



CS & IT ENGINEERING

Graph Theory

DPP 02

Discussion Notes

[MCQ]

1. Which of the following is a graphic sequence?

(a) $5, 3, 3, 2, 2, 1 \rightarrow$ graphical.(b) $2, 1, 1, 1, 1, 1$ (c) $6, 5, 4, 3, 2, 1$ (d) $5, 5, 2, 2, 1, 1$ b) $2 \underline{\underline{\underline{\underline{\underline{1}}}}}$

not graphical

d) $\underline{5} \underline{5} \underline{2} \underline{2} \underline{1} \underline{1}$ $n=6$ c) $6 5 4 3 2 1$

not possible

 $n-1, n-1, \dots, \frac{n}{2}$
not graphicala) $\cancel{5} \underline{3} \underline{3} \underline{2} \underline{2} \underline{1}$
 $\cancel{2} \dot{1} \dot{1} \dot{0}$
 $1 0 1 0$ $\overset{0}{\text{---}} \overset{0}{\text{---}}$
 $1 1 0 0$

[NAT]

2. Find the number of edges of an undirected graph having degree sequence 2, 4, 4, 3, 4, 1?

$$\sum d(v_i) = 2e$$

Ans : 9.

$$2 + \frac{4+4}{\downarrow} + \underline{3+4+1} = 2e$$

$$2 + 8 + 8 = 2e$$

$$18 = 2e$$

$$e = 9.$$

[NAT]

3. Let δ denote the minimum degree of any vertices of a given graph and let Δ denote the maximum degree of any vertex in the graph. Suppose a certain graph has 8 vertices and that $\delta = 4$ and $\Delta = 6$, then this graph must contains at least 16 edges.

$$n = 8 \quad \delta(G) = 4 \quad \Delta(G) = 6.$$

$$\delta(G) \leq \frac{2e}{n} \leq \Delta(G)$$

$$2 \times 8 \leq \frac{2e}{8}$$

$$16 \leq e$$

$$2 \times 8 \leq e$$

[NAT]

4. There are 24 routers in Physics Wallah. Find the number of cable required to connect them such that each router is connected with exactly 6 others.

~~18~~
~~24~~ × 6 = ~~12~~ e

Ans : 72.

o — . . .
o . . .
o . . .
o . . .

$$e = 72$$

[MCQ]

5. What is the maximum value of minimum degree (δ) with a graph of order 10 and size 16?

- (a) 4
- (b) 3 ✓
- (c) 2
- (d) 1

$$n = 10 \quad e = 16$$

$$\delta(n) \leq \frac{2e}{n}$$

$$\delta(n) \leq \frac{2 \times 16}{10}$$

$$\delta(n) \leq \underline{\underline{3.2}}$$

$$\underline{(0 \ 1 \ 2 \ 3)} \leq 3.2$$

$$\left. \begin{array}{l} 0 \leq 3.2 \\ 1 \leq 3.2 \\ 2 \leq 3.2 \\ 3 \leq 3.2 \end{array} \right\} \rightarrow$$

[NAT]

1. Consider a complete graph with size 2016. Suppose after deletion of 2 vertices from the above graph, the modified graph have x number of edges and y number of vertices. Find the value of $x - y$?

$$e = 2016.$$

$$\frac{n(n-1)}{2} = 2016.$$

$$n(n-1) = 2016 \times 2.$$

$$n(n-1) = 4032$$

$$64 \times 63 = 4032$$

$$n = 64 \text{ modified } n = 62. \quad \begin{matrix} n \rightarrow \text{edges} \\ y \rightarrow \text{vertices} \end{matrix}$$

K_{62}

$$e = \frac{n(n-1)}{2}$$

$$= \frac{62 \times 61}{2}$$

$$(30+1)(60+1)$$

$$y = 62$$

$$n = 1891 ;^2$$

$$y = 62$$

$$1829$$

[MSQ]

2. Which of the following options is/are True?

- (a) Some k-regular graph can be complete graph. (τ)
- (b) A graph with more than 2 vertices, it must have at least 2 vertices with same degree. (τ)
- (c) The degree sum of odd degree vertices must be even. (τ)
- (d) The degree sum of odd degree vertices must be odd. (f)

(a, b, c)

[MCQ]

3. Consider a wheel graph (W_n) with $n \geq 4$. Which of the following is minimum number of edges added to the above wheel graph to make it complete graph?

