

# Assignment - 7

## **Aim**

8-Queens Matrix is Stored using JSON/XML having first Queen placed, use back-tracking to place remaining Queens to generate final 8-queen's Matrix using Python. Create a backtracking scenario and use HPC architecture (Preferably BBB) for computation of next placement of a queen.

## **Learning Objective**

To understand:

- Basics of the Backtracking Strategy for problem solving.
- HPC(High Performance Computing) Architecture.
- Working and implementation of N-Queens problem

## **Learning Outcome**

We will be able to

- Understand the internals of the HPC Architecture by designing the 8-Queens problem using backtracking strategy.

## **Software And Hardware Requirements**

- Latest 64-BIT Version of Linux Operating System.
- Python Interpreter

# Mathematical Model

Let  $y=f(x)$  be the solution to the above problem.

Let  $S$  be a system such that  $S=\{s,e,X,Y,DD,NDD,se,fe,f1,P,sharedMem \mid \emptyset\}$

$s$ : Start state of system i.e  $Y = \emptyset$

$e$ : End state of system when i.e. when  $Y=X$

$X$ : Set of inputs  $X=\{x_1\}$  where  $x_1 \in \mathbb{N}$  where  $\mathbb{N}$  is a even Number  $\geq 4$

$Y$ : Set of Outputs i.e  $\{Y_1..Y_n\}$  i.e i.e The N-Queens Matrix where  $Y_i=\{y_1..y_n\}$

$f1$ : Function to Accept Input of  $N$  from user

$f2$ : Function to Place Queen

$f3$ : Function to display result of multiplication

$f3: X \rightarrow Y$   $se$ : Success state is when we get correct placement of queens without conflicts

$fe$ : Failure State is when we do not get correct placement of queens i.e with conflicts

## Deterministic Data

Value of  $N$

## Non Deterministic Data

Placement of Queens

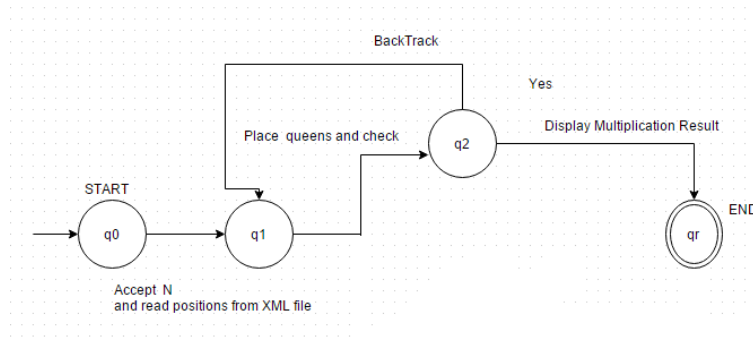
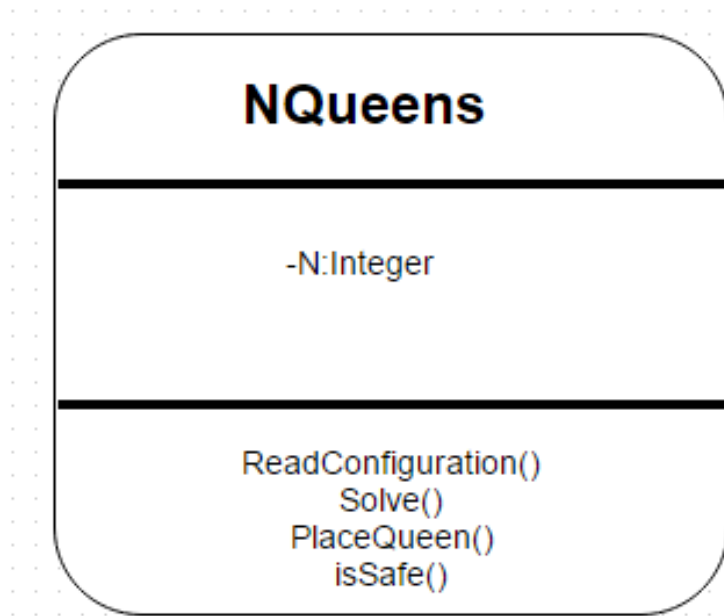


Figure 1: State Disagram

## UML-CLASS DIAGRAM



## Theory

### N-Queens Problem

The eight queens problem is the problem of placing eight queens on an 8x8 chessboard such that none of them attack one another (no two are in the same row, column, or diagonal). More generally, the n queens problem places n queens on an nxn chessboard.

### Pseudocode

```
SolveQueens (Integer boardSize, Queue queen[boardSize]); // i ← 0
//Begin by placing the queen number 0
while i ≤ boardSize
    queen[i].row ← queen[i].row + 1
```

```

//Place queen[i] to next row /* If queen[i] exceeds the row count, reset the
queen and re-place queen[i-1]

    if(queen[i].row  $\geq$  boardSize)
queen[i]  $\leftarrow$  -1;
i  $\leftarrow$  i - 1;
else
//While the queen[i] is under attack move it down the row
while(isUnderAttack(queen[i])
queen[i].row  $\leftarrow$  queen[i] + 1;
//if queen[i] exceeds the row count, reset it, re-place queen[i-1]
if(queen[i].row  $\geq$  boardSize)
queen[i].row  $\leftarrow$  -1
i  $\leftarrow$  i - 1;
else
i++;
end while

```

## Backtracking Algorithmic Strategy

Backtracking is a general algorithm for finding all (or some) solutions to some computational problems, notably constraint satisfaction problems, that incrementally builds candidates to the solutions, and abandons each partial candidate  $c$  ("backtracks") as soon as it determines that  $c$  cannot possibly be completed to a valid solution.

