

CS & IT ENGINEERING

Mathematical Logic

DPP 04
Discussion Notes



[MCQ]

1. Let $R(x, y, z)$ denote the statement
$$"x + y = z"$$

Which of the following proposition will evaluate truth value True?

- (a) $R(1, 2, 3)$ ✓ (b) $R(0, 0, 1)$ (F)
- ✓ (c) $R(1, 1, 2)$ (T) (d) $R(2, 3, 4)$ (F)

$$\begin{array}{c} R(\overset{x}{1} \overset{y}{2} \overset{z}{3}) \\ R(1 \ 2 \ 3) \end{array}$$

[MCQ]

2. Let $p(x)$, $q(x)$ denote the following open statements.

$$p(x): x \leq 3 \quad q(x): x + 1 \text{ is odd}$$

D: 2

If the universe consists of all integers, what are the truth values of the following

statements?

$$S_1: \sim(p(-4) \vee q(-3)) \quad \text{F}$$

$$S_2: \sim(p(-4) \wedge \sim q(-3))$$

(a) S_1 : True, S_2 : False

(b) S_1 : False, S_2 : True

(c) S_1 : True, S_2 : True

(d) S_1 : False, S_2 : False

$$p(n): q(n): n+1 \text{ is odd}$$

$$n \leq 3$$

$$\underline{p(-4)}$$

$$-4 \leq 3 \quad (\text{T})$$

$$q(-3) \rightarrow \text{F}$$

$$\underline{q'}$$

$$-3+1 \text{ is odd}$$

$$-2 \text{ is odd (F)}$$

[NAT]

P
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3. Let $p(x)$, $q(x)$ denote the following open statements.

$$p(x): x + 1 > x \quad q(x): x^2 > 0$$

3

How many expressions evaluate to True?

I. $p(3) \vee [q(3) \vee \neg p(3)]$ $\top \vee (\top \vee \perp) \equiv \top$

II. $p(2) \rightarrow [q(2) \rightarrow p(2)]$ $\top \rightarrow (\top \rightarrow \top) \equiv \top$

III. $[p(2) \rightarrow q(2)] \wedge p(-3)]$ $(\top \rightarrow \top) \wedge \perp \equiv \perp$

[MCQ]

4. Consider the English sentence

"You can not ride the roller coaster if you are under 4 feet tall unless you are older than 16 years old".

if R

$\neg q$ if R unless s

$(\neg q \text{ if } R) \text{ unless } s$

$\neg s \rightarrow (R \rightarrow \neg q)$

Which of the following correctly represent the logical expression for the sentence?

$s \vee (\neg R \vee \neg q)$

(a) $q \rightarrow \neg(r \wedge \neg s) \equiv \neg q \vee \neg R \vee s$

(b) $(r \vee \neg s) \rightarrow q \times$

(c) $(r \wedge \neg s) \rightarrow \neg q$

(d) None of these

PW

$P \rightarrow q$

$q \text{ unless } \neg P$

$P \rightarrow q$

[MCQ]

5. Let $p(x)$ be the statement
$$x + 1 > x$$

Now, consider the truth value of quantification, where the domain consists of all real numbers.

$$L_1 = \forall x \ p(x) \quad \checkmark$$

$$L_2 = \exists x \ p(x) \quad \checkmark$$

Which of the following is True?

- (a) L_1 only
- (b) L_2 only
- (c) Both L_1 and L_2 are True \checkmark
- (d) Neither L_1 nor L_2

