



# Compilers

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## Implementing Type Checking

- COOL type checking can be implemented in a single traversal over the AST
- Type environment is passed down the tree
  - From parent to child
- Types are passed up the tree
  - From child to parent

$$\frac{O, M, C \vdash e_1 : \text{Int} \quad O, M, C \vdash e_2 : \text{Int}}{O, M, C \vdash e_1 + e_2 : \text{Int}} [\text{Add}]$$

```
TypeCheck(Environment, e1 + e2) = {  
  T1 = TypeCheck(Environment, e1);  
  T2 = TypeCheck(Environment, e2);  
  Check T1 == T2 == Int;  
  return Int; }
```

$$\frac{\begin{array}{c} O \vdash e_0 : T_0 \\ O[T/x] \vdash e_1 : T_1 \\ T_0 \leq T \end{array}}{O \vdash \text{let } x:T \leftarrow e_0 \text{ in } e_1 : T_1} \quad [\text{Let-Init}]$$

```
TypeCheck(Environment, let x:T ← e0 in e1) = {  
  T0 = TypeCheck(Environment, e0);  
  T1 = TypeCheck(Environment.add(x:T), e1);  
  Check subtype(T0, T1);  
  return ; T1}
```