

1 Investigation of industrially relevant
2 rheometer geometries for improved
3 scale-up of lamellar structured liquids
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5 Cunningham, Grace E.^{1,2}; Deshpande, Shreyasi²; Simmons, Mark J.H.^{1*}; O'Sullivan, Jonathan J.²

6 ¹ Centre for Formulation Engineering, School of Chemical Engineering, University of
7 Birmingham, Edgbaston, Birmingham, B15 2TT, UK; ² Unilever Research & Development, Port
8 Sunlight Laboratory, Quarry Road East, Bebington, Wirral, CH63 3JW, UK

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10 * Corresponding author. E-mail address: M.J.Simmons@bham.ac.uk (M.J.H. Simmons)

11 **Abstract**

12 Lamellar gel networks (LGNs) are complex multiphase systems comprising the basis of
13 many cosmetic and pharmaceutical formulations, owing to their stability and desirable rheology.
14 There is comparatively little insight into the effects of processing conditions on their final
15 rheological properties. The aim of this work is to determine the dual impact of geometry and
16 processing conditions on mixing efficiency and resultant rheological properties of the LGN. A
17 controlled stress rheometer with three close-clearance agitators were used to prepare LGNs under
18 different processing conditions (temperature, speed, and time) using a fractional factorial design
19 of experiments. Differences between the viscosity-time profiles, power requirements and aged
20 yield stress were used to compare mixing parameters, and compared to previous work using a
21 vane geometry. Mixing time was found to have the largest effect on yield stress ($p = 0.0058$),
22 whilst 3D-ANC and 3D-HR geometries were the only ones which showed a significant difference
23 in yield stress ($p = 0.0392$). The TA-HR produced homogeneous samples with the lowest power
24 input (0.327 J/g), whereas the vane required 1.18 J/g using the same processing conditions.
25 Overall, the study showed that to produce a homogeneous product, a viscosity peak is required
26 before the end of the process. Moreover, a shorter mixing time following the peak viscosity
27 produces a sample with a higher yield stress. The study expands understanding of differences in
28 mixing profiles between geometries during manufacture of LGNs, and how processing conditions
29 can be optimised to generate a higher yield stress system, using less energy.

30

31 **Keywords:** Lamellar structured liquids; Rheological mapping; Rheometer geometries; Process
32 development; Mixing performance

33 1 Introduction

34 The global beauty and personal care market is projected to continue growing to a value of
35 around 758 billion USD by 2025, and in order to remain competitive, businesses must reduce
36 their time to market for new products [1]. Furthermore, with growing supply chain uncertainty
37 due to global instabilities (*e.g.*, pandemics, global conflicts, climate change, *etc.*), it is ever more
38 important to understand how feedstock flexibility (*i.e.*, material changes and variable quality) and
39 process robustness could impact the formulation and properties of manufactured products [2], [3].
40 When a formulated product is brought to market, it is first developed at a traditional laboratory
41 scale (<1kg), before being progressed to a pilot plant environment (5-50kg), and once the
42 formulation and process conditions are confirmed, then deployed to factory-scale at a sourcing
43 unit (>1,000kg). The scale of the process impacts both mixing and temperature profiles
44 experienced by the raw materials, which affects the final product microstructure and physical
45 properties [4]. Having a representative scaled-down version of the manufacturing process would
46 enable improved screening of new ingredients, better understanding of the impact of process
47 conditions on microstructure formation and aid the scale-up process by improving geometric
48 similarity and understanding of power requirements.

49 Previous work by Cunningham *et al.* [5] employed a rheometer to monitor the evolution of
50 the structure of lamellar gel networks (LGNs) as a function of process conditions such as time,
51 agitator speed and temperature. However, one of the limitations of this work was the use of a vane
52 geometry as the agitator. The vane geometry has gained popularity for measuring the yield stress
53 and other rheological properties of complex fluids (*e.g.*, thixotropic, viscoelastic, plastic, *etc.*) due
54 to its ability to inhibit slip, as the shape of the vane generates a cylindrical stress field around the
55 rotating central axis, but the blades of the vane reduce slip compared to a cylindrical Couette
56 geometry [6]. Whilst it is known that in practice this is not always the case, and that there can be
57 mixing between the quadrants of the vane, it would be pertinent to utilise rheometer geometries
58 that both promote mixing and possess geometric similarities to industrial mixing elements [7].
59 Therefore, the main objective of this work was to utilise bespoke rheometer geometries which

60 more accurately reflect the geometric considerations of agitators employed at industrial scale. The
61 study will aim to determine any differences in viscosity profile, mixing efficiencies, power
62 requirements and final product characteristics that arise from using different geometries to
63 manufacture lamellar structured liquids. The application of such capabilities at a rheometer scale
64 could enable such tools to be used for broader process understanding, minimising the number of
65 pilot scale trials that are required, reducing material and energy consumption.

66 2 Materials and Methods

67 2.1 Materials

68 The fatty alcohol (FA) used as part of this study was a commercially available blend of cetyl
69 alcohol (30 wt. %) and stearyl alcohol (70 wt. %) (cetostearyl alcohol) sourced from Godrej
70 Industries (India). The surfactant used was behentrimonium trimethyl ammonium chloride
71 (BTAC), supplied by Clariant International Ltd. (Germany). This surfactant is provided at 70 wt.
72 % purity, where the remaining 30 wt. % is comprised of dipropyl glycol. Distilled water was used
73 for all experiments.

