ASSIGNMENT 3

CS5691 Pattern Recognition and Machine Learning

CS5691 Assignment 3 Code

Team Members:

BE17B007	N Sowmya Manojna
PH17B010	Thakkar Riya Anandbhai
PH17B011	Chaithanya Krishna Moorthy

Indian Institute of Technology, Madras



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1 Dataset 1A

1.1 Perceptron

1.2 MLFFNN

The code written for analyzing Dataset 1A, using an MLFFNN model is as follows:

```
1 #!/usr/bin/env python
2 # coding: utf-8
4 # # Assignment 3 - 1A (MLFFNN)
5 #
6 # Team members:
7 # - N Sowmya Manojna (BE17B007)
8 # - Thakkar Riya Anandbhai (PH17B010)
  # - Chaithanya Krishna Moorthy (PH17B011)
10
11 # ## Importing Essential Libraries
12
13 # In[1]:
14
15
16 import numpy as np
17 import pandas as pd
18 import seaborn as sns
19 from sklearn.pipeline import Pipeline
20 from sklearn.metrics import confusion_matrix
21 from sklearn.neural_network import MLPClassifier
22 from sklearn.preprocessing import StandardScaler
23 from sklearn.model_selection import GridSearchCV
24 from sklearn.model_selection import train_test_split
25 from sklearn.model_selection import StratifiedShuffleSplit
27 import matplotlib.pyplot as plt
28 plt.rcParams["font.size"] = 18
29 plt.rcParams["axes.grid"] = True
30 plt.rcParams["figure.figsize"] = 12,8
31 plt.rcParams['font.serif'] = "Cambria"
32 plt.rcParams['font.family'] = "serif"
34 get_ipython().run_line_magic('load_ext', 'autoreload')
35 get_ipython().run_line_magic('autoreload', '2')
37 import warnings
38 warnings.filterwarnings("ignore")
40 from gridsearch import GridSearch1A
41
42
43 # ## Reading the data, Splitting it
45 # In[2]:
46
47
48 # Get the data
49 column_names = ["x1", "x2", "y"]
50 df = pd.read_csv("../datasets/1A/train.csv", names=column_names)
51 df_test = pd.read_csv("../datasets/1A/dev.csv", names=column_names)
52 display(df.head())
54 # Split dev into test and validation
55 df_val, df_test = train_test_split(df_test, test_size=0.3, random_state=42)
56 display(df_val.head())
57 display(df_test.head())
```

```
58
   # In[3]:
60
63 X_train = df.drop("y", axis=1).to_numpy()
   y_train = df["y"].to_numpy().astype("int")
64
66 X_val = df_val.drop("y", axis=1).to_numpy()
67 y_val = df_val["y"].to_numpy().astype("int")
69 X_test = df_test.drop("y", axis=1).to_numpy()
70 y_test = df_test["y"].to_numpy().astype("int")
73 # ## Training the Model
74
75 # In [4]:
76
77
78 parameters = {"hidden_layer_sizes":[5,8,10,15], "activation":["logistic", "tanh", "...
                              "solver":["lbfgs", "sgd", "adam"], "batch_size":[100, ...
       relu"].
       200],
                            "alpha":[0, 0.0001], "learning_rate":["constant", "adaptive"...
       , "invscaling"],
