

Large problems may involve 10^6 cameras
 → Formulation
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broken down to a
 relation of linear system \Rightarrow thousands of param SE(3) problem \equiv $\begin{pmatrix} 6 \text{ thousands of variables} \\ \vdots \\ 6000 \times 6000 \text{ matrices} \end{pmatrix}$

But

If matrix, in each case of problems, # non-zero blocks $\ll \ll \ll$ # matrix blocks
 (given judiciously)

if all measurement, only add 1/lines about to matrix

e.g. FOV 180° would only observe the things in the room
 new things depend on the motion

\hookrightarrow is upper bound \Rightarrow # factors / observations that correspond
 to new poses is at most M

Locality \rightarrow measurements only depend on
 relatively small set of variables
 in our state

\Downarrow
 $M \times N$ new non-0 blocks
 inserted in the matrix

Factor Graph is a method to formulate / describe problem

$\mathcal{C}^{[k]}$ \rightarrow what we want to minimize
 $\mathcal{X}^{[k]} =$ subset of variables affecting $\mathcal{C}^{[k]}$

e.g.

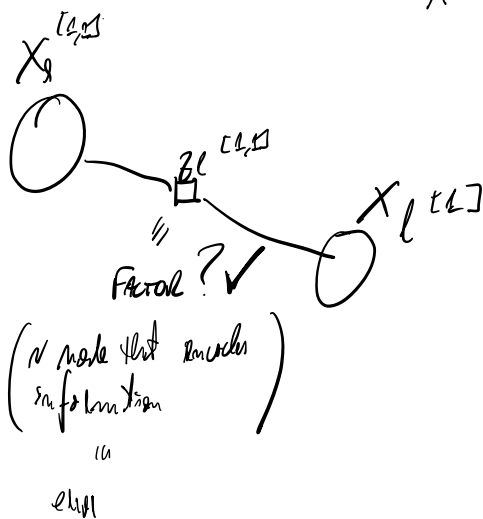
$$\begin{matrix} x^p \\ x^l \end{matrix} \rightarrow z^{[4,1]}$$

→ linear function
only dependent on both x^p and x^l

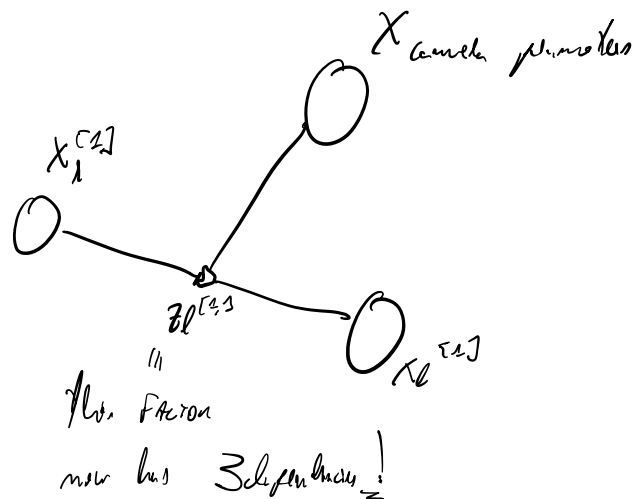
another example

odometry

$$\begin{matrix} x^+ \\ x^{++} \end{matrix} \rightarrow \text{odometry measurement}$$



OR



$$g^2 = \frac{1}{g} \text{ is the dimension of } g$$

Cholesky decomposition gives numerically stable solution if H is symmetric

$$Ly = -b \rightarrow \text{solve triangular system}$$

(much easier!!!)

