

# Index

Any inaccuracies in this index may be explained by the fact that it has been prepared with the help of a computer.

—Donald E. Knuth, *Fundamental Algorithms*  
(Volume 1 of *The Art of Computer Programming*)

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# Colophon

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<sup>2</sup><https://hmemcpy.com>

<sup>3</sup><https://mercury.postlight.com/web-parser/>

<sup>4</sup><https://www.crummy.com/software/BeautifulSoup/>

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<sup>7</sup><https://www.gnu.org/philosophy/free-sw.en.html>

