<과제물 작성시 주의사항>

[공통]

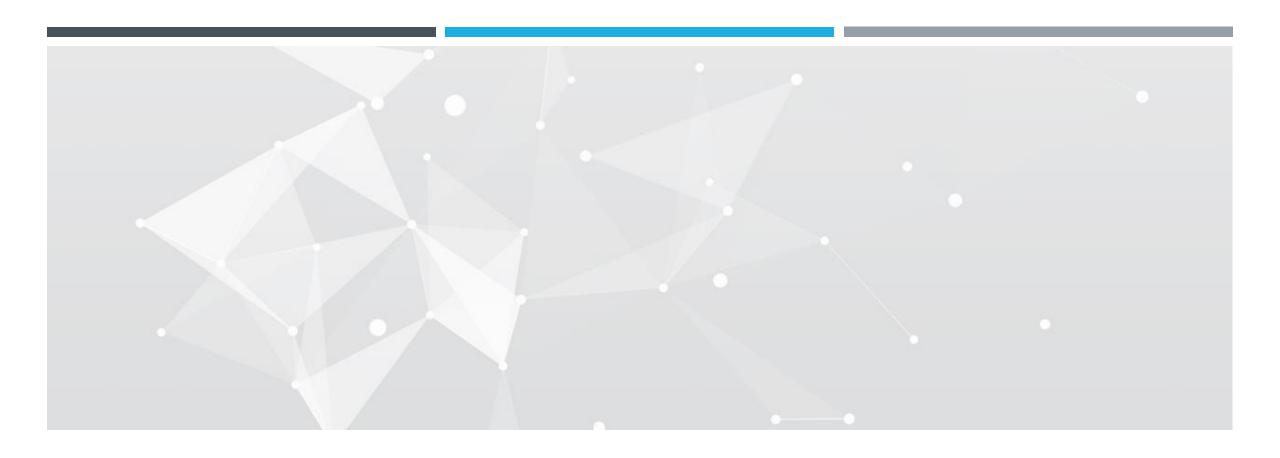
과제물 제출시 완성된 소스파일 및 보고서를 반드시 'HW_02_학번.zip' 형식으로 압축하여 첨부합니다. (이름 약어.py, HW_02_학번.pdf)

[소스파일]

- 1. 소스파일은 .py파일만 작성하며 반드시 문제에서 지시 또는 요구한 조건에 맞추어서 작성합니다.
- (jupyter로 작성하였어도 코드를 제출 시 py파일로 작성하여 제출하여야 합니다.)
- 2. 각 코드마다 반드시 주석을 달아 주셔야 합니다. 주석을 달지 않을 경우, 부분적으로 감점이 있을 수 있습니다. 이번 과제 특히
- 3. 결과가 올바르더라도 과정이 옳지 않을 경우, 부분적으로 감점이 있을 수 있습니다.
- 4. 제출한 파일이 실행되지 않을 경우, 제출한 과제물은 0점 처리됩니다.

[보고서]

- 1. PDF로 제출하며, 표지를 포함해야 합니다.
- 2. 보고서에는 (과제 제목 및 목적), (소스 코드에 대한 설명), (실행 결과 + Plot), (참고문헌)이 포함되어야 합니다.
- 3. 자신의 코드에 대한 설명이 명확하지 않거나 copy한 글이라면 0점 처리됩니다.
- 4. 실행 결과는 실행 결과를 캡처하여 첨부하도록 합니다.
- 5. 참고문헌은 반드시 적어도 한 개 이상을 명시하여야 합니다.



Machine learning homework-2

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You should build 6 python functions at Name.py

| | initialization | (10 points) |
|---|------------------------------------|-------------------------------------|
| ٠ | multivariate_gaussian_distribution | (10 points) |
| • | expectation | (20 points) |
| ٠ | maximization | (20 points) |
| • | fit | (20 points) |
| | plotting | (20 points) including report scores |

- An unclear comment is a deduction factor 科ない
- Implement using Python built-in functions and Numpy functions only + plotting methods

SYC

- Submission : change below files to zip file and submit it by KLAS
 - Name.py (please change CSL.py to your name.py)
 - E.g. if your name is 홍길동 --> (CSL.py --> GDH.py)
 - HW_02_student ID.pdf (E.g. HW_02_202110605.pdf) <= report</p>

Algorithm 1: EM algorithm for GMM **Input** : a given data $X = \{x_1, x_2, ..., x_n\}$ **Output**: $\pi = \{\pi_1, \pi_2, ..., \pi_K\},$ $\mu = \{\mu_1, \mu_2, ..., \mu_K\},\$ $\Sigma = \{\Sigma_1, \Sigma_2, ..., \Sigma_K\}$ 1 Randomly initialize π, μ, Σ — Initialize 2π 2 for t = 1 : T do // E-step for n = 1 : N do for k = 1 : K do $\gamma(z_{nk}) = \frac{\pi_k N(x_n | \mu_k, \Sigma_k)}{\sum_{i=1}^K \pi_i N(x_n | \mu_i, \Sigma_i)}$ end 7 end 8 // M-step for k = 1 : K do $\mu_{k} = \frac{\sum_{n=1}^{N} \gamma(z_{nk}) x_{n}}{\sum_{n=1}^{N} \gamma(z_{nk})}$ $\Sigma_{k} = \frac{\sum_{n=1}^{N} \gamma(z_{nk}) (x_{n} - \mu_{k}) (x_{n} - \mu_{k})^{T}}{\sum_{n=1}^{N} \gamma(z_{nk})}$ 11 end