74 2.2 Preparation of lamellar structured liquids

75 A Discovery HR-III stress controlled rheometer (TA Instruments, UK) was used to prepare
76 the lamellar structured liquids according to the methods given in [5], with some slight differences.
77 In this work, three, new different geometries were investigated: TA helical rotor (TA Instruments,
78 part no. 546018.901), 3D printed helical ribbon, and 3D printed anchor scraper (Figure 1) where
79 the 3D printing process was direct metal laser sintering of titanium conducted by Laser Prototypes
80 Europe Ltd (UK). The geometric considerations for the bespoke mixing elements were based on
81 representative pilot-scale examples.

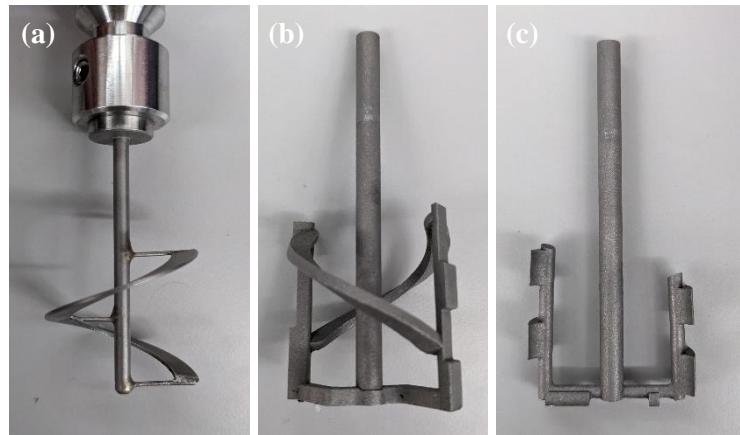


Figure 1 – (a) TA Instruments helical rotor (TA-HR), (b) 3D printed helical ribbon (3D-HR), and (c) 3D printed anchor (3D-ANC)

82

83 Similar to the previous study [5], variables were changed during the structuring stage of the
 84 process (addition of BTAC to a molten mix of FA and water). A fractional factorial design of
 85 experiments was used to investigate the effects of process temperature (T , $^{\circ}\text{C}$), agitator speed (N ,
 86 rad s^{-1}) mixing time (t , min) and rheometer geometry (Table 1). Process conditions utilised in the
 87 previous study have been repeated in this work to enable direct comparison. Two temperatures
 88 from the previous work were selected for further investigation - the reference temperature, and
 89 the highest temperature (referred to in this work as $T = \text{REF}$, $T = \text{HIGH}$, respectively) [5].
 90 Furthermore, it should be noted that angular velocity has been used to quantify agitator speed
 91 rather than shear rate, in order to directly compare differences in speed across different
 92 geometries.

93

94 *Table 1. Fractional factorial design of experiments of process variables (geometry, temperature, agitator speed and*
 95 *time) for the structuring stage of lamellar gel formation. Sample naming system is*
 96 *Geometry_Temperature_Speed_Time*

Sample	Rheometer geometry	Temperature (-)	Speed (rad s ⁻¹)	Time (min)
3D-HR_REF_48_30	3D-HR	REF	48	30
TA-HR_REF_16_30	TA-HR	REF	16	30
3D-ANC_REF_16_30	3D-ANC	REF	16	30
TA-HR_REF_48_10	TA-HR	REF	48	10
TA-HR_HIGH_48_30	TA-HR	HIGH	48	30
TA-HR_HIGH_16_10	TA-HR	HIGH	16	10
3D-ANC_HIGH_48_10	3D-ANC	HIGH	48	10
3D-ANC_REF_48_10	3D-ANC	REF	48	10
3D-HR_HIGH_48_30	3D-HR	HIGH	48	30
3D-ANC_HIGH_16_30	3D-ANC	HIGH	16	30
3D-HR_REF_16_10	3D-HR	REF	16	10
3D-HR_HIGH_16_10	3D-HR	HIGH	16	10
3D-HR_REF_16_30	3D-HR	REF	16	30

97

98 2.3 Calibration of Rheometer Geometries

99 The TA-HR, 3D-HR, and 3D-ANC were calibrated using the Couette analogy as
 100 recommended by the rheometer equipment supplier, TA Instruments [8], and described by Ait-
 101 Kadi *et al.* [9]. The calibration fluid was glycerine (Palmera G995E; >99.5% purity; supplied by
 102 KLK Oleo; viscosity at 0.25°C = 0.95 Pa s). The values calculated for the shear stress constant
 103 (K_τ) and the shear rate constant ($K\gamma$) are given below in Table 2.

