# Class 8 Mini-Project: Unsupervised Learning Analysis of Human Breast Cancer Cells

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The goal of this miniproject is for you to explore a complete analysis using the unsupervised learning techniques covered in class. You will extend what you've learned by combinding PCA as a preprocessing step to clustering using data that consist of measurements of cell nuclei of human breast masses:

Our data from today come for FNA of breast tissue

```
# Save your input data file into your Project directory
fna.data <- "WisconsinCancer.csv"

# Complete the following code to input the data and store as wisc.df
wisc.df <- read.csv(fna.data, row.names=1)
head(wisc.df)</pre>
```

	diagnosis 1	radius_mean	texture_mean	perimeter_mean	n area_mean	
842302	M	17.99	10.38	122.8	0 1001.0	
842517	M	20.57	17.77	132.9	0 1326.0	
84300903	M	19.69	21.25	130.0	0 1203.0	
84348301	M	11.42	20.38	77.5	8 386.1	
84358402	M	20.29	14.34	135.1	0 1297.0	
843786	M	12.45	15.70	82.5	7 477.1	
	smoothness	_mean compac	ctness_mean c	oncavity_mean	concave.poi	nts_mean
842302	0.1	11840	0.27760	0.3001		0.14710
842517	0.0	08474	0.07864	0.0869		0.07017
84300903	0.1	10960	0.15990	0.1974		0.12790
84348301	0.1	14250	0.28390	0.2414		0.10520
84358402	0.1	10030	0.13280	0.1980		0.10430
843786	0.1	12780	0.17000	0.1578		0.08089
symmetry_mean fractal_dimension_mean radius_se texture_se perimeter_se						erimeter_se
842302	0.24	419	0.078	71 1.0950	0.9053	8.589

842517	0.1812		0.05667	0.5435	0.7339	3.398
84300903	0.2069		0.05999	0.7456	0.7869	4.585
84348301	0.2597	0.2597		0.4956	1.1560	3.445
84358402	0.1809		0.05883	0.7572	0.7813	5.438
843786	0.2087		0.07613	0.3345	0.8902	2.217
	area_se smoothne	ess_se compa	actness_se	concavity_se	concave.po	ints_se
842302	153.40 0.0	006399	0.04904	0.05373		0.01587
842517	74.08 0.0	005225	0.01308	0.01860		0.01340
84300903	94.03 0.0	006150	0.04006	0.03832		0.02058
84348301	27.23 0.0	009110	0.07458	0.05661		0.01867
84358402	94.44 0.0	011490	0.02461	0.05688		0.01885
843786	27.19 0.0	007510	0.03345	0.03672		0.01137
	symmetry_se frac	ctal_dimensi	on_se radi	ius_worst text	ture_worst	
842302	0.03003	0.0	006193	25.38	17.33	
842517	0.01389	0.0	03532	24.99	23.41	
84300903	0.02250	0.0	04571	23.57	25.53	
84348301	0.05963	0.0	09208	14.91	26.50	
84358402	0.01756	0.0	05115	22.54	16.67	
843786	0.02165	0.0	05082	15.47	23.75	
	perimeter_worst	area_worst	smoothness	s_worst compa	ctness_wors	t
842302	184.60	2019.0		0.1622	0.665	
842517	158.80	1956.0		0.1238	0.186	6
84300903	152.50	1709.0		0.1444	0.424	5
84348301	98.87	567.7		0.2098	0.866	3
84358402	152.20	1575.0		0.1374	0.205	0
843786	103.40	741.6		0.1791	0.524	9
	concavity_worst	concave.poi	nts_worst	symmetry_wors	st	
842302	0.7119	-	0.2654	0.460		
842517	0.2416		0.1860	0.27	50	
84300903	0.4504		0.2430	0.36	13	
84348301	0.6869		0.2575	0.663	38	
84358402	0.4000		0.1625	0.236	64	
843786	0.5355		0.1741	0.398	35	
	fractal_dimension	on_worst				
842302		0.11890				
842517		0.08902				
84300903		0.08758				
84348301		0.17300				
84358402		0.07678				
843786		0.12440				

Q1. How many observations are in this dataset?