80 mlp = MLPClassifier(random_state=1)
82 clf = GridSearch1A(mlp, parameters)
83 clf.fit(X_train, y_train, X_val, y_val)
84 result_df = pd.DataFrame(clf.cv_results_)
85 result_df.to_csv("../parameter_search/1A_MLFFNN_train_val.csv")
86 result_df.head()
89 # In[5]:
92 print("Best Parameters Choosen:")
93 for i in clf.best_params_:
                - ", i, ": ", clf.best_params_[i], sep="")
94
       print("
95
  best_mlp = MLPClassifier(random_state=1, **clf.best_params_)
96
   best_mlp.fit(X_train, y_train)
97
98
99
100 # ## Best Model Predictions
102 # In[6]:
103
104
105  y_pred = best_mlp.predict(X_train)
106 print("Accuracy:", 100*np.sum(y_pred==y_train)/y_train.size)
107 conf_mat = confusion_matrix(y_train, y_pred)
108 plt.figure()
sns.heatmap(conf_mat, annot=True)
110 plt.title("1A - Train Confusion Matrix (MLFFNN)")
plt.xlabel("Predicted Class")
plt.ylabel("Actual Class")
113 plt.savefig("images/1A_MLFFNN_train_confmat.png")
114 plt.show()
115
116  y_val_pred = best_mlp.predict(X_val)
print("Validation Accuracy:", 100*np.sum(y_val_pred==y_val)/y_val.size)
val_conf_mat = confusion_matrix(y_val, y_val_pred)
119 plt.figure()
120 sns.heatmap(val_conf_mat, annot=True)
121 plt.title("1A - Validation Confusion Matrix (MLFFNN)")
122 plt.xlabel("Predicted Class")
123 plt.ylabel("Actual Class")
```

```
124 plt.savefig("images/1A MLFFNN val confmat.png")
125 plt.show()
127 y_test_pred = best_mlp.predict(X_test)
   print("Validation Accuracy:", 100*np.sum(y_test_pred==y_test)/y_test.size)
129 test_conf_mat = confusion_matrix(y_test, y_test_pred)
130 plt.figure()
sns.heatmap(test_conf_mat, annot=True)
132 plt.title("1A - Test Confusion Matrix (MLFFNN)")
133 plt.xlabel("Predicted Class")
134 plt.ylabel("Actual Class")
135 plt.savefig("images/1A_MLFFNN_test_confmat.png")
136 plt.show()
138
139 # ## Visualising the decision boundaries
140
141 # In[7]:
142
143
144 h = 0.02
145 x_min, x_max = X_train[:,0].min() - .5, X_train[:,0].max() + .5
146 y_min, y_max = X_train[:,1].min() - .5, X_train[:,1].max() + .5
148 xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))
149 Z_pro = np.argmax(best_mlp.predict_proba(np.c_[xx.ravel(), yy.ravel()]), axis=1)
150 Z_pro = Z_pro.reshape(xx.shape)
151
152 color_list = ["springgreen", "gold", "palevioletred", "royalblue"]
153 plt.title("1A - Decision Region Plot (MLFFNN)")
154 plt.contourf(xx, yy, Z_pro, np.unique(Z_pro).size-1, colors=color_list, alpha=0.1)
155 plt.contour(xx, yy, Z_pro, np.unique(Z_pro).size-1, colors=color_list, alpha=1)
156 plt.scatter(X_train[:,0], X_train[:,1], c=[color_list[i] for i in y_train])
157 plt.xlabel("X1")
158 plt.ylabel("X2")
159 plt.savefig("images/1A_MLFFNN_Decision_Plot.png")
160 plt.show()
161
162
163 # In[]:
```