104 *Table 2. Summary of shear rate and shear stress constants for the different geometries investigated*

Geometry	Shear stress constant (Pa. Nm)	Shear rate constant (rad ⁻¹)
Vane	16141	12.21
3D-ANC	23836	3.43
3D-HR	21891	4.51
TA-HR	26800	2.46

105

106 2.4 Rheological and Homogeneity Characterisation of LGN Samples

107 The samples were characterised by measuring rheological properties and visual assessment
 108 of homogeneity, in addition to the in-situ process data that was captured during the manufacture
 109 of the LGN samples. Rheological characterisation of all samples was carried out using the

110 Discovery DHR-III stress controlled rheometer (TA Instruments, UK) equipped with cross-
111 hatched parallel plates to minimise slip effects. All measurements were carried out at 25°C on
112 samples aged for at least 24 h. The yield stress was measured using an oscillation amplitude sweep
113 method described in [5], [10]. A visual assessment of homogeneity was carried out by spreading
114 *ca.* 1 g sample of LGN to a thickness of *ca.* 1 mm on to a matte black tile and observing for both
115 lumps of unincorporated FA or BTAC, and opacity.

116 **2.5 Statistical Analysis**

117 All samples were manufactured in triplicate, and an average of the viscosity profile is
118 presented in this work. In addition, yield stress measurements were completed in triplicate
119 (individual measures on samples prepared in triplicate) and an average and standard deviation is
120 presented. ANOVA was used to determine the difference between single effects on single outputs,
121 where a 95% confidence interval was employed, and data was considered statistically significant
122 when $p < 0.05$.

123 3 Results & Discussion

124 3.1 Comparison of viscosity-time profiles of industrially relevant
125 geometries to vane geometry

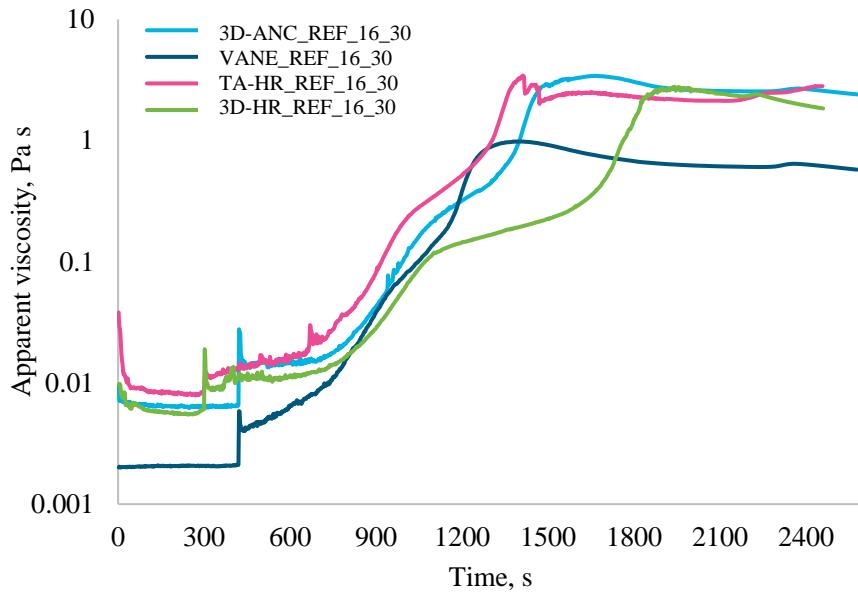


Figure 2. Viscosity profiles for samples prepared at $T=REF$, $N = 16 \text{ rad s}^{-1}$, $t = 30 \text{ min}$

126 The impact of different rheometer geometries (vane, 3D-ANC, TA-HR, 3D-HR) on the
127 formation of lamellar gel structure was initially investigated at the same processing conditions of
128 $T=REF$, $N=16 \text{ rad s}^{-1}$, $t=30 \text{ min}$ (*i.e.*, REF_16_30 according to the naming convention used).

129 Figure 2 shows the viscosity profiles for these samples (VANE_REF_16_30, 3D-
130 ANC_REF_16_30, TA-HR_REF_16_30, 3D-HR_REF_16_30). In general, the viscosity profiles
131 predominantly follow the same trend of a slow initial increase in viscosity, followed by two
132 changes in the rate of viscosity increase, before reaching a peak value. After this point, the
133 viscosity plateaus until the cooling stage commences, where there is another slight peak.
134 However, the rate of viscosity increase, and the point at which the system reaches the peak
135 viscosity varies between geometries. The relationship between viscosity and structure formation
136 has been discussed previously by Cunningham *et al.* [5].

137 Whilst they generally follow the same trend, the viscosity measurements for 3D-ANC and
138 TA-HR were significantly greater than for the vane throughout the process, where this can be

139 accounted for by the difference in shear rate constants for the different geometries (Table 2). The
140 equivalent shear rate for the same speed was at least three times higher for the vane than the other
141 investigated geometries; thus, for a shear thinning LGN system, the apparent viscosity was lower
142 (Figure 2) [11]. However, it would be expected that the viscosity values for 3D-HR would also
143 be similar to the 3D-ANC based on their similar shear rate constants. The viscosities start at
144 similar values, but around 900 s, the rate of viscosity increase is much slower for the 3D-HR than
145 the 3D-ANC, and the 3D-HR does not achieve the peak viscosity until much later than the rest of
146 the samples (1942 s). The peak viscosities for the vane and TA-HR occur around the same time
147 (1400 s, 1414 s, respectively), whilst the peak viscosity for 3D-ANC occurs later (1670 s). If we
148 consider the time of peak viscosity as an indicator of mixing efficiency, the vane and TA-HR are
149 the most efficient, followed by 3D-ANC and then 3D-HR.