There are 569 individuals in this dataset

ANS: We have 357 benignant diagnosis and 212 malignant diagnosis. # One approach sum(wisc.df\$diagnosis=="M") [1] 212 sum(wisc.df\$diagnosis=="B") [1] 357 #Other approach using `table()` table(wisc.df\$diagnosis) В Μ 357 212 Q3. How many variables/features in the data are suffixed with \_mean? length(grep("\_mean",colnames(wisc.df),value="TRUE")) [1] 10 Q3. How many variables/dimensions have we? ncol(wisc.df) [1] 31

Q2. What is in the \$diagnosis column? How many of each type?

## diagnosis<- as.factor(wisc.df\$diagnosis)</pre>

and remove or exclude this column form any of our analysis

```
wisc.data<-wisc.df[,-1]
head(wisc.data)</pre>
```

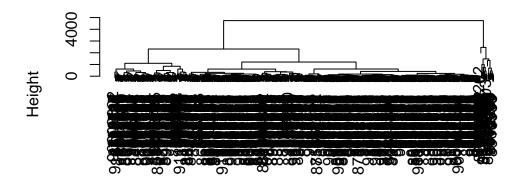
	radius_mean text	ıro moon	norimot	or moon	2222 222	n amooth	
842302	17.99	10.38	berimer	122.80	1001.		0.11840
842517	20.57	17.77		132.90	1326.		0.08474
84300903		21.25		130.00	1203.		0.10960
84348301		20.38		77.58	386.		0.14250
84358402		14.34		135.10	1297.		0.14230
843786	12.45	15.70		82.57	477.		0.10030
040700	compactness_mean		tv mean (				
842302	0.27760	COHCAVI	0.3001	JOIICA V C .	0.14	•	0.2419
842517	0.07864		0.0869		0.07		0.1812
84300903			0.1974		0.12		0.2069
84348301			0.2414		0.10		0.2597
84358402	0.13280		0.1980		0.10	430	0.1809
843786	0.17000		0.1578		0.08	089	0.2087
	fractal_dimension	n_mean ra	adius_se	texture	e_se peri	meter_se	area_se
842302		.07871	1.0950		9053	8.589	153.40
842517	0	.05667	0.5435	0.7	7339	3.398	74.08
84300903	0	.05999	0.7456	0.7	7869	4.585	94.03
84348301	0	.09744	0.4956	1.1	1560	3.445	27.23
84358402	0	.05883	0.7572	0.7	7813	5.438	94.44
843786	0	.07613	0.3345	0.8	3902	2.217	27.19
	smoothness_se com	npactness	s_se con	cavity_s	se concav	e.points	_se
842302	0.006399	0.04	4904	0.0537	73	0.01	587
842517	0.005225	0.03	1308	0.0186	30	0.013	340
84300903	0.006150	0.04	4006	0.0383	32	0.020	058
84348301	0.009110	0.0	7458	0.0566	31	0.018	367
84358402			2461	0.0568		0.018	385
843786	0.007510		3345	0.0367		0.01	
	symmetry_se frac	_	_	radius_	_worst te	<del>-</del>	
842302	0.03003		0.006193		25.38		. 33
842517	0.01389		0.003532		24.99		.41
84300903			0.004571		23.57		. 53
84348301			0.009208		14.91		.50
84358402			0.005115		22.54		. 67
843786	0.02165	(	0.005082		15.47	23	.75

	perimeter_worst	area_worst	smoothness	s_worst	compactnes	ss_worst
842302	184.60	2019.0		0.1622		0.6656
842517	158.80	1956.0		0.1238		0.1866
84300903	152.50	1709.0		0.1444		0.4245
84348301	98.87	567.7		0.2098		0.8663
84358402	152.20	1575.0		0.1374		0.2050
843786	103.40	741.6		0.1791		0.5249
	concavity_worst	concave.po	ints_worst	symmeti	ry_worst	
842302	0.7119		0.2654		0.4601	
842517	0.2416		0.1860		0.2750	
84300903	0.4504		0.2430		0.3613	
84348301	0.6869		0.2575		0.6638	
84358402	0.4000		0.1625		0.2364	
843786	0.5355		0.1741		0.3985	
	fractal_dimension	on_worst				
842302		0.11890				
842517		0.08902				
84300903		0.08758				
84348301		0.17300				
84358402		0.07678				
843786		0.12440				

Let's try clustering this data:

Hierachical clustering with hclust()

```
wisc.hc <- hclust(dist(wisc.data))
plot(wisc.hc)</pre>
```



dist(wisc.data) hclust (\*, "complete")

# Principal Coponent Analysis (PCA)

Let's try PCA on this data. Before doing any analysis like this, we should check if our input data needs to be scaled first.

