

CS & IT ENGINEERING

Graph Theory

DPP 05

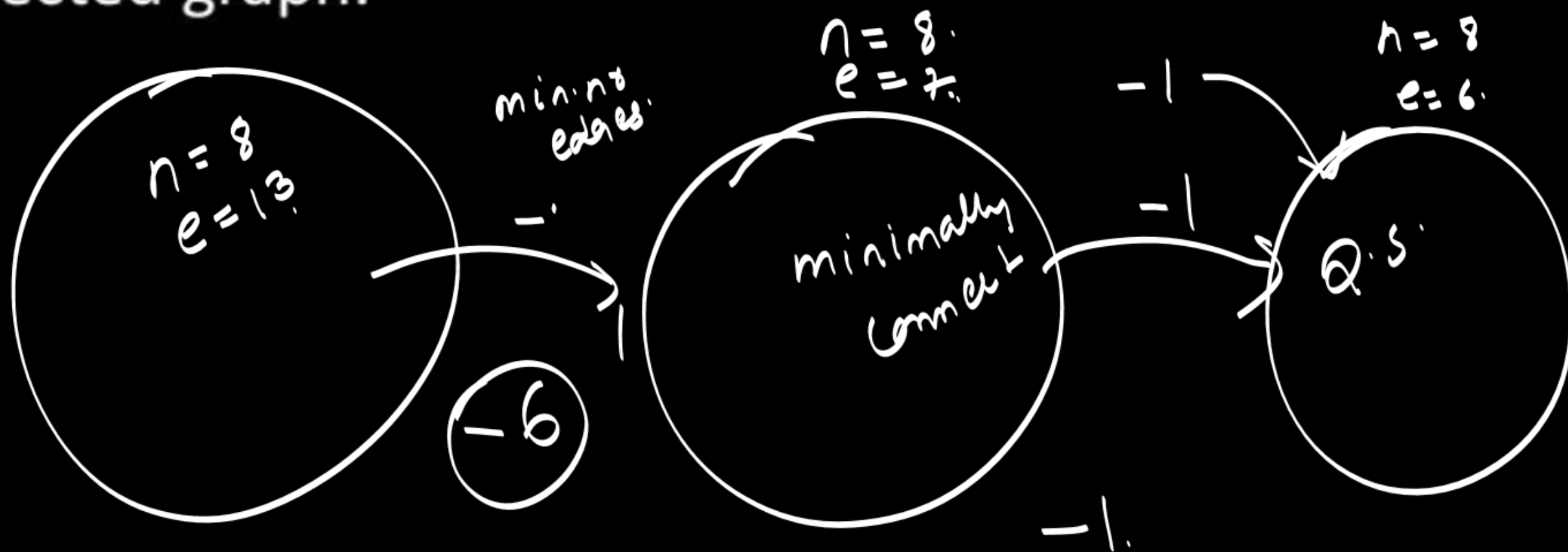
Discussion Notes

$$13 - 7 = 6.$$

7.



Consider an undirected graph G , which is connected and have 8 vertices and 13 edges. Find the minimum number edges, whose deletion from graph G is always guarantee that it would be disconnected graph.



Q. 2

MCQ



$$e = 162 \quad \underline{K_{m,n}} \quad e(K_{m,n}) = m \times n$$

The order (Number of vertices) of a complete bipartite graph in which there are 162 edges and one of the partitions has twice the number of vertices as of other _____?

- (a) 20
- (b) 25
- (c) 27 ✓
- (d) 29

$$\begin{aligned}
 &K_{x,y} \quad x = 2y \\
 &e(K_{2y,y}) = 2y \times y \\
 &K_{18,9} : 18 + 9 = 27
 \end{aligned}$$

$$2y \times y = 162$$

$$2y^2 = 162$$

$$y^2 = 81$$

$$y = 9$$

Q. 3

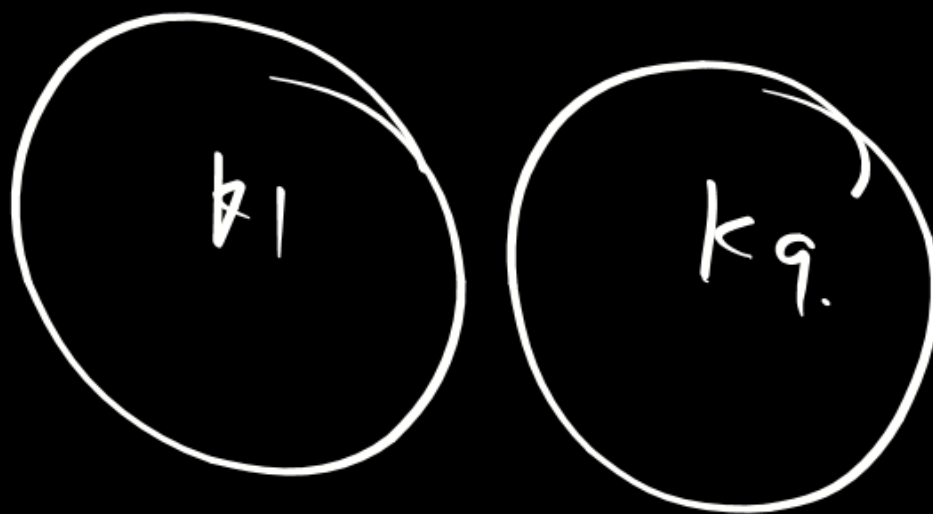
NAT



Consider a simple graph of 10 vertices. If the graph is disconnected, then the maximum number of edges, it can have is ~~36~~ ?

