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EE274_ProgEx03

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Also accessible through http://www.github.com/soymarwin/ee274/EE274_ProgEx03.

A. The Bilateral Z-Transform

(a) $x(n) = (\frac{4}{3})^n u(1-n)$

Manual Solution

$$x(n) = (\frac{4}{3})^n u(-n+1)$$

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) z^{-n}$$

$$X(z) = \sum_{n=-\infty}^{\infty} (\frac{4}{3})^n u(-n+1) z^{-n}$$

$$\text{Let } k = -n + 1 \text{ and } n = 1 - k$$

$$X(z) = \sum_{n=-\infty}^{\infty} (\frac{4}{3})^{1-k} u(k) z^{k-1}$$

$$X(z) = \sum_{n=0}^{\infty} (\frac{4}{3}) \cdot ((\frac{4}{3})^{-1})^k \cdot ((1/z)^{-1})^k \cdot z^{-1}$$

$$X(z) = (\frac{4z^{-1}}{3}) \sum_{n=0}^{\infty} (\frac{3}{4z^{-1}})^k$$

$$X(z) = (\frac{4z^{-1}}{3}) \cdot (\frac{1}{1-\frac{3}{4z^{-1}}}), \quad 0 < |z| < \frac{4}{3}$$

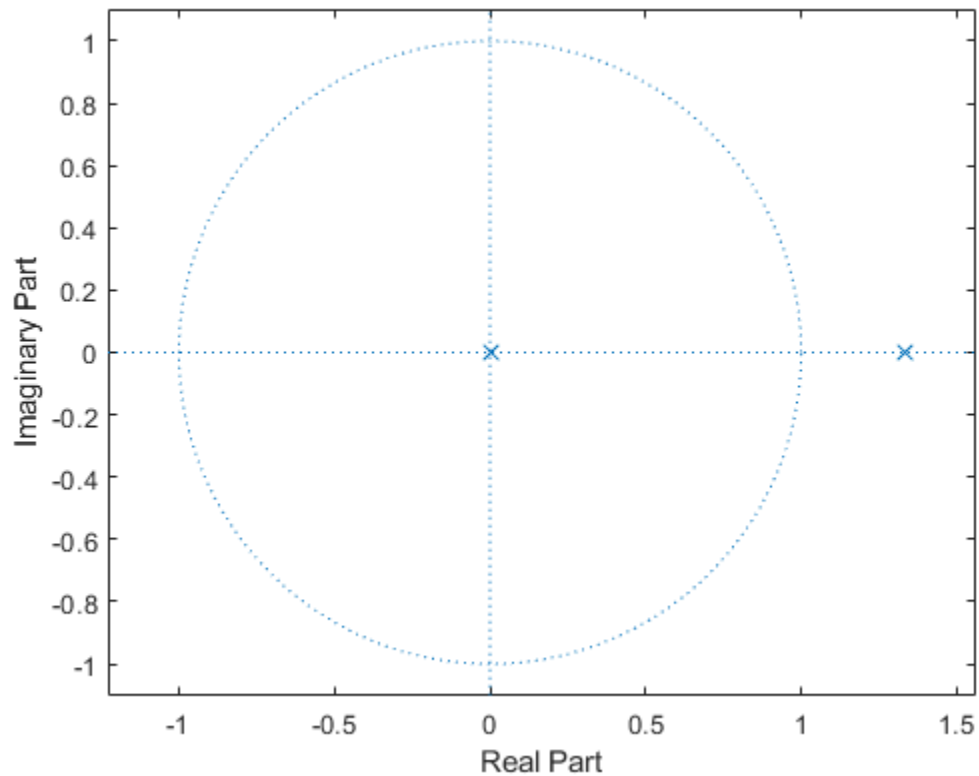
$$\text{or } X(z) = \frac{16z^{-2}}{-9+12z^{-1}}, \quad 0 < |z| < \frac{4}{3}$$

$$\text{or } X(z) = \frac{-16z^{-2}}{9-12z^{-1}}, \quad 0 < |z| < \frac{4}{3}$$

z-plane for 1.(a)

$$A1_a_a = [-9, 12, 0];$$

```
A1_a_b=[0, 0, -16];  
zplane(A1_a_b,A1_a_a);
```



Verification of z-transform v. original sequence with first 8-coef.

```
[delta,n]= impseq(0,0,7);  
A_a_Xz=filter(A1_a_b,A1_a_a,delta) %A_a_Xz is z-transform sequence  
A_a_Xn=[(4/3).^n].*stepseq(1,0,7) %A_a_Xn is the original sequence
```

A_a_Xz =

Columns 1 through 7

0	0	1.7778	2.3704	3.1605	4.2140	5.6187
---	---	--------	--------	--------	--------	--------

Column 8

7.4915

A_a_Xn =

Columns 1 through 7

0	0	1.7778	2.3704	3.1605	4.2140	5.6187
---	---	--------	--------	--------	--------	--------

