# Marwin B. Alejo 2020-20221 EE274\_ProgEx03

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Also accessible through http://www.github.com/soymarwin/ee274/EE274 ProgEx03.

# A. The Bilateral Z-Transform

(a) 
$$x(n) = (\frac{4}{3})^n u(1-n)$$

#### **Manual Solution**

$$x(n) = (\frac{4}{3})^n u(-n+1)$$

$$X(z) = \sum_{n=-\infty}^{\infty} x(n)z^{-n}$$

$$X(z) = \sum_{n=-\infty}^{\infty} (\frac{4}{3})^n u(-n+1) z^{-n}$$

Let 
$$k = -n + 1$$
 and  $n = 1 - k$ 

$$X(z) = \sum_{n=-\infty}^{\infty} (\frac{4}{3})^{1-k} u(k) z^{k-1}$$

$$X(z) = \sum_{n=0}^{\infty} (\frac{4}{3}) \cdot ((\frac{4}{3})^{-1})^k \cdot ((1/z)^{-1})^k \cdot z^{-1}$$

$$X(z) = (\frac{4z^{-1}}{3}) \sum_{n=0}^{\infty} (\frac{3}{4z^{-1}})^k$$

$$X(z) = (rac{4z^{-1}}{3}) \cdot (rac{1}{1 - rac{3}{4z^{-1}}}), \ 0 \ < \mid z \mid < \ rac{4}{3}$$

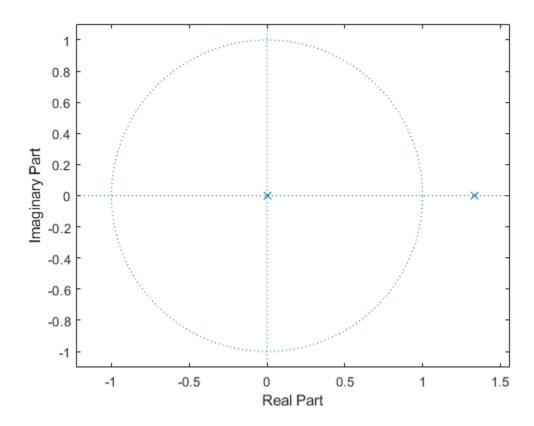
or 
$$X(z) = \frac{16z^{-2}}{-9+12z^{-1}}, \ 0 \ < \mid z \mid < \ \frac{4}{3}$$

or 
$$X(z) = \frac{-16z^{-2}}{9-12z^{-1}}, \ 0 \ < \mid z \mid < \ \frac{4}{3}$$

#### z-plane for 1.(a)

$$A1_a_a=[-9, 12, 0];$$

Al\_a\_b=[0, 0, -16]; zplane(Al\_a\_b,Al\_a\_a);



#### Verification of z-transform v. original sequence with first 8-coef.

[delta,n]= impseq(0,0,7);  $A_a_Xz=filter(Al_a_b,Al_a_a,delta) %A_a_Xz is z-transform sequence$  $<math>A_a_Xn=[(4/3).^n].*stepseq(1,0,7) %A_a_Xn is the original sequence$ 

 $A_a_Xz =$ 

Columns 1 through 7

0 0 1.7778 2.3704 3.1605 4.2140 5.6187

Column 8

7.4915

 $A_a_Xn =$ 

Columns 1 through 7

0 0 1.7778 2.3704 3.1605 4.2140 5.6187

Column 8

7.4915

Therefore, based on coef values generated from X(z) and x(n), the z-transform for sequence(a) is correct.

(b) 
$$x(n) = 2^{-|n|} + (\frac{1}{3})^{|n|}$$

$$X(z) = \sum_{n=0}^{\infty} 2^{-n} z^{-n} + \sum_{n=0}^{\infty} (\frac{1}{3})^n z^{-n}$$

$$X(z) = \sum_{n=0}^{\infty} (\frac{z^{-1}}{2})^n + \sum_{n=0}^{\infty} (\frac{z^{-1}}{3})^n$$

$$X(z) = \frac{1}{1 - \frac{z^{-1}}{2}} + \frac{1}{1 - \frac{z^{-1}}{3}}$$

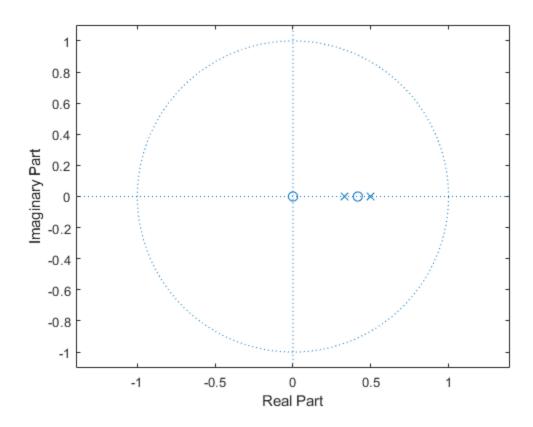
$$X(z) = \frac{2}{2-z^{-1}} + \frac{3}{3-z^{-1}}$$

$$X(z) = \frac{12 - 5z^{-1}}{(2 - z^{-1})(3 - z^{-1})}, \ \frac{1}{3} \ < \mid z \mid < \ \frac{1}{2}$$

$$orX(z) = \frac{12-5z^{-1}}{6-5z^{-1}+z^{-2}}, \ \frac{1}{3} \ < \mid z \mid < \ \frac{1}{2}$$

%

#### z-plane for 1.(b)



#### Verification of z-transform v. original sequence with first 8-coef.

```
[delta,n] = impseq(0,0,7);
A_b_Xz=filter(A1_b_b,A1_b_a,delta) %A_b_Xz is z-transform sequence
A_b_Xn=((2).^(-abs(n)))+((1/3).^(abs(n))) %A_b_Xn is the original
 sequence
% \times \mathbb{R}^{n} *Therefore, based on coef values generated from X(z) and X(n),
% the z-transform for sequence(b) is correct.*
A_b_Xz =
  Columns 1 through 7
    2.0000
              0.8333
                        0.3611
                                  0.1620
                                           0.0748
                                                       0.0354
                                                                 0.0170
  Column 8
    0.0083
A_b_Xn =
  Columns 1 through 7
    2.0000
              0.8333
                        0.3611
                                  0.1620
                                             0.0748
                                                       0.0354
                                                                 0.0170
```

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Column 8

0.0083

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