The classic textbook example of the use of backtracking is the eight queens puzzle, that asks for all arrangements of eight chess queens on a standard chessboard so that no queen attacks any other. In the common backtracking approach, the partial candidates are arrangements of  $k$  queens in the first  $k$  rows of the board, all in different rows and columns. Any partial solution that contains two mutually attacking queens can be abandoned.

Backtracking can be applied only for problems which admit the concept of a "partial candidate solution" and a relatively quick test of whether it can possibly be completed to a valid solution. It is useless, for example, for locating a given value in an unordered table. When it is applicable, however, backtracking is often much faster than brute force enumeration of all complete candidates, since it can eliminate a large number of candidates with a

single test.

Backtracking is an important tool for solving constraint satisfaction problems, such as crosswords, verbal arithmetic, Sudoku, and many other puzzles. It is often the most convenient (if not the most efficient technique for parsing, for the knapsack problem and other combinatorial optimization problems.

## PsuedoCode

```
procedure bt(c)
if reject(P,c) then return
if accept(P,c) then output(P,c)
s ? first(P,c)
while s ≠ ? do
bt(s)
s ? next(P,s)
```

## Program Code and Output

### queensserver.py

```
import socket , pickle

import sys
import numpy as num_p
from xml.dom import minidom
xmlfilename = minidom.parse( 'data.xml' )
itemlist = xmlfilename.getElementsByTagName( 'Item' )

s = socket.socket()           # Create a socket object
host = socket.gethostname()   # Get local machine name
port = 12348                  # Reserve a port for your
    service.
s.bind((host , port))         # Bind to the port
```

```

s.listen(3)                                # Now wait for client
connection.

while True:
    c, addr = s.accept()                    # Establish connection
                                           with client.
    print 'Got connection from', addr

    c.send(pickle.dumps(itemlist))

    op = c.recv(10000)
    print "Soln is "
    print op

    c.close()
'''
[bbuhariwala@localhost B1]$ python queens_server.py
Got connection from ('127.0.0.1', 34474)
Soln is
Q*****Q*****Q*****Q*****Q*****Q**Q
*****Q*****
^CTraceback (most recent call last):
  File "queens_server.py", line 22, in <module>
    c, addr = s.accept()                    # Establish connection
                                           with client.
  File "/usr/lib64/python2.7/socket.py", line 202, in
    accept
    sock, addr = self._sock.accept()
KeyboardInterrupt
[bbuhariwala@localhost B1]$
'''

```

## queensclient.py

```
import socket , pickle , sys

import numpy as num_p

sys.setrecursionlimit(1000000000)

placed_first=0
class nQueens:

    def __init__(self , dimension_of_board):
        self.dimension = dimension_of_board
        self.columns = [] * self.dimension
        self.num_of_places = 0
        self.num_of_backtracks = 0

    def placeFirst(self):
        self.columns.append(placed_first)

    def place(self , row_start=0):
        if len(self.columns) == self.dimension:
            print('Solution found! The board dimension
                was: ' + str(self.dimension))
            print(str(self.num_of_places) + ' total
                places were made. ')
            print(str(self.num_of_backtracks) + ' total
                backtracks were executed. ')
            print(self.columns)
            board = [[0 for x in range(8)] for x in
                range(8)]
            board[0][self.columns[0]]=1;
            board[1][self.columns[1]]=1;
            board[2][self.columns[2]]=1;
            board[3][self.columns[3]]=1;
            board[4][self.columns[4]]=1;
            board[4][self.columns[5]]=1;
            board[6][self.columns[6]]=1;
```

```

board[7][self.columns[7]]=1;
print board
for i in range(8):
    for j in range(8):
        print str(board[i][j])+” ”,
        print ”\n”
return board
else:
    for row in range(row_start , self.dimension)
        :

        if self.isSafe(len(self.columns), row)
            is True:
                self.columns.append(row)
                self.num_of_places += 1
                return self.place()
        else:
            row_last = self.columns.pop()
            self.num_of_backtracks += 1
            return self.place(row_start=row_last +
                               1)

def isSafe(self, col, row):
    for row_threat in self.columns:
        col_threat = self.columns.index(row_threat)
        if row == row_threat or col == self.columns
            .index(row_threat):
            return False
        elif row_threat + col_threat == row + col
            or row_threat - col_threat == row - col:
            return False
    return True

```

n = 8

```

HOST = socket.gethostname()
HOST = 'localhost'
PORT = 12348

```



```

socket = socket.socket(socket.AF_INET, socket.
    SOCK_STREAM)
socket.connect((HOST, PORT))
data = socket.recv(10000)

itemlist = pickle.loads(data)
print itemlist
dataList = []
for s in itemlist:
    dataList.append(s.getAttribute("index").encode("utf
        -8"))
print dataList

for s in dataList:

    if (s != ' '):
        placed_first=int(s)
        break

print "First queen placed in first row at: ",
    placed_first
queens = nQueens(8)
queens.placeFirst()
queens.place(0)

#convert board to numpy array for pretty printing
board = num_p.array([[ '*' ] * n] * n)
for queen in queens.columns:
    board[queens.columns.index(queen), queen] = 'Q'
socket.send(board)

'''
[root@localhost B1]# python queens_client.py
[<DOM Element: Item at 0x1e12200>, <DOM Element: Item
    at 0x1e55710>, <DOM Element: Item at 0x1e557a0>, <
    DOM Element: Item at 0x1e55830>, <DOM Element: Item

```



## **Result**

Thus,we have designed and implemented Nqueens problem using Backtracking Strategy in python language and tested the same.