150 For the sample prepared using the TA-HR, after the peak viscosity ($t = 1414$ s), there are two
151 perturbations in the curve. This behaviour is thought to be associated with when the system
152 became too viscous at the peak viscosity for the TA-HR to mix the fluid properly, as it was
153 visually observed that the material started moving as a solid body in the vessel and this was seen
154 for the other investigated process conditions with the TA-HR geometry. This issue could
155 potentially be resolved using a serrated or roughened cup to reduce slip effects. The shear rate
156 constant for the TA-HR is the lowest for all the geometries investigated (Table 2), which means
157 that for the same speed, the least power is inputted into the system in comparison to the other
158 investigated geometries. Mihailova *et al.* [12] noted a relationship between the torque and power
159 requirements and the surface area of the agitator which is in contact with the liquid, where a larger
160 surface area provides greater resistance to motion, and thus a higher torque response. A similar
161 relationship has been seen in this work, in which the TA-HR has the smallest surface
162 area and smallest power draw, and this is reflected in the value of the shear rate constant (Table
163 2).

164 The peak viscosity value was lowest for the sample prepared with the vane (0.99 Pa s), as
165 expected due to the difference in shear rate constants previously discussed. However, when

166 comparing the three industrially relevant geometries, the peak viscosity for 3D-HR (2.78 Pa s)
167 was lower than that for 3D-ANC and TA-HR (3.43 Pa s and 3.45 Pa s, respectively). This, in
168 addition with the longer time to achieve peak viscosity again suggests poorer mixing by the 3D-
169 HR geometry than by the 3D-ANC and TA-HR.

170 Nevertheless, the yield stress of the samples discussed here, prepared at the same processing
171 conditions, were not significantly different ($p > 0.05$; vane = 108 ± 5 Pa; 3D-ANC = 111 Pa, TA-
172 HR = 106 Pa, 3D-HR = 108 Pa).

173 The energy required to achieve the peak viscosity is similar for the vane and the 3D-ANC,
174 but not for TA-HR (vane = 1.18 J/g, 3D-ANC = 1.18 J/g, TA-HR = 0.327 J/g). Again, this suggests
175 that the TA-HR promotes better mixing than the anchor and the vane and is able to achieve
176 homogeneity with a smaller power input. For the process conditions discussed above, the
177 geometry appears to have minimal effect on the type of structure formed, or the final rheological
178 properties of the system (yield stress), but does affect the mixing characteristics, evidenced by the
179 difference in times to achieve peak viscosity and the inflections in the viscosity-time profile for
180 the TA-HR, in comparison to the other investigated geometries (Figure 2).

181 3.2 Effect of mixing time on LGN formation

182 In [5], the conditions which provided the highest yield stress sample were T = REF, N = 16
183 rad s⁻¹, t = 10 min. Thus, it was hypothesised that a shorter mixing time would also increase the
184 yield stress for the geometries investigated in this study. Figure 3 shows the viscosity profiles for
185 four samples prepared with a 10 minute structuring stage time and 16 rad s⁻¹ agitator speed (vane
186 and 3D-HR at T=REF, TA-HR and 3D-HR at T=HIGH).

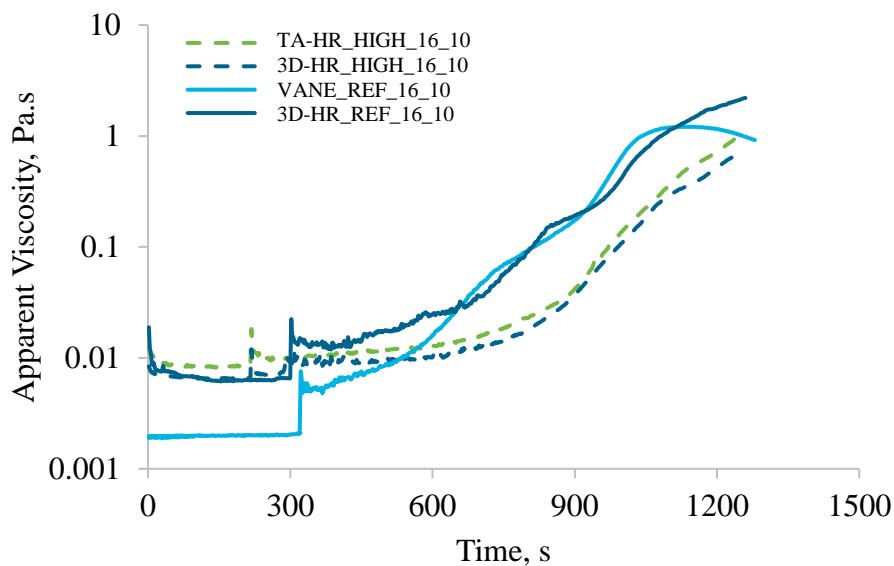


Figure 3. Viscosity-time profiles for samples with 10 minute mixing time and 16. rad.s⁻¹ agitator speed