Side-note:

head(mtcars)

```
mpg cyl disp hp drat
                                            wt
                                               qsec vs am gear carb
Mazda RX4
                  21.0
                            160 110 3.90 2.620 16.46
                                                         1
Mazda RX4 Wag
                  21.0
                            160 110 3.90 2.875 17.02
                                                                    4
                                                         1
Datsun 710
                  22.8
                            108
                                 93 3.85 2.320 18.61
                                                         1
                                                                    1
                            258 110 3.08 3.215 19.44
Hornet 4 Drive
                  21.4
                                                                    1
                                                               3
                                                                    2
Hornet Sportabout 18.7
                            360 175 3.15 3.440 17.02
                         6 225 105 2.76 3.460 20.22
                                                               3
Valiant
                  18.1
                                                                    1
```

apply(mtcars, 2, mean)

```
drat
                 cyl
                            disp
                                          hp
                                                                          qsec
      mpg
20.090625
            6.187500 230.721875 146.687500
                                               3.596563
                                                          3.217250
                                                                    17.848750
       VS
                            gear
                                        carb
                  am
 0.437500
            0.406250
                        3.687500
                                   2.812500
```

```
apply(mtcars, 2, sd)
```

```
cyl
                              disp
                                             hp
                                                        drat
                                                                       wt
      mpg
6.0269481
            1.7859216 123.9386938
                                     68.5628685
                                                   0.5346787
                                                               0.9784574
     qsec
                                           gear
                                                        carb
                                      0.7378041
1.7869432
            0.5040161
                         0.4989909
                                                   1.6152000
```

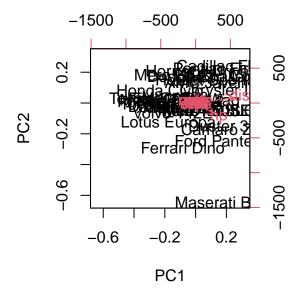
Let's try a PCA on this car dataset

```
pc<- prcomp(mtcars)
summary(pc)</pre>
```

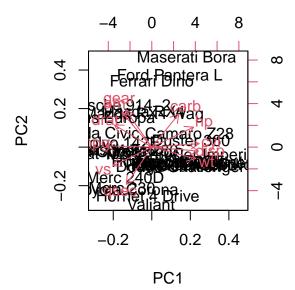
#### Importance of components:

```
PC1
                                    PC2
                                            PC3
                                                    PC4
                                                             PC5
                                                                    PC6
                                                                            PC7
                       136.533 38.14808 3.07102 1.30665 0.90649 0.66354 0.3086
Standard deviation
Proportion of Variance
                                0.07237 0.00047 0.00008 0.00004 0.00002 0.0000
                         0.927
                                0.99937 0.99984 0.99992 0.99996 0.99998 1.0000
Cumulative Proportion
                         0.927
                         PC8
                                PC9
                                      PC10
Standard deviation
                       0.286 0.2507 0.2107 0.1984
Proportion of Variance 0.000 0.0000 0.0000 0.0000
Cumulative Proportion 1.000 1.0000 1.0000 1.0000
```

```
biplot(pc)
```



pc.scale<- prcomp(mtcars,scale=TRUE)
biplot(pc.scale)</pre>



We have to scale the data since the SD is really high. Some values are really high while other are really low. We need to scale in order to have more comparable numbers.

