

# Assignment 1

Sowmya Bandi

Download all python codes from

<https://github.com/sachinomdubey/Matrix-theory/codes>

and latex-tikz codes from

<https://github.com/sachinomdubey/Matrix-theory>

From 2.0.3,

$$c - b = 3.5 \quad (2.0.11)$$

$$\implies c - 33.45 = 3.5 \quad (2.0.12)$$

$$c = 36.95 \quad (2.0.13)$$

Then,

$$AB = \|\mathbf{A} - \mathbf{B}\| = \|\mathbf{A}\|^2 = c^2 \quad (2.0.14)$$

$$BC = \|\mathbf{C} - \mathbf{B}\|^2 = \|\mathbf{C}\|^2 = a^2 \quad (2.0.15)$$

$$AC = \|\mathbf{A} - \mathbf{C}\|^2 = b^2 \quad (2.0.16)$$

From 2.0.16,

$$\implies b^2 = \|\mathbf{A} - \mathbf{C}\|^2 = (\mathbf{A} - \mathbf{C})^T (\mathbf{A} - \mathbf{C}) \quad (2.0.17)$$

$$b^2 = \mathbf{A}^T \mathbf{A} + \mathbf{C}^T \mathbf{C} - \mathbf{A}^T \mathbf{C} - \mathbf{A} \mathbf{C}^T \quad (2.0.18)$$

$$b^2 = \|\mathbf{A}\|^2 + \|\mathbf{C}\|^2 - 2\mathbf{C}^T \mathbf{A} \quad (2.0.19)$$

$$b^2 = a^2 + c^2 - \quad (2.0.20)$$

yielding,

$$p = \frac{a^2 + c^2 - b^2}{2c} \quad (2.0.21)$$

$$p = \frac{(8)^2 + (36.95)^2 - (33.45)^2}{2(36.95)} \quad (2.0.22)$$

$$p = \frac{310.9}{73.9} \quad (2.0.23)$$

$$p = 4.2 \quad (2.0.24)$$

Given,

$$BC = 8, \angle B = 45^\circ \text{ and } AB - AC = 3.5 \quad (2.0.1)$$

let the vertices of  $\triangle ABC$  and D be

$$\mathbf{A} = \begin{pmatrix} p \\ q \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} a \\ 0 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} p \\ 0 \end{pmatrix} \quad (2.0.2)$$

we have,

$$c - b = 3.5 \quad (2.0.3)$$

$$\implies c = 3.5 + b \quad (2.0.4)$$

From  $\triangle ABC$ , we use the law of cosines:

$$b^2 = a^2 + c^2 - 2ac \cos B \quad (2.0.5)$$

$$b^2 = (8)^2 + (3.5 + b)^2 - 2(8)(3.5 + b) \cos 45 \quad (2.0.6)$$

$$b^2 = 64 + 12.25 + 7b + b^2 - 29.4168 - 8.4b \quad (2.0.7)$$

$$\implies 0 = 46.83 - 1.4b \quad (2.0.8)$$

$$\implies b = \frac{46.83}{1.4} \quad (2.0.9)$$

$$\implies b = 33.45 \quad (2.0.10)$$

From 2.0.14,

$$\|\mathbf{A}\|^2 = c^2 = p^2 + (2q)^2 \quad (2.0.25)$$

$$q^2 = \frac{c^2 - p^2}{4} \quad (2.0.26)$$

$$q^2 = \frac{(36.95)^2 - (4.2)^2}{4} \quad (2.0.27)$$

$$q^2 = 336.91 \quad (2.0.28)$$

$$q = \pm 18.35 \quad (2.0.29)$$

As we consider  $\triangle ABC$  in first quadrant. we consider

$q = 18.35$

Therefore,  $q = 18.35$

so, the vertices of  $\triangle ABC$  and  $D$  are

$$\mathbf{A} = \begin{pmatrix} 4.2 \\ 18.35 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 8 \\ 0 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} 4.2 \\ 0 \end{pmatrix}$$

(2.0.30)

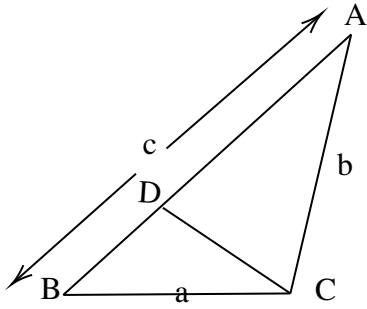


Fig. 2.1:  $\triangle ABC$