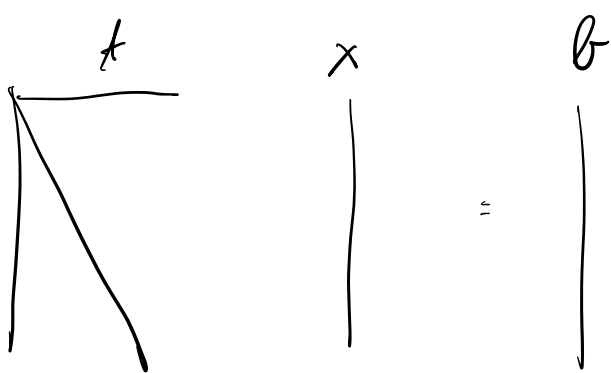
2 steps

⇓

$$L^T \Delta x = y$$

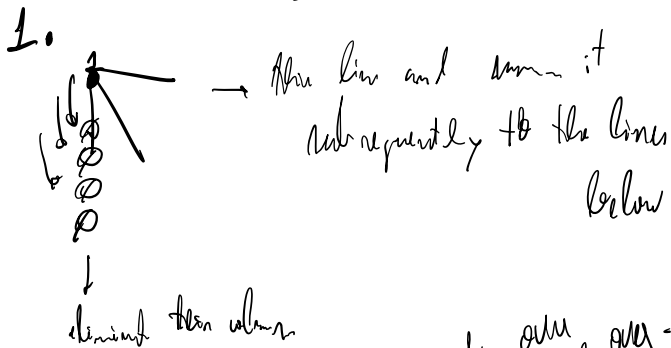
↪
Bar

H spec does not mean L spec!



L span depend on non-0 elements in H \odot
 strongly influenced by order!

To solve, triangulate



and over and over...
 by doing triangulation \Rightarrow we end up with a dirty dense system

what if we swap the first and last column?

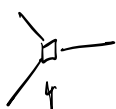
Special case of orthogonal matrix $(A^T = A^{-1})$
 we may end up with a sparse matrix (just by swapping rows and columns)

permutation matrix multiplies by left and right only (just shuffles the values) to swap variables

→ correct ordering of the matrix coefficients (we need to know the ordering)

4. Covariance Example (part II)

in general



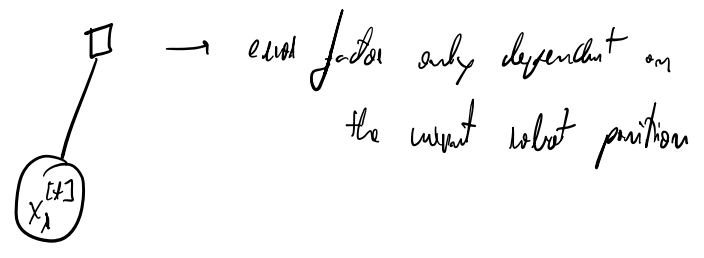
measurement may connect several variables

all models of the ~~type~~ that predict that measurement

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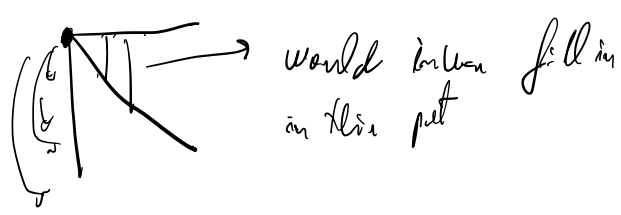
what if we had GPS?

sensor that depends on current robot position (with this, great...)



E.g.

1. choose how w/ least elements / corner degree / blocks non-zero
2. sketching this would result in filling in all the elements below and above that row...



→ Total Least Squares (some methodology while also taking into account prior structure)

Pose-Pose (3D)

Pose-Landmark (3D)

→ State: collection of SE(3) objects (robot, pos.)

⊗ collection of SE(3) points (landmarks)

↓ Pose-Landmark (Projection: 2D)

given that we are moving and rotating things, position ROBOT → world

is more intuitive?

K camera matrix

\mathcal{H} = homogeneous division of ICD projection

Pose-Landmark (3D)

Pose-Landmark (3D)

⋮ Pose-Pose

⋮ only robot position

⋮ Pose-Landmark

$$Z_l = \text{rma}(3, \emptyset)$$

$$Z_g = \text{bvar}(3, \emptyset)$$

⋮

→ comment to not
 suppress the
 perfect measurements!