#### Back to our cancer data set

Do we need to scale this data set? Yes, we do since the spread is very different.

```
apply(wisc.data,2,sd)
```

texture_mean	perimeter_mean
4.301036e+00	2.429898e+01
${\tt smoothness\_mean}$	compactness_mean
1.406413e-02	5.281276e-02
concave.points_mean	symmetry_mean
3.880284e-02	2.741428e-02
radius_se	texture_se
2.773127e-01	5.516484e-01
area_se	smoothness_se
4.549101e+01	3.002518e-03
concavity_se	concave.points_se
3.018606e-02	6.170285e-03
fractal_dimension_se	radius_worst
2.646071e-03	4.833242e+00
perimeter_worst	area_worst
3.360254e+01	5.693570e+02
compactness_worst	concavity_worst
1.573365e-01	2.086243e-01
symmetry_worst	<pre>fractal_dimension_worst</pre>
6.186747e-02	1.806127e-02
	4.301036e+00 smoothness_mean 1.406413e-02 concave.points_mean 3.880284e-02 radius_se 2.773127e-01 area_se 4.549101e+01 concavity_se 3.018606e-02 fractal_dimension_se 2.646071e-03 perimeter_worst 3.360254e+01 compactness_worst 1.573365e-01 symmetry_worst

```
wisc.pr <- prcomp(wisc.data,scale=TRUE )</pre>
```

How well do the PCs capture the variance un the original data?

```
summary(wisc.pr)
```

Importance of components:

```
Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
                           PC8
                                  PC9
                                         PC10
                                                         PC12
                                                PC11
                                                                 PC13
                                                                         PC14
Standard deviation
                       0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
Cumulative Proportion
                       0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
                          PC15
                                  PC16
                                          PC17
                                                   PC18
                                                           PC19
                                                                   PC20
                                                                          PC21
Standard deviation
                       0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
Cumulative Proportion
                       0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                          PC22
                                  PC23
                                         PC24
                                                 PC25
                                                          PC26
                                                                  PC27
                                                                          PC28
                       0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
Standard deviation
Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
Cumulative Proportion
                       0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                          PC29
                                  PC30
Standard deviation
                       0.02736 0.01153
Proportion of Variance 0.00002 0.00000
Cumulative Proportion
                       1.00000 1.00000
```

Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?

ANS: 44.27%

Q5. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

ANS: 3 (PC1, PC2, PC3)

Q6. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

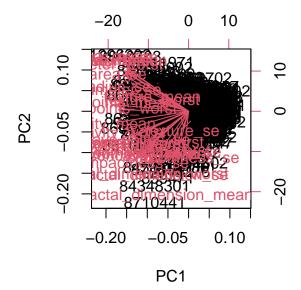
ANS: 7 (PC1, PC2, PC3, PC4, PC5, PC6, PC7)

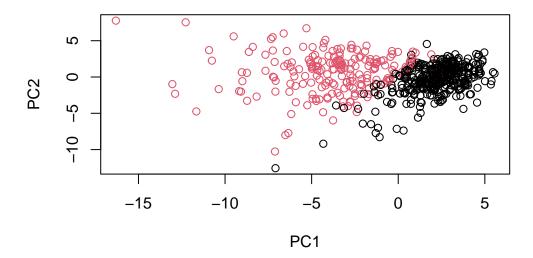
## **Interpreting PCA results**

Create a biplot of the wisc.pr using the biplot() function.

Q7. What stands out to you about this plot? Is it easy or difficult to understand? Why?

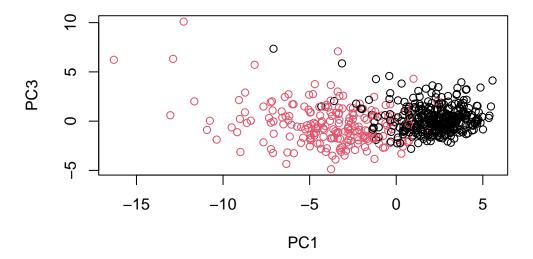
ANS: The interpretation is very difficult. The labels are overlapped and there appears to be a high density of data points clustered in the center of the plot





Q8. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?