Dis + maximum no of edges \rightarrow 2 components.

$$e = \frac{9 \times 8}{2} = \underline{\underline{36}}$$

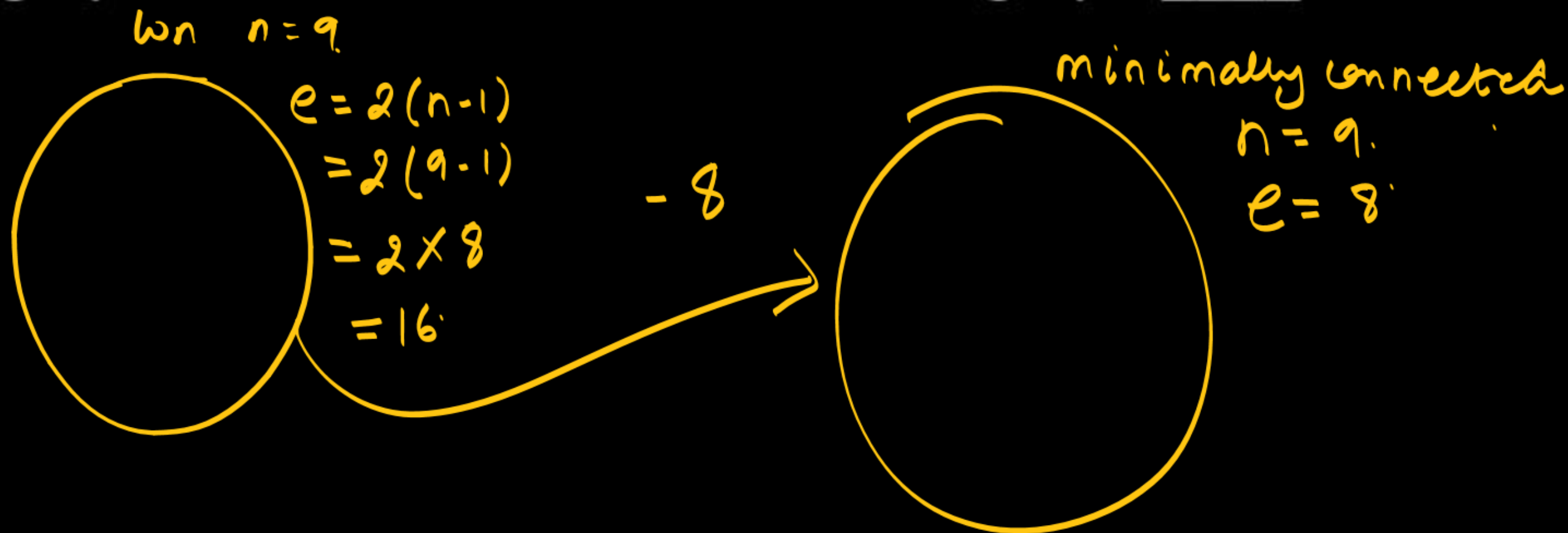


Q. 4

MSQ



Consider a wheel graph (w_n) of 9 vertices. Find the number of edges to be deleted from the above graph, such that the resultant graph must be minimal connected graph 8?



Q. 5

MCQ



If G is a simple disconnected graph with 16 vertices and 3 components, then maximum number of edges possible in G is _____?

(a) 90

☒ (b) 91

(c) 92

(d) 93

$$13 \times 7$$

$$(13 + 3) \times 7$$

$$= 70 + 21 = 91$$

$$n = 16 \quad k = 3$$

$$e = \frac{(n-k)(n-k+1)}{2}$$

$$= \frac{(16-3)(16-3+1)}{2}$$

$$= \frac{13 \cdot 14}{2}$$

What is the maximum number of edges present in a disconnected graph $n > 2$ vertices?

- (a) $nC_2 - 1$
- (b) $n - 2$
- (c) $(n - 1)C_2$
- (d) $(n - 2)C_2$

Q. 7

MCQ



Which of the following statements is/are true?

S1: A graph $G(V, E)$ is called tree if there is an exactly one path between every 2 vertices. *unique*

S2: A graph $G(V, E)$ is tree iff it is connected, and it does not contain cycle. *Connected + does not contains cycle.*

- (a) S1 only
- (b) S2 only
- (c) Both S1 and S2 ✓
- (d) None of these.

