

El proceso de Dyson determinista

T E S I S

Que para obtener el grado de
Maestro en Ciencias con Especialidad en Probabilidad y Estadística

Presenta

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Autorización de la versión final

Dedicatoria ...

Abstract

Palabras clave:

Agradecimientos

A mis padres ...

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