- See comments for additional information
- In initialization step line 1
- Initialize (mean) sigma, and pi values



```
Algorithm 1: EM algorithm for GMM
   Input : a given data X = \{x_1, x_2, ..., x_n\}
   Output: \pi = \{\pi_1, \pi_2, ..., \pi_K\},
              \mu = \{\mu_1, \mu_2, ..., \mu_K\},\
              \Sigma = \{\Sigma_1, \Sigma_2, ..., \Sigma_K\}
1 Randomly initialize \pi, \mu, \Sigma
2 for t = 1 : T do
       // E-step
       for n = 1 : N do
            for k = 1 : K do
            end
        end
8
       // M-step
       for k = 1 : K do
11
       end
15 end
```

$$g_{(\mu,\Sigma)}(\mathbf{x}) = \frac{1}{\sqrt{2\pi}^d \sqrt{\det(\Sigma)}} e^{-\frac{1}{2}(\mathbf{x}-\mu)^T \Sigma^{-1}(\mathbf{x}-\mu)}$$

- In multivariate_gaussian_distribution_
- Since iris has four features, a multivariate normal distribution(MVN) should be used
- Use the linear algebraic functions of Numpy

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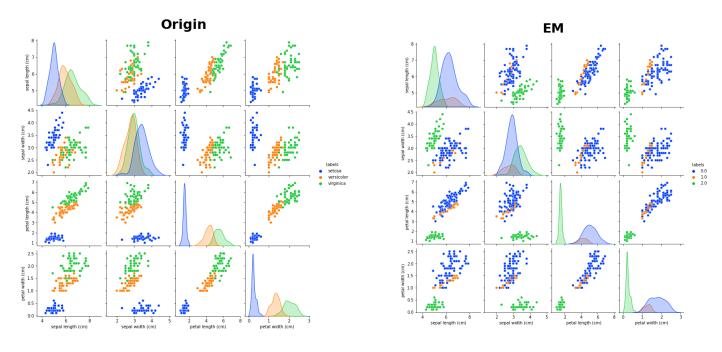
- In expectation step line 4~8
- Use MVN to calculate a posterior probability

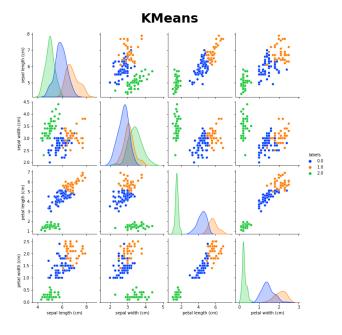
Algorithm 1: EM algorithm for GMM **Input** : a given data $X = \{x_1, x_2, ..., x_n\}$ Output: $\pi = \{\pi_1, \pi_2, ..., \pi_K\},\$ $\mu = \{\mu_1, \mu_2, ..., \mu_K\},\$ $\Sigma = \{\Sigma_1, \Sigma_2, ..., \Sigma_K\}$ 1 Randomly initialize π, μ, Σ 2 for t = 1 : T do // E-step for n = 1 : N do for k = 1 : K do $\gamma(z_{nk}) = \frac{\pi_k N(x_n | \mu_k, \Sigma_k)}{\sum_{i=1}^K \pi_i N(x_n | \mu_i, \Sigma_i)}$ end end 8 // M-step for k = 1 : K do11 end

- In maximization step line 10~14
- Use the posterior probability to calculate the parameters for MVN

Algorithm 1: EM algorithm for GMM **Input** : a given data $X = \{x_1, x_2, ..., x_n\}$ **Output**: $\pi = \{\pi_1, \pi_2, ..., \pi_K\},$ $\mu = \{\mu_1, \mu_2, ..., \mu_K\},\$ $\Sigma = \{\Sigma_1, \Sigma_2, ..., \Sigma_K\}$ 1 Randomly initialize π, μ, Σ 2 for t = 1 : T do // E-step for n = 1 : N do for k = 1 : K do $\gamma(z_{nk}) = \frac{\pi_k N(x_n | \mu_k, \Sigma_k)}{\sum_{i=1}^K \pi_i N(x_n | \mu_i, \Sigma_i)}$ end end 8 // M-step for k = 1 : K do11 end

- In fit clustering line 1 ~ 15
- Repeat the preceding functions to find the final posterior
- Implement termination conditions (Shallow copy caution)





- In plotting function
- Implement a plot function for comparison
- The default is pairplot
- The plot should be attached to your report
- It's 20 points, including the report score

RESULT

Print out the results at least 10 times and write them in the report with plot figures

```
In [1]: runcell(0, 'C:/Users/() 各台/Desktop/solution.py')
pi: [0.36747348 0.29919319 0.33333333]
count / total : [0.36666667 0.3 0.33333333]
EM Accuracy: 0.97 Hit: 145 / 150
KM Accuracy: 0.89 Hit: 134 / 150
```

```
In [4]: runcell(0, 'C:/Users/이충설/Desktop/solution.py')
pi : [0.35431522 0.33319345 0.31249134]
count / total : [0.35333333 0.33333333 0.31333333]
EM Accuracy: 0.82 Hit: 123 / 150
KM Accuracy: 0.89 Hit: 134 / 150
```

- Check the distribution of scores in both ways and analyze why
- A structural explanation (class, main) is also required along with the source code
- Bonus points, explain the reason based on what you learned in lecture

```
# Why are these two elements almost the same? additional 10 points
print(f'pi : {EM_model.pi}')
print(f'count / total : {np.bincount(EM_pred) / 150}')
```