ANS: Since PC1 and PC2 contains the more variance, we can observe a better differentiation between two groups



## Make a nice ggplot version

```
pc <- as.data.frame(wisc.pr$x)
library(ggplot2)
ggplot(pc, aes(x=PC1,y=PC2, col=diagnosis)) + geom_point()</pre>
```



```
v<- summary(wisc.pr)
v$importance[2,]</pre>
```

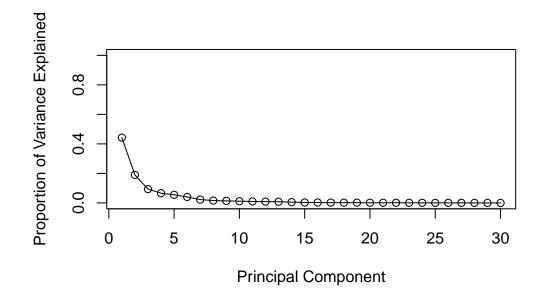
PC1 PC2 PC3 PC4 PC5 PC6 PC7 PC8 PC9 PC10 0.44272 0.18971 0.09393 0.06602 0.05496 0.04025 0.02251 0.01589 0.01390 0.01169 PC12 PC13 PC14 PC15 PC16 PC17 PC18 PC19 PC20 0.00980 0.00871 0.00805 0.00523 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 PC21 PC22 PC23 PC24 PC25 PC26 PC29 PC27 PC28 PC30 0.00100 0.00091 0.00081 0.00060 0.00052 0.00027 0.00023 0.00005 0.00002 0.00000

#### Variance explained

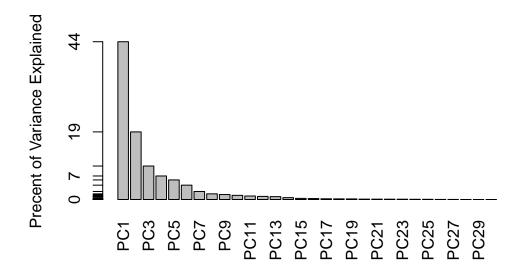
```
# Calculate variance of each component
pr.var <- wisc.pr$sdev^2
head(pr.var)</pre>
```

[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357

Calculate the variance explained by each principal component by dividing by the total variance explained of all principal components. Assign this to a variable called pve and create a plot of variance explained for each principal component.



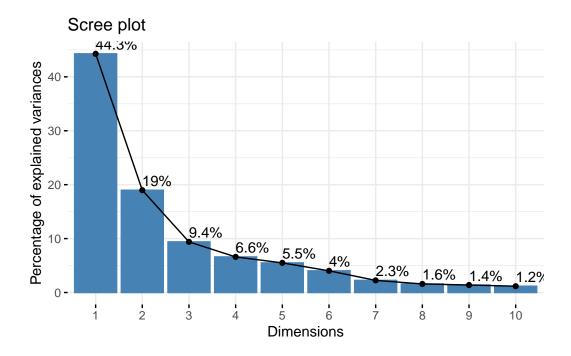
## Alternative scree plot of the same data, note data driven y-axis



```
## ggplot based graph
#install.packages("factoextra")
library(factoextra)
```

Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

```
fviz_eig(wisc.pr, addlabels = TRUE)
```



#### **Communicating PCA results**

Q9. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points\_mean? This tells us how much this original feature contributes to the first PC.

ANS: The loading vector (i.e. wisc.prformula = 0.26085376) for the feature concave.points\_mean is -0.26085376

#### Hierarchical clustering

First scale the wisc.data data and assign the result to data.scaled.

```
# Scale the wisc.data data using the "scale()" function
data.scaled <- scale(wisc.data)</pre>
```

Calculate the (Euclidean) distances between all pairs of observations in the new scaled dataset and assign the result to data.dist

```
# Scale the wisc.data data using the "scale()" function
data.dist <- dist(data.scaled)</pre>
```

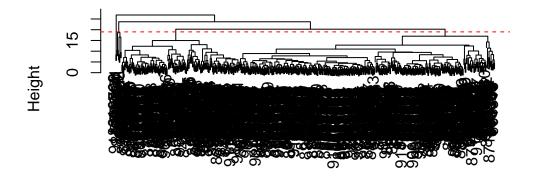
Create a hierarchical clustering model using complete linkage. Manually specify the method argument to hclust() and assign the results to wisc.hclust.

```
wisc.hclust <- hclust(data.dist,method="complete")</pre>
```

Q10. Using the plot() and abline() functions, what is the height at which the clustering model has 4 clusters?

```
plot(wisc.hclust)
abline(h=19, col="red", lty=2)
```