The helper functions used are as follows:

```
1 import numpy as np
2 import pandas as pd
3 from time import time
4 from tqdm import tqdm
  from collections import defaultdict
6 from sklearn.neural_network import MLPClassifier
  class GridSearch1A():
8
       def __init__(self, model, parameters, verbose=0):
9
           self.model = model
10
           self.parameters = parameters
11
           self.verbose = verbose
12
           params_list = []
13
           self.params_keys = self.parameters.keys()
           for hls in parameters["hidden_layer_sizes"]:
               for act in parameters["activation"]:
17
                   for s in parameters["solver"]:
18
                        for bs in parameters["batch_size"]:
19
                            for a in parameters["alpha"]:
20
21
                                for lr in parameters["learning_rate"]:
                                    params_list.append({"hidden_layer_sizes":hls, \
22
                                                          "activation":act, \
23
                                                         "solver":s, \
24
                                                         "batch_size":bs, \
25
```

```
"alpha":a, \
26
27
                                                          "learning_rate":lr})
           self.params_list = params_list
28
       def fit(self, X_train, y_train, X_val, y_val):
30
31
           self.cv_results_ = pd.DataFrame(columns=self.params_keys)
32
           self.params_ = defaultdict(list)
33
           self.acc_list_ = []
34
           self.val_acc_list_ = []
35
           self.t_inv_list_ = []
36
38
           for params in tqdm(self.params_list):
               st = time()
               mlp = MLPClassifier(random_state=1, **params)
41
               mlp.fit(X_train, y_train)
42
               et = time()
43
44
               y_pred = mlp.predict(X_train)
45
               acc = 100*np.sum(y_pred==y_train)/y_train.size
46
47
48
               y_val_pred = mlp.predict(X_val)
49
               val_acc = 100*np.sum(y_val_pred==y_val)/y_val.size
50
               for i in params:
52
                    self.params_[i].append(params[i])
53
                self.acc_list_.append(acc)
54
                self.val_acc_list_.append(val_acc)
55
                self.t_inv_list_.append(1/(et-st))
56
57
           for i in params:
58
                self.cv_results_[i] = self.params_[i]
60
           self.cv_results_["accuracy"] = self.acc_list_
           self.cv_results_["val_accuracy"] = self.val_acc_list_
63
           self.cv_results_["sum_accuracy"] = self.cv_results_["accuracy"] + self....
               cv_results_["val_accuracy"]
           self.cv_results_["t_inv"] = self.t_inv_list_
64
           self.cv_results_ = self.cv_results_.sort_values(by=["accuracy", "...
65
               sum_accuracy", "t_inv"], ascending=False, ignore_index=True)
66
           self.best_params_ = self.cv_results_.iloc[0].to_dict()
67
           del self.best_params_["accuracy"]
68
           del self.best_params_["val_accuracy"]
           del self.best_params_["sum_accuracy"]
70
71
           del self.best_params_["t_inv"]
72
73
  class GridSearch1B():
74
       def __init__(self, model, parameters, verbose=0):
75
           self.model = model
76
77
           self.parameters = parameters
78
           self.verbose = verbose
           params_list = []
           self.params_keys = self.parameters.keys()
           for hls in parameters["hidden_layer_sizes"]:
82
               for act in parameters["activation"]:
83
                    for bs in parameters["batch_size"]:
84
                        for a in parameters["alpha"]:
85
86
                            for lr in parameters["learning_rate"]:
87
                                 for es in parameters["early_stopping"]:
                                     params_list.append({"hidden_layer_sizes":hls, \
88
                                                           "early_stopping":es, \setminus
89
                                                          "learning_rate":lr, \
90
                                                          "activation":act,
91
92
                                                          "batch_size":bs, \
```

```
"alpha":a})
93
            self.params_list = params_list
95
        def fit(self, X_train, y_train, X_val, y_val):
            self.cv_results_ = pd.DataFrame(columns=self.params_keys)
97
98
            self.params_ = defaultdict(list)
99
            self.acc_list_ = []
100
            self.val_acc_list_ = []
101
            self.t_inv_list_ = []
102
103
            for params in tqdm(self.params_list):
104
105
                st = time()
                mlp = MLPClassifier(random_state=1, **params)
106
107
108
                mlp.fit(X_train, y_train)
                et = time()
109
110
                y_pred = mlp.predict(X_train)
111
                acc = 100*np.sum(y_pred==y_train)/y_train.size
112
113
                y_val_pred = mlp.predict(X_val)
114
115
                val_acc = 100*np.sum(y_val_pred==y_val)/y_val.size
116
117
                for i in params:
118
                    self.params_[i].append(params[i])
119
                self.acc_list_.append(acc)
120
                self.val_acc_list_.append(val_acc)
121
                self.t_inv_list_.append(1/(et-st))
122
123
            for i in params:
124
                self.cv_results_[i] = self.params_[i]
125
126
            self.cv_results_["accuracy"] = self.acc_list_
            self.cv_results_["val_accuracy"] = self.val_acc_list_
128
129
            self.cv_results_["sum_accuracy"] = self.cv_results_["accuracy"] + self....
                cv_results_["val_accuracy"]
130
            self.cv_results_["t_inv"] = self.t_inv_list_
            self.cv_results_ = self.cv_results_.sort_values(by=["accuracy", "...
131
                sum_accuracy", "t_inv"], ascending=False, ignore_index=True)
132
            self.best_params_ = self.cv_results_.iloc[0].to_dict()
133
            self.best_params_["early_stopping"] = bool(self.best_params_["...
134
                early_stopping"])
            del self.best_params_["accuracy"]
            del self.best_params_["val_accuracy"]
136
            del self.best_params_["sum_accuracy"]
137
            del self.best_params_["t_inv"]
138
```

