

* Manual Calculations for Two Iterations

$$f(x) = x^4 + 3x^2 + 10$$

$$\eta = 0.001$$

Let, initial value of x be 2 ($x=2$).

$$\frac{\partial f(x)}{\partial x} = 4x^3 + 6x$$

Iteration -1:

$$\text{Gradient at } x=2. \left. \frac{\partial f(x)}{\partial x} \right|_{x=2} = 4(2)^3 + 6(2) = 44.$$

$$\text{Step length } \Delta x = -0.001 \times 44 = -0.044$$

update x :

$$x = 2 - 0.044 = 1.956$$

Iteration -2:

$$\text{Gradient at } x=1.956 \left. \frac{\partial f(x)}{\partial x} \right|_{x=1.956} = 4(1.956)^3 + 6(1.956) = 41.670.$$

$$\text{Step length } \Delta x = -0.001 \times 41.670 = -0.0416.$$

update x :

$$x = 1.956 - 0.0416 = 1.9144$$

⋮