## **Cluster Dendrogram**



data.dist hclust (\*, "complete")

#### Selecting number of clusters

Use cutree() to cut the tree so that it has 4 clusters. Assign the output to the variable wisc.hclust.clusters.

```
wisc.hclust.clusters <- cutree(wisc.hclust,h=19)
#We can use the table() function to compare the cluster membership to the actual diagnoses
table(wisc.hclust.clusters, diagnosis)</pre>
```

```
diagnosis
wisc.hclust.clusters B M
1 12 165
2 2 5
3 343 40
4 0 2
```

Q11. OPTIONAL: Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10? How do you judge the quality of your result in each case?

ANS: The quality of the results are based on the purity of clusters: the sum of the largest class in each cluster divided by the total number of observations. We have better results when the height number is higher. Therefore, any of the numbers between 2 and 10 show better results than height 19

```
#Function to determine the purity of the clusters
purity<-function(h,hclust_data){
  wisc.hclust.clusters <- cutree(hclust_data,h=h)
  table_clust<-table(wisc.hclust.clusters, diagnosis)
  purity <- sum(apply(table_clust, 2, max)) / sum(table_clust)
  print(purity)
}

#Using height = 2
  h=2
  purity(h,wisc.hclust)

[1] 0.01230228

#Using height = 6
  h=6
  purity(h,wisc.hclust)</pre>
```

1

```
#Using height = 10
h=10
purity(h,wisc.hclust)
```

[1] 0.4393673

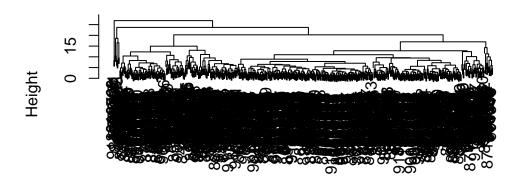
#### Using different methods

As we discussed in our last class videos there are number of different "methods" we can use to combine points during the hierarchical clustering procedure. These include "single", "complete", "average" and (my favorite) "ward.D2".

Q12. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

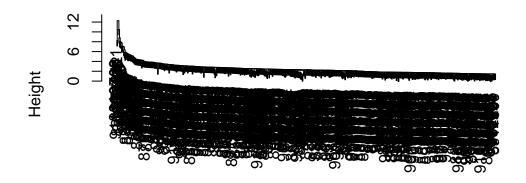
ANS: There is not a "best" method. However, we can choose the method depending on the nature of your data. For this specific project, we are looking for clusters that can differentiate between benign and malign samples. Therefore, my favorite method would be "ward.D2" since it shows more clearly the two separate clusters

```
#Using "complete" method
wisc.hclust.complete <- hclust(data.dist,method="complete")
plot(wisc.hclust.complete)</pre>
```



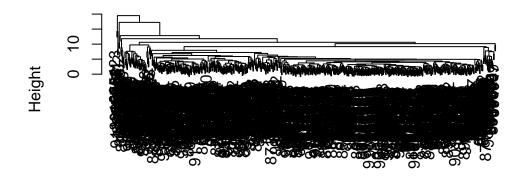
data.dist hclust (\*, "complete")

```
#Using "single" method
wisc.hclust.single<- hclust(data.dist,method="single")
plot(wisc.hclust.single)</pre>
```



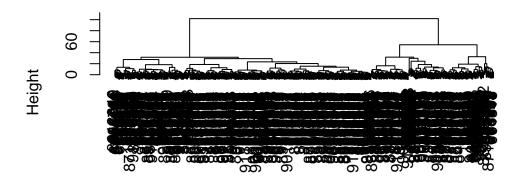
data.dist hclust (\*, "single")

```
#Using "average" method
wisc.hclust.avg<- hclust(data.dist,method="average")
plot(wisc.hclust.avg)</pre>
```



data.dist hclust (\*, "average")

```
#Using "ward.D2 method
wisc.hclust.ward<- hclust(data.dist,method="ward.D2")
plot(wisc.hclust.ward)</pre>
```



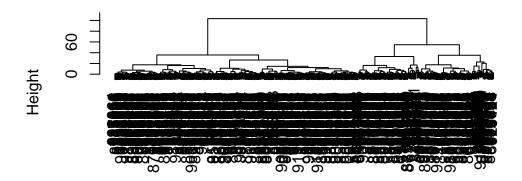
data.dist hclust (\*, "ward.D2")

## 4. Combining methods

Here, we will use the results of PCA as the input to a clustering analysis.