1.3 Linear SVM

2 Dataset 1B

2.1 MLFFNN

The code written for analyzing Dataset 1B, using an MLFFNN model is as follows:

```
1 #!/usr/bin/env python
2 # coding: utf-8
3
4 # # Assignment 3 - 1B (MLFFNN)
5 #
6 # Team members:
7 # - N Sowmya Manojna (BE17B007)
8 # - Thakkar Riya Anandbhai (PH17B010)
9 # - Chaithanya Krishna Moorthy (PH17B011)
```

```
10
11 # ## Import Essential Libraries
13 # In[1]:
14
15
16 import numpy as np
17 import pandas as pd
18 import seaborn as sns
19 from sklearn.pipeline import Pipeline
20 from sklearn.metrics import confusion_matrix
21 from sklearn.neural_network import MLPClassifier
22 from sklearn.preprocessing import StandardScaler
23 from sklearn.model_selection import GridSearchCV
24 from sklearn.model_selection import train_test_split
25 from sklearn.model_selection import StratifiedShuffleSplit
27 import matplotlib.pyplot as plt
28 plt.rcParams["font.size"] = 18
29 plt.rcParams["axes.grid"] = True
30 plt.rcParams['font.serif'] = "Cambria"
31 plt.rcParams['font.family'] = "serif"
33 get_ipython().run_line_magic('load_ext', 'autoreload')
  get_ipython().run_line_magic('autoreload', '2')
36 import warnings
37 warnings.filterwarnings("ignore")
39 from gridsearch import GridSearch1B
40
41
42 # ## Read the data, Split it
44 # In[2]:
45
47 # Get the data
48 column_names = ["x1", "x2", "y"]
49 df = pd.read_csv("../datasets/1B/train.csv", names=column_names)
50 df_test = pd.read_csv("../datasets/1B/dev.csv", names=column_names)
51 display(df.head())
53 # Split dev into test and validation
54 df_val, df_test = train_test_split(df_test, test_size=0.3, random_state=42)
55 display(df_val.head())
56 display(df_test.head())
57
58
59 # In[3]:
60
61
62 X_train = df[["x1", "x2"]].to_numpy()
63 y_train = df["y"].to_numpy().astype("int")
65 X_val = df_val[["x1", "x2"]].to_numpy()
66 y_val = df_val["y"].to_numpy().astype("int")
68  X_test = df_test[["x1", "x2"]].to_numpy()
69 y_test = df_test["y"].to_numpy().astype("int")
70
71
72 # ## Training the Model
73
  # In[4]:
74
75
  parameters = {"hidden_layer_sizes":[(5,5),(6,6),(7,7),(8,8),(9,9),(10,10)], ...
                    "activation":["logistic", "relu"],
                                                                       "batch_size":[50, ...
```

```
100, 200], "early_stopping":[True, False],
                                                                  "learning_rate":["...
       constant", "adaptive", "invscaling"],
                                                            "alpha": [0.01, 0.001]
78
79
  mlp = MLPClassifier(random_state=1)
82 clf = GridSearch1B(mlp, parameters)
83 clf.fit(X_train, y_train, X_val, y_val)
84 result_df = pd.DataFrame(clf.cv_results_)
85 result_df.to_csv("../parameter_search/1B_MLFFNN_train_val.csv")
86 result df.head(10)
88
89 # In[5]:
92 print("Best Parameters Choosen:")
93 for i in clf.best_params_:
       print(" - ", i, ": ", clf.best_params_[i], sep="")
94
95
96 best_mlp = MLPClassifier(random_state=1, **clf.best_params_)
97 best_mlp.fit(X_train, y_train)
98
100 # ## Best Model Predictions
102 # In[6]:
103
104
105  y_pred = best_mlp.predict(X_train)
print("Accuracy:", 100*np.sum(y_pred==y_train)/y_train.size)
107 conf_mat = confusion_matrix(y_train, y_pred)
108 plt.figure(figsize=(8,6))
109 sns.heatmap(conf_mat, annot=True)
110 plt.title("1B - Train Confusion Matrix (MLFFNN)")
plt.xlabel("Predicted Class")
plt.ylabel("Actual Class")
plt.savefig("images/1B_MLFFNN_train_confmat.png")
114 plt.show()