187 Firstly, examining the vane geometry at T=REF, the system reached a peak viscosity before
188 the end of the process and had started to plateau. However, for the 3D-HR, the viscosity of the
189 system is still increasing at the end of the processing time and has not stabilised, resulting in
190 inhomogeneous final samples (Figure 4). The same result is seen at T=HIGH. The viscosity
191 profiles for the TA-HR and 3D-HR are very similar to each other, suggesting a similar mixing
192 profile, but again there is a failure to achieve a peak viscosity value resulting in inhomogeneous
193 samples. The failure to achieve homogeneity could be related to the energy input to the system.
194 For the vane geometry, the energy input to the peak was 1.24 J/g, and the total energy input 1.95
195 J/g. For the 3D-HR, the total energy input is 0.71 J/g at T=REF and 0.2 J/g at T=HIGH, and for
196 TA-HR, 0.18 J/g, which are all considerably lower. Whilst the energy input is an important factor,
197 it is known from the previous discussion of sample TA-HR_REF_16_30 (*cf.*, 3.2) that it cannot

198 be used to quantify mixing efficiency in these geometries, as the TA-HR is capable of producing
199 similar viscosity profiles and homogenous samples with lower energy inputs than the other
200 investigated geometries.

201 The effect of temperature can be seen by the differences in the 3D-HR samples prepared at
202 T=REF and T=HIGH. The higher processing temperature demonstrates apparent viscosity as a
203 function of time (Figure 3). It is difficult to decouple the temperature effects on the viscosity of
204 the continuous phase vs. the differences in LGN microstructure that are formed. Typically,
205 differences in yield stress of the final sample would give an indication of differences in
206 microstructure formation, however as both samples were inhomogeneous, it is difficult to make
207 direct comparisons. Examples of homogeneity of the samples listed in Table 1 are provided in
208 Figure 4 using the methodology outlined in section 2.4.

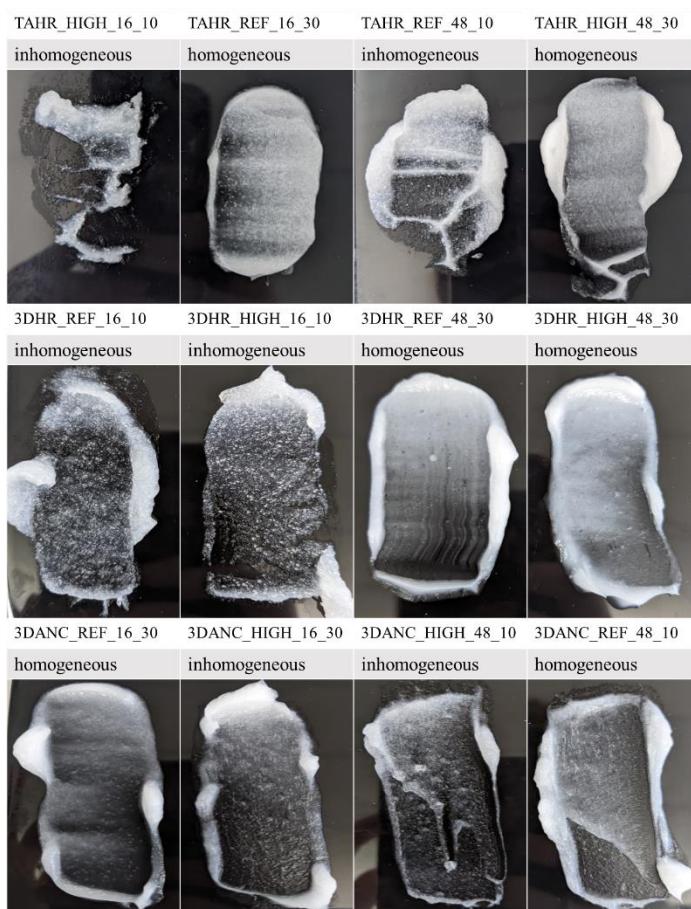


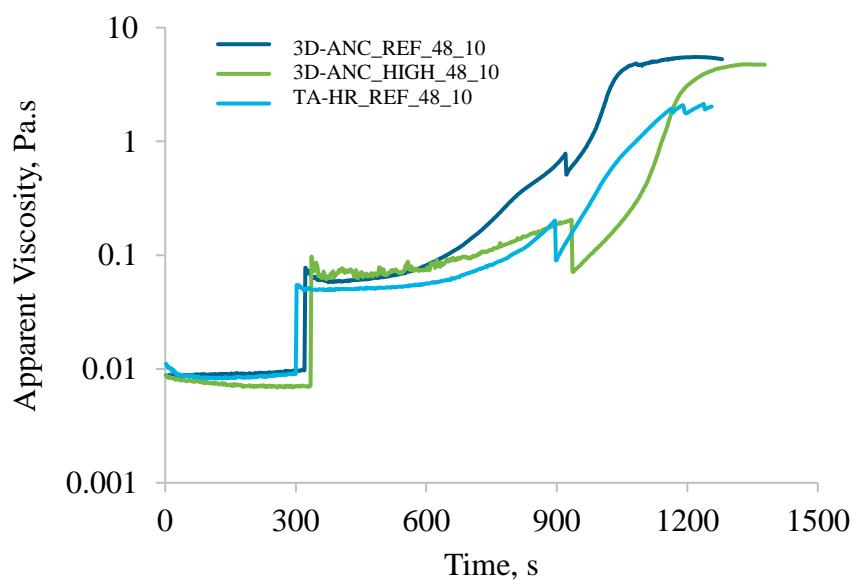
Figure 4. Images of samples detailed in Table 1 showing the degree of homogeneity, where each sample is categorised as homogenous or inhomogeneous based on number of particulates observed