We start with using  $3~\mathrm{PCs}$ 

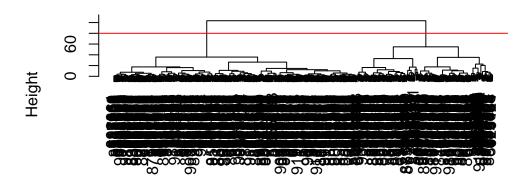
```
wisc.pr.hclust <- hclust(dist(wisc.pr$x[,1:3]), method="ward.D2")
plot(wisc.pr.hclust)</pre>
```



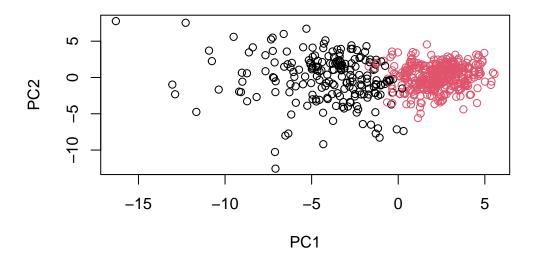
dist(wisc.pr\$x[, 1:3]) hclust (\*, "ward.D2")

plot(wisc.pr.hclust)
abline(h=80,col="red")

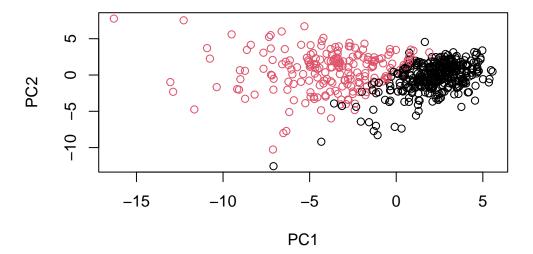
# **Cluster Dendrogram**



dist(wisc.pr\$x[, 1:3]) hclust (\*, "ward.D2")



plot(wisc.pr\$x[,1:2], col=diagnosis)



Note the color swap here as the hclust cluster 1 is mostly "M" and cluster 2 is mostly "B" as we saw from the results of calling table(grps, diagnosis). To match things up we can turn our groups into a factor and reorder the levels so cluster 2 comes first and thus gets the first color (black) and cluster 1 gets the second color (red).

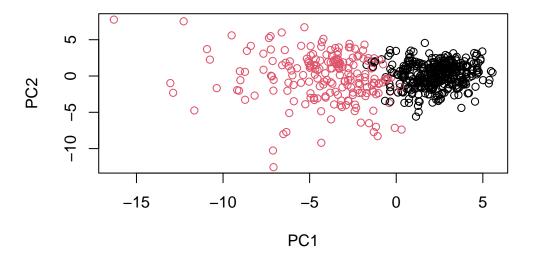
```
g <- as.factor(grps)
levels(g)

[1] "1" "2"

g <- relevel(g,2)
levels(g)

[1] "2" "1"

# Plot using our re-ordered factor
plot(wisc.pr$x[,1:2], col=g)</pre>
```



Now, we will use the results of PCA as the input to a clustering analysis using 7 PCs

```
## Use the distance along the first 7 PCs for clustering i.e. wisc.pr$x[, 1:7]
wisc.pr.hclust <- hclust(dist(wisc.pr$x[,1:7]), method="ward.D2")

#Cut this hierarchical clustering model into 2 clusters and assign the results to wisc.pr.
wisc.pr.hclust.clusters <- cutree(wisc.pr.hclust, k=2)</pre>
```

Q13. How well does the newly created model with four clusters separate out the two diagnoses?