115
116  y_val_pred = best_mlp.predict(X_val)
117 print("Validation Accuracy:", 100*np.sum(y_val_pred==y_val)/y_val.size)
val_conf_mat = confusion_matrix(y_val, y_val_pred)
plt.figure(figsize=(8,6))
120 sns.heatmap(val_conf_mat, annot=True)
121 plt.title("1B - Validation Confusion Matrix (MLFFNN)")
122 plt.xlabel("Predicted Class")
123 plt.ylabel("Actual Class")
124 plt.savefig("images/1B_MLFFNN_val_confmat.png")
125 plt.show()
126
127  y_test_pred = best_mlp.predict(X_test)
128 print("Test Accuracy:", 100*np.sum(y_test_pred==y_test)/y_test.size)
129 test_conf_mat = confusion_matrix(y_test, y_test_pred)
130 plt.figure(figsize=(8,6))
sns.heatmap(test_conf_mat, annot=True)
132 plt.title("1B - Test Confusion Matrix (MLFFNN)")
133 plt.xlabel("Predicted Class")
134 plt.ylabel("Actual Class")
plt.savefig("images/1B_MLFFNN_test_confmat.png")
136 plt.show()
137
138
139 # ## Visualising the decision boundaries
140
141 # In[7]:
142
143
144 h = 0.02
```

```
145 x_min, x_max = X_train[:,0].min() - .5, X_train[:,0].max() + .5
146 y_min, y_max = X_train[:,1].min() - .5, X_train[:,1].max() + .5
148 xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))
149 Z_pro = np.argmax(best_mlp.predict_proba(np.c_[xx.ravel(), yy.ravel()]), axis=1)
150 Z_pro = Z_pro.reshape(xx.shape)
151
152 color_list = ["springgreen", "gold", "palevioletred", "royalblue"]
plt.figure(figsize=(12,8))
154 plt.title("1B - Decision Region Plot (MLFFNN)")
plt.contourf(xx, yy, Z_pro, np.unique(Z_pro).size-1, colors=color_list, alpha=0.1)
156 plt.contour(xx, yy, Z_pro, np.unique(Z_pro).size-1, colors=color_list, alpha=1)
157 plt.scatter(X_train[:,0], X_train[:,1], c=[color_list[i] for i in y_train])
158 plt.xlabel("X1")
plt.ylabel("X2")
160 plt.savefig("images/1B_MLFFNN_Decision_Plot.png")
161 plt.show()
162
163
   # ## Visualising Neuron Responses
164
165
   # In[8]:
166
167
168
   def get_values(weights, biases, X_train):
170
        ip = X_train.T
        h1 = weights[0].T @ ip + biases[0].reshape(-1,1)
171
172
        a1 = np.maximum(0, h1)
        h2 = weights[1].T @ a1 + biases[1].reshape(-1,1)
173
        a2 = np.maximum(0, h2)
174
        h3 = weights[2].T @ a2 + biases[2].reshape(-1,1)
175
        pred = np.exp(h3)/np.sum(np.exp(h3))
176
177
        return a1, a2, pred
178
179
180
181 # In [9]:
182
183
184 from matplotlib import cm
   from mpl_toolkits import mplot3d
185
   from mpl_toolkits.mplot3d import axes3d
186
   grid = np.c_[xx.ravel(), yy.ravel()]
187
188
   for epochs in [1, 5, 20, 100]:
189
        mlp = MLPClassifier(random_state=1, max_iter=epochs, **clf.best_params_)
190
        mlp.fit(X_train, y_train)
191
192
193
        weights = mlp.coefs_
        biases = mlp.intercepts_
194
195
196
        a1, a2, op = get_values(weights, biases, grid)
        a1 = a1.reshape(a1.shape[0], *xx.shape)
197
198
        a2 = a2.reshape(a2.shape[0], *xx.shape)
        op = op.reshape(op.shape[0], *xx.shape)
199
200
201
        for i in range(a1.shape[0]):
202
203
            fig = plt.figure(figsize=(8,8))
            ax = plt.axes(projection="3d")
204
205
            # ax.contour3D(xx, yy, a1[i,:], 500)
206
            ax.contourf(xx, yy, a1[i,:], 500, cmap=cm.CMRmap)
207
            ax.set_xlabel("X1")
208
209
            ax.set_ylabel("X2")
            ax.set_zlabel("HL1-Neuron "+str(i+1));
210
            ax.set_title("Epoch: "+ str(epochs) + "; Surface for Layer 1, Neuron "+str(...
211
                i+1))
            plt.tight_layout()
212
```

```