209

210 There was a clear effect of mixing time on the homogeneity of the samples that were
211 prepared, whereby all samples that were produced with a mixing time of 30 min were classified
212 as homogeneous, in contrast to samples with a mixing time of 10 min of which 83.33% were
213 categorised as inhomogeneous, regardless of investigated mixing geometry and processing
214 temperature (Figure 4). This behaviour was ascribed to insufficient time being provided to achieve
215 adequate mixing of the system and achievement of a peak viscosity before cooling, as previously
216 discussed (Figure 3). Excluding the yield stress values for the inhomogeneous samples, mixing
217 time also had a significant effect on the yield stress of the final samples ($p = 0.0058$), where the
218 mean yield stress was higher for the samples produced with a 10 minute mixing time (149 Pa)
219 than the 30 minute mixing time (114 Pa).

220 3.3 Effect of agitator speed on LGN formation

221 When the agitator speed was increased from 16 rad s^{-1} to 48 rad s^{-1} , more power was imparted
222 to the system. Three samples were prepared at 48 rad s^{-1} and 10 min mixing time (Table 1), shown
223 in Figure 5.



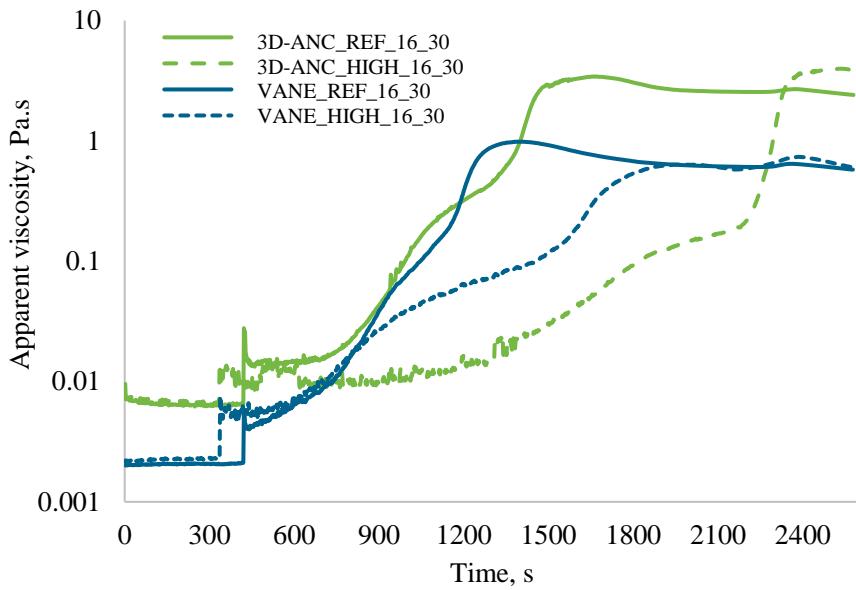
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225 *Figure 5. Viscosity-time profiles of samples prepared with 10 min mixing time and 48 rad.s^{-1} agitator speed (3D-ANC_REF_48_10, 3D-ANC_HIGH_48_10, TA-HR_REF_48_10)*

226 For sample 3D-ANC_HIGH_48_10 and TA-HR_REF_48_10, the viscosity has not achieved
227 a plateau by the end of the process, and the resulting LGN samples are inhomogeneous (*cf.*,Figure
228 4). However, for 3D-ANC_REF_48_10, the peak viscosity occurs before the end of the 10 min
229 processing time, resulting in a homogeneous sample (*cf.*, Figure 4). The energy input to the peak
230 viscosity for 3D-ANC_REF_48_10 was 1.33 J/g, and the sample possessed a final yield stress of
231 141 Pa (the second highest yield stress for the homogeneous samples). This supports the
232 hypothesis in [5] that a reduced processing time increases the final yield stress of the sample (vane
233 yield stress at same conditions = 139 Pa). Due to the nature of the fractional factorial design of
234 experiments, data for the 3D-ANC at lower processing speeds and 10-minute mixing time was
235 not conducted. At other processing conditions, the 3D-ANC has outperformed the 3D-HR,
236 however it is thought that based on the results for the 3D-HR, which possess a similar shear rate
237 constant (Table 2), that the mixing would not be sufficient at 16 rad s⁻¹, 10 mins to produce a
238 homogeneous sample (Figure 4).

239 3.4 Effect of processing temperature on LGN formation

240 Viscosity profiles for the vane and 3D-ANC at two different temperatures (T=REF and
241 T=HIGH) are shown in Figure 6, where the mixing time and agitator speed were the same for
242 each trial, 30 min and 16 rad s⁻¹, respectively. Distinct differences were demonstrated on the rate
243 of viscosity increase during the process due to the dual effect of temperature and mixer type (vane
244 and the anchor geometry).



245

Figure 6. Viscosity-time profiles for samples prepared at different temperatures using the vane and 3D-ANC (Table 1)

246

247 For the vane geometry, structure formation occurred at a faster rate when the temperature
 248 was at T=REF, however ultimately the final viscosity of the samples was similar for both
 249 investigated temperatures (Figure 6). This was reflected in the final characteristics of the sample,
 250 where the yield stresses were not significantly different ($p > 0.05$; T=REF = 108 ± 3 Pa; T=HIGH
 251 = 104 ± 5 Pa). A comparison between the 3D-ANC and vane at T=REF have already been
 252 discussed (*cf.*, 3.1); whilst the apparent viscosity appeared higher for 3D-ANC, the samples had
 253 similar final yield stress values, suggesting that this is due to the lower shear rate constant for the
 254 3D-ANC compared to the vane, and the peak viscosity for the 3D-ANC was achieved later,
 255 suggesting better mixing in the vane system.