ANS: If we compare the model with 2 cluster vs 4 clusters we can say that the four-cluster solution appears to provide a finer distinction since our goal is to separate benign from malignant cases.

```
wisc.pr.hclust.clusters.four <- cutree(wisc.pr.hclust, k=4)
# Compare to actual diagnoses
two<-table(wisc.pr.hclust.clusters, diagnosis)
two</pre>
```

```
diagnosis
wisc.pr.hclust.clusters
                            В
                                М
                          28 188
                       2 329
                              24
  four<-table(wisc.pr.hclust.clusters.four, diagnosis)</pre>
  four
                              diagnosis
wisc.pr.hclust.clusters.four
                                 В
                                    45
                             2
                                 2
                                    77
                                26
                             3
                                    66
                             4 329
                                    24
```

Q14. How well do the hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table() function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

ANS: It looks that wisc.pr.hclust.clusters with four clusters separated after PCA (variable called "four") provides the best separation in terms of diagnostic clarity, especially for identifying malignant cases, which is often the priority in medical diagnostics.

```
wisc.hclust.clusters <- cutree(wisc.hclust,h=19)
thclust<-table(wisc.hclust.clusters, diagnosis)
thclust</pre>
```

```
diagnosis
wisc.hclust.clusters B M
1 12 165
2 2 5
3 343 40
4 0 2
```

two

diagnosis
wisc.pr.hclust.clusters B M
1 28 188
2 329 24

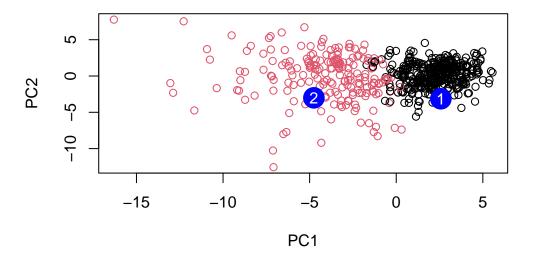
```
four
```

```
diagnosis
wisc.pr.hclust.clusters.four B M
1 0 45
2 2 77
3 26 66
4 329 24
```

#### **Prediction**

We will use the predict() function that will take our PCA model from before and new cancer cell data and project that data onto our PCA space.

```
#url <- "new_samples.csv"</pre>
  url <- "https://tinyurl.com/new-samples-CSV"</pre>
  new <- read.csv(url)</pre>
  npc <- predict(wisc.pr, newdata=new)</pre>
  npc
           PC1
                     PC2
                                PC3
                                            PC4
                                                      PC5
                                                                  PC6
                                                                             PC7
[1,] 2.576616 -3.135913 1.3990492 -0.7631950 2.781648 -0.8150185 -0.3959098
[2,] -4.754928 -3.009033 -0.1660946 -0.6052952 -1.140698 -1.2189945
                                                                       0.8193031
            PC8
                      PC9
                                PC10
                                                     PC12
                                           PC11
                                                                PC13
                                                                         PC14
[1,] -0.2307350 0.1029569 -0.9272861 0.3411457 0.375921 0.1610764 1.187882
[2,] -0.3307423 0.5281896 -0.4855301 0.7173233 -1.185917 0.5893856 0.303029
          PC15
                     PC16
                                  PC17
                                              PC18
                                                          PC19
                                                                      PC20
[1,] 0.3216974 -0.1743616 -0.07875393 -0.11207028 -0.08802955 -0.2495216
[2,] 0.1299153 0.1448061 -0.40509706 0.06565549 0.25591230 -0.4289500
           PC21
                      PC22
                                  PC23
                                             PC24
                                                         PC25
                                                                       PC26
[1,] 0.1228233 0.09358453 0.08347651 0.1223396 0.02124121 0.078884581
[2,] -0.1224776 0.01732146 0.06316631 -0.2338618 -0.20755948 -0.009833238
             PC27
                         PC28
                                       PC29
                                                    PC30
[1,] 0.220199544 -0.02946023 -0.015620933 0.005269029
[2,] -0.001134152  0.09638361  0.002795349 -0.019015820
  plot(wisc.pr$x[,1:2], col=g)
  points(npc[,1], npc[,2], col="blue", pch=16, cex=3)
  text(npc[,1], npc[,2], c(1,2), col="white")
```



Q16. Which of these new patients should we prioritize for follow up based on your results?

Patient 2 appears to be in the "malign" diagnosis group. Therefore, patient 2 should be prioritized.