plt.savefig("images/1B_MLFFNN_E"+str(epochs)+"_HL1_N"+str(i+1)+".png")
213
214
            plt.show()
215
        for i in range(a2.shape[0]):
216
217
            fig = plt.figure(figsize=(8,8))
218
            ax = plt.axes(projection="3d")
219
            # ax.contour3D(xx, yy, a2[i,:], 500)
220
            ax.contourf(xx, yy, a2[i,:], 500, cmap=cm.CMRmap)
221
            ax.set_xlabel("X1")
222
223
            ax.set_ylabel("X2")
224
            ax.set_zlabel("HL2-Neuron "+str(i+1));
            ax.set_title("Epoch: "+ str(epochs) + "; Surface for Layer 2, Neuron "+str(...
225
226
            plt.tight_layout()
            plt.savefig("images/1B_MLFFNN_E"+str(epochs)+"_HL2_N"+str(i+1)+".png")
227
228
            plt.show()
229
        for i in range(op.shape[0]):
230
            fig = plt.figure(figsize=(8,8))
231
            ax = plt.axes(projection="3d")
232
233
            # ax.contour3D(xx, yy, op[i,:], 500)
234
235
            ax.contourf(xx, yy, op[i,:], 500, cmap=cm.CMRmap)
236
            ax.set_xlabel("X1")
237
            ax.set_ylabel("X2")
238
            ax.set_zlabel("OP-Neuron "+str(i+1));
            ax.set_title("Epoch: "+ str(epochs) + "; Surface for Output Layer, Neuron "...
239
                +str(i+1))
            plt.tight_layout()
240
            plt.savefig("images/1B_MLFFNN_E"+str(epochs)+"_OP_N"+str(i+1)+".png")
241
            plt.show()
242
243
244
   mlp = MLPClassifier(random_state=1, max_iter=1000, **clf.best_params_)
245
   mlp.fit(X_train, y_train)
247
248
   weights = mlp.coefs_
249
   biases = mlp.intercepts_
250
251 a1, a2, op = get_values(weights, biases, grid)
252 a1 = a1.reshape(a1.shape[0], *xx.shape)
   a2 = a2.reshape(a2.shape[0], *xx.shape)
253
   op = op.reshape(op.shape[0], *xx.shape)
254
255
256
257
   for i in range(a1.shape[0]):
258
        fig = plt.figure(figsize=(8,8))
259
        ax = plt.axes(projection="3d")
260
        # ax.contour3D(xx, yy, a1[i,:], 500)
261
262
        ax.contourf(xx, yy, a1[i,:], 500, cmap=cm.CMRmap)
        ax.set_xlabel("X1")
263
        ax.set_ylabel("X2")
264
        ax.set_zlabel("HL1-Neuron "+str(i+1));
265
266
        ax.set_title("Converged; Surface for Layer 1, Neuron "+str(i+1))
        plt.tight_layout()
267
        plt.savefig("images/1B_MLFFNN_conv_HL1_N"+str(i+1)+".png")
268
269
        plt.show()
270
   for i in range(a2.shape[0]):
271
        fig = plt.figure(figsize=(8,8))
272
        ax = plt.axes(projection="3d")
273
274
275
        # ax.contour3D(xx, yy, a2[i,:], 500)
276
        ax.contourf(xx, yy, a2[i,:], 500, cmap=cm.CMRmap)
        ax.set_xlabel("X1")
277
278
        ax.set_ylabel("X2")
279
        ax.set_zlabel("HL2-Neuron "+str(i+1));
```

```
ax.set_title("Converged; Surface for Layer 2, Neuron "+str(i+1))
280
281
        plt.tight_layout()
        plt.savefig("images/1B_MLFFNN_conv_HL2_N"+str(i+1)+".png")
282
283
        plt.show()
284
   for i in range(op.shape[0]):
285
        fig = plt.figure(figsize=(8,8))
286
        ax = plt.axes(projection="3d")
287
288
        # ax.contour3D(xx, yy, op[i,:], 500)
289
290
        ax.contourf(xx, yy, op[i,:], 500, cmap=cm.CMRmap)
        ax.set_xlabel("X1")
291
        ax.set_ylabel("X2")
292
        ax.set_zlabel("OP-Neuron "+str(i+1));
293
        ax.set_title("Converged; Surface for Output Layer, Neuron "+str(i+1))
294
295
        plt.tight_layout()
        plt.savefig("images/1B_MLFFNN_conv_OP_N"+str(i+1)+".png")
296
297
        plt.show()
298
299
300 # In[]:
```