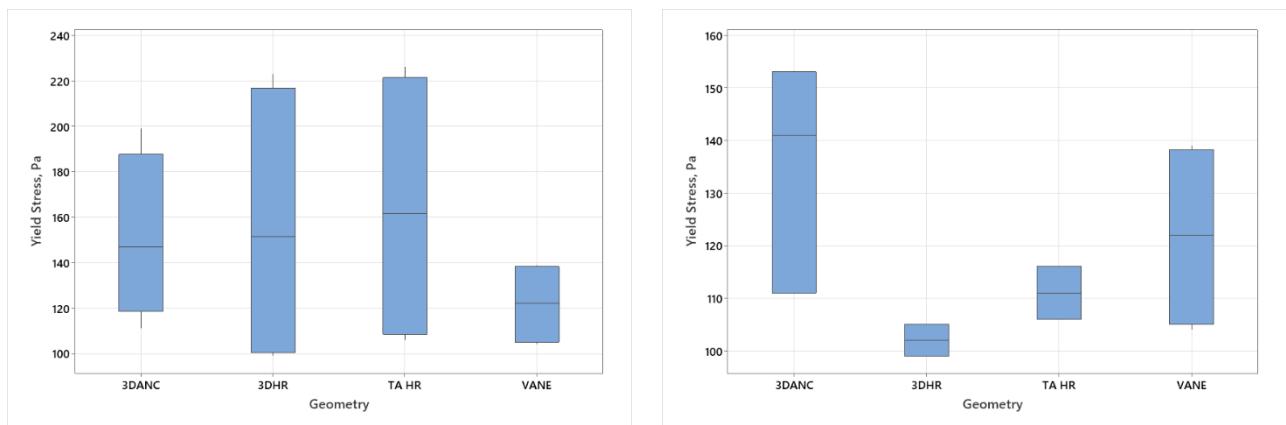
256 Interesting behaviour was seen for the 3D-ANC at T=HIGH, which did not have repeatable
 257 viscosity profiles. In the sample shown here, initially the apparent viscosity was lower for the 3D-
 258 ANC in comparison to the vane, and there were fluctuations in the data until the process achieved
 259 the cooling stage (*ca.* 2,100s). At this point, the viscosity of the system drastically increased, and
 260 the final apparent viscosity was higher than for the sample prepared at T=REF. This correlated
 261 with the yield stress of the final product, which was significantly higher for 3D-

262 ANC_HIGH_16_30 (153 Pa s) than the VANE_HIGH_16_30 (104 \pm 5 Pa) and 3D-
263 ANC_REF_16_30 (111 Pa). However, in another repeat of these conditions (data not shown
264 here), the viscosity did not increase at \sim 2100s, and stayed within the same order of magnitude.
265 This produced a sample which was not homogeneous and on visual inspection, a large lump of
266 fats had collected around the central shaft of the agitator. Perhaps the lower viscosity of the system
267 resulted in a tangentially or radially dominant mixing regime which meant the fats were not able
268 to be incorporated properly [13].

269

270 3.5 Effect of processing variables on final product yield stress of LGNs

271 Figure 7a shows the range of yield stress measurements for the samples collected for each
272 geometry type for all process conditions, including samples which were not homogeneous (Figure
273 4). The differences in means of the yield stresses of the samples produced using each geometry
274 were not significantly different ($p = 0.645$ using ANOVA). However, this does not preclude the
275 fact that the geometries perform differently at different process conditions, evidenced by the range
276 of yield stresses, and the fact that the means have been compared across different process
277 conditions.



278 *Figure 7. Box plot of yield stress measurements of final product samples by geometry type ((a) including heterogeneous samples; (b)
279 excluding heterogeneous samples)*

278 It should be noted that the majority of the high yield stress measurements were for samples
279 which were inhomogeneous, and the high value was likely due to the fact that the LGN
280 microstructure had not been fully formed. The presence of unincorporated solid fatty alcohol and

281 surfactant in the sample causes jamming in the rheometer and affects the measurement (Figure
282 4). Examining examples of amplitude sweeps, the difference between the loss modulus (G'') and

