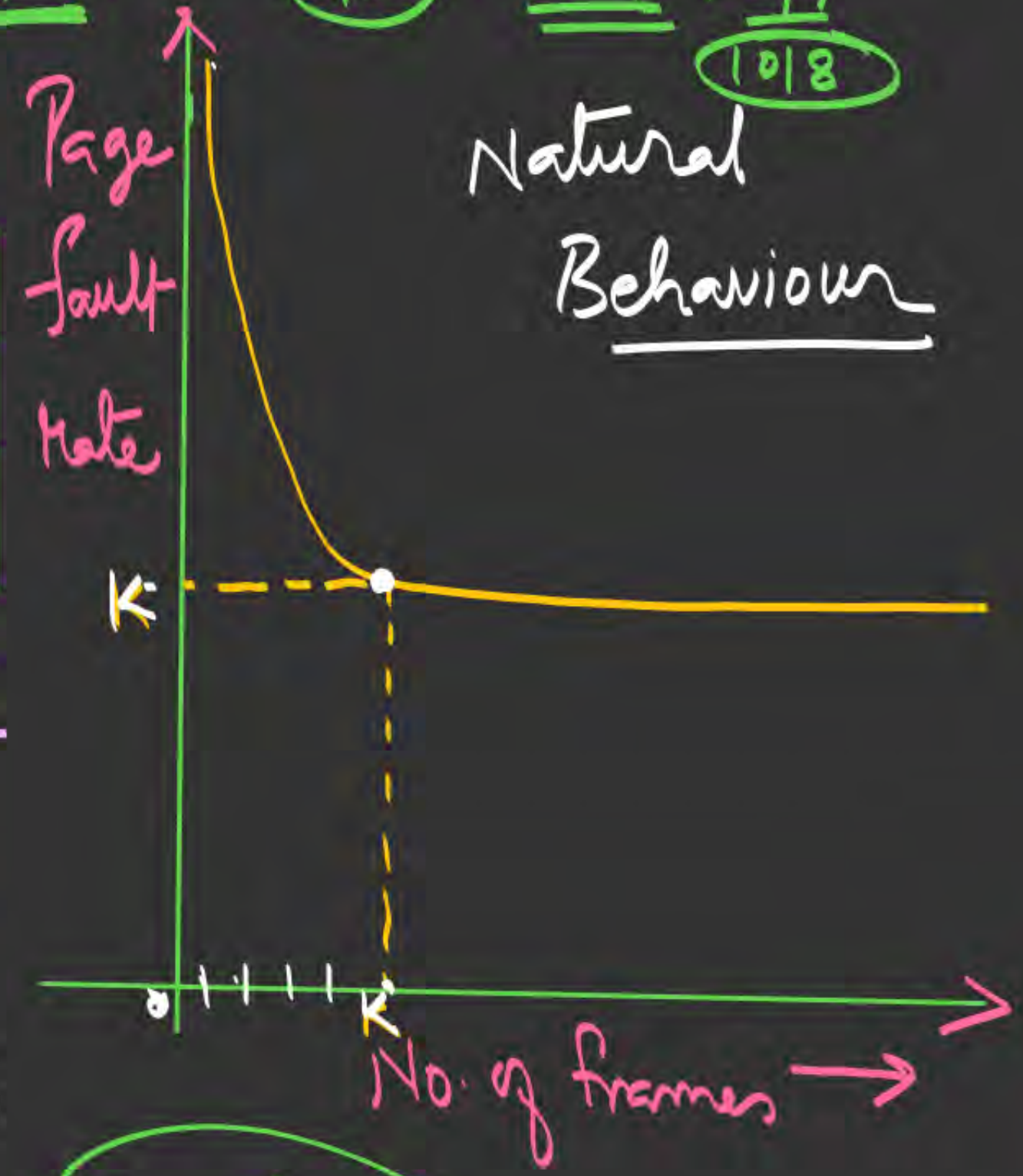
Frames

② Optimal Replacement

3F → 7
 4F → 6 ↓

Belady's Anomaly:

\langle As the no. of frames allocated to the process increases, Page fault also Sometimes increases \rangle



Sec. chance

Only FIFO & FIFO-Based Suffers from Bel. Anom.

II. * LRU Approximations

< Reference bit (R) >

These Algo's are not really LRU, but they approximate to the behaviour of LRU

a) Reference bit (R):

Each Page in the P.T will be associated with a Ref bit 'R';

Criteria: 'R':

- 0: Page is not referred so far during present Epoch.