The helper functions used are as follows:

```
1 import numpy as np
2 import pandas as pd
3 from time import time
4 from tqdm import tqdm
5 from collections import defaultdict
6 from sklearn.neural_network import MLPClassifier
  class GridSearch1A():
8
       def __init__(self, model, parameters, verbose=0):
9
           self.model = model
10
           self.parameters = parameters
11
           self.verbose = verbose
           params_list = []
13
           self.params_keys = self.parameters.keys()
14
15
           for hls in parameters["hidden_layer_sizes"]:
16
                for act in parameters["activation"]:
17
                    for s in parameters["solver"]:
18
                        for bs in parameters["batch_size"]:
19
                            for a in parameters["alpha"]:
20
                                 for lr in parameters["learning_rate"]:
21
                                     params_list.append({"hidden_layer_sizes":hls, \
22
                                                          "activation":act, \
23
                                                          "solver":s, \
24
                                                          "batch_size":bs, \
25
                                                          "alpha":a, \
26
                                                          "learning_rate":lr})
27
           self.params_list = params_list
28
29
       def fit(self, X_train, y_train, X_val, y_val):
30
           self.cv_results_ = pd.DataFrame(columns=self.params_keys)
31
32
           self.params_ = defaultdict(list)
           self.acc_list_ = []
           self.val_acc_list_ = []
35
           self.t_inv_list_ = []
36
37
           for params in tqdm(self.params_list):
38
                st = time()
39
               mlp = MLPClassifier(random_state=1, **params)
40
41
               mlp.fit(X_train, y_train)
42
               et = time()
43
```

```
y_pred = mlp.predict(X_train)
45
                acc = 100*np.sum(y_pred==y_train)/y_train.size
46
47
                y_val_pred = mlp.predict(X_val)
48
                val_acc = 100*np.sum(y_val_pred==y_val)/y_val.size
49
50
51
                for i in params:
                     self.params_[i].append(params[i])
52
53
                self.acc_list_.append(acc)
54
                self.val_acc_list_.append(val_acc)
55
                self.t_inv_list_.append(1/(et-st))
56
            for i in params:
58
                self.cv_results_[i] = self.params_[i]
            self.cv_results_["accuracy"] = self.acc_list_
61
            self.cv_results_["val_accuracy"] = self.val_acc_list_
            self.cv_results_["sum_accuracy"] = self.cv_results_["accuracy"] + self....
63
                cv_results_["val_accuracy"]
            self.cv_results_["t_inv"] = self.t_inv_list_
64
            self.cv_results_ = self.cv_results_.sort_values(by=["accuracy", "...
65
                sum_accuracy", "t_inv"], ascending=False, ignore_index=True)
66
            self.best_params_ = self.cv_results_.iloc[0].to_dict()
            del self.best_params_["accuracy"]
            del self.best_params_["val_accuracy"]
            del self.best_params_["sum_accuracy"]
70
            del self.best_params_["t_inv"]
71
72
73
   class GridSearch1B():
74
75
        def __init__(self, model, parameters, verbose=0):
            self.model = model
76
77
            self.parameters = parameters
            self.verbose = verbose
78
            params_list = []
79
80
            self.params_keys = self.parameters.keys()
81
            for hls in parameters["hidden_layer_sizes"]:
82
                for act in parameters["activation"]:
83
                    for bs in parameters["batch_size"]:
84
                         for a in parameters["alpha"]:
85
                             for lr in parameters["learning_rate"]:
86
                                 for es in parameters["early_stopping"]:
87
                                      params_list.append({"hidden_layer_sizes":hls, \
88
                                                           "early_stopping":es, \
89
                                                           "learning_rate":lr, \
90
                                                           "activation":act, \
91
                                                           "batch_size":bs, \
92
                                                           "alpha":a})
93
            self.params_list = params_list
94
95
        def fit(self, X_train, y_train, X_val, y_val):
96
            self.cv_results_ = pd.DataFrame(columns=self.params_keys)
98
            self.params_ = defaultdict(list)
            self.acc_list_ = []
            self.val_acc_list_ = []
101
            self.t_inv_list_ = []
102
103
            for params in tqdm(self.params_list):
104
                st = time()
105
                mlp = MLPClassifier(random_state=1, **params)
106
107
                mlp.fit(X_train, y_train)
108
                et = time()
109
110
111
                y_pred = mlp.predict(X_train)
```

```
112
                acc = 100*np.sum(y_pred==y_train)/y_train.size
113
                y_val_pred = mlp.predict(X_val)
114
                val_acc = 100*np.sum(y_val_pred==y_val)/y_val.size
115
116
117
                for i in params:
                     self.params_[i].append(params[i])
118
119
                self.acc_list_.append(acc)
120
                self.val_acc_list_.append(val_acc)
121
122
                self.t_inv_list_.append(1/(et-st))
123
124
            for i in params:
                self.cv_results_[i] = self.params_[i]
126
            self.cv_results_["accuracy"] = self.acc_list_
127
            self.cv_results_["val_accuracy"] = self.val_acc_list_
128
            self.cv_results_["sum_accuracy"] = self.cv_results_["accuracy"] + self....
129
                cv_results_["val_accuracy"]
            self.cv_results_["t_inv"] = self.t_inv_list_
130
            self.cv_results_ = self.cv_results_.sort_values(by=["accuracy", "...
131
                sum_accuracy", "t_inv"], ascending=False, ignore_index=True)
132
133
            self.best_params_ = self.cv_results_.iloc[0].to_dict()
            self.best_params_["early_stopping"] = bool(self.best_params_["...
                early_stopping"])
            del self.best_params_["accuracy"]
135
            del self.best_params_["val_accuracy"]
136
            del self.best_params_["sum_accuracy"]
137
            del self.best_params_["t_inv"]
138
```

