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## EE274\_ProgEx03

### Table of Contents

|   |   |
|---|---|
| A. The Bilateral Z-Transform .....                | 1 |
| (a) $x(n) = (\frac{4}{3})^n u(1-n)$ .....         | 1 |
| (b) $x(n) = 2^{- n } + (\frac{1}{3})^{ n }$ ..... | 1 |

Also accessible through [http://www.github.com/soymarwin/ee274/EE274\\_ProgEx03](http://www.github.com/soymarwin/ee274/EE274_ProgEx03)

## A. The Bilateral Z-Transform

(a)  $x(n) = (\frac{4}{3})^n u(1-n)$

$$x(n) = (\frac{4}{3})^n u(-n+1)$$

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) z^{-n}$$

$$X(z) = \sum_{n=-\infty}^{\infty} (\frac{4}{3})^n u(-n+1) z^{-n}$$

$$\text{Let } k = -n + 1 \text{ and } n = 1 - k$$

$$X(z) = \sum_{n=-\infty}^{\infty} (\frac{4}{3})^{1-k} u(k) z^{k-1}$$

$$X(z) = \sum_{n=0}^{\infty} (\frac{4}{3}) \cdot (\frac{4}{3})^{-k} \cdot z^k \times z^{-1}$$

$$X(z) = (\frac{4z^{-1}}{3}) \sum_{n=0}^{\infty} (\frac{3z}{4})^k$$

$$X(z) = \begin{cases} (\frac{4z^{-1}}{3}) \cdot (\frac{1}{1-\frac{3z}{4}}), & \frac{4}{3} > |z| \\ \text{diverges,} & \text{else} \end{cases}$$

$$\text{or } X(z) = \begin{cases} \frac{4z^{-1}}{3-\frac{9z}{4}}, & \frac{4}{3} > |z| \\ \text{diverges,} & \text{else} \end{cases}$$

$$\text{or } X(z) = \begin{cases} \frac{\frac{16z^{-1}}{12z-9z^2}, & \frac{4}{3} > |z| \\ \text{diverges,} & \text{else} \end{cases}$$

$$\text{or } X(z) = \begin{cases} \frac{16}{12z-9z^2}, & \frac{4}{3} > |z| \\ \text{diverges,} & \text{else} \end{cases}$$

(b)  $x(n) = 2^{-|n|} + (\frac{1}{3})^{|n|}$

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