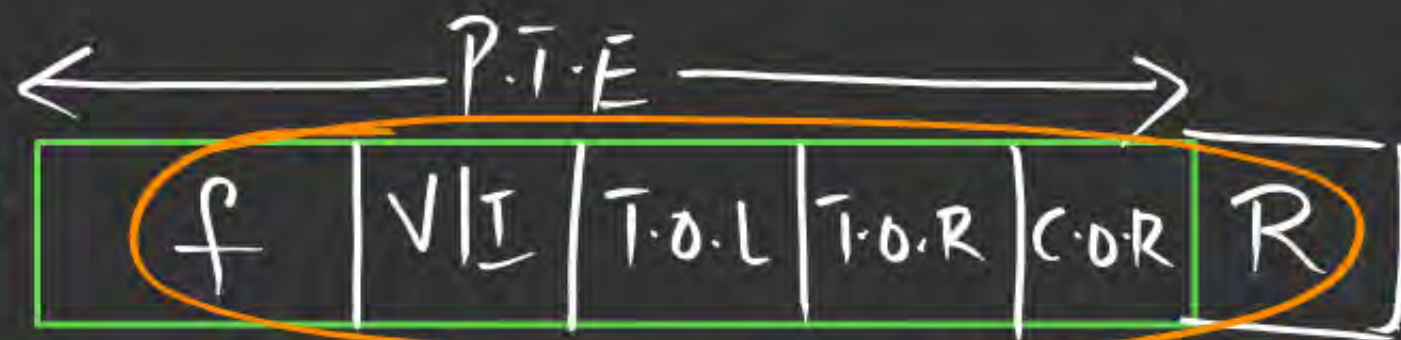
1: Page has been referred atleast once during Present Epoch;

P	f	VLI	TOL	R
0	a	1	2	1
①	e	1	3	1
2	d	1	0	1
③	-	0	-	-
4	c	1	4	1
⑤	b	1	1	1

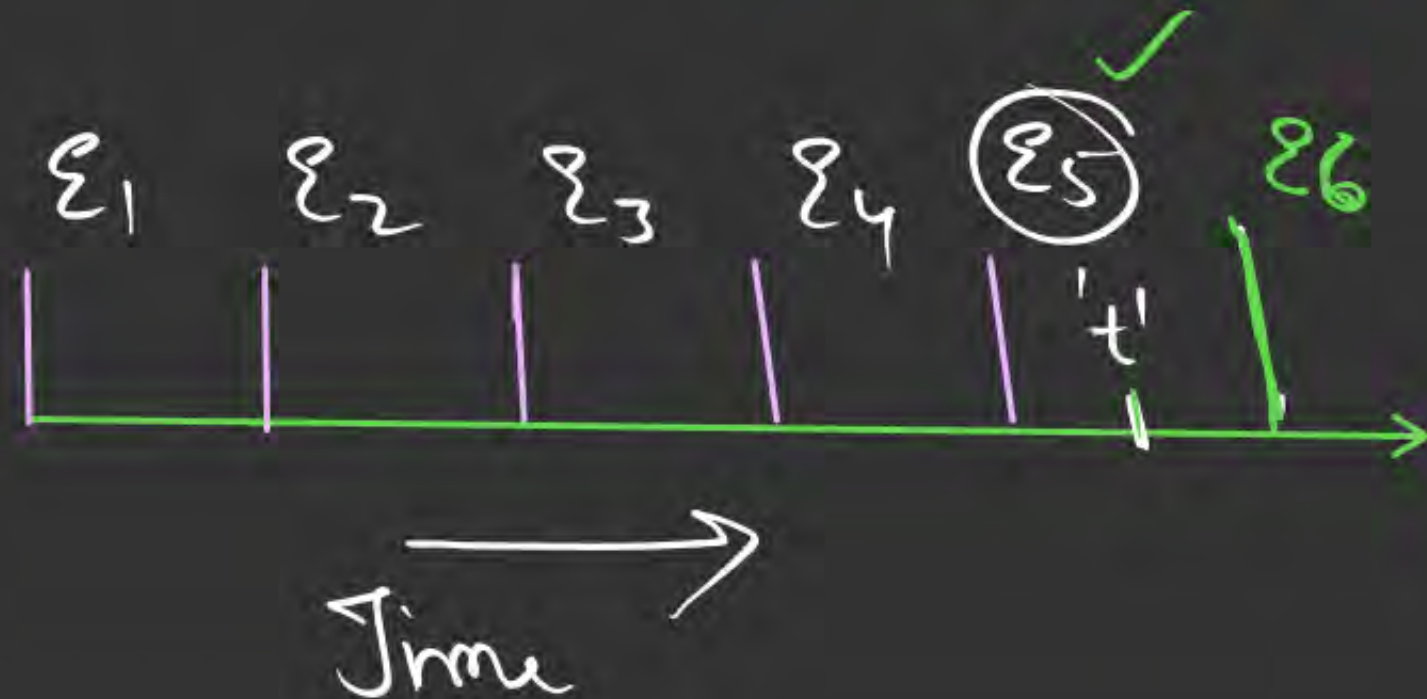
Page-Table

Ref bit Algo fails

Index



Attributes of Page



b) Additional Ref bits : < Each Page is associated with more than 1-Ref bits (Say 8)

Current Epoch

	R_1	R_2	R_3	R_4	R_5	R_6	R_7	R_8
P_i	1	0	0	1	0	1	1	1
✓ P_j	0	0	1	1	1	0	1	1
P_k	0	0	1	1	0	1	1	1

(P_e) X : Cause P.F

When Current Epoch gets over

⇓
(Shift left of n 's)

c) Second-chance [clock Algo]

Criteria: $\left[\underline{T.O.L} + R \right]$

P.T.E

P	f	V/I	T.O.L	R
0	e	1	2	1 0
1	a	1	3	1 0
✓ 2	b	1	0	1 0
③	—	0	—	—
4	c	1	1	1 0
5	d	1	4	1 0

(Page-Table)

When all Pages 'R' value is 1
then FIFO Page gets
Selected

Second chance ~ FIFO

↓
Belady's Anomaly



**THANK
YOU!**