(a) $n(n - 1)$

(b) $\frac{n^2 - 5n + 4}{2}$ ✓

(c) $\frac{n(n - 1)}{4}$

(d) None of these.

$$\frac{\partial(n-1)}{2} + \frac{n}{2} = \frac{n(n-1)}{2}$$

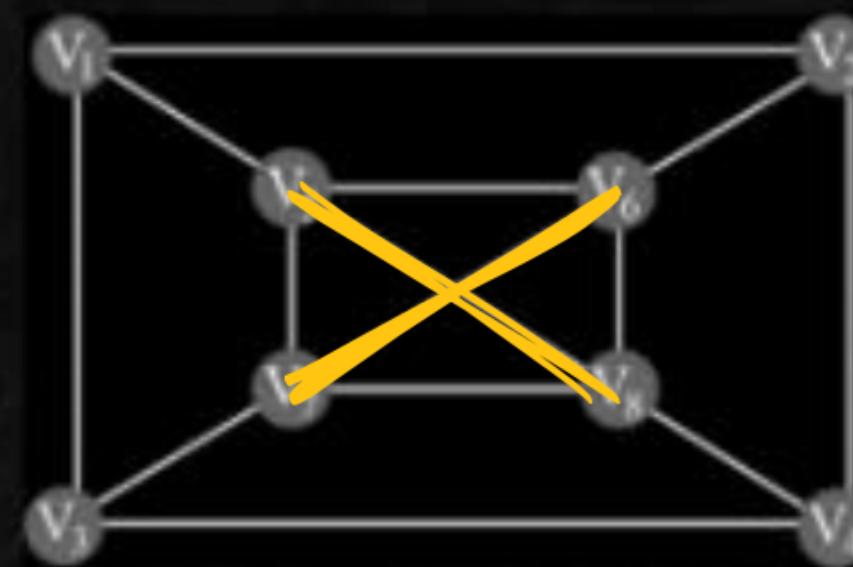
$$\frac{n^2 - n - 4n + 4}{2}$$

$$n = \frac{n(n-1)}{2} - 2(n-1) = \frac{n^2 - 5n + 4}{2}$$

$$= \frac{n^2 - n}{2} - \frac{\partial(n-1)}{2}$$

[NAT]

4. Consider the given graph $G(V,E)$ with order is 8 $\{V_1, V_2, V_3, \dots, V_8\}$. Find the minimum number of edges to be deleted from the graph, such that the graph become bipartite graph $\underline{\text{?}}$



[MSQ]

5. Which of the following options is/are correct?

- (a) Every NULL graph is always bipartite graph. (F) (b,c)
- (b) Some cycle graph is complete graph. (T)
- (c) A cyclic graph is different from cycle graph. (T)
- (d) A graph G is bipartite graph if and only if it has even cycle. (F)

[MSQ]

6. Consider a regular graph with order 6 and size 12. Which of the following is the minimum degree(δ) and maximum degree (Δ)?

- (a) $\delta = 3, \Delta = 4$
- (b) $\delta = 4, \Delta = 3$
- (c) $\delta = 4, \Delta = 4$
- (d) None of these

$$n = 6 \quad e = 12$$

$$\delta(G) \leq \frac{2e}{n} \leq \Delta(G)$$

$$\leq \frac{2 \times 12}{6}$$

$$\delta(G) \leq 4 \leq \Delta(G)$$



THANK YOU GW
SOLDIERS !