Column 8

7.4915

Therefore, based on coef values generated from X(z) and x(n), the z-transform for sequence(a) is correct.

$$(b) \quad x(n) = 2^{-|n|} + \left(\frac{1}{3}\right)^{|n|}$$

$$X(z) = \sum_{n=0}^{\infty} 2^{-n} z^{-n} + \sum_{n=0}^{\infty} \left(\frac{1}{3}\right)^n z^{-n}$$

$$X(z) = \sum_{n=0}^{\infty} \left(\frac{z^{-1}}{2}\right)^n + \sum_{n=0}^{\infty} \left(\frac{z^{-1}}{3}\right)^n$$

$$X(z) = \frac{1}{1-\frac{z^{-1}}{2}} + \frac{1}{1-\frac{z^{-1}}{3}}$$

$$X(z) = \frac{2}{2-z^{-1}} + \frac{3}{3-z^{-1}}$$

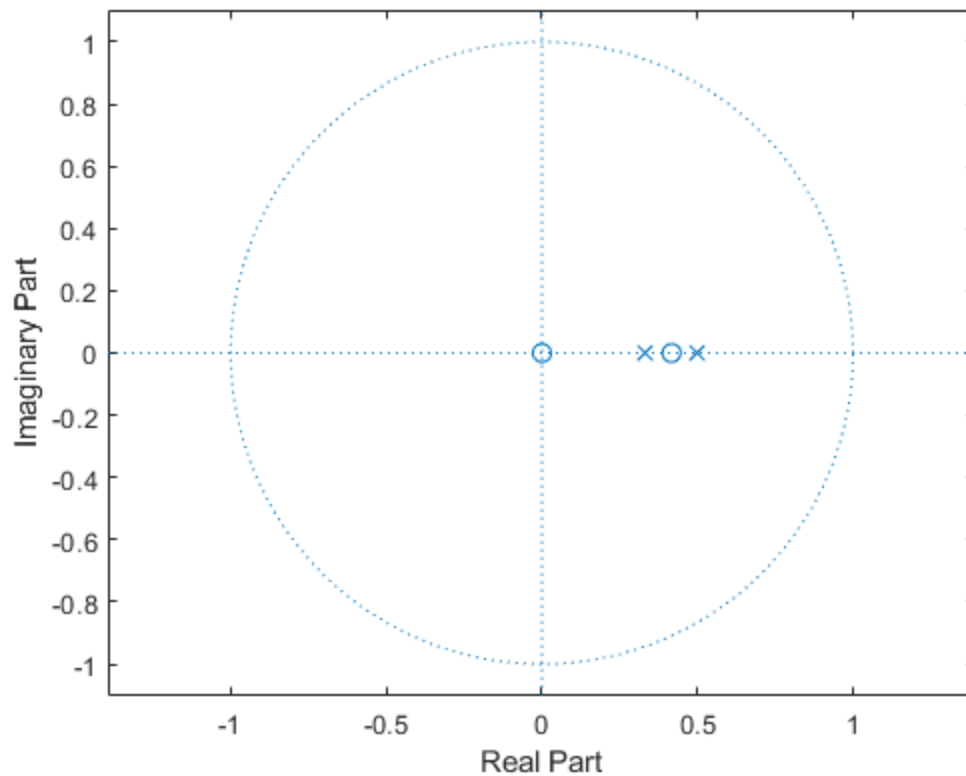
$$X(z) = \frac{12-5z^{-1}}{(2-z^{-1})(3-z^{-1})}, \quad \frac{1}{3} < |z| < \frac{1}{2}$$

$$\text{or } X(z) = \frac{12-5z^{-1}}{6-5z^{-1}+z^{-2}}, \quad \frac{1}{3} < |z| < \frac{1}{2}$$

⌘

z-plane for 1.(b)

```
A1_b_a=[6 -5 1];  
A1_b_b=[12 -5 0];  
zplane(A1_b_b,A1_b_a);
```



Verification of z-transform v. original sequence with first 8-coef.

```
[delta,n]= impseq(0,0,7);
A_b_Xz=filter(A1_b_b,A1_b_a,delta) %A_b_Xz is z-transform sequence
A_b_Xn=((2).^(-abs(n)))+(1/3).^(abs(n))) %A_b_Xn is the original
sequence
```

A_b_Xz =

Columns 1 through 7

2.0000	0.8333	0.3611	0.1620	0.0748	0.0354	0.0170
--------	--------	--------	--------	--------	--------	--------

Column 8

0.0083

A_b_Xn =

Columns 1 through 7

2.0000	0.8333	0.3611	0.1620	0.0748	0.0354	0.0170
--------	--------	--------	--------	--------	--------	--------

Column 8

0.0083

Therefore, based on coef values generated from $X(z)$ and $x(n)$, the z-transform for sequence(b) is correct.

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