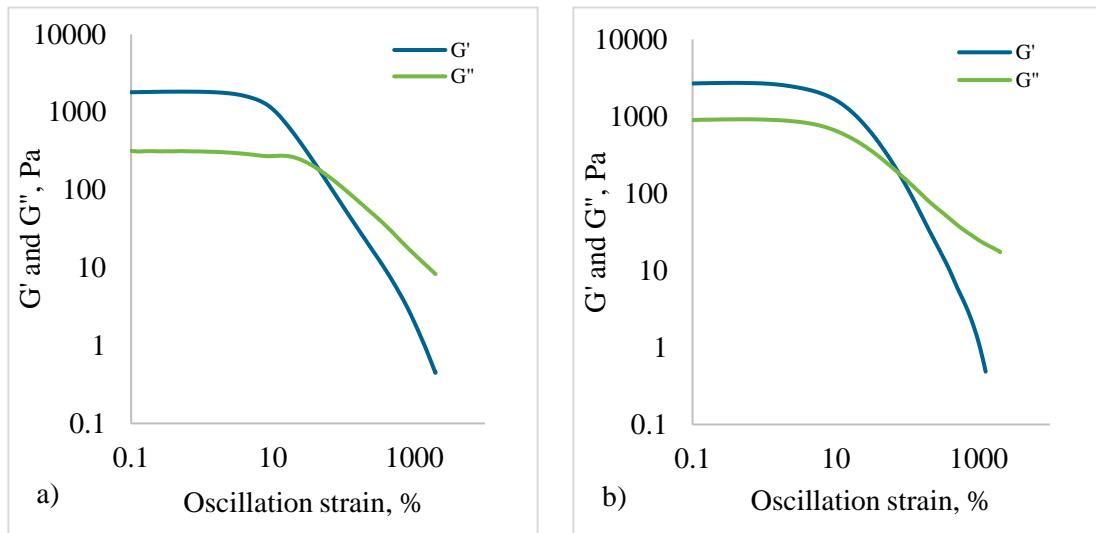


Figure 8. a) Oscillation amplitude sweep for 3D-HR_REF_16_30 b) Oscillation amplitude sweep for 3D-HR_REF_16_10

283 storage modulus (G') were smaller for samples that were processed with a 10 min mixing time,
284 which suggests less viscoelasticity (Figure 8b). Conversely, for a sample which was processed
285 with a 30 min mixing time, it exhibited the characteristic overshoot in the loss modulus prior to
286 the cross over-point, which depicts the breakdown of a cross-linked gel structure, similar to that
287 observed for LGNs (Figure 8a) [13].

288 Further analysis of the effect of geometry on yield stress was conducted, excluding the
289 inhomogeneous samples (Figure 7b) comparing the mean yield stress for each geometry when
290 samples are prepared at a range of conditions, the 3D-ANC is highest (137 Pa), followed by the
291 vane (121.75 Pa), TA-HR (111 Pa), 3D-HR (104 Pa). This could be due to effects of the fractional
292 factorial design, where optimal processing conditions have been randomly selected for certain
293 geometries; but does suggest that generally the 3D-ANC is capable of producing samples with
294 higher yield stresses. Using a student's t-test, it was also shown that the yield stresses were
295 significantly different for 3D-ANC and 3D-HR ($p = 0.0392$).

296

297 4 Conclusions

298 This study monitored the structure formation of lamellar gel liquids in-situ using a rheometer
299 with different mixing rheometer geometries: conventional four-bladed vane, commercially
300 available helical rotor (TA-HR) and two bespoke geometries, 3D printed in titanium, a helical
301 ribbon (3D-HR) and an anchor scraper (3D-ANC). Viscosity-time profiles as a function of process
302 variables and yield stress measurements on manufactured samples as per design of experiments
303 were used to assess the impact of changing geometry. The results suggested that there were
304 differences in the mixing capability of each investigated geometry, particularly for short
305 processing times. For the 10 min samples prepared at 16 rad s^{-1} , the 3D-HR and TA-HR were not
306 capable of producing a homogeneous sample, whereas the vane was (3D-ANC was not tested at
307 these conditions due to the nature of the fractional factorial design of experiments). This was
308 likely due to differences in energy input into the system which was related to the shape, mass, and
309 surface area of the rheometer geometry. The two samples with the highest yield stresses (which
310 were homogeneous) were both produced using the 3D-ANC, yet at different process conditions
311 (3D-ANC_HIGH_16_30 = 153 Pa; 3D-ANC_REF_48_10 = 141 Pa). The energy input to the
312 peak viscosity for these samples was 1.152 J/g and 1.327 J/g, respectively. Hence, the longer
313 mixing time at a lower speed was more energy efficient for this geometry. Overall, the industrially
314 relevant geometries did not follow the same trends as the vane geometry, highlighting the
315 importance of investigating how the mixing characteristics are affected by the interplay between
316 geometry and processing conditions. The next steps for this work are to utilise the information
317 collected to generate information around the power requirements of each type of geometry, and
318 how this could be optimised to produce an LGN which is homogenous, achieves peak viscosity
319 efficiently and possessing a high yield stress, with the lowest possible energy consumption. Power
320 numbers for the geometries will be generated in order to determine the usefulness of this technique
321 in scale-up. Overall, the application of industrially relevant geometries has provided a better
322 insight into how the combination of processing conditions and geometry can result in different
323 mixing characteristics within the vessel, and the resulting impact on the product characteristics.

324

Acknowledgments

325 The authors would like to acknowledge Darren Lamb, Emily Robinson, Serena Todd, and
326 Adam Rowatt from University of Strathclyde for their support designing the bespoke mixing
327 elements, and Alan Magowan from Laser Proto Europe Ltd for providing 3D printing services.
328 Additionally, the authors acknowledge financial support received from the Centre for Doctoral
329 Training in Formulation Engineering (EPSRC grant no.EP/S023070.1)

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Conflict of Interest Statement

331 The authors declare that they have no known competing financial interests or personal
332 relationships that could have appeared to influence the work reported in this paper.

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