2.2 Non-Linear SVM

3 Dataset 2A

3.1 MLFFNN

The helper function used is as follows:

```
1 import os
2 import numpy as np
3 import pandas as pd
4 from tqdm import tqdm
6
  def get_consolidated_data2A(classes_present):
       df = pd.DataFrame()
7
       df_test = pd.DataFrame()
8
       for i in classes_present:
9
           df_new = pd.read_csv("../datasets/2A/"+i+"/train.csv")
10
           df_new["image_names"] = classes_present[i]
11
           df_new = df_new.rename(columns={"image_names":"class"})
12
           df = df.append(df_new)
13
           df_new_test = pd.read_csv("../datasets/2A/"+i+"/dev.csv")
15
           df_new_test["image_names"] = classes_present[i]
16
           df_new_test = df_new_test.rename(columns={"image_names":"class"})
17
           df_test = df_test.append(df_new_test)
18
19
       df.to_csv("../datasets/2A/train.csv", index=False)
20
       df_test.to_csv("../datasets/2A/dev.csv", index=False)
21
22
  if __name__ == "__main__":
       classes_present = {"coast":0, "highway":1, "mountain":2, "opencountry":3, "...
24
           tallbuilding":4}
       get_consolidated_data2A(classes_present)
```

3.2 